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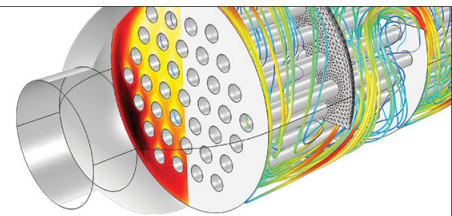
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## Electroacoustic properties of $\langle 110 \rangle$ -oriented $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $\text{PbTiO}_3$ crystals under uniaxial stress

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The electromechanical properties of  $\langle 110 \rangle$ -oriented  $0.7\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $0.3\text{PbTiO}_3$  crystals have been investigated under uniaxial stress ( $\sigma$ ).  $\langle 110 \rangle$ -oriented crystals have a longitudinal electromechanical coupling coefficient ( $k_{33}$ ) of  $\sim 0.9$  and an acoustic power density of 12 dB which decreases to 8 dB with increasing  $\sigma$  between 0 and  $4 \times 10^7$  N/m<sup>2</sup>. The results demonstrate that the advantages in terms of power density and coupling coefficient of oriented piezocrystals are not constrained to the  $\langle 001 \rangle$ -orientation, but rather can also be obtained along the  $\langle 110 \rangle$ . © 2003 American Institute of Physics. [DOI: 10.1063/1.1591240]

Single crystals of  $(1-x)\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $x\text{PbTiO}_3$  (PMN– $x\%$  PT) and  $\text{Pb}(\text{Zn}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $\text{PbTiO}_3$  (PZN– $x\%$  PT) are currently under development for use in transducer and projector applications.<sup>1,2</sup> Previous investigations have focused on  $\langle 001 \rangle$ -oriented crystals, for compositions in the ferroelectric rhombohedral phase ( $\text{FE}_r$ ) ( $x < 30$  at. %), close to the morphotropic phase boundary. In poled  $\langle 001 \rangle$ -oriented single crystals, longitudinal piezoelectric ( $d_{33}$ ) and electromechanical coupling ( $k_{33}$ ) coefficients of 1800 pC/N and 0.94 have been reported,<sup>1,2</sup> respectively. Strain levels of up to 1.2% were reported at field levels of  $\sim 30$  kV/cm. The potential advantages of  $\langle 001 \rangle$ -oriented PMN–PT crystals in transducer applications are twofold. First, the crystals have the potential for higher bandwidth due to an enhanced electromechanical coupling coefficient. Second, the crystals have the potential for higher projected acoustical energy density due to their higher strain. Acoustic power densities of  $\sim 12$  dB have recently been obtained for  $\langle 001 \rangle$ -oriented specimens, under prestress.<sup>3,4</sup>

Recent investigations have shown high electromechanical coefficients for  $\langle 110 \rangle$ -oriented PMN–PT crystals.<sup>5,6</sup> Values of  $d_{33}$  and  $k_{33}$  were found to be equally high as those along the  $\langle 001 \rangle$ . An unusual electromechanical and elastic equivalence was found between the  $\langle 110 \rangle$  and  $\langle 001 \rangle$  directions. These investigations clearly demonstrated that the potential advantages of PMN–PT crystals for transducer applications are not constrained to a single crystallographic orientation, but rather to the (011) plane.

The purpose of this investigation was to study the effects of uniaxial stress on  $\langle 110 \rangle$ -oriented single crystals of  $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $30\%$   $\text{PbTiO}_3$ . In acoustic transducer applications,<sup>7,8</sup> uniaxial prestress inherently needs to be used, in order to keep the transducer from going into tension and consequently to be able to harness the highest electromechanical response. Investigations have been performed using polarization versus field ( $P$ – $E$ ), strain versus field ( $\varepsilon$ – $E$ ), and strain versus stress ( $\varepsilon$ – $\sigma$ ) methods.

$\langle 110 \rangle$ -oriented  $\text{Pb}(\text{Mg}_{1/3}\text{Nb}_{2/3})\text{O}_3$ – $30\%$   $\text{PbTiO}_3$  grown by seeded vertical Bridgman methods<sup>9–11</sup> have been obtained from HC Materials (Urbana, IL). Plate-like specimens were cut into dimensions of  $\sim 0.4$  cm  $\times$   $0.4$  cm  $\times$   $0.04$  cm, and bar-like specimens were cut into dimensions of  $\sim 0.4$  cm  $\times$   $0.4$  cm  $\times$   $1.2$  cm. All specimens were electroded with gold. The specimens were poled at room temperature in a silicon oil bath, using a current-limiting method to prevent breakdown.  $P$ – $E$  measurements were made using a modified Sawyer–Tower bridge. In addition,  $\varepsilon$ – $E$  measurements were simultaneously performed using a strain gauge (bar-shaped specimens) or a LVDT method (plate-like specimens). For the bar-shaped specimens, strain gauges were mounted on the side of the bars and a mechanical load was applied using a pneumatic cylinder. These measurements were performed using a drive frequency of 10 Hz at maximum applied field strengths of 15 kV/cm. Measurements were performed as a function of mechanical prestress between 0 and  $6 \times 10^7$  N/m<sup>2</sup>.

Figures 1(a) and 1(b) show the unipolar  $P$ – $E$  and  $\varepsilon$ – $E$  characteristics for the plate-like specimens. These data are pronouncedly anhysteretic, over the entire range of  $E$  investigated all the way to saturation. In particular, the integrated area of the hysteresis loop in the  $P$ – $E$  response was nearly zero, at least within the limits of instrumentation error. Data are shown for three different maximum ac electric fields of 10, 20, and 40 kV/cm. The data demonstrate an induced phase transformation near 10 kV/cm, reaching saturation near 12 kV/cm. It is important to notice that this induced phase transformation was also anhysteretic. The magnitude of  $\Delta P$  and  $\varepsilon$  at 12 kV/cm was  $0.07$  C/m<sup>2</sup> and  $3 \times 10^{-3}$ , respectively, which is a relatively high induced strain for a small  $\Delta P$ . Accordingly, the piezoelectric ( $d_{33}$ ) and electromechanical coupling ( $k_{33}$ ) coefficients are high along the  $\langle 110 \rangle$ . Resonance-antiresonance investigations of  $\langle 110 \rangle$ -oriented PMN–PT crystals demonstrated equally high values of  $d_{33}$  (1500 pC/N) and  $k_{33}$  (0.94) coefficients. This dismisses the notion that the high electromechanical performance can only be due to an induced FE<sub>r</sub> phase and/or po-

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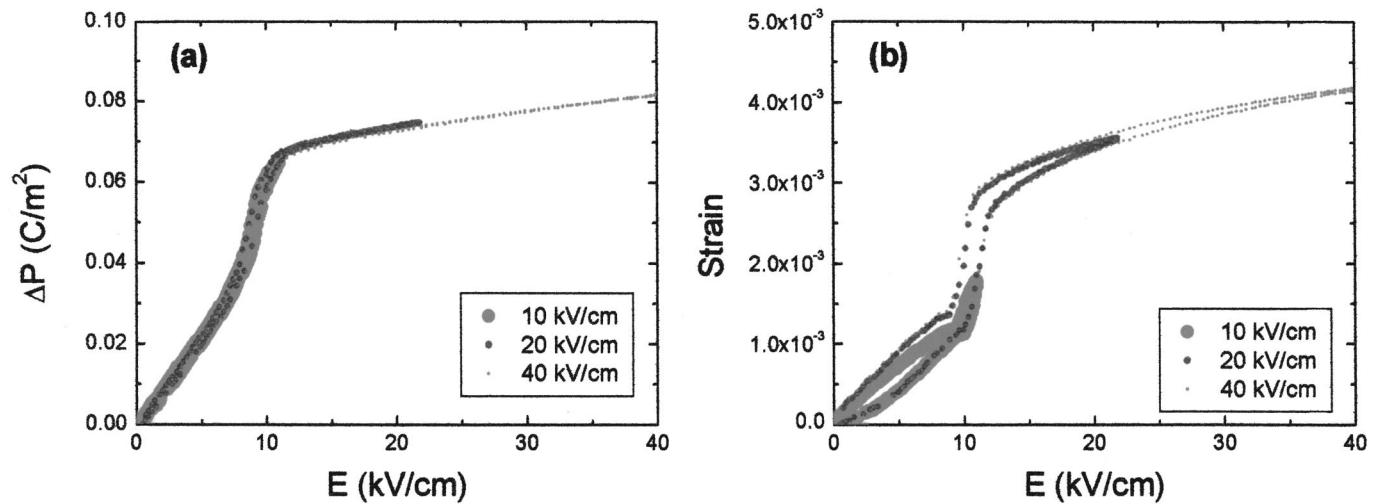


FIG. 1. Unipolar  $P-E$  and  $\epsilon-E$  characteristics of  $\langle 110 \rangle$ -oriented PMN-PT plate-like crystals. (a)  $P-E$  response, and (b)  $\epsilon-E$  response. Data are shown for various maximum ac drives of 10, 20, and 40 kV/cm. The data for the various maximum ac drives are distinguished by the size of the points in the figure.

larization rotation towards  $\langle 001 \rangle$ . In addition, the value of Young's modulus  $Y_1$  was measured calculated to be  $1.8 \times 10^{10}$  N/m<sup>2</sup> from the standard resonance-antiresonance IEEE method.

Figures 2(a) and 2(b) show the unipolar  $\Delta P-E$  and  $\epsilon-E$  responses for a bar-shaped  $\langle 110 \rangle$ -oriented crystal under various uniaxial stresses. Decreases in  $\Delta P$  and  $\epsilon$  are noticeable with increasing  $\sigma$ , in particular for  $E > 10$  kV/cm where the induced phase transition occurred. At  $E = 15$  kV/cm,  $\Delta P$  decreased from  $\sim 0.07$  C/m<sup>2</sup> under small loads to  $\sim 0.058$  C/m<sup>2</sup> under  $6 \times 10^7$  N/m<sup>2</sup>. Correspondingly,  $\epsilon$  decreased from  $\sim 1.9 \times 10^{-3}$  to  $\sim 1.4 \times 10^{-3}$  with increasing  $\sigma$ . The data reveal essentially no change in the hysteretic losses with increasing  $\sigma$ . The dominant change with increasing  $\sigma$  was to suppress the induced phase transformation, resulting in the  $\Delta P-E$  and  $\epsilon-E$  responses becoming increasingly linear with increasing  $\sigma$ . For  $\sigma = 6 \times 10^7$  N/m<sup>2</sup>, the electromechanical behavior is nearly ideally linear and anhysteretic, with an effective  $d_{33}$  of  $\sim 1000$  pC/N, as determined from the slope. These results are in contrast to the stress-dependent

electromechanical properties of  $\langle 001 \rangle$ -oriented crystals, which become increasingly nonlinear and hysteretic with increasing  $\sigma$ .<sup>3,4</sup> It is also important to note that there was a difference in the field level at which the step in strain occurred between the plate-like specimen of Fig. 1(b) (10 kV/cm), and the long-rectangular one of Fig. 2(b) (12 kV/cm). The differences are attributed to small composition variations that shift the critical field of the induced transition.

The electromechanical coupling coefficient ( $k_{33}$ ) at various uniaxial loads can be calculated,<sup>7,8</sup> as given in Eq. (1):

$$k_{33}^2 = d_{33}^2 Y_1 / (\chi_0 K), \tag{1}$$

where  $Y_1$  is Young's modulus,  $\chi_0$  is the permittivity of free space ( $8.85 \times 10^{-12}$  F/m),  $K$  is the relative dielectric constant, and  $d_{33}$  is the longitudinal piezoelectric coefficient.  $K$  can be approximated from the  $P-E$  response over a quasilinear range as  $\delta P_3 / \delta E_3$ , and  $d_{33}$  can be approximated over a quasilinear range as  $\delta \epsilon_3 / \delta E_3$ , both of which have limitations. Quasilinear approximations were performed for an  $E_{dc}$  of 8 kV/cm and an  $E_{ac}$  of 4 kV/cm. The value of  $Y_1$  can be

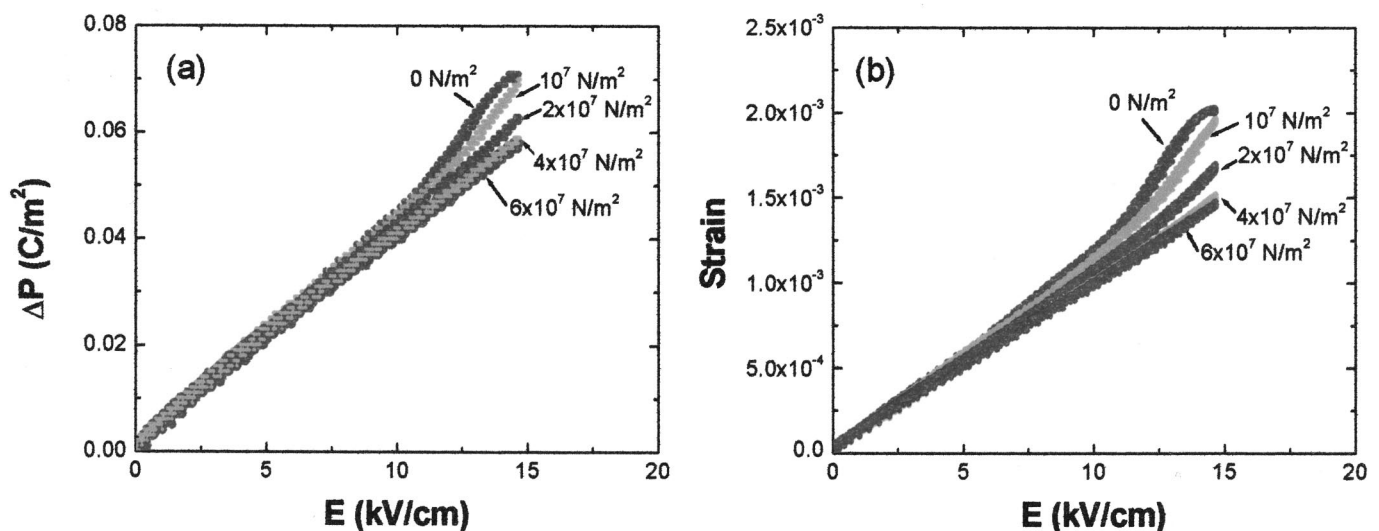


FIG. 2.  $P-E$  and  $\epsilon-E$  responses for  $\langle 110 \rangle$ -oriented long-rectangular shaped crystals, taken at various uniaxial stresses between 0 and  $6 \times 10^7$  N/m<sup>2</sup>. (a)  $P-E$  response, and (b)  $\epsilon-E$  response.

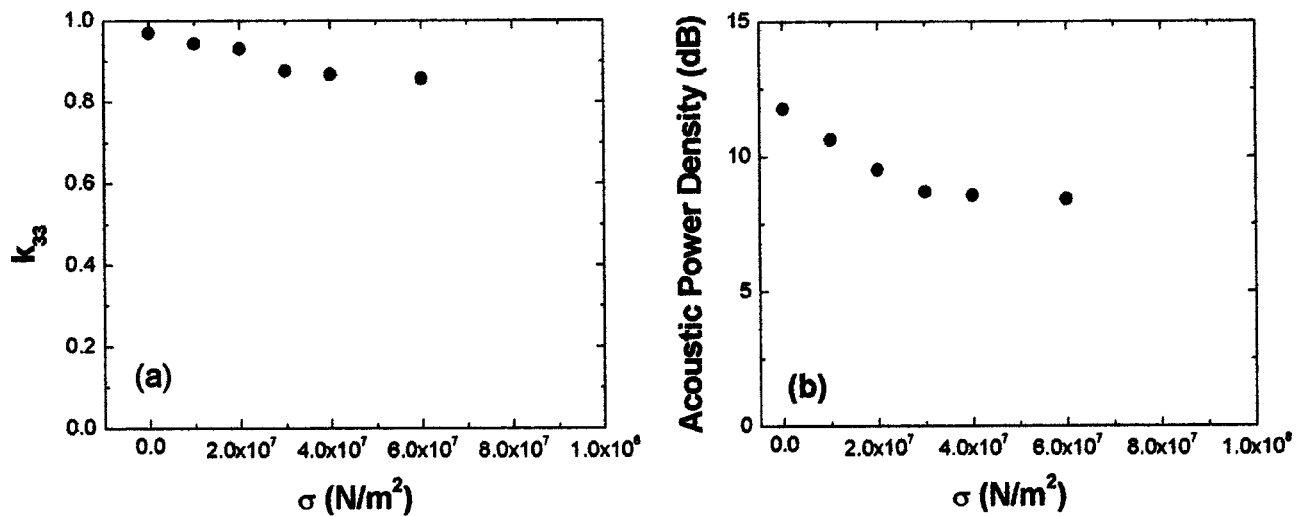


FIG. 3. Coupling coefficient and acoustic power density of  $\langle 110 \rangle$ -oriented PMN–PT long-rectangular crystals as a function of stress. (a) Coupling coefficient and (b) acoustic power density.

determined from measurements of the  $\varepsilon$ – $\sigma$  response. Accordingly,  $Y_1$  was determined at various dc bias levels ( $E_{dc}$ ) by stress-strain ( $\varepsilon$ – $\sigma$ ) measurements. The  $\varepsilon$ – $\sigma$  curves were linear and  $Y_1$  was calculated from the slopes. The value of  $k_{33}$  is shown in Fig. 3(a) as a function of  $\sigma$ . In this figure,  $k_{33}$  can be seen to be somewhat independent of  $\sigma$ . For example,  $k_{33}$  varied between 0.95 at  $\sigma = 0$   $\text{N/m}^2$  to  $\sim 0.86$  at  $\sigma = 6 \times 10^7$   $\text{N/m}^2$ . The value of  $k_{33}$  under zero uniaxial stress is close to that determined by the resonance-antiresonance method earlier. These results clearly demonstrate  $\langle 110 \rangle$ -oriented crystals maintain a high electromechanical coupling coefficient under realistic operational conditions for use in acoustic transducers. In fact,  $k_{33}$  is equally as high along the  $\langle 110 \rangle$ , as along the  $\langle 001 \rangle$ .<sup>1–4</sup> This is essential to their use in high performance applications that require enhanced bandwidth.

By convention, the acoustical energy density can be defined relative to that of a standard PZT-8 material, as given in Eq. (2a),<sup>7,8</sup> where

$$\text{acoustic energy density (dB)} = 10 \log(E_{\text{elastic}}/E_{\text{PZT-8}}), \quad (2a)$$

$$E_{\text{elastic}} = 1/2 Y_1 \varepsilon_{\text{rms}}^2. \quad (2b)$$

$E_{\text{PZT-8}}$  is the acoustical energy density of the standard PZT-8.  $E_{\text{PZT-8}}$  is calculated by assuming a linear piezoelectric response over the operational field range, i.e.,  $\varepsilon_{ij} = d_{ijk} E_k$ . The accepted values of  $d_{ijk}$  and  $Y_1$  for PZT-8 are equal to  $2.25 \times 10^{-10}$  C/N and  $7.4 \times 10^{10}$  N/m<sup>2</sup>. Thus, the value of  $E_{\text{PZT-8}}$  can be estimated as  $936.6 \text{ J/m}^3$  under an applied electric field of 10 kV/cm. Using the values for  $E_{\text{elastic}}$ , the corresponding acoustical energy density can be calculated using Eq. (2a). Figure 3(b) shows the acoustical power density (dB) as a

function of  $\sigma$ . In this figure, the acoustical power density can be seen to decrease with some with increasing  $\sigma$ . For example, the acoustic power density varied between 11.75 dB at  $\sigma = 0$  to  $\sim 8.5$  dB at  $\sigma = 6 \times 10^7$   $\text{N/m}^2$ .

The results demonstrate that  $\langle 110 \rangle$ -oriented PMN–PT crystals are near linear electromechanical materials with high acoustic energy densities, high coupling, and essentially no loss. For  $\sigma < 2 \times 10^7$   $\text{N/m}^2$ , they offer a  $k_{33} > 0.95$  and an acoustic power density of  $\sim 10$  dB. We believe that  $\langle 110 \rangle$ -oriented crystals have a unique character, which offers promise for transducer applications, even potentially over that of  $\langle 001 \rangle$  crystals. This is that twinning occurs along the  $\langle 110 \rangle$ . A stress applied along the  $\langle 110 \rangle$  will not favor one twin state over another. Thus, the electromechanical response has increased linearity and lower losses due to a lack of domain contributions, and better accommodation to applied stress.

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