

HerMES: CANDIDATE HIGH-REDSHIFT GALAXIES DISCOVERED WITH *HERSCHEL*/SPIRE^{*,†}

C. DARREN DOWELL^{1,2}, A. CONLEY³, J. GLENN^{3,4}, V. ARUMUGAM⁵, V. ASBOTH⁶, H. AUSSSEL⁷, F. BERTOLDI⁸, M. BÉTHÉRMIN⁷, J. BOCK^{1,2}, A. BOSELLI⁹, C. BRIDGE¹, V. BUAT⁹, D. BURGARELLA⁹, A. CABRERA-LAVERS^{10,11,12}, C. M. CASEY¹³, S. C. CHAPMAN^{14,15}, D. L. CLEMENTS¹⁶, L. CONVERSI¹⁷, A. COORAY^{1,18}, H. DANNERBAUER¹⁹, F. DE BERNARDIS¹⁸, T. P. ELLSWORTH-BOWERS⁴, D. FARRAH²⁰, A. FRANCESCHINI²¹, M. GRIFFIN²², M. A. GURWELL²³, M. HALPERN⁶, E. HATZIMINAOGLOU²⁴, S. HEINIS⁹, E. IBAR^{25,26}, R. J. IVISON^{5,25}, N. LAPORTE^{10,11}, L. MARCHETTI^{21,27}, P. MARTÍNEZ-NAVAJAS^{10,11}, G. MARSDEN⁶, G. E. MORRISON^{13,28}, H. T. NGUYEN^{1,2}, B. O'HALLORAN¹⁶, S. J. OLIVER²⁹, A. OMONT³⁰, M. J. PAGE³¹, A. PAPAGEORGIOU²², C. P. PEARSON^{27,32}, G. PETITPAS²³, I. PÉREZ-FOURNON^{10,11}, M. POHLEN²², D. RIECHERS^{1,33}, D. RIGOPOULOU^{32,34}, I. G. ROSEBOOM^{5,29}, M. ROWAN-ROBINSON¹⁶, J. SAYERS¹, B. SCHULZ^{1,35}, DOUGLAS SCOTT⁶, N. SEYMOUR³⁶, D. L. SHUPE^{1,35}, A. J. SMITH²⁹, A. STREBLYANSKA^{10,11}, M. SYMEONIDIS³¹, M. VACCARI^{21,37}, I. VALTCHANOV¹⁷, J. D. VIEIRA¹, M. VIERO¹, L. WANG²⁹, J. WARDLOW¹⁸, C. K. XU^{1,35}, AND M. ZEMCOV¹

¹ California Institute of Technology, 1200 E. California Blvd., Pasadena, CA 91125, USA; cdd@astro.caltech.edu

² Jet Propulsion Laboratory, 4800 Oak Grove Drive, Pasadena, CA 91109, USA

³ Center for Astrophysics and Space Astronomy 389-UCB, University of Colorado, Boulder, CO 80309, USA

⁴ Department of Astrophysical and Planetary Sciences, CASA 389-UCB, University of Colorado, Boulder, CO 80309, USA

⁵ Institute for Astronomy, University of Edinburgh, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

⁶ Department of Physics & Astronomy, University of British Columbia, 6224 Agricultural Road, Vancouver, BC V6T 1Z1, Canada

⁷ Laboratoire AIM-Paris-Saclay, CEA/DSM/Irfu-CNRS-Université Paris Diderot, CE-Saclay, pt courrier 131, F-91191 Gif-sur-Yvette, France

⁸ Argelander Institute für Astronomy, Universität Bonn, Auf dem Hügel 71, D-53121 Bonn, Germany

⁹ Aix-Marseille Université, CNRS, LAM (Laboratoire d'Astrophysique de Marseille), UMR7326, F-13388 Marseille, France

¹⁰ Instituto de Astrofísica de Canarias (IAC), E-38200 La Laguna, Tenerife, Spain

¹¹ Departamento de Astrofísica, Universidad de La Laguna (ULL), E-38205 La Laguna, Tenerife, Spain

¹² GTC Project, E-38205 La Laguna, Tenerife, Spain

¹³ Institute for Astronomy, University of Hawaii, 2680 Woodlawn Drive, Honolulu, HI 96822, USA

¹⁴ Department of Physics and Atmospheric Science, Dalhousie University, Halifax, NS B3H 3J5, Canada

¹⁵ Institute of Astronomy, University of Cambridge, Madingley Road, Cambridge CB3 0HA, UK

¹⁶ Astrophysics Group, Imperial College London, Blackett Laboratory, Prince Consort Road, London SW7 2AZ, UK

¹⁷ Herschel Science Centre, European Space Astronomy Centre, Villanueva de la Cañada, E-28691 Madrid, Spain

¹⁸ Department of Physics & Astronomy, University of California, Irvine, CA 92697, USA

¹⁹ Universität Wien, Institut für Astrophysic, Türkenschanzstraße 17, A-1180, Wien, Austria

²⁰ Department of Physics, Virginia Tech, Blacksburg, VA 24061, USA

²¹ Dipartimento di Fisica e Astronomia, Università di Padova, vicolo Osservatorio, 3, I-35122 Padova, Italy

²² School of Physics and Astronomy, Cardiff University, Queens Buildings, The Parade, Cardiff CF24 3AA, UK

²³ Harvard-Smithsonian Center for Astrophysics, 60 Garden Street, Cambridge, MA 02138, USA

²⁴ ESO, Karl-Schwarzschild-Str. 2, D-85748 Garching bei München, Germany

²⁵ UK Astronomy Technology Centre, Royal Observatory, Blackford Hill, Edinburgh EH9 3HJ, UK

²⁶ Universidad Católica de Chile, Departamento de Astronomía y Astrofísica, Vicuña Mackenna 4860, Casilla 306, Santiago 22, Chile

²⁷ Department of Physical Sciences, The Open University, Milton Keynes MK7 6AA, UK

²⁸ Canada–France–Hawaii Telescope, Kamuela, HI 96743, USA

²⁹ Astronomy Centre, Department of Physics & Astronomy, University of Sussex, Brighton BN1 9QH, UK

³⁰ Institut d'Astrophysique de Paris, UMR 7095, CNRS, UPMC Univ. Paris 06, 98bis boulevard Arago, F-75014 Paris, France

³¹ Mullard Space Science Laboratory, University College London, Holmbury St. Mary, Dorking, Surrey RH5 6NT, UK

³² RAL Space, Rutherford Appleton Laboratory, Chilton, Didcot, Oxfordshire OX11 0QX, UK

³³ Department of Astronomy, Space Science Building, Cornell University, Ithaca, NY 14853-6801, USA

³⁴ Department of Astrophysics, Denys Wilkinson Building, University of Oxford, Keble Road, Oxford OX1 3RH, UK

³⁵ Infrared Processing and Analysis Center, MS 100-22, California Institute of Technology, JPL, Pasadena, CA 91125, USA

³⁶ CSIRO Astronomy & Space Science, P.O. Box 76, Epping, NSW 1710, Australia

³⁷ Astrophysics Group, Physics Department, University of the Western Cape, Private Bag X17, 7535, Bellville, Cape Town, South Africa

Received 2013 July 12; accepted 2013 October 25; published 2013 December 13

ABSTRACT

We present a method for selecting $z > 4$ dusty, star-forming galaxies (DSFGs) using *Herschel*/Spectral and Photometric Imaging Receiver 250/350/500 μm flux densities to search for red sources. We apply this method to 21 deg^2 of data from the HerMES survey to produce a catalog of 38 high- z candidates. Follow-up of the first five of these sources confirms that this method is efficient at selecting high- z DSFGs, with 4/5 at $z = 4.3\text{--}6.3$ (and the remaining source at $z = 3.4$), and that they are some of the most luminous dusty sources known. Comparison with previous DSFG samples, mostly selected at longer wavelengths (e.g., 850 μm) and in single-band surveys, shows that our method is much more efficient at selecting high- z DSFGs, in the sense that a much larger fraction are at $z > 3$. Correcting for the selection completeness and purity, we find that the number of bright ($S_{500\mu\text{m}} \geq 30 \text{ mJy}$), red *Herschel* sources is $3.3 \pm 0.8 \text{ deg}^{-2}$. This is much higher than the number predicted by current models, suggesting that the DSFG population extends to higher redshifts than previously believed. If the shape of the luminosity function for high- z DSFGs is similar to that at $z \sim 2$, rest-frame UV based studies may be missing a significant component of the star formation density at $z = 4\text{--}6$, even after correction for extinction.

Key words: galaxies: high-redshift – galaxies: starburst – infrared: galaxies – submillimeter: galaxies

Online-only material: color figures

1. INTRODUCTION

The study of massive, dusty, star-forming galaxies (DSFGs) since their discovery more than a decade ago (Smail et al. 1997; Hughes et al. 1998; Barger et al. 1998) has fundamentally changed our understanding of the cosmic history of star formation and galaxy evolution (e.g., Lagache et al. 2005). These sources are generally believed to be the progenitors of massive elliptical galaxies in the current epoch. They were first studied in the submillimeter and millimeter,³⁸ where they have the remarkable property that their observed brightness at a fixed luminosity is almost independent of redshift over roughly $1 < z < 10$ (Blain & Longair 1993; Blain et al. 2002) due to the shape of their spectral energy distributions (SEDs), an effect which is known as a negative K -correction. The technology and instrumentation to exploit this advantage is challenging, however, and ground-based submillimeter/millimeter instruments have typically only been able to map areas down to depths of a few mJy over hundreds of arcminutes² through narrow atmospheric windows (Eales et al. 2000; Scott et al. 2002; Borys et al. 2003; Greve et al. 2004; Laurent et al. 2005; Coppin et al. 2006; Bertoldi et al. 2007; Perera et al. 2008; Scott et al. 2008; Weiß et al. 2009; Austermann et al. 2010; Aretxaga et al. 2011).

Obtaining redshifts for these objects is a painstaking process (see, e.g., Chapman et al. 2005). The most common technique up to this point, which relies on identifying the radio or mid-IR counterparts (e.g., Ivison et al. 2007; Roseboom et al. 2010) to provide sufficiently precise localizations and the source being sufficiently bright for successful optical spectroscopy, works relatively poorly at $z > 3$ because such observations do not benefit from negative K -corrections. Furthermore, even for very high- z sources, ground-based submillimeter/millimeter observations are generally limited to probing only the red, Rayleigh–Jeans side of the thermal SED, and hence can only provide extremely crude redshift estimates.

As a result, until recently the number of known $z > 4$ DSFGs was relatively limited, although there were some (mostly photometric) hints that the redshift distribution extended beyond $z = 3$ (e.g., Dannerbauer et al. 2002; Younger et al. 2007, 2009). However, the known $z > 4$ DSFGs were selected in a fairly irregular fashion, making it difficult to place any quantitative limits on the number of such sources. Theoretically, the existence of even the lower- z DSFGs ($z \approx 2.5$) has proven somewhat challenging to explain (e.g., Baugh et al. 2005). The primary challenge is to accrete enough gas into the center of massive dark matter halos at early times in order to fuel these starbursts. These difficulties are only exacerbated at higher redshifts because the number of massive galaxies is expected to decrease rapidly at high z (Hayward et al. 2013). Therefore, a significant population of $z > 4$ massive starbursts would be a significant challenge to models. Despite this, there are some indirect lines of evidence that suggest that the most massive galaxies may have formed stars at such early times. In contrast to the bulk of the field galaxy population, for which most star formation occurs after $z = 2$ (e.g., Sobral et al. 2012), studies of the K -band luminosity function of clusters show that the stellar mass in the brightest members is already in place earlier

(Capozzi et al. 2012). Detailed study of individual sources favors a star formation epoch of $z > 4$ (Stott et al. 2011; Kaviraj et al. 2013). However, what is missing is an effective technique for selecting such sources directly while they are experiencing a starburst.

The *Herschel Space Observatory* (Pilbratt et al. 2010), which observed at multiple bands spanning the peak of the SED at effectively all redshifts, and mapped much larger areas down to the confusion limit than previous surveys, could measure $T_{\text{dust}}/(1+z)$ for a large number of individually detected sources. Since most known distant DSFGs have dust temperatures in the range $\sim 20\text{--}80$ K (e.g., Kovács et al. 2006; Casey et al. 2012), the observed *Herschel* colors can be used to select potential high- z sources. In this paper we use a map-based technique to search for red, and hence potentially $z > 4$, sources in 21.4 deg² within the Science Demonstration Phase (SDP) fields from the HerMES project (Oliver et al. 2012) at 250, 350, and 500 μm . In particular, we select “red” sources with $S_{500\mu\text{m}} \geq S_{350\mu\text{m}} \geq S_{250\mu\text{m}}$ —so-called 500 μm risers—to provide a catalog of high- z DSFGs candidates with $S_{500\mu\text{m}} \geq 30$ mJy. The highlight of this initial catalog was the discovery of the highest- z massive starburst to date, a $z = 6.34$ source with a star formation rate of $3000 M_{\odot} \text{ yr}^{-1}$ (First Look Summary (FLS) 3; Riechers et al. 2013).

We present follow-up of some of these sources, including redshifts for four additional targets from our sample. We find that four of five 500 μm risers selected with our technique and with measured redshifts lie at $z > 4$ (and the remaining source is at $z = 3.4$), demonstrating that this technique is an effective method of selecting high- z DSFGs. Returning to the full catalog, we characterize our selection using completeness and purity simulations in order to measure the number density of red sources (Section 5), show that existing literature models in general significantly under-predict the number of bright, red sources we find (Section 7.1), and estimate their contribution to the star formation history of the universe (Section 7.5). Comparison with other surveys of our fields shows that our sources are redder than typical sources selected at 1 mm (Section 7.2).

2. SPIRE OBSERVATIONS AND DATA ANALYSIS

In this paper, we analyze maps of three extragalactic fields observed as part of the HerMES program with the Spectral and Photometric Imaging Receiver (SPIRE; Griffin et al. 2010) on board *Herschel*: *Spitzer* FLS, GOODS North, and the Lockman Hole. The latter has been further subdivided based on mapped depth into the North, East, and SWIRE regions (Table 1). SPIRE observed simultaneously at 250, 350, and 500 μm . Although the fields were selected based on availability of *Herschel* SDP data, all available data for these fields, including those beyond the SDP, have been used in the generation of our maps. The basic observation and calibration procedures are described by Griffin et al. (2010) and Bendo et al. (2013).

Under the hypothesis that redshift dominates temperature evolution in producing the observed SEDs of distant galaxies, we select objects which have “red” SPIRE colors in the hope of forming a high-redshift sample. This should not be expected to select *all* such sources. For example, the $z = 3$ lensed DSFG LSW 1 (Conley et al. 2011) would not be red in the SPIRE bands unless it were at $z > 7$.

A natural question is why we do not simply search for targets using pre-existing single-band HerMES catalogs by imposing our color and minimum flux density requirements. Catalogs

* <http://hermes.sussex.ac.uk>.

† *Herschel* is an ESA space observatory with science instruments provided by European-led Principal Investigator consortia and with important participation from NASA.

³⁸ Classic submillimeter galaxies (SMGs) are simply DSFGs selected at $\sim 850 \mu\text{m}$.

Table 1
Summary of Fields Used in This Analysis

Field	R.A. (deg)	Decl. (deg)	Area (deg ²)	$\sigma_{250\mu\text{m}}$ (mJy)	$\sigma_{350\mu\text{m}}$ (mJy)	$\sigma_{500\mu\text{m}}$ (mJy)
GOODS-N	189.23	62.22	0.33	0.8	0.8	1.0
Lockman-East	163.14	57.49	0.34	3.6	3.6	4.0
Lockman-North	161.49	59.01	0.46	3.6	3.5	4.1
FLS	259.05	59.29	6.83	5.1	5.3	6.5
Lockman-SWIRE	161.68	57.97	13.46	4.2	4.1	5.3

Notes. Properties of the fields used in this analysis. The R.A. and decl. are the approximate field centers (J2000), the area excludes regions masked due to the lack of cross-scans, and the depths are the approximate 1σ instrument noise in mJy beam⁻¹ in the center of each field using FWHM/3 map pixels, and not including confusion noise. The Lockman-East and Lockman-North regions are excluded from Lockman-SWIRE. The rms due to confusion in the SPIRE bands is ~ 6 mJy beam⁻¹ (Nguyen et al. 2010).

have been produced for these fields in the SPIRE bands which provide a suitable list of 500 μm sources (Smith et al. 2012; Roseboom et al. 2010). However, at present such catalogs are not optimal for our selection purposes. In many cases, they require detection in the other SPIRE bands or at an alternate wavelength (e.g., 24 μm)—requirements which will bias against red and therefore, for our purposes, interesting sources. Furthermore, even in those fields where 500 μm selected catalogs are available, detailed inspection and tests on simulated data show that catalog selection is currently both significantly less pure (i.e., a larger portion of the detected sources are not, in fact, red) and less complete than the map-based method described below.

2.1. Map Construction

Our map-based search uses products from the SPIRE-HerMES Iterative Map maker (SHIM; Levenson et al. 2010; Viero et al. 2013). Briefly, we use redundant sampling of the same position on the sky with multiple scan directions (cross-scans) to suppress correlated $1/f$ noise via baseline polynomial subtraction and to remove artifacts such as “glitches” caused by cosmic rays. Our maps are astrometrically aligned with pre-existing radio and *Spitzer*/MIPS 24 μm data to better than 1'' accuracy using stacking.

Because SPIRE is diffraction limited, the beam size varies considerably over the three bands from 17''.6 at 250 μm to 35''.3 at 500 μm (FWHM). In the absence of confusion noise, and for instrument noise that is as white as in the SHIM maps, the mathematically optimum procedure for point-source selection is to smooth the maps by the beam. Since our sources are, by definition, brightest at 500 μm , we therefore smooth all three maps to an identical resolution of $\sqrt{2} \times 35''.3 = 49''.8$. Since SPIRE maps have significant confusion noise, this approach is not ideal—in the future we plan to improve this procedure by adopting a filtering procedure that takes confusion noise into account, such as that described by Chapin et al. (2011).

In order to facilitate this beam matching, we construct SHIM maps with 4'' pixels at all bands. This results in incomplete coverage, particularly at 500 μm (where SPIRE has the lowest sampling density), which is a problem for the convergence of the default SHIM map-maker. However, SHIM makes it possible to re-use baseline and glitch information from maps made at a standard resolution, where convergence is not a problem, and so we have done so for our analysis. We then Gaussian-smooth all the maps to the final resolution, which also fills in the missing coverage due to the small pixels, and then suppress large-scale structure by subtracting a smoothed version of the map (using a

smoothing scale of 3''). Tests on simulated data show that these steps have no significant effect on the accuracy of photometry from the resulting maps, although the smoothing does increase the confusion noise.

2.2. Object Identification in Difference Maps

Prior to source identification, we form a weighted combination of the SPIRE maps to reduce the confusion from typical, bluer SPIRE galaxies. For simplicity—and because experiments with more complicated (quadratic or cubic) map combinations do not seem to provide better performance—we restrict ourselves to a linear combination. With no loss in generality this can be formulated as

$$D = k_1 M_{500\mu\text{m}} + k_2 M_{350\mu\text{m}} \pm \sqrt{1 - k_1^2 - k_2^2} M_{250\mu\text{m}}, \quad (1)$$

with $|k_1|$ and $|k_2|$ both ≤ 1 . The term multiplying the 250 μm map is simply an arbitrary normalization convention, since overall scale factors do not affect our analysis. The sign of this term is another parameter. However—as one would expect, because we are trying to select sources with $S_{500\mu\text{m}} \geq S_{250\mu\text{m}}$ —the minus sign performs much better, so we adopt it henceforth. Because the maps considered in this paper are confusion-noise dominated, there is little advantage to adopting different k values for the different fields (e.g., applying further noise weighting). We optimized the values of k_1 and k_2 through simulation, starting with the Béthermin et al. (2011, hereafter B11) model. This model predicts essentially no bright 500 μm risers (see Section 7.1), and so we also include additional red sources in order to evaluate our efficiency at detecting them.

For this purpose we used a preliminary version of the k 's—which turned out to be very similar to their final values—and injected fake red sources over a range of flux densities and at approximately the observed space density into maps generated from the B11 model, including instrument noise. We then explored a range of values for k_1 and k_2 by applying the source selection procedure (described in the next section), and used this to estimate the purity (the fraction of detected sources which are red and above our $S_{500\mu\text{m}}$ cutoff) and completeness (the fraction of the injected red sources which are recovered) for various values of the k 's. Adopting the product of these two factors as our metric, we identified a broad locus of k_1, k_2 values which provide similar performance.

In order to down-select to the final set of parameters from this set, we further simplified by choosing $k_2 = 0$ and then adopting the value of k_1 from the high-performance locus that minimized the variance in the D map for our deepest field (GOODS-N). Our final values are $k_1 = 0.92, k_2 = 0.0$. Therefore, for the rest of this analysis, we work with the specific difference map

$$D = 0.920 M_{500\mu\text{m}} - 0.392 M_{250\mu\text{m}}. \quad (2)$$

It is somewhat surprising that including the 350 μm map in the combination did not improve the performance of the source finding, but this set of parameters performs as well as any other set of parameters in our tests. Any modifications to our procedure (such as changing the applied smoothing, or applying this procedure to shallower, instrument noise dominated maps) are likely to change the optimum values of the k 's.

We use the measured instrument noise properties of the input SHIM maps to estimate the instrument noise in the difference map (D), including the effects of the smoothing, but neglecting the correlations that it imposes between neighboring pixels.

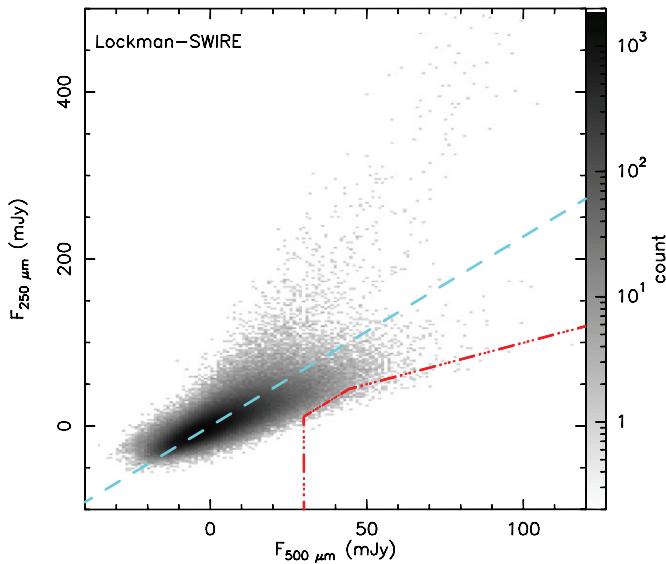


Figure 1. Two-dimensional histogram illustrating the difference map selection used in this paper. The axes are SPIRE 500 μm and 250 μm map-based flux densities. The grayscale gives the number of counts in each flux–flux bin for the Lockman-SWIRE field. The cyan, dashed line shows the “average” color of the galaxies, based on minimizing the variance in the difference image $D(k_1)$. The dot-dashed red line segments show the boundary for object selection, a combination of the threshold in D , the requirement $S_{500\mu\text{m}} \geq S_{250\mu\text{m}}$, and the $S_{500\mu\text{m}} \geq 30$ mJy requirement. The further selection criteria $S_{500\mu\text{m}} \geq S_{350\mu\text{m}}$ and $S_{350\mu\text{m}} \geq S_{250\mu\text{m}}$ are not illustrated here. The input data are the oversampled images; a single galaxy occupies multiple pixels and hence multiple bins. This potential redundancy in object selection is eliminated by the peak finding algorithm. Note that the maps have zero mean before and after point-source filtering, and the bins with significant negative flux densities represent pixels between objects.

(A color version of this figure is available in the online journal.)

We measure the confusion noise in the D maps following the approach of Nguyen et al. (2010), and find a confusion noise of $\sigma_{\text{conf}} = 4.2$ mJy. This is less than the confusion noise in the un-smoothed single-band SPIRE maps (~ 6 mJy), despite the fact that we have degraded the resolution significantly by smoothing; this, in some sense, is the point of forming the difference map—it effectively removes, or at least de-weights, the bulk of the (non-red) SPIRE-detected population, while reducing the signal from red sources by considerably less. Note that the slope of the mean relation between $S_{500\mu\text{m}}$ and $S_{250\mu\text{m}}$ map pixels is ~ 2.3 (Figure 1). The fact that this is so close to the ratio of our coefficients (2.36), which were derived from a process that also included considerations related to red source recovery, is encouraging.

The noise in areas of the maps without cross scans is more complicated and difficult to simulate. Therefore, we masked the edges of our maps to exclude such regions as well as to provide better uniformity in sampling density. We then search for sources in the difference map using StarFINDER³⁹ (Diolaiti et al. 2000), a package designed for source detection in crowded fields. Because the instrument noise estimate ignores the correlations induced by the smoothing procedure, and because the confusion noise distribution is highly non-Gaussian, it is important to use simulations to select the minimum signal-to-noise (S/N) requirement to impose on the source finding in order to optimize the purity and completeness of the resulting catalog. Based on such simulations (see Section 5.4), we have adopted a minimum S/N of 4, where the noise is the quadrature sum

of the 1σ instrument and confusion noise. Because our fields range considerably in depth, the S/N requirement translates to different limits in D for different fields. For the large, shallow fields that dominate our catalog, $D > 25.0$ mJy in FLS, and $D > 23.4$ mJy in Lockman-SWIRE. The depths for the smaller, deeper fields are $D > 19.4$ mJy in Lockman-North and Lockman-East, and $D > 17.3$ mJy in GOODS-N.

2.3. Selection of Sources Rising at 500 μm

The choice $k_1 = 0.92, k_2 = 0$ in the difference images allows “leakage” of bright sources which are somewhat blue ($1 < S_{250\mu\text{m}}/S_{500\mu\text{m}} < 2.3$). Selecting only sources which rise in 500 μm band thus requires an additional selection step. At the position of each detected source in the difference maps, we measure the three SPIRE flux densities from the smoothed maps, since, given our typical positional uncertainties (Section 4.3), measuring the flux densities from the un-smoothed maps results in significant biases. We use these measurements to further impose the requirements $S_{500\mu\text{m}} \geq S_{350\mu\text{m}} \geq S_{250\mu\text{m}}$ and $S_{500\mu\text{m}} \geq 30$ mJy, the effects of which are shown in Figure 1. The last criterion selects sources which are bright enough for relatively easy follow-up. Furthermore, sources fainter than this limit generally have very low detection efficiencies in the SPIRE data using our method (typically 5%–20%), and the uncertainties in those efficiencies are quite large because we do not know their flux densities precisely. Therefore, if we were to include sources below this limit, it would significantly degrade the precision of our source density measurement (see Section 5).

Once sources are identified from the difference maps, we match our targets against the HerMES SCAT catalogs (Smith et al. 2012), which are based on the un-smoothed maps, and provide more precise flux measurements; recall that the reason for not using the catalogs to select red targets is because a catalog search results in a larger number of false sources, but once red targets are identified by the map search this concern no longer applies. This is not possible in all cases, because some of our red sources were not detected by SCAT, possibly because they are too faint in the bluer (250 and 350 μm) SPIRE bands. We use the SCAT v21 catalogs selected at 350 μm for this purpose—the 250 and 500 μm selected catalogs (where available) are generally too incomplete for red sources for our purposes.

In addition, we have visually inspected all sources which pass these cuts in order to remove (rare) noise artifacts, and to note blends of faint sources. The more difficult cases involve noise artifacts on top of real sources which cause them to appear red. However, in general, such false sources are quite easy to detect in the un-smoothed maps, and have been removed from our analysis. In Section 5.2 we make use of simulations to quantify the effects of instrument noise scattering “orange” sources across the selection boundary.

The 38 sources which meet all selection criteria are listed in Table 2 and form the basic sample for this paper. There is one in GOODS-N, 18 in FLS, and 19 in the combined Lockman regions. In addition we include in the table two bright sources (LSW 28 and LSW 102) from outside our field mask (due to the lack of cross-scans at their positions), but do not include them in our formal catalog. Both sources easily pass our selection criteria, and are clearly real; in fact the redshift of LSW 102 is 5.3 (I. Pérez-Fournon et al., in preparation). LSW 28 is a few arcminutes away from the second magnitude star β Ursa Major, which causes complications for optical/near-IR follow-up. For comparison, we also include in the table (but not in the statistical analysis) the known $z = 4$ source pair

³⁹ <http://www.bo.astro.it/StarFinder/paper6.htm>.

Table 2
SPIRE and Radio Fluxes for Sources Selected as Described in Section 2.3

Source Name	Position		Smoothed Map				SCAT			Radio
	α_{2000} (deg)	δ_{2000} (deg)	$S_{250\mu\text{m}}$ (mJy)	$S_{350\mu\text{m}}$ (mJy)	$S_{500\mu\text{m}}$ (mJy)	D (mJy)	$S_{250\mu\text{m}}$ (mJy)	$S_{350\mu\text{m}}$ (mJy)	$S_{500\mu\text{m}}$ (mJy)	$S_{21\text{cm}}$ (μJy)
GOODSN 8 ^x	188.964	62.363	22.7	33.6	35.9	20.9	27 ± 4 (Section 4.4)
FLS 1	257.072	58.479	50.7	82.9	87.4	61.6	62.3	94.0	98.2	<840
FLS 3	256.697	58.772	13.4	26.8	47.5	37.9	12.0	32.4	47.3	59 ± 11
FLS 5	260.204	59.773	17.1	40.0	47.7	37.3	24.7	45.1	48.2	<920
FLS 6	256.797	60.470	39.3	53.0	53.7	26.6	<1200
FLS 7 ^{b,x}	257.511	59.089	24.2	50.2	51.7	40.4	<1030
FLS 17	260.794	60.331	33.7	43.0	48.7	27.7	28.4	42.5	48.6	<960
FLS 19	258.754	60.429	11.5	21.9	36.9	27.2	15.0	21.2	31.4	<980
FLS 20	256.407	60.370	29.9	39.5	50.8	36.4	25.1	34.7	43.5	<1080
FLS 22	257.863	60.632	2.5	31.9	40.0	34.3	14.5	33.2	37.1	<1010
FLS 23 ^b	260.334	58.571	29.6	39.6	41.6	32.9	12.3	26.7	31.7	<1010
FLS 24	261.196	59.556	2.0	26.1	32.6	31.7	16.3	32.2	34.3	<960
FLS 25	259.788	60.121	29.6	41.2	45.6	32.6	31.6	40.3	42.9	<1020
FLS 26 ^x	257.798	58.963	15.8	30.8	35.0	30.8	<980
FLS 30 ^x	258.364	58.401	47.5	52.3	54.7	29.7	<910
FLS 31 ^x	257.644	58.639	-2.0	26.4	33.0	27.6	<990
FLS 32 ^x	261.148	60.053	10.9	20.6	34.2	26.4	<1000
FLS 33	259.879	60.475	26.3	42.1	44.3	26.9	21.6	39.6	40.6	<1010
FLS 34 ^x	257.110	59.680	16.7	33.7	40.7	27.8	16.7	33.7	40.7	<950
LSW 20	162.885	56.605	4.5	21.5	39.0	33.1	17.6	36.6	43.9	<920
LSW 25 ^r	159.435	57.198	47.5	59.9	64.3	41.6	51.3	66.9	69.7	127,000
LSW 26 ^y	161.056	58.770	13.4	30.3	31.4	27.4	23.9	39.0	34.2	<980
LSW 29	161.935	57.942	30.1	50.0	51.2	31.5	32.5	47.5	50.3	<980
LSW 31 ^x	160.973	59.361	40.6	53.8	57.2	39.8	<970
LSW 47 ^x	162.148	57.936	29.0	52.5	53.5	38.7	<960
LSW 48 ^y	163.427	56.590	3.4	22.1	29.8	34.1	22.6	41.7	40.9	<950
LSW 49	159.652	57.698	27.2	44.4	48.1	33.9	23.1	38.5	40.1	<1040
LSW 50 ^x	163.274	56.684	-2.1	18.0	30.3	32.7	<950
LSW 52	163.954	57.566	17.3	32.6	43.7	31.6	16.3	33.0	40.2	<990
LSW 53	163.135	58.607	31.5	40.7	44.9	31.9	15.8	29.7	32.6	<1030
LSW 54	163.743	57.061	31.9	41.0	44.0	30.9	36.6	46.0	46.7	<920
LSW 55 ^x	164.774	57.751	7.7	24.7	31.2	29.2	<970
LSW 56	165.086	58.028	23.6	41.1	43.3	29.5	28.4	41.7	44.8	<1020
LSW 58	163.391	56.608	7.2	28.8	32.3	27.8	15.6	29.5	34.1	<950
LSW 60 ^x	161.914	60.087	28.6	47.3	47.6	32.9	<1210
LSW 76 ^x	165.353	59.063	41.1	60.1	61.3	40.4	<1030
LSW 81 ^y	163.649	56.522	20.2	38.7	41.4	26.6	29.6	45.0	43.1	<1010
LSW 82	165.420	58.227	21.9	33.4	37.5	25.9	16.4	34.7	37.2	<920
LSW 28 ^c	165.366	56.326	35.1	53.6	64.0	45.2	33.4	55.9	60.0	<960
LSW 102 ^c	160.211	56.115	51.0	122.3	140.0	109.4	49.7	118.1	140.4	<1010
GN20/20.2 ^{b,o}	189.300	62.370	52.3	68.6	65.4	38.2	59.4	75.2	74.1	289 ± 13

Notes. SPIRE and radio parameters for sources detected via our map-based method. The first three 250/350/500 μm flux densities are those derived from the smoothed maps, and D is the flux density measured in the linear map combination described in the text. The SCAT-derived SPIRE flux densities are measured from the un-smoothed maps at the native SPIRE resolution, and are from the SCAT v21 HerMES catalogs. The typical instrumental noise uncertainty in both sets of SPIRE flux densities is 2–3 mJy. The calibration uncertainties for SPIRE are about 5%, and the confusion noise is ~ 6 mJy in the un-smoothed maps; note, however, that both are highly correlated between bands, so have a minor effect on the color ratios between SPIRE bands. The SCAT flux densities, where available, are expected to be more accurate. The $\sim 1000 \mu\text{Jy}$ 21 cm flux density upper limits are from the FIRST or NVSS catalogs. For brighter sources, the positional accuracy is $\sim 5''$ (see Section 4.3). The names of these sources are drawn from a master list that includes additional, non-red HerMES sources.

^b Source is clearly detected as blended in un-smoothed 250 μm maps.

^c Source is in a region of the maps that does not have redundant scans, and hence not included in the statistical analysis.

^o Known $z = 4$ source not detected by our pipeline, but included for comparison.

^r Radio-loud object dominated by synchrotron emission; omitted from sample.

^x Source not present in SCAT v21 350 μm selected catalog.

^y Source with $S_{350\mu\text{m}} > S_{500\mu\text{m}}$ in the SCAT catalog.

GN20/20.2 (Pope et al. 2005; Daddi et al. 2009); it barely fails our selection criteria. Note that this pair has a separation of $24''$, and hence is resolved in the 250 μm channel. The quoted SCAT and radio fluxes are the sum of both. The positions in Table 2,

and throughout this paper, are the centroids in the difference (D) images and have $\sim 5''$ 1σ uncertainty (see Section 4.3). Sources identified as blends or which do not satisfy $S_{500\mu\text{m}} \geq S_{350\mu\text{m}}$ are identified in the table. For comparison, the SCAT

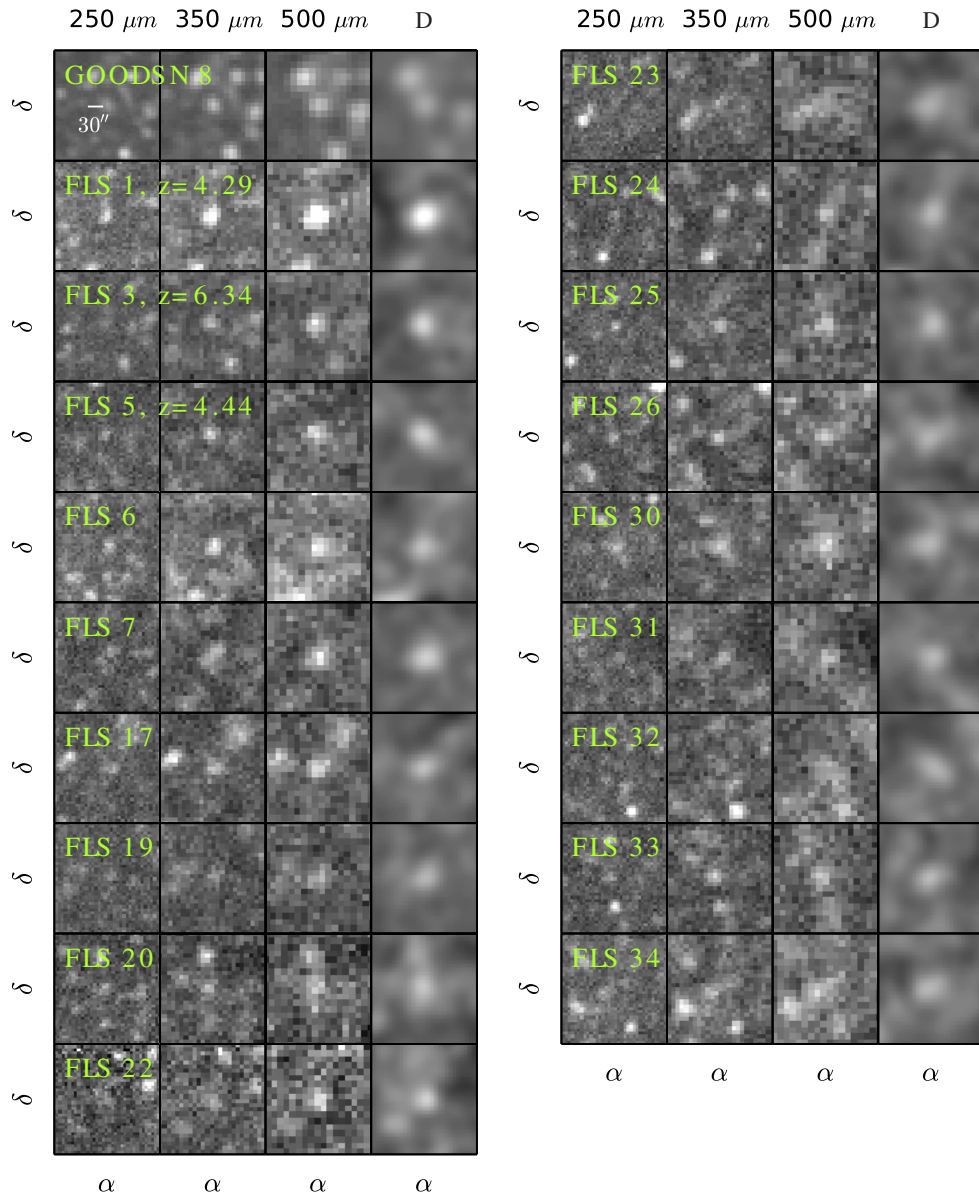


Figure 2. Postage stamps of all of the GOODS-N and FLS sources in our catalog. The grayscale range for each cutout is -35 to $+50$ mJy. Sources with secure spectroscopic redshifts are noted. For explanation of the “D” image, see Section 2.2.

(A color version of this figure is available in the online journal.)

catalogs of these fields contain ~ 1400 non-red sources with $S_{500\mu\text{m}} > 30$ mJy. Based on their flux densities, pre-existing lensing models for the DSFG population predict that most of our sources should not be significantly lensed (e.g., Negrello et al. 2007; Wardlow et al. 2013). However, these models were developed for lower- z DSFGs, so this will have to be tested against future interferometric observations. Cutouts of all of the sources in our final catalog are shown in Figures 2 and 3.

2.4. Screening against Synchrotron Sources

Since bright synchrotron-emitting galaxies may have far-IR spectra consistent with our selection criteria at modest (≤ 1) redshifts, we screen against such objects by searching for bright (> 1 mJy) radio counterparts. We used the NVSS and FIRST 21 cm catalogs (Becker et al. 1995; Condon et al. 1998), which cover our fields, and found one such radio-bright source coincident with a SPIRE source in our sample: LSW 25. This turns out to be a known BL Lac object at a redshift

of $z = 0.83$ (Richards et al. 2009), and we exclude it from all further analysis. Another SPIRE source, LSW 48, lies $21''$ away from a radio source with a 21 cm flux density of 2.8 mJy; given the typical positional accuracy, this is unlikely to be due to the same source, so we retain LSW 48 in our sample. FLS 3 and GOODSN 8 have significantly deeper 21 cm observations (see Section 4.4). For the remaining sources we provide the catalog detection limit at that position in Table 2. Four more of our targets are covered by deeper, narrower observations at 19–20 cm, which are presented in Section 4.4. Other than LSW 25, the radio flux densities of all our sources are faint enough to be consistent with the FIR/radio correlation seen for star-forming galaxies at $z \simeq 4$ (Ivion et al. 2010), implying that they are dust-emission dominated.

3. BASIC OBSERVED FAR-IR SOURCE PROPERTIES

For each source, we fit a modified blackbody spectrum to the three SPIRE flux densities, with the primary goal of

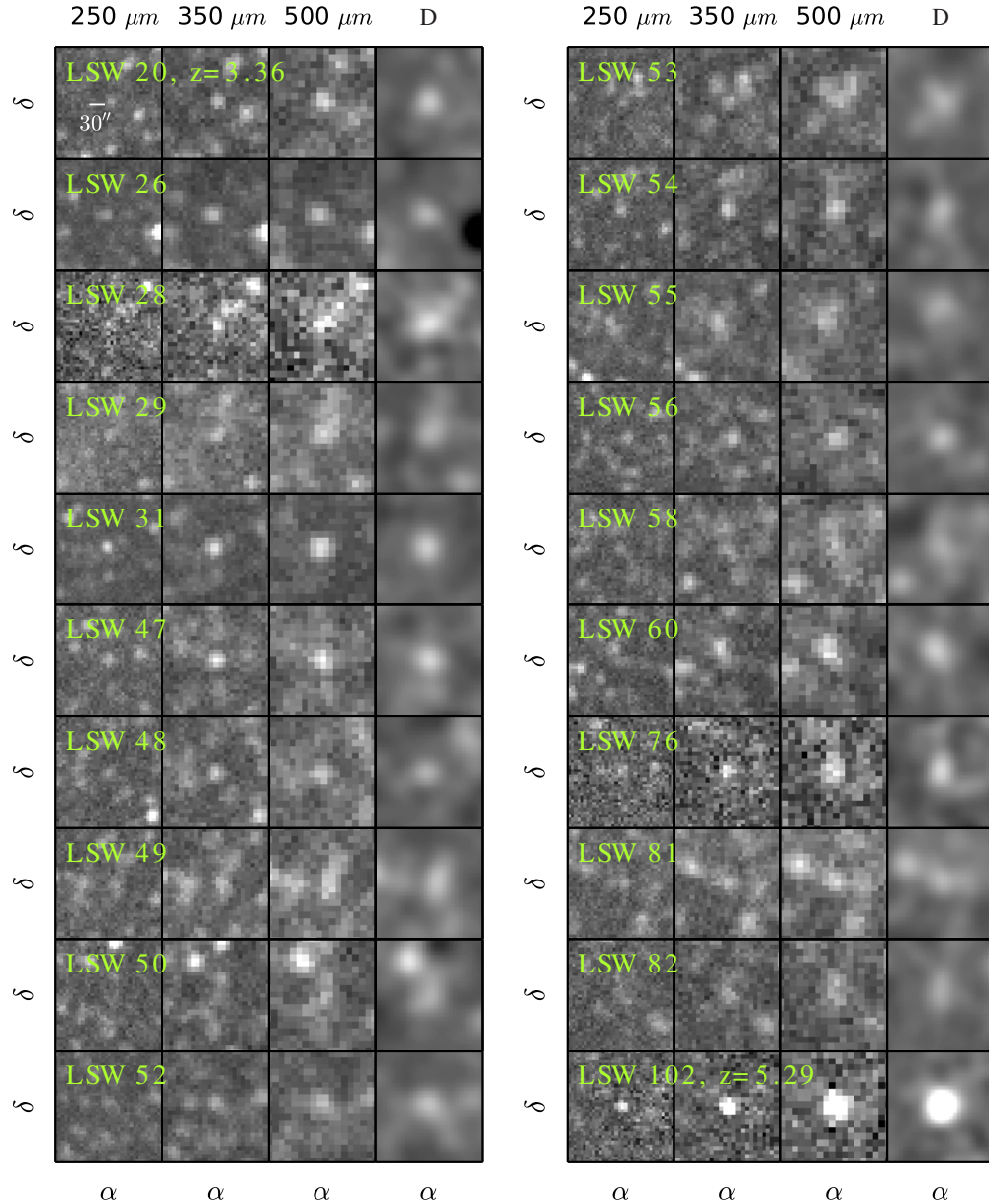


Figure 3. Postage stamps of all of the LSW sources in our catalog. The grayscale range for each cutout is -35 to $+50$ mJy. Sources with secure spectroscopic redshifts are noted. For explanation of the “D” image, see Section 2.2.

(A color version of this figure is available in the online journal.)

determining the wavelength at which the spectrum reaches its maximum. This information is used to estimate the redshift distribution of the population in Section 7.4. Given the small number of SPIRE bands, it is not possible to fully constrain such a model. In such cases it is common in the literature to assume that the emission is optically thin and furthermore to fix the log-slope β of the optical depth curve to some nominal value (≈ 1.5): $S_\nu(\lambda_{\text{obs}}) \propto \lambda_{\text{obs}}^{-\beta} B_\nu(T_d/(1+z))$, where B_ν is the Planck function, T_d the dust temperature, and λ_{obs} the observer frame wavelength. (Note that, as is common in submillimeter/millimeter astronomy, we work in S_ν units but expressed as a function of wavelength.)

In this paper we instead use the slightly more general formalism of an optically thick modified blackbody:

$$S_\nu(\lambda_{\text{obs}}) = \Omega(1 - \exp[-(\lambda_0(1+z)/\lambda_{\text{obs}})^\beta]) \times B_\nu(\lambda_{\text{obs}}; T_d/(1+z)), \quad (3)$$

where λ_0 is the (rest-frame) wavelength where the optical depth reaches unity and Ω is the solid angle subtended by the source. To the blue side of this relation we attach a power law $S_\nu \propto \lambda^\alpha$, joining the two by requiring the SED and first derivative to be continuous. We fit this model to the data using an affine-invariant Markov Chain Monte-Carlo (MCMC) approach, as discussed in the Appendix. In the current section, where we only analyze SPIRE photometry, we marginalize over broad priors in the less well constrained model parameters rather than fixing them. Later, for sources where more photometry is available (Section 4.7) we remove these priors. In all cases in this paper, α is poorly constrained, with the fits only providing a lower limit. Because of the way the blue-side power law is joined to the modified blackbody portion of the SED (requiring that the first derivatives match), this simply amounts to a statement that the merge point between the power law and the thermal SED lies at wavelengths lower than the shortest wavelength photometry point ($250 \mu\text{m}$). That is, in all cases, the quality of our fits is

not improved by the addition of the Wien-side power law, and, while formally included, α is effectively not a parameter of our fits.

Due to the poor constraints possible with only SPIRE data, we marginalize over broad Gaussian priors in β and $\lambda_0(1+z)$. There is relatively little guidance in the literature for the appropriate value for λ_0 , although $100\ \mu\text{m}$ has been adopted in some studies. In general, both *Herschel* and longer λ observations are required to constrain λ_0 , and hence it has been measured for relatively few sources. In order to determine an appropriate prior, we have applied this same model to literature sources with a sufficient quantity of high quality photometry such as Arp 220 (Rangwala et al. 2011), LSW 1 (Conley et al. 2011), the Cosmic Eyelash (Swinbank et al. 2010), FLS 3 (Riechers et al. 2013), XMM 1 (Fu et al. 2013), ID 141 (Cox et al. 2011), as well as three of the red sources presented in this paper (Section 4.7). We conclude that, with the exception of FLS 3, all sources are significantly better fit by an optically thick model rather than an optically thin one, with $\Delta\chi^2$ values of >6 , and that λ_0 ranges from 190 to $270\ \mu\text{m}$ (rest frame). If our sources have a typical redshift of 4.5 ± 1 , this corresponds to a Gaussian prior on $\lambda_0(1+z)$ of $1100 \pm 400\ \mu\text{m}$, which we adopt (truncating the prior to exclude negative values). We further assume a Gaussian prior on β of 1.8 ± 0.3 (Draine 2006). β is typically believed to be below 2, but examples of larger values are known (e.g., Schwartz 1982), so we do not set a hard upper limit in our analysis.

We use the SCAT v21 catalog flux densities where available, and otherwise the smoothed map fluxes (Table 2). In addition to the instrumental uncertainties in the catalog fluxes (typically 2–3 mJy), we include 4% grayscale calibration uncertainty, a 1.5% per-band uncorrelated calibration uncertainty (Bendo et al. 2013), and confusion noise due to the modest SPIRE resolution. We estimate the covariance matrix of the latter using simulations based on the B11 model, (slightly) scaled to match the observed confusion noise (Nguyen et al. 2010). Note that we use a different confusion noise covariance matrix for fluxes derived from the un-smoothed and smoothed maps (SCAT versus map based)—in the latter case the confusion noise is larger. However, in either case, as the confusion noise and calibration uncertainties are highly correlated among the bands, they have relatively little effect on estimates of the peak wavelength and temperature. It is clear that longer-wavelength observations ($\lambda = 750\text{--}2000\ \mu\text{m}$) would significantly improve our SED constraints.

The fit results are given in Table 3. For most of our sources, the SPIRE data are well fit by a single temperature modified blackbody, with the possible exception of FLS 31. Histograms of $T_d/(1+z)$ and λ_{max} (the observer frame peak wavelength of S_ν estimated from our SED fits)⁴⁰ are shown in Figure 4. These central values are relatively insensitive to the exact form of the priors, although λ_{max} is less sensitive than $T_d/(1+z)$. For example, if we change the β prior to 1.5 ± 0.3 , λ_{max} changes by $<1\%$ and $T_d/(1+z)$ increases by about 5%. L_{IR} , however, is fairly sensitive to the β prior (in the absence of additional photometry and assuming a fixed z). The results are even less sensitive to the λ_0 prior, particularly λ_{max} , although if we adopt an optically thin model ($\lambda_0 \rightarrow 0$), $T_d/(1+z)$ drops by about 15%.

FLS 3 ($z = 6.3$) is one of the reddest sources, but there are others as red in our sample. Some of the sources have

⁴⁰ Note that in an optically thick modified blackbody model $\lambda_{\text{max}} \propto (1+z)/T_d$, even if all other parameters are fixed.

Table 3
Quantities Derived from the SPIRE Observations

Source	$T_d/(1+z)$ (K)	λ_{max} (μm)	$L_{\text{IR}} (z = 4.7)^a$ ($10^{12} L_\odot$)	χ^2	ϵ^b
GOODSN 8	11.3 ± 3.0	433 ± 83	37 ± 20	0.08	0.51 ± 0.17
FLS 1	10.8 ± 0.8	440 ± 21	Section 4.7	0.02	0.68 ± 0.08
FLS 3	8.1 ± 1.2	550 ± 56	...	0.02	0.88 ± 0.04
FLS 5	10.3 ± 1.2	452 ± 37	Section 4.7	0.12	0.57 ± 0.08
FLS 6	11.4 ± 2.6	423 ± 68	57 ± 26	0.09	0.57 ± 0.12
FLS 17	9.9 ± 1.9	466 ± 50	40 ± 15	0.05	0.63 ± 0.13
FLS 19	7.2 ± 3.3	558 ± 117	24^{+14}_{-11}	0.05	0.62 ± 0.15
FLS 20	8.3 ± 3.5	507 ± 87	44^{+25}_{-21}	0.08	0.58 ± 0.18
FLS 22	9.6 ± 1.4	479 ± 49	24 ± 7	0.45	0.50 ± 0.18
FLS 24	9.9 ± 1.6	463 ± 53	24 ± 7	0.21	0.51 ± 0.17
FLS 25	10.6 ± 3.0	436 ± 60	50^{+31}_{-23}	0.15	0.34 ± 0.11
FLS 26	11.1 ± 2.6	437 ± 75	37 ± 18	0.02	0.47 ± 0.13
FLS 30	9.6 ± 3.8	475 ± 108	69^{+54}_{-42}	0.11	0.48 ± 0.15
FLS 31	10.7 ± 2.3	442 ± 68	30^{+11}_{-13}	1.88	0.56 ± 0.13
FLS 32	6.7 ± 3.0	588 ± 122	28 ± 13	0.07	0.52 ± 0.12
FLS 33	10.5 ± 1.0	444 ± 43	34 ± 9	0.01	0.43 ± 0.13
FLS 34	9.2 ± 1.5	494 ± 55	26 ± 8	0.02	0.60 ± 0.09
LSW 20	9.3 ± 1.3	490 ± 49	Section 4.7	0.03	0.68 ± 0.08
LSW 26	11.5 ± 1.7	406 ± 40	30^{+7}_{-10}	0.64	0.38 ± 0.12
LSW 29	11.1 ± 1.4	432 ± 37	43 ± 13	0.12	0.59 ± 0.09
LSW 31	10.6 ± 2.5	450 ± 73	57 ± 28	0.04	0.61 ± 0.09
LSW 47	11.6 ± 2.0	412 ± 50	49^{+15}_{-19}	0.21	0.53 ± 0.12
LSW 48	10.7 ± 1.4	434 ± 38	31 ± 8	0.53	0.37 ± 0.09
LSW 49	10.6 ± 1.1	440 ± 43	32 ± 10	0.02	0.45 ± 0.15
LSW 50	8.1 ± 2.5	541 ± 102	26^{+8}_{-11}	0.34	0.58 ± 0.11
LSW 52	9.1 ± 1.5	495 ± 54	25 ± 6	0.02	0.59 ± 0.09
LSW 53	9.7 ± 1.8	470 ± 59	23^{+6}_{-8}	0.05	0.27 ± 0.13
LSW 54	11.4 ± 2.2	413 ± 44	55^{+30}_{-22}	0.16	0.46 ± 0.14
LSW 55	10.3 ± 3.0	455 ± 90	32 ± 15	0.17	0.46 ± 0.07
LSW 56	10.5 ± 1.8	443 ± 46	40 ± 14	0.06	0.62 ± 0.04
LSW 58	9.5 ± 1.8	483 ± 63	24 ± 7	0.01	0.45 ± 0.17
LSW 60	11.8 ± 2.3	410 ± 59	48^{+18}_{-21}	0.05	0.52 ± 0.14
LSW 76	11.5 ± 2.1	421 ± 54	56^{+17}_{-22}	0.04	0.57 ± 0.12
LSW 81	11.4 ± 1.6	414 ± 35	39 ± 13	0.06	0.42 ± 0.10
LSW 82	9.8 ± 1.4	471 ± 51	26 ± 7	0.43	0.40 ± 0.08
LSW 28	10.5 ± 1.1	448 ± 32	42 ± 9	0.02	...
LSW 102	8.7 ± 0.8	476 ± 18	75 ± 9	1.02	...

Notes. The dust temperature, wavelength at which S_ν peaks (observer frame), L_{IR} , and χ^2 values are from modified blackbody fits to the SPIRE photometry of our sources, as detailed in Section 3. The effective number of degrees of freedom for the χ^2 values is one. The uncertainties are the 68.3% confidence limits, which are quite non-Gaussian for some sources. Known blended sources (FLS 7 and FLS 23) are not included because their intrinsic flux densities are not known.

^a Inferred 8–1000 μm (rest frame) infrared luminosity, assuming $z = 4.7$ (Section 7.4). These values assume no lensing. L_{IR} for FLS 3 is discussed in Riechers et al. (2013).

^b Selection efficiency (see Section 5.1).

millimeter-wave follow-up (see Section 4). We can use this to check whether our priors were reasonable by using our model to predict these flux densities and comparing them with observations, and by comparing the predicted λ_{max} from SPIRE data to that measured when the peak is better constrained by

Table 4
Additional Follow-up

Source	Optical	Z-Spec		Bolocam	SMA	PdBI	Radio			
		$S_{1016\mu\text{m}}$	$S_{1113\mu\text{m}}$					$S_{1210\mu\text{m}}$	$S_{1311\mu\text{m}}$	$S_{1411\mu\text{m}}$
FLS 1	✓	34.1 ± 0.7	28.3 ± 0.7	21.8 ± 0.5	15.0 ± 0.6	12.1 ± 0.8	...	13.8 ± 0.8	14.5 ± 0.9	✓
FLS 5		20.3 ± 0.7	16.6 ± 0.5	12.5 ± 0.6	11.4 ± 0.6	9.5 ± 0.7	...	17.2 ± 1.1	...	✓
LSW 20	✓	16.8 ± 1.1	14.9 ± 0.8	12.0 ± 0.8	7.0 ± 0.9	7.2 ± 1.1	...	18.4 ± 1.3	8.7 ± 1.8	✓
FLS 6		8.4 ± 0.6	
FLS 17		1.5 ± 0.4	
FLS 19		9.1 ± 0.8	
LSW 29		8.4 ± 1.9	
LSW 48		13.0 ± 2.4	
LSW 52		7.5 ± 1.6	

Notes. Additional observations for our sources. The optical spectroscopy and radio observations are discussed in Sections 4.5 and 4.4, respectively. The millimeter-band flux densities are given in mJy, and only instrumental noise is included in the quoted uncertainties. Observations of FLS 3 are described in Riechers et al. (2013). Sources in the top portion of the table have known redshifts. The SMA flux density for LSW 20 is the sum of the two components, but for PdBI is only for the brighter of the two components. The Z-Spec flux densities are binned into five equal sized bins in wavelength.

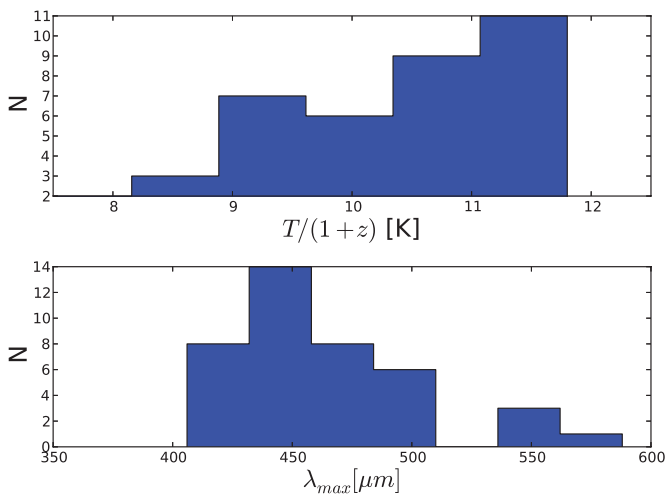


Figure 4. Results of the modified blackbody fits to the SPIRE photometry of our sources. The top panel shows the measured $T_d / (1+z)$ distribution, and the bottom panel the observer-frame wavelength at which S_ν peaks. (A color version of this figure is available in the online journal.)

adding millimeter-data. With the exception of FLS 17, which is significantly fainter than predicted at 1.3 mm, we find that this model does a good job predicting the millimeter-fluxes and λ_{max} , albeit with large (10%–25%) uncertainties. For example, for FLS 5 λ_{max} (SPIRE) = $452 \pm 37 \mu\text{m}$, while the value measured with the addition of millimeter data is $445 \pm 20 \mu\text{m}$. For FLS 3 the values are $550 \pm 86 \mu\text{m}$ and $537 \pm 22 \mu\text{m}$; the modest improvement in the precision on λ_{max} when millimeter-data are added is because of the additional priors applied to the SPIRE-only fits.

4. FOLLOW-UP OBSERVATIONS

We are carrying out a multi-wavelength follow-up program of these sources. By design, the SPIRE data only sample the blue side of the thermal SED well, and so longer-wavelength submillimeter/millimeter observations are particularly critical. They are used to determine whether our sources do, in fact have thermal SEDs, and constrain their total IR luminosity, dust mass, etc. In addition, millimeter-wave line searches can be used to measure redshifts and model molecular gas excitation properties, and high-resolution interferometric observations can

be used to identify counterparts at other wavelengths and to study source morphologies (e.g., Riechers et al. 2013).

In this section we describe the relevant observations of the targets for this paper (Table 4), concentrating on the millimeter-band and radio continuum flux densities and redshifts. Other details, such as precise positions, morphologies, and line ratios, will be presented elsewhere. Four of our sources (FLS 1, FLS 3, FLS 5, and LSW 20) have submillimeter/millimeter observations and known redshifts from Plateau de Bure Interferometer (PdBI), Submillimeter Array (SMA), Z-Spec, and CARMA, as described below. FLS 3 ($z = 6.34$) has particularly extensive follow-up, which is described elsewhere (Riechers et al. 2013). How the sources with redshifts relate to the rest of the catalog sources presented here, as well as to 500 μm risers selected from the literature by other means, is shown in Figure 5.

4.1. Pre-existing Multi-wavelength Observations

All of the HerMES fields have deep ancillary data partially covering the SPIRE maps, and the majority of our sources have *Spitzer* observations from 3.5 to 160 μm . However, counterpart identification is found to be challenging for our galaxy sample due to the relatively large SPIRE beam, the expected faintness of our sources at other wavelengths compared with the depth of the available observations, and the large number of potential counterparts in the 3.5–8 μm bands. While it would be tempting to simply assume that the brightest or closest *Spitzer* 24 μm source in the vicinity of each candidate, if there is one, is the correct match, it is difficult to justify—or check—this assumption without additional data. Therefore, we postpone discussion of the near- and mid-IR counterparts of our sources for a later publication, by which time the number of sources with precise interferometric positions will have increased.

4.2. Millimeter Single-dish Observations: Z-Spec and Bolocam

Four of the sources in our final catalog were observed with Z-Spec on the Caltech Submillimeter Observatory (CSO) in 2010 March–May during favorable conditions ($\tau_{225\text{GHz}}(\text{zenith}) = 0.05\text{--}0.11$): FLS 1, FLS 3, FLS 5, and LSW 20. Z-Spec is an $R \approx 250$ grating spectrometer covering the full spectral range from $\lambda = 0.97$ to 1.58 mm (Earle et al. 2006), with a beam FWHM ranging from 25'' to 33'' over the band. All of the sources were detected, with 1.1 mm continuum flux densities of 10–30 mJy. The spectra for FLS 1, FLS 3, FLS 5, and LSW 20 are shown in Figure 6 and Table 4. We performed a search for

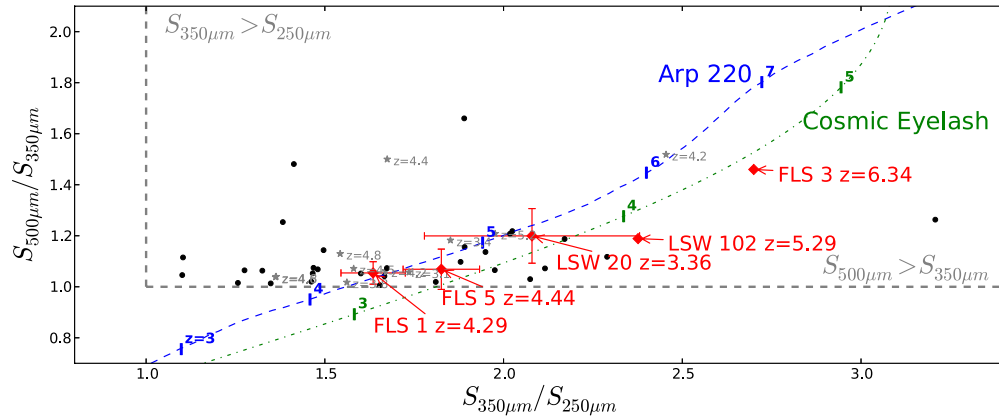


Figure 5. SPIRE color ratios for sources presented in this paper (black dots). The sources with redshifts are shown as red diamonds. For comparison, 500 μm riser sources with redshifts selected via other methods (i.e., not on the basis of their SPIRE colors) are shown as gray stars (see Section 6). SED tracks based on Arp 220 and the Cosmic Eyelash (Swinbank et al. 2010) are shown for comparison. Their gray dashed lines represent our selection in color space. Note that the uncertainties vary considerably, and are quite large for some of the sources. Example uncertainties are shown for FLS 1, 5, and LSW 20.

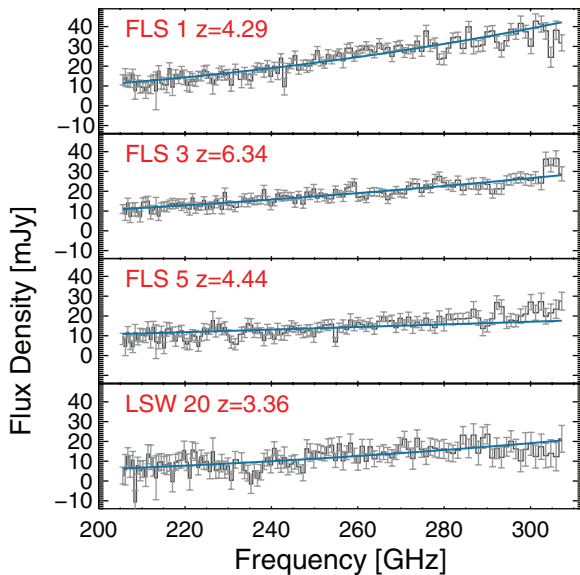


Figure 6. Z-Spec observations of our sources. All four have known redshifts from either CARMA or Keck as described in the text. Line searches in these data will be discussed in D. A. Riechers et al. (2014, in preparation).

lines in these spectra using the redshift search algorithm detailed in Lupu et al. (2012), but did not detect any features at greater than 3σ . These spectra are analyzed further by D. A. Riechers et al. (2014, in preparation).

Two of our targets, LSW 48 and LSW 52, were observed with Bolocam at 1.1 mm in 2012 December under excellent conditions ($\tau_{225\text{ GHz}}(\text{zenith}) = 0.03\text{--}0.06$) using a Lissajous scan pattern. Bolocam is a facility 144-element bolometer camera at the CSO that can operate at either 1.1 or 2.1 mm (Glenn et al. 2003). The beam FWHM at 1.1 mm is $31''$, and the fractional bandwidth is 0.17. The total integration time for LSW 48 was 2.0 hr, and for LSW 52 was 4.3 hr. The reduction procedures are as described in Wu et al. (2012). Both sources were detected, and are unresolved by the Bolocam beam.

4.3. Submillimeter/Millimeter Interferometric Continuum Observations: SMA and PdBI

Four sources (FLS 1, FLS 3, FLS 5, and LSW 20) were observed with the SMA at $\lambda = 1.1$ mm using a combination of

compact, sub-compact, and extended configurations. Similarly, nine of our targets (FLS 1, FLS 3, FLS 6, FLS 17, FLS 19, LSW 20, LSW 28, LSW 29, and LSW 102) were observed with the PdBI at ~ 1.3 mm. In the majority of the cases—including all five with redshifts—the large millimeter-wave fluxes are confirmed, and in most cases the emission at $3''$ resolution is dominated by a single spatial component. Further details of these observations, including source morphologies and more precise interferometric positions, will be presented by D. L. Clements et al. (2014, in preparation) and I. Perez-Fournon et al. (in preparation), respectively.

The SMA and PdBI detections allow us to measure the positional accuracy of our SPIRE detections. For those sources—which tend to be the brighter members in the sample—the median separation of the interferometric source and the centroid of the source in the SPIRE difference map is $5''.1$. For sources which are isolated and clearly detected in the 250 or 350 μm bands, a significantly better SPIRE position can be derived by using those images alone. For fainter and blended sources, the positional accuracy is probably somewhat worse.

The SMA and PdBI flux densities of eight of our sources were measured from Gaussian fits in the uv -plane, and are given in Table 4; final flux densities for the other sources are awaiting the completion of all scheduled observations. LSW 20 is resolved into two sources with a separation of $\sim 3''.8$ by the SMA observations (also see Section 4.5). Because the SPIRE and Z-Spec beams are much larger than this ($>18''$), we add the flux densities of the two components for our analysis. The PdBI observations of this source also show indications of a faint component at the same position, but the flux density is poorly constrained. Combined with the Z-Spec and Bolocam observations, we can see that, with the exception of FLS 17, our targets are among the strongest known optically faint dusty galaxies at $\lambda \approx 1$ mm that are not known to be significantly lensed.

4.4. Radio Continuum Observations

FLS 3 was the subject of deep targeted Jansky Very Large Array (JVLA) and follow-up at 21 cm once its redshift was determined (Riechers et al. 2013). A radio source is detected at 6σ in the deep Morrison et al. (2010) JVLA survey of GOODS-N close to the position of GOODS-N 8. There are no other detected sources within $15''$. However, without a precise

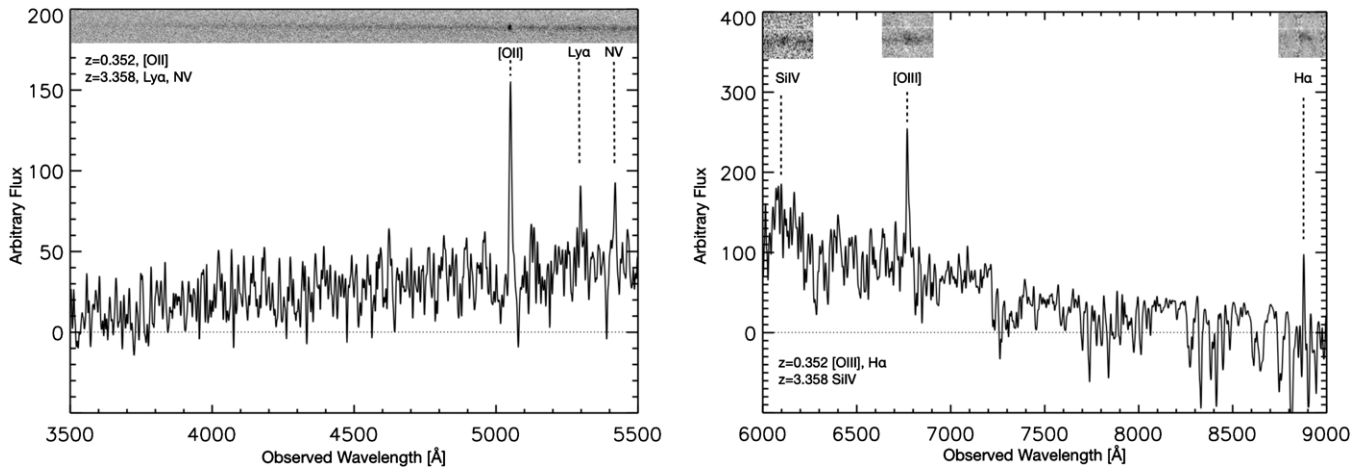


Figure 7. Blue (left) and red (right) Keck/LRIS spectra of LSW 20. Two sources are detected in multiple lines—a $z = 0.352$ foreground source, and a background $z = 3.358$ source. The CO redshift of the DSFG is $z = 3.32$.

submillimeter/millimeter interferometric position for this source (unlike FLS 3), we are unable to determine if this is, in fact, a radio detection of our source. LSW 26, which lies within the region covered by the deep Owen & Morrison (2008) 20 cm survey of the Lockman Hole, is not detected in those data, but without knowing the source size the exact detection limit is uncertain.

Enhanced Multi-Element Radio Linked Interferometer Network (e-MERLIN) observations of four of the sources in this paper (FLS 1, FLS 3, FLS 5, and LSW 20) were carried out in 2012 March. A central tuning of 1.55 GHz with an instantaneous bandwidth of 348 MHz was used. All seven stations were available, resulting in a $0''.3$ synthesized beam. 3C286 was used as the primary flux calibrator and OQ208 was used as the band-pass calibrator. The sources were observed for 6 hr each from 26th–30th of 2011 March. The data were flagged spectrally, averaged in frequency, fringe fitted and then calibrated using standard methods for phase referencing experiments. However, none of the sources were detected, with map rms value of 15–18 μJy .

We can compare these observations with those predicted by the far-IR/radio correlation, which is parameterized by q_{IR} , the logarithmic ratio of L_{IR} and the 1.4 GHz flux density. The lack of redshifts, as well as the poor constraints on L_{IR} in the absence of Rayleigh–Jeans-side (longer- λ) data (Table 3), make this comparison uninformative for GOODSN 8 and LSW 26. For the other sources, if we assume $S_{\nu} \propto \nu^{-0.8}$ in the radio, and adopt the value for q_{IR} measured for $z \sim 2$ Herschel-selected DSFGs from Ivison et al. (2010), we can predict the range of expected $S_{1.55\text{GHz}}$ flux densities for comparison with our detection limits. Including the scatter in q_{IR} and the measurement uncertainties in each L_{IR} , we predict 95% central confidence limits of 50–324, 15–94, 21–151, and 15–116 μJy for FLS 1, FLS 3, FLS 5, and LSW 20, respectively. The non-detections of FLS 3, FLS 5 and LSW 20 are consistent with the far-IR/radio correlation, while FLS 1 is fainter in the radio than expected at moderate significance. However, the e-MERLIN non-detection of FLS 3 also disagrees with the JVLA 1.4 GHz measurement ($S_{1.4\text{GHz}} = (59 \pm 11) \mu\text{Jy}$), which is consistent with the far-IR/radio correlation (Riechers et al. 2013). This discrepancy suggests that e-MERLIN may be partially resolving out the radio emission for these sources.

4.5. Optical Spectroscopy: Keck and GTC

In addition to the submillimeter through radio observations, FLS 1 and LSW 20 were targeted for optical spectroscopy in 2010 July and 2011 May using the Low Resolution Imaging Spectrograph (LRIS; Oke et al. 1995) on the Keck I 10 m telescope, making use of their high-precision SMA interferometric positions. We utilized a $1''$ slit width, and the D560 dichroic with the 4000 Å, 600 line mm^{-1} grism (blue side) and 400 line mm^{-1} grating (red side) blazed at ~ 7800 Å. The data were binned (1×2) in the spectral direction on the blue side and unbinned on the red, providing similar wavelength dispersions of 1.26 and 1.16 Å per pixel, respectively. The targets were observed with median seeing of $\sim 1''.0$, with a total integration time of 2.2 and 1.2 hr, respectively. The LRIS data were reduced using standard IRAF procedures. No continuum or emission lines were detected toward the SMA position for FLS 1. However, spectroscopy of LSW 20 (Figure 7) reveals multiple emission lines from both a foreground $z = 0.352$ and high redshift $z = 3.358$ galaxy, both toward the brighter component in the SMA image. No continuum or emission lines were detected from the fainter SMA component. This possible lensing system will be discussed further elsewhere. FLS 3 was also observed with LRIS, as discussed in Riechers et al. (2013).

Optical spectroscopic observations of FLS 1 were also carried out on 2013 May 16 (UT) using the Optical System for Imaging and low Resolution Integrated Spectroscopy (OSIRIS)⁴¹ on the Gran Telescopio Canarias (GTC) 10.4 m telescope. Observing conditions were photometric, with a median seeing of $0''.75$, and the total integration time was 1.5 hr. We utilized a $1''.2$ slit width, and the high throughput R2500R VPH grism, which provides a spectral range of 5630–7540 Å and a wavelength dispersion of 1.04 Å per pixel. The slit was positioned at an angle of $343^\circ.5$ including a faint optical object close to the radio interferometric position and a faint galaxy at 1 arcmin to the NW. No continuum or emission lines were detected close to the FLS 1 position. However, faint continuum and emission lines were detected at R.A. $17^{\text{h}}08^{\text{m}}15^{\text{s}}.727$, decl. $+58^{\text{d}}29^{\text{m}}29^{\text{s}}.35$, about $52''$ from FLS 1 and $8''$ from the galaxy used to position the slit. Careful analysis of the two-dimensional spectrum at this position reveals emission lines ($\text{H}\beta$ and $[\text{O III}]$ 4959, 5007 Å) from a low redshift galaxy at $z = 0.415$ and a narrow line at

⁴¹ <http://www.gtc.iac.es/instruments/osiris/osiris.php>

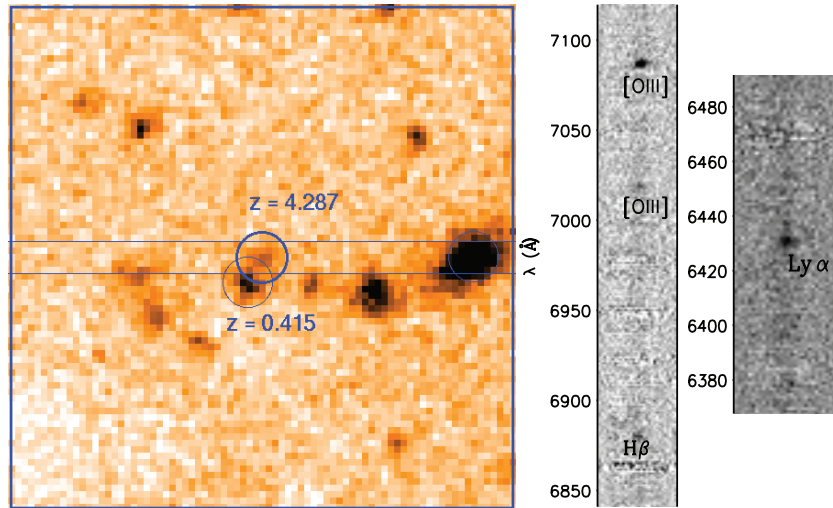


Figure 8. GTC observations of galaxies near FLS 1. The left panel shows a GTC z -band image of the field around a high redshift galaxy discovered during the long-slit observations of FLS 1. The spectra of two galaxies overlap in the long-slit spectrum. The slit is shown by the horizontal lines, and the circled galaxy on the right was used to align the slit. The middle panel shows the two-dimensional GTC OSIRIS spectrum of the $z = 0.415$ galaxy showing emission lines of $H\beta$ and $[O III]$ 4959, 5007 Å, and the right panel the spectrum of the $z = 4.287$ galaxy showing narrow $Ly\alpha$ emission. FLS 1 is $30''$ outside the frame of the z -band image.

(A color version of this figure is available in the online journal.)

6430 Å which we identify as $Ly\alpha$ at $z = 4.287$ (Figure 8), very close to the CO redshift of FLS 1 ($z = 4.286$; see below). The serendipitous detection of a galaxy at the same redshift as FLS 1 in a narrow long-slit is highly improbable unless there is an overdensity of galaxies close to FLS 1 as detected around other high redshift submillimeter galaxies (SMGs; e.g., Capak et al. 2011). The GTC observations will be presented in more detail elsewhere.

4.6. CARMA Millimeter-Wavelength Line Search

Five of our sources have been observed with CARMA with the main goal of redshift detection. These observations are described by D. A. Riechers et al. (2014, in preparation). The redshift for LSW 20 has been confirmed with a CO line; the measured CO value is $z = 3.32$, corresponding to a relative velocity of 2600 km s^{-1} in the source frame with respect to the optical redshift. The source of this discrepancy is currently not clear. FLS 1 has a redshift of 4.29 based on two CO lines. FLS 3 has a redshift of 6.34 based on multiple emission lines (Riechers et al. 2013). FLS 5 has a redshift of 4.44 based on multiple CO lines, and LSW 102 has a redshift of 5.29 based on clear detections of CO $J(6-5)$, $(5-4)$, and $[N II]$ 205 μm . The uncertainties in these redshifts are negligible for the purposes of this paper.

4.7. Fits to SPIRE Plus Submillimeter/Millimeter Photometry

Here we present modified blackbody fits to FLS 1, FLS 5, and LSW 20, all of which have known redshifts and millimeter-band observations to constrain the red side of the thermal SED. We use the same MCMC code as described in Section 3 and the Appendix, but omit the priors on β and λ_0 . A similar analysis for FLS 3 is presented by Riechers et al. (2013). The millimeter-band observations of LSW 102 are ongoing. We use the results to constrain the dust temperature, far-IR luminosity (and hence star-formation rate), and dust mass for these sources. The calibration uncertainties and confusion noise are handled as previously for SPIRE data. In addition, we assume 10% calibration uncertainties for SMA, PdBI, and Z-Spec that are uncorrelated between observatories, but are perfectly correlated between the Z-Spec channels. Given the high resolution of

the interferometric observations, we do not include confusion noise for the SMA or PdBI observations, since it is negligible compared with the other uncertainties. We expand our estimates of the correlation in the confusion noise to the binned Z-Spec channels using the same simulations as for the SPIRE bands. The Z-Spec and SMA 1.1 mm flux densities for FLS 1 disagree significantly. We have been unable to determine why this is the case, but given the good agreement for this source between the Z-Spec and PdBI 1.3 mm observations, we do not use the SMA observations for this source. As noted in Section 3, the blue-side power law (λ^α), does not improve our fits.

In addition to the SED parameters, we measure L_{IR} (the integrated IR luminosity between 8 and 1000 μm in the rest frame), and the dust mass, M_d . For these calculations, and elsewhere in this paper, we assume a flat universe and a cosmological constant with $\Omega_m = 0.27$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The dust mass is estimated using

$$M_d = S_\nu D_L^2 [(1+z)\kappa_\nu B_\nu]^{-1} \tau_\nu [1 - \exp(-\tau_\nu)]^{-1},$$

where S_ν is the flux density, D_L the luminosity distance, κ_ν the mass absorption coefficient, τ_ν the optical depth, and B_ν the Planck function, with all quantities expressed in the observer frame. For the mass absorption coefficient we adopt $\kappa_\nu = 2.64 \text{ m}^2 \text{ kg}^{-1}$ at 125 μm (rest frame; Dunne et al. 2003). Our quoted uncertainties on M_d do not include the uncertainty in κ_ν , which is at least a factor of 0.3 dex. To compute the star formation rate, we use the relation of Kennicutt (1998), which assumes a Salpeter initial mass function. Note that L_{IR} , M_d , and the star formation rate assume no lensing magnification. Lensing constraints from interferometric observations will be described in future papers.

The results of these fits are given in Table 5 and shown in Figure 9. The derived properties of these sources (T_d , β) are fairly typical of the most luminous *Herschel*-selected DSFGs at lower z . The β values are somewhat higher than usual, but consistent, given the uncertainties, with the often assumed value $\beta = 2$. Due to the large uncertainties in β for LSW 20, M_d and the area of emission (A_{em}) are not well constrained, so only

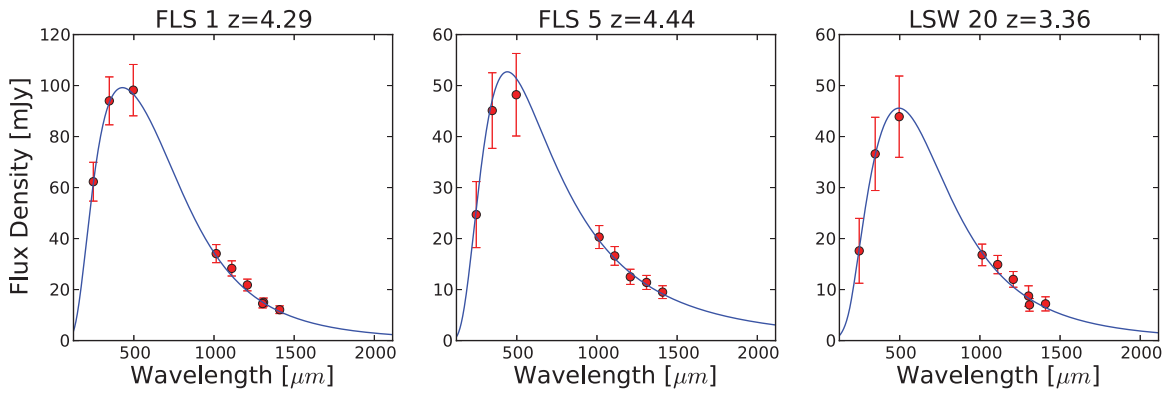


Figure 9. Modified blackbody dust SED fits to sources with known redshifts, as described in Section 4.7. The displayed uncertainties include calibration and confusion noise.

(A color version of this figure is available in the online journal.)

Table 5
Fits to Sources with Known Redshifts

Parameter	Value	Description	Note
FLS 1, $z = 4.29$			
χ^2	4.83	χ^2	5 dof; $P(> \chi^2) = 0.44$
T_d	63^{+3}_{-4} K	Dust temperature	
β	2.8 ± 0.6	Extinction slope	
$f_{500\mu\text{m}}$	91 ± 11 mJy	Normalization at $500 \mu\text{m}$	Observer frame
λ_0	200^{+26}_{-23} μm	λ where $\tau = 1$	Rest frame
α	> 3.6	Blue side power-law slope	68.3% limit
L_{IR}	$5.6^{+0.7}_{-0.9} \times 10^{13} L_{\odot}$	IR luminosity	8–1000 μm (rest frame)
M_d	$5.1^{+1.6}_{-2.4} \times 10^9 M_{\odot}$	Dust mass	
SFR	$9700^{+1200}_{-1600} M_{\odot} \text{yr}^{-1}$	Star formation rate	
A_{em}	$82^{+12}_{-21} \text{kpc}^2$	Dust emission area	
FLS 5, $z = 4.44$			
χ^2	2.5	χ^2	4 dof; $P(> \chi^2) = 0.64$
T_d	59 ± 6 K	Dust temperature	
β	1.7 ± 0.5	Extinction slope	
$f_{500\mu\text{m}}$	47 ± 7 mJy	Normalization at $500 \mu\text{m}$	Observer frame
λ_0	191 ± 62 μm	λ where $\tau = 1$	Rest frame
α	> 3.9	Blue side power-law slope	68.3% limit
L_{IR}	$2.8^{+0.5}_{-0.6} \times 10^{13} L_{\odot}$	IR luminosity	8–1000 μm (rest frame)
M_d	$2.0^{+0.6}_{-0.8} \times 10^9 M_{\odot}$	Dust mass	
SFR	$4800 \pm 900 M_{\odot} \text{yr}^{-1}$	Star formation rate	
A_{em}	$67^{+26}_{-31} \text{kpc}^2$	Dust emission area	
LSW 20, $z = 3.36$			
χ^2	6.0	χ^2	5 dof; $P(> \chi^2) = 0.31$
T_d	48 ± 6 K	Dust temperature	
β	2.8 ± 1.2	Extinction slope	
$f_{500\mu\text{m}}$	41 ± 8 mJy	Normalization at $500 \mu\text{m}$	Observer frame
λ_0	210 ± 59 μm	λ where $\tau = 1$	Rest frame
α	> 3.9	Blue side power-law slope	68.3% limit
L_{IR}	$1.1^{+0.2}_{-0.3} \times 10^{13} L_{\odot}$	IR luminosity	8–1000 μm (rest frame)
M_d	$> 2.0 \times 10^9$ (95%)	Dust mass	
SFR	$1900^{+300}_{-500} M_{\odot} \text{yr}^{-1}$	Star formation rate	
A_{em}	$> 32 \text{kpc}^2$ (95%)	Dust emission area	

Notes. The results of modified blackbody fits to FLS 1, FLS 5, and LSW 20, as detailed in the text. L_{IR} , M_d , A_{em} , and the SFR assume no lensing magnification.

lower limits on these two quantities are provided. The χ^2 values are acceptable for all fits. The fits favor using an optically thick model, with a typical decrease in the χ^2 of about 3 for adding one additional parameter. However, the data are not sufficient to rule out an optically thin model for any of these sources.

The derived L_{IR} values suggest that these sources are among the most luminous IR sources known (assuming no magnification). Unlike FLS 3 (Riechers et al. 2013), where the data is consistent with an optically thin model, the SEDs for all three sources presented here moderately favor becoming optically

thick near $200 \mu\text{m}$ (rest-frame). Therefore, CO excitation modeling of these sources may have to consider extinction.

5. THE NUMBER DENSITY OF RED SPIRE SOURCES

In order to estimate the space density of bright, red SPIRE sources, we must determine both how efficient our selection is at finding red sources and the expected false detection rate. Given the modest number of sources detected, and the large observational uncertainties in the SPIRE colors, we do not attempt to measure the differential number counts as a function of color or flux density, but simply the number of sources per deg^2 . If we denote the efficiency for the detection of the i th source by ϵ_i and the expected purity of our catalog by p (so $1 - p$ is the fraction of the detected sources that do not belong in our sample), then the space density of sources N is

$$N = \frac{p}{A} \sum_i \frac{1}{\epsilon_i}, \quad (4)$$

where A is the area of the survey and the sum is over the sources in our final catalog. We now discuss how we compute ϵ_i and p .

5.1. Efficiency

Our approach for computing the efficiencies is to work as closely as possible with the observables rather than try to compress the information by assuming some SED model and reducing the problem to a smaller number of variables (e.g., assuming an optically thin, fixed β modified blackbody and computing ϵ as a function of T_d and a suitable normalization variable). It is not clear how well the data are described by such simple models, particularly on the blue side of the thermal SED (see, e.g., Blain et al. 2003). Furthermore, even if they were perfectly described in the mean by such a simple model, the degree of intrinsic deviation of individual DSFGs from such models is not well characterized.

Therefore, we measure the efficiency directly using the observed flux density of each source in the SPIRE bands, which should be significantly more accurate than using an SED model. Because our efficiency is a complicated mix of these variables, however, we cannot make any statement that we are complete up to some simply expressible threshold. Thus, while our model should be substantially better than one based on a simple SED model, it is not trivial to visualize how ϵ depends on the SPIRE flux densities.

Therefore, purely for this purpose, we illustrate our selection efficiency for a modified blackbody SED model as a function of temperature and $S_{500 \mu\text{m}}$ in Figure 10, using the approach detailed below. The model is an optically thin modified blackbody coupled with a $nu^{-\alpha}$ power law (on the Wien side), fixing $\beta = 1.5$ and $\alpha = 4$ based on the properties of nearby (hence well observed) IR-luminous galaxies. Note that many of our actual sources are not well fit by these parameters, and so we do not use this model in any way while computing the actual detection efficiencies. This figure does, however, correctly illustrate that the detection efficiency decreases quite rapidly at low flux densities, which is the basis of our selection requirement $S_{500 \mu\text{m}} \geq 30 \text{ mJy}$.

Due to the relatively small number of sources in our catalog, rather than attempt to compute the efficiencies on a grid of the three flux densities (for each field) and then interpolate, it is more efficient to compute them individually for each source. Our basic tool for doing so is, for each source in our catalog,

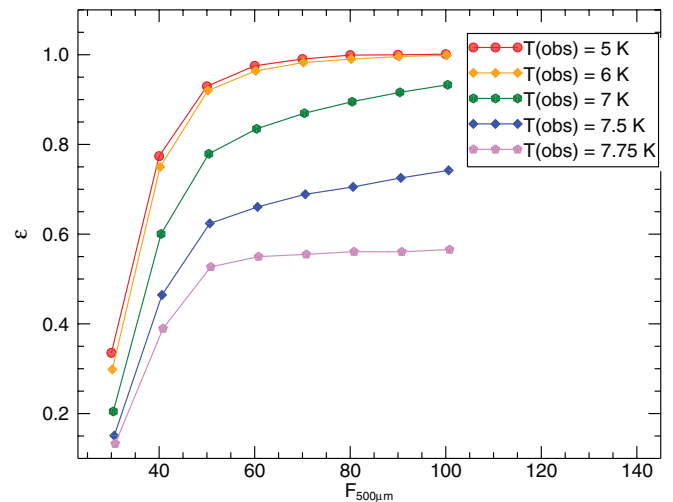


Figure 10. Illustration of our selection efficiency for a simple optically thin modified blackbody (with $\beta = 1.5$) plus blue-side power law model ($S_\nu \propto \nu^{-4}$) as a function of $S_{500 \mu\text{m}}$ and the observer frame dust temperature $T(\text{obs}) = T_d / (1 + z)$. The color ratios are a strong function of temperature, and, for these values of β and α , sources with $T(\text{obs}) > 7.75 \text{ K}$ are not “red.” For sources with $S_{350 \mu\text{m}} \simeq S_{500 \mu\text{m}}$ the selection efficiency is relatively independent of flux density, since the dominant factor is the uncertainty in whether the source actually satisfies $S_{500 \mu\text{m}} \geq S_{350 \mu\text{m}}$ due to instrument and confusion noise. These simulations were carried out for the FLS field. (A color version of this figure is available in the online journal.)

to inject false sources into the actual maps for each field with properties that match the measurements of each source, and then determine how many are recovered using the search pipeline.

An important point is that we do not know the precise flux densities of any source due to observational uncertainties (instrument and confusion noise), and therefore each efficiency has an associated uncertainty which cannot be reduced without additional observations. We include this effect in our simulations by generating a moderate number (N_σ) of flux density triplets for each source drawn from a multi-variate Gaussian centered on the observed flux densities and using the estimated uncertainties. We then carry out N_{sim} simulations for each of the flux density triplets, each of which has N_{src} sources injected, averaging to form N_σ estimates of ϵ for each source. The final ϵ is then the average of the N_σ values, and the uncertainty is given by the distribution of values.

N_σ does not have to be very large to provide a good estimate of the uncertainty, and so we generally adopt a value of $N_\sigma = 60$, except for a few sources where we used $N_\sigma > 1500$ in order to verify convergence. N_{src} is limited by the desire to avoid two sources overlapping within the matching radius, m_{rad} . We have conservatively adopted $m_{\text{rad}} = 15''$, compared with the typical positional uncertainty of $5''$ for our faintest sources in simulations (and from interferometric observations: Section 4.3). With these values, the correction for sources lost due to positional uncertainties are negligible compared with our other uncertainties. We adopt $N_{\text{src}} = 800$ for our FLS simulations, $N_{\text{src}} = 2500$ for those of the combined Lockman fields, and $N_{\text{src}} = 50$ for GOODS-N, which limits the effects of overlap on the recovered counts to less than 1%, again much smaller than our other sources of uncertainty. It is important that $N_{\text{sim}} \times N_{\text{src}}$ is large enough that ϵ is measured for each flux triplet to much better precision than the variation between flux triplets for the same source. We have adopted $N_{\text{sim}} = 60, 30, 800$ for FLS, Lockman, and GOODS-N, respectively, based on tests with much larger N_{sim} values. In total, therefore, the efficiency

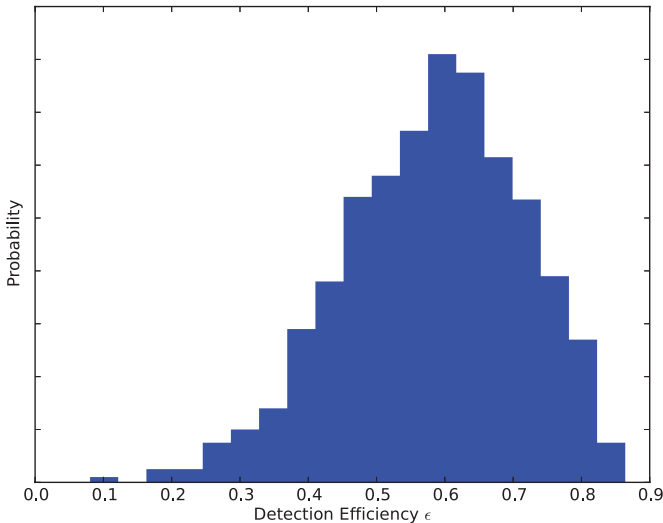


Figure 11. Histogram of efficiencies (ϵ) for FLS 5. Each entry represents a different flux density triplet reflecting the observational (instrumental and confusion) uncertainties. For this source, $N_\sigma = 1500$ simulations were carried out. The resulting efficiency has significant non-Gaussian tails.

(A color version of this figure is available in the online journal.)

for each FLS source is based on 2.4 million injected sources, GOODS-N on 2.4 million, while in Lockman that value is 4.5 million; more sources are desirable for the Lockman fields because the noise properties of the map are less uniform.

The resulting efficiencies and uncertainties are provided in Table 3. They range from $\sim 90\%$ for FLS 3 (the $z = 6.34$ source) to $\sim 20\%$ for faint sources with $S_{500\mu\text{m}} \simeq S_{350\mu\text{m}} \simeq S_{250\mu\text{m}}$. The uncertainties in each ϵ_i are generally non-Gaussian (Figure 11), especially for sources with $S_{500\mu\text{m}} \simeq S_{350\mu\text{m}}$. We use the measured ϵ distribution for each source when computing the source density, as discussed below. Again, note that the uncertainties in the ϵ 's primarily arise from the uncertainties in the flux densities of each source, not from the finite number of simulations we carried out, and hence are irreducible given current observations.

5.2. Purity

There are two classes of contaminants in our analysis: faint red sources below our $S_{500\mu\text{m}} \geq 30$ mJy cut, and non-red sources. The effects of the former are commonly referred to as “boosting” or “Eddington bias” in the submillimeter/millimeter literature, and can be caused by both instrument noise and blending effects, while those of the latter almost entirely arise from instrument noise because blending tends to make sources bluer. The rate of contamination of fainter sources is easy to estimate using the same methods as in Section 5.1, but the second is much more difficult to characterize. False detections caused by map artifacts, evaluated through jack-knife tests on our maps, are negligible.

5.2.1. Boosting

There are two ingredients required to estimate the contamination by red but faint ($S_{500\mu\text{m}} < 30$ mJy) sources: a measurement of the efficiency of detecting such sources; and an estimate of their number density. For the former, we use the same technique as in the previous section to measure the detection efficiency as a function of $S_{500\mu\text{m}}$, omitting the N_σ sampling over photometric errors. Here we must assume SPIRE color ratios. We adopt

the median of our catalog sources, $S_{500\mu\text{m}}/S_{350\mu\text{m}} = 1.09$ and $S_{500\mu\text{m}}/S_{250\mu\text{m}} = 1.88$, and later check to see how changing these values affects our results. The detection efficiency would be essentially zero in the absence of boosting effects, and is a strong function of $S_{500\mu\text{m}}$. We perform a series of simulations, sampling $S_{500\mu\text{m}}$ from 29 to 2 mJy in 1 mJy steps. As expected, the recovery efficiency falls quite rapidly, from 8.9% at $S_{500\mu\text{m}} = 29$ mJy to $< 0.01\%$ at 5 mJy, crossing 1% at 18 mJy. We carry out separate simulations for each field with at least 250,000 sources per mJy bin per field, and find that the values are essentially identical for all fields.

Unfortunately, we do not yet have good measurements of the number counts of red sources, especially at faint flux densities. Our approach is therefore to scale from the observed SPIRE number counts, which are expected to be dominated by sources at lower z . Assuming our source population has $\langle z \rangle = 4.7$ (Section 7.4), a flux cut of $S_{500\mu\text{m}} \geq 30$ mJy corresponds to a cut of $S_{350\mu\text{m}} \geq 61$ mJy at $z = 3$, or $S_{250\mu\text{m}} \geq 140$ mJy at $z = 1.9$. The DSFG population is thought to peak closer to $z = 3$ (Chapman et al. 2005; Weiß et al. 2013), so we adopt the 350 μm counts for our calculations, using the 250 μm value as a comparison to estimate the uncertainty. For these calculations we adopt the differential number counts in each band from Oliver et al. (2010), normalizing them to match the observed number of red sources.

Using the above ingredients, we find an expected boosting contamination of 0.8 sources in FLS, 1.4 in Lockman-SWIRE, and $\ll 1$ in GOODS-N, Lockman-East, and Lockman-North. In all cases these correspond to $\sim 0.1 \text{ deg}^{-2}$, a small value compared to the catalog source density of $> 2 \text{ deg}^{-2}$. Making the simulated sources as red as FLS 3 (our $z = 6.3$ source, and one of the reddest sources in the sample) increases this value by only 0.03 deg^{-2} . Using the 250 μm counts decreases it by 0.02 deg^{-2} , and using the shape of the number counts from the B11 model at $z > 3$ increases it by 0.05 deg^{-2} . We therefore adopt a value for the contamination by faint red sources below our flux density cutoff of $0.11 \pm 0.06 \text{ deg}^{-2}$, which is negligible compared with the other sources of uncertainty.

5.2.2. Non-red Contaminants

The basic tool for our analysis of contamination by non-red sources is again simulations, but here rather than injecting sources into real maps we generate simulated maps based on models of the DSFG population, but with intrinsically red, bright sources omitted, and run our search pipeline on those maps. The most common type of false detections, according to models, are *nearly red* (“orange”) sources combined with noise fluctuations or blended with faint red sources. Therefore, the critical model ingredient is the number of almost-red sources. Unfortunately, it is not clear how well current models represent this population, given that, as discussed later, they generally significantly underpredict the number of truly red sources.

There are a number of such models in the literature. However, as shown by Oliver et al. (2010), Glenn et al. (2010), and Clements et al. (2010), pre-*Herschel* models do a poor job of reproducing the observed number counts at 250–500 μm , and therefore are not a good choice for our simulations. We instead make use of the post-*Herschel* backward-evolution B11 model, which is a good match to current number count constraints. For each field, we generate a number of simulations using this model with genuinely red sources brighter than $S_{500\mu\text{m}} = 3$ mJy removed, adding the measured noise at each position of the map. Simply distributing the sources randomly (i.e., in an unclustered

fashion) will underestimate the false detection rate, so we include clustering using the measured $350\ \mu\text{m}$ power spectrum of Amblard et al. (2011); note that this is purely clustering in the plane of the sky. If “orange” sources are more strongly clustered on the sky, then this may underestimate contamination effects. However, increasing the simulated clustering by a factor of three does not have any measurable effect on our false detection results. We generate 200 simulations of each field, and then run them through the same detection pipeline as the real data, and then count the number of sources detected.

We visually inspect all of our actual catalog sources to note blends. We therefore must carry out the same procedure on at least a subset of our purity simulations. Doing so for 100 simulated maps of each field removes approximately half the detected sources—more precisely 83 out of 145 in FLS, and 174 of 320 in Lockman-SWIRE. These are all blends of sources which can clearly be identified in the un-smoothed maps, and where the individual constituents are too faint to belong in our catalog. This blend rate—2.6 sources for FLS and Lockman-SWIRE combined—is consistent with the observed number (two) in our catalog. The false detection rates for the smaller, deeper fields (Lockman-North, Lockman-East, and GOODS-N) are less than 0.3 per field.

The purity is then given by $p = (N_{\text{cat}} - N_{\text{false}}) / N_{\text{cat}}$, where N_{cat} is the number of sources in our catalog for a given field, and N_{false} is the estimated number of false detections from simulations of the same field. Note that N_{false} is determined much more precisely than N_{cat} , which suffers from Poisson noise. We conclude that the purity of our catalog sample is approximately 90%, somewhat higher in FLS (93%) and somewhat lower in Lockman-SWIRE (91%). Interestingly, increasing the S/N requirement for detection to 5, 6, or 7 does not have much effect on the purity—while increasing the S/N requirement cuts down the number of false sources in simulations, it removes a large fraction of real sources from the actual maps. Some of the false detections, due to unresolved blends, are as bright as 80 mJy at $500\ \mu\text{m}$. Decreasing the S/N requirement to 3, on the other hand, decreases the purity to 75%, so our value of 4 is a good compromise. Note that this appears to be true for all our fields, despite their range of depths.

During the preparation of this paper but too late to be used as the primary model for our purity simulations, the B11 model was updated (B  thermin et al. 2012, hereafter B12). The B12 model predicts significantly more “orange” sources than the B11 model, implying a lower purity fraction for our catalog. Based on $40\ \text{deg}^2$ of simulated data (compared with the several hundred for the B11 model), we find a predicted number density of “orange” interlopers of $0.41\ \text{deg}^{-2}$, corresponding to a purity of $\sim 80\%$. In the future, once more models have been updated to reflect the *Herschel* number counts, it will be helpful to compare the false detection rates for different models to estimate the systematic uncertainties in the purity. The parameters of the B11 model do have estimated uncertainties, but adjusting the model parameters to increase the number of red (and near-red) sources by those uncertainties does not produce any detectable change in the purity rate. It seems likely that the systematic uncertainty term is dominated by more fundamental assumptions related to the SED models, etc., which we currently are not able to estimate.

5.3. Blends

Including blends presents a problem for our source density estimate. In the absence of instrument noise, any blended source

which appears red must include at least one genuinely red source. However, such a source may lie below our detection threshold, and hence would not belong in our catalog. Therefore, for a blend of two sources detected at $250\ \mu\text{m}$, it is not clear if the source should count as zero, one, or two sources in our density estimate. The probability of the first two can be estimated from models for the color distribution of non-red sources. Furthermore, because the observed number density of sufficiently bright $500\ \mu\text{m}$ risers is considerably smaller than non-red sources, it seems reasonable to assume that a red source is much more likely to be blended with a blue source than another red one—which will make the resulting blend bluer, but also may make it bright enough to be selected. This amounts to the assumption that the spatial clustering of bright red sources is not strong enough to compensate for the much larger number of non-red sources, an assumption that we are currently not in a position to test.

Because available models are trained on differential number counts in each band rather than colors (which largely have not been measured), the uncertainty in these predictions is hard to quantify. Therefore, we have chosen to exclude clear blends from our source counts but include their presence as a systematic uncertainty. There are two sources in our catalog that are detected as likely two-component blends in the $250\ \mu\text{m}$ data (but not in the other two bands): FLS 7 and FLS 23. We are able to make crude estimates of the $S_{250\ \mu\text{m}}$ flux densities of the constituent sources in both cases. Starting with this information, we randomly select single sources that are at least this bright at $250\ \mu\text{m}$ from a large simulation of the B11 model, but which are also fainter than the blended source in all bands. We then subtract the fluxes of the simulated source from the blended fluxes of the actual source, use this as an estimate of the flux of the other, red component, and finally determine what fraction of the time the de-blended source would pass our selection criteria.

For FLS 7, we find that 99.8% of the time the de-blended source is sufficiently bright and red to belong in our catalog. For FLS 23, which is significantly fainter, we find that for 110,000 simulated companions, the resulting de-blended source belongs in our catalog zero times. Therefore, we conclude that FLS 7 very likely contains a genuinely red, bright source, while FLS 23 at best contains a red source that is too faint to pass our D selection, and hence does not belong in our catalog.

In order to estimate the systematic uncertainty due to the fact that FLS 7 should be included in our catalog—but with unknown true fluxes and hence unknown efficiency—we compute the efficiency as above but using the ensemble of de-blended model fluxes, and then include 99.8% of that as a positive systematic uncertainty in our final source density estimate. This results in a positive systematic uncertainty of $0.24\ \text{deg}^{-2}$ in our FLS source density measurement.

5.4. Source Density

Combining the results of the purity and efficiency simulations with the input catalog, we finally arrive at our measurement of the source density of red sources in *Herschel* data. One complication is that our S/N requirement of 4 corresponds to slightly different depths in different fields, but in simulations the S/N seems to be a better predictor of the purity than the difference map flux density D .

The uncertainties in the efficiencies are quite non-Gaussian. To fold these into our calculation, when computing N from Equation (4), we randomly select an efficiency for each catalog source from our N_σ simulation sets, compute N using those

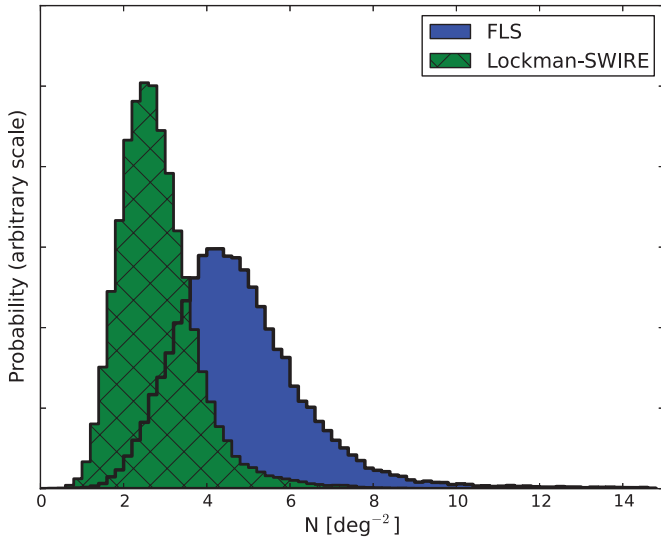


Figure 12. Estimated red source density per deg^2 for our two large fields, FLS and Lockman-SWIRE, including all identified statistical uncertainties. The smaller fields (Lockman-North, Lockman-East, and GOODS-N) are not shown because of their significantly different depths, and because their limited size (a total of 1.1 deg^2 compared with the 20.3 deg^2 of the fields shown) means that they make very little contribution to our final catalogs.

(A color version of this figure is available in the online journal.)

values, and then repeat this process several thousand times. We also include the uncertainty in p and the Poisson uncertainties from the number of detected sources in this step. The result is an ensemble of values for each field, drawn from the underlying N distribution. For the FLS field, we find that $N = 4.90^{+1.35}_{-1.47}$ (stat) $^{+0.24}$ (sys) deg^{-2} and for Lockman-SWIRE $N = 2.91^{+0.80}_{-0.86}$ (stat) deg^{-2} , not including the boosting correction, and where here the systematic uncertainties include only the effect of identified blends. The resulting number density distributions are shown in Figure 12. Given these uncertainties, the two fields are in reasonable agreement, with the difference corresponding to 1.2σ . Due to the modest size of our catalogs, Poisson errors dominate our uncertainty budget.

Since the sources in FLS and Lockman-SWIRE completely dominate our catalog (given their much larger areas), and the difference in depth is relatively minor considering the other uncertainties in our computation, we combine the results from these two fields using inverse variance weighting, then apply the boosting correction to give our final estimate of the red-source sky density of $N = 3.27^{+0.67}_{-0.84}$ (stat) deg^{-2} for sources with $S_{500\mu\text{m}} \geq 30 \text{ mJy}$ and $D \geq 23.9 \text{ mJy}$, with an identified systematic uncertainty due to partially resolved blends and boosting of $^{+0.06}_{-0.05} \text{ deg}^{-2}$. The corresponding 95% lower limit is $N > 2.04 \text{ deg}^{-2}$. Note that these values ignore any potential multiplicity of our sources, which will have to be constrained with interferometric observations. As noted in Section 4.3, high-resolution observations of a handful of red targets show that the multiplicity fraction appears to be relatively low. This is apparently at odds with the findings of Hodge et al. (2013)—but this requires further study, which will be presented by D. L. Clements et al. (2014, in preparation) and I. Perez-Fournon et al. (in preparation) using a larger sample. The number densities should therefore be interpreted as the number density of sources at the resolution of the SPIRE beam.

We can use the fact that 4/5 of our sources with measured redshifts are at $z > 4$ to estimate the sky density of $z > 4$ DSFGs satisfying our selection. This assumes that the sources

with redshifts are representative of our population (see Figure 5), which may not be entirely valid. In particular, FLS 3 and LSW 102 are redder than most of our catalog sources, and most are brighter than the average catalog source at $500 \mu\text{m}$. Evaluating the effects of this bias requires observations of additional sources. With this caveat in mind, if we denote this fraction by $f_{z>4}$, and assume a flat prior, then, from a simple application of Bayes theorem, the probability distribution for $f_{z>4}$ is given by $P(f_{z>4}) \propto (f_{z>4})^4 (1 - f_{z>4})$. This translates into a mean value of $f_{z>4} = 0.71^{+0.16}_{-0.17}$ (68.3% confidence limits), with a mode of 4/5. The corresponding frequentist confidence interval is $f_{z>4} = 0.48\text{--}0.96$. Similarly defining the fraction of our sources with $z > 3$ ($f_{z>3}$), we can provide a 95% Bayesian lower limit of $f_{z>3} > 0.61$ (>0.83 at 68.3%). Combining this with the sky density value quoted above, we therefore calculate the number density of $z > 4$ red sources to be $N_{z>4} = 2.37^{+0.75}_{-0.79} \text{ deg}^{-2}$, and $N_{z>3} > 1.68 \text{ deg}^{-2}$ (95% lower limit; we do not provide a central confidence interval here because our constraint on $f_{z>3}$ is a lower limit). Note that these results do not make use of photometric redshifts, and in fact the largest contribution to the uncertainty budget in the number of high- z DSFGs selected by our method is due to the small number of sources with spectroscopic redshifts. Clearly the highest priority for future work is to obtain additional redshifts, which will also allow detailed studies of the physical properties of these galaxies. None of these values attempt to correct for non-red DSFGs at high- z .

6. OTHER RED SOURCES IN THE LITERATURE

There are a number of $500 \mu\text{m}$ riser sources in the literature with spectroscopic redshifts, the majority of which are at $z > 4$. However, we suspect that this sample suffers from “publication bias”: it is highly inhomogeneous, and the fact that these sources were singled out for publication may have been influenced by the fact that they were at high z . Therefore, it is very difficult to draw any quantitative conclusions about how they relate to the population described in this paper. One exception is the recently published South Pole Telescope (SPT) selected sample of bright, lensed DSFGs of Vieira et al. (2013). Here the sources were selected at 1.4 mm in a uniform fashion, but SPIRE observations reveal that most of those at $z > 4$ are $500 \mu\text{m}$ risers. In this section we summarize information about red literature sources, particularly the SPT sample, which is discussed at the end of the section.

Combes et al. (2012) discovered a bright ($S_{500\mu\text{m}} > 200 \text{ mJy}$) $500 \mu\text{m}$ riser at $z = 5.2$ highly magnified by the cluster A773. Similarly, Cox et al. (2011) discusses a strongly lensed $500 \mu\text{m}$ riser with $z = 4.24$. Both sources would be easily detected by our method, and in fact were selected using SPIRE data. Swinbank et al. (2012) describes two sources at $z = 4.4$ with redshifts serendipitously measured during a high-resolution continuum mapping program in GOODS-S. Examination of the deep HerMES GOODS-S map shows that both sources are $500 \mu\text{m}$ risers, but are fainter than our $S_{500\mu\text{m}}$ cutoff.

There are also a number of known $z > 4$ DSFGs detected at longer wavelengths ($>850 \mu\text{m}$) that are too faint to be detected in SPIRE data (irrespective of our selection technique), such as the $z = 4.8$ source described by Coppin et al. (2009), or the one at $z = 5.2$ from Walter et al. (2012). Perhaps more interestingly, there are at least two examples of $z > 4$ DSFGs that are detected in the SPIRE bands, but have $S_{350\mu\text{m}} > S_{500\mu\text{m}}$: AzTEC-3 ($z = 5.3$; Capak et al. 2011; Riechers et al. 2010),

and GN20/20.2 ($z = 4$; Pope et al. 2005; Daddi et al. 2009). A reasonable inference is that some $z > 4$ DSFGs have warmer dust temperatures, and hence are not selected by our method.

Casey et al. (2012) performed an optical redshift survey of *Herschel*-selected sources, some of which were 500 μm risers. In order to be included in this sample, a 24 μm or radio counterpart was required, which is expected to bias against high- z sources. Furthermore, the spectroscopic success rate also has a redshift dependence, and it is possible that the counterpart-identification process may have a higher mis-identification rate for high- z sources. Together, these effects make it somewhat difficult to compare this sample to ours. Using the flux densities derived as part of the counterpart identification process, there are two sources that would satisfy our selection criteria. One of those is clearly an error—there is no detected source in any of the SPIRE bands. Analysis of the maps at the location of the other source shows that it would barely fail our selection criteria in $S_{500\mu\text{m}}$ and D , but that the source appears to be red. It has a optical redshift of 0.47. It is possible that this is a lensed source, and that the redshift is that of the foreground lens; submillimeter/millimeter interferometry would be required to be sure.

Vieira et al. (2013) and Weiß et al. (2013) present the results of a redshift survey of SPT-selected DSFGs from 1300 deg^2 of observations. The selection requirements are $S_{1.4\text{mm}} > 20$ mJy and that the 1.4 mm versus 2 mm flux density ratio is dust-like rather than synchrotron-like, with additional screening against $z < 0.03$ candidates and radio loud sources. They obtained secure, multi-line spectroscopic redshifts, primarily from the ^{12}CO ladder, for 19 sources, as well as single- or low S/N multi-line, redshifts for an additional six objects. Furthermore, they obtained *Herschel*/SPIRE observations of this sample. By selection, these sources are significantly brighter than the sample presented here, and therefore, as expected from models (e.g., Negrello et al. 2007), follow up reveals that all of these sources are strongly lensed. This is a well defined sample with SPIRE coverage, and hence is useful to compare with our study.

While the authors argue that the redshifts of several of the SPT sources with single line detections can be inferred from the shape of the thermal SED (by assuming “typical” dust temperatures) or the lack of additional lines, the possibility of weak CO lines or unusual dust temperatures—examples of which are known from the literature (e.g., Conley et al. 2011; Casey et al. 2012)—remains. Therefore, here we consider only SPT sources with secure, multi-line spectroscopic redshifts. With this requirement, the band coverage of the redshift search (primarily from 84 to 115 GHz) imposes a somewhat complicated redshift selection effect which favors $z > 3$ —that is, for sources at $z < 3$ only single lines could be detected in most cases at the depth of their observations, resulting in ambiguous redshifts. For some of the SPT sources this is alleviated by the presence of additional follow-up observations at other frequencies. Furthermore, the addition of the 1.4 mm flux selection clearly introduces a relative selection bias between the SPT sources and the sample presented here, even for SPT sources that are also 500 μm risers—although the amount cannot be estimated without adding strong assumptions about the underlying population. Detailed lens models are available for four of the SPT sources, but if we assume lens magnification factors of 5–25, as suggested by those four sources, then, on average, the SPT population is intrinsically less luminous than our sample, assuming that our sources are not highly lensed on average. Our method is substantially more efficient at selecting high- z sources (in terms

of the overall fraction of sources at high z as well as the source density), but, because they are strongly lensed, the SPT sources are much easier to study in detail.

Ignoring these complications, seven of the 10 SPT sources with $z > 4$ are 500 μm risers, while the other three are brightest at 350 μm . One of these is clearly not red in the SPIRE bands, while the other two have $S_{500\mu\text{m}} \simeq S_{350\mu\text{m}}$ to within 1σ . In addition, there are three SPT 500 μm risers with $3 < z < 4$ and an additional four 500 μm risers with single line redshifts which we exclude from this discussion. This suggests that red SPIRE colors are a relatively efficient and complete method of finding 1.4 mm selected sources at $z > 4$.

7. INTERPRETATION

7.1. Comparison of Observed Number Density with Galaxy Evolution Models

To compare the number of observed bright and red SPIRE sources to the number predicted by pre-existing models, we consulted models by Béthermin et al. (2011, 2012), Fernandez-Conde et al. (2008), Franceschini et al. (2010), Le Borgne et al. (2009), Valiante et al. (2009), and Xu et al. (2001) using mock catalogs. The comparisons are summarized in Table 6 and discussed in detail in this section. Generally, these models are not physically motivated, and are developed based on the properties of lower- z DSFGs. The goals of this comparison are to test if the properties of the DSFG population can be simply extrapolated from $z \sim 2$, or if additional evolution is required, and how well these models can be used to plan for future surveys of high- z DSFGs.

For the Fernandez-Conde et al. (2008) simulations, which are based on Lagache et al. (2004), we used a simulated data set covering 5.2 deg^2 and with a bias parameter 1.5. For the Le Borgne et al. (2009) model, we used a mock catalog covering 10 deg^2 and containing 2 million galaxies. In both cases we found zero sources satisfying our selection criteria. We can therefore conclude that the predictions of these models for the number of red sources are overwhelmingly ruled out by our observations.

The other models predict some red sources, but in general they do not match the properties of our observed population. A 93 deg^2 simulation of the B11 model, containing 20 million galaxies, predicts 1.1 deg^{-2} red sources satisfying our selection criteria, but only 0.05 deg^{-2} lie at $z > 3$ and 0 at $z > 4$, corresponding to a 95% upper limit of $<0.03 \text{deg}^{-2}$. Hence, this model over-predicts the number of low- z sources, and significantly under-predicts the number of high- z ones. The Valiante et al. (2009) model, which is based on observed galaxies with luminosities up to $10^{12.8} L_{\odot}$ and incorporates a correlation of luminosity and mean dust temperature, predicts 15 sources satisfying our selection criteria in a simulated area of 10 deg^2 and containing 8.2 million galaxies. However, zero of these galaxies are at $z > 4$, and only three are at $z > 3$. Furthermore, they have significantly colder dust temperatures (~ 30 K) than our sources with known redshifts.

The Franceschini et al. (2010) model over-predicts the number of sources that meet our observational selection criterion, predicting 10 deg^{-2} . However, their predictions for the number of sources at high- z are closer to our limits: 1.2 deg^{-2} at $z > 4$ and 3.4 deg^{-2} at $z > 3$. Thus, their prediction for $z > 4$ is only lower than the observed number by a factor of 2 (1.5σ), although they also predict a large number of red sources at lower z that are not consistent with observations.

Table 6
Predicted Number of Red SPIRE Sources

Model	Predicted Density (deg^{-2})			Reference
	Red	Red $z > 3$	Red $z > 4$	
B�ethermin 11	1.1	0.05	<0.03	B�ethermin et al. (2011); B11
B�ethermin 12	0.58	0.58	0.49	B�ethermin et al. (2012); B12
F-Conde	<0.6	<0.6	<0.6	Fernandez-Conde et al. (2008)
LeBorgne	<0.3	<0.3	<0.3	Le Borgne et al. (2009)
Valiante	1.5	0.2	<0.3	Valiante et al. (2009)
Franceschini	10	3.4	1.2	Franceschini et al. (2010)
Xu	12	0.34	0.08	Xu et al. (2001)
Observed	$3.27^{+0.67}_{-0.84}$	>1.68 (95%)	$2.37^{+0.75}_{-0.79}$	This work

Notes. Comparison of the prediction of various pre-existing models with the observed number of red sources satisfying our detection criteria ($D \geq 23.9$ mJy, $S_{500\mu\text{m}} \geq 30$ mJy, $S_{500\mu\text{m}} \geq S_{350\mu\text{m}} \geq S_{250\mu\text{m}}$). The upper limits, which are provided when no such sources were generated in our simulations, are the 95% one-sided frequentist limits, and are set by the sky area simulated for each model. The number of red sources at $z > 3$ and $z > 4$ are based on combining the measured sky density with the observation that 4/5 of our sources with redshifts are at $z > 4$, and 5/5 at $z > 3$.

For the Xu et al. (2001) models, we used mock catalogs covering 10 deg^2 which have been updated to better match the *Spitzer* number counts. This substantially over-predicts the number density of red sources at 12 deg^{-2} . However, the predicted number of $z > 4$ sources is much smaller, 0.08 deg^{-2} , which is strongly ruled out. Again, this model also predicts a very large number of red sources at lower z which are not seen in the data. Inspection of these sources show that most are classified as having “active galactic nucleus (AGN)” rather than “starburst” templates. Closer inspection of the templates that meet our source selection criteria indicate that the models may have poor applicability for these types of sources. For example, the template within the model catalogs which most often passes the selection criteria is based on the $10^{11.8} L_{\odot}$ galaxy Mrk 0309, which is assumed to have a dust temperature of ~ 22 K (for $\beta = 1.5$), despite being scaled up by a factor of five in luminosity for the catalogs, and despite having no published measurements for the template fit at $\lambda > 100 \mu\text{m}$. Galaxies with luminosity of $10^{12.5} L_{\odot}$ and average dust temperature 22 K may exist, but the Mrk 0309-based template is not yet a convincing example of one.

The B12 models fare considerably better. We generated catalogs representing 200 deg^2 , and found a predicted red source density of 0.58 deg^{-2} . Furthermore, all of the red sources predicted by this model are at $z > 3$, with 0.49 deg^{-2} at $z > 4$. Folding in the efficiency distribution, and including the predicted contamination rate by “orange” sources, the B12 model predicts that we should select 14.7 sources over our fields, compared with the 38 actually found. This corresponds to a P value of 3×10^{-7} , so formally this model is still excluded at very high significance. However, it is clear that it is much closer to our observations than the other models, and it is worth attempting to understand why this is the case. There are two primary reasons. First, the B12 predicts more high- z , luminous DSFGs than many of the other models—although not, for example, the B11 model. Second, the SED templates for luminous DSFGs are redder, on average, than for most of the other models—this is the most important difference in comparison with the B11 model. In addition, the B12 model implements some scatter in the templates for a fixed z and luminosity, which most of the other models do not. However, this seems to have a relatively modest effect—doubling the scatter increases the predicted source density by about 25%, but entirely by adding bright $z < 3$ red sources which, so far, have

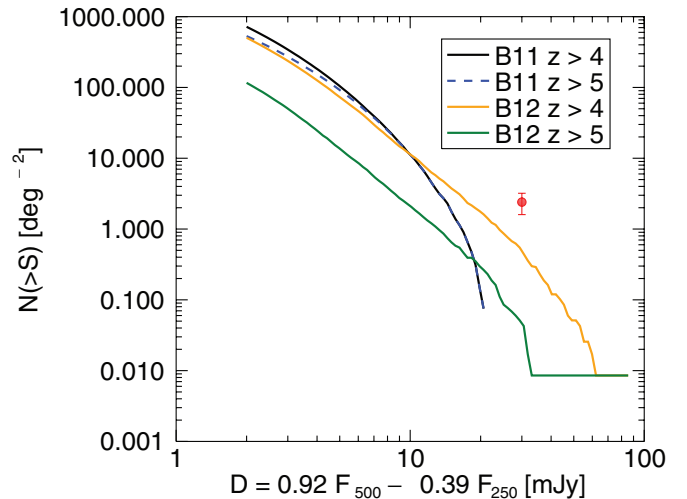


Figure 13. Cumulative number counts (red DSFGs brighter than a specified flux density in the difference map, D) for the B11 and B12 models, based on the simulations discussed in the text. Shown, for comparison, is our measurement of the number density of $z > 4$ red DSFGs from Section 5.4.

(A color version of this figure is available in the online journal.)

not been observed. Furthermore, it disturbs the agreement of this model with the observed far-IR/submillimeter monochromatic differential number counts. The cumulative number counts for the B11 and B12 models, compared with our observations, are shown in Figure 13.

One possibility for improving the agreement of these models with observations is that there may be significantly more strong lensing at high redshifts than expected. Here we explore how much *more* lensing would be required to match our observations with current population models using the B11 model. The B11 model already contains lensing, but we can consider the effects of modifying this prescription. If we substitute the lensing model of Wardlow et al. (2013), the number of red sources is significantly increased to 1.4 deg^{-2} . However, most of these are at $z < 2$; the number densities at $z > 3$ and $z > 4$ are increased to 0.3 and 0.2 deg^{-2} , respectively. This is a step in the right direction, but is clearly still inconsistent with our observations. Furthermore, the observed flux density distribution clearly does not match our population—the number of $S_{500\mu\text{m}} > 50$ mJy sources at $z > 3$ is only 0.05 deg^{-2} . The five sources with

redshifts that we have, even ignoring efficiency corrections, already rule this out at $>99.8\%$.

Next we consider modifying the Wardlow et al. (2013) lensing model. If we scale up all lensing probabilities above $\mu = 1.5$ by a constant factor, we find that we must increase them by $20\times$ in order to match our source density at $z > 3$, which is extremely unlikely. Rather than increasing the frequency of large magnifications, which does not seem to work, a different way to look at the problem is to impose a minimum magnification floor at $z > 3$ on the model. We cannot do so for all sources, because for physical reasons the mean magnification over all lines of sight must be one to any redshift. However, because large magnifications are rare in any such model, a reasonable approach is to adjust the Wardlow et al. (2013) model by setting $P(\mu) = 0.5$ between $\mu = 1$ and $\mu = \mu_{\text{low}}$ (with the probability distribution above μ_{low} unaltered), and explore how large μ_{low} must be to reconcile models with observations. Carrying out this procedure, we find that, for the B11 model, we require $\mu_{\text{low}} = 2.1$. In other words, *half* of all sight-lines to $z > 3$ must be magnified by a factor of two or more. This is not realistic. Applying the same analysis to the B12 model does not change much—to match observations either the high-magnification tail must be increased by $15\times$, or half of all sight-lines must be magnified by more than $\mu = 1.8$.

As discussed in Section 5.4, our measured number density is effectively at the resolution of SPIRE ($>18''$). While our counts are corrected for blends with non-red objects, if our sources have a high multiplicity (i.e., all of our catalog objects are in fact composed of two or more red sources), then this will affect the (dis-)agreement with models. The best way to investigate this topic is to obtain higher-resolution (interferometric) submillimeter/millimeter observations. However, because the above phenomenological models are trained to match observed number counts that have the same resolution issues, in order for multiplicity to bring their predictions in agreement with our observations it must be a strong function of redshift such that it affects our sources much more than lower- z DSFGs. This does not seem particularly likely, but it cannot be ruled out at this point. For example, if luminous DSFGs at all redshifts are actually comprised of two sources too close to each other to be resolved, then, in order to maintain agreement with the overall observed number counts of all sources, the number of predicted red (but now undetectably blended) sources at SPIRE resolutions would not change.

Overall, pre-existing models significantly under-predict the number of high- z , red sources we detect. The one exception is the model of Franceschini et al. (2010), which is a reasonable match for the number of high- z galaxies detected by our technique, but also predicts a very numerous population of lower- z red sources highly inconsistent with *Herschel* observations. Of the models that do not share this issue, the B12 model performs the best, although it is still ruled out at high significance. In any case, this comparison suggests that there must be additional evolution in the DSFG population at $z > 3$ beyond that predicted by simple extrapolations from lower redshift. It seems certain that gravitational lensing will play a role in reconciling population models with observations, but for the current generation of such models the required amount of lensing is not reasonable.

7.2. Overlap of Our Red SPIRE Sample with Millimeter-selected Galaxies

Given our selection criterion of monotonically rising spectra with increasing wavelength in the SPIRE bands, we would

expect the selected objects to be strong emitters at $\lambda \approx 1$ mm. This is now demonstrated for a subset of the sample, as discussed in Section 4. In this section, we examine the reverse implication using millimeter-wave observations that cover a small fraction of the HerMES fields: do millimeter-selected sources have properties similar to the red SPIRE sources in this paper?

With two exceptions,⁴² existing $\lambda \approx 1$ mm “blind” surveys sensitive enough to detect significant numbers of high-redshift galaxies cover areas less than 1 deg^2 , and measure a population with $\sim 100\times$ the surface density of our red SPIRE galaxies. Therefore, by virtue of observational selection, we cannot have good correspondence with these surveys. It is reasonable to expect that the degree-sized millimeter surveys will uncover objects that are typically fainter at far-IR through millimeter wavelengths and likely have lower luminosity. The comparison with lensed, millimeter-selected SPT sources (which also have SPIRE observations) was already presented in Section 6.

Within the SPIRE SDP fields discussed in this paper, the AzTEC 1.1 mm survey of Lockman Hole East (Austermann et al. 2010) covers the largest area with ~ 1 mJy depth. The AzTEC survey produced a primary catalog of 43 sources with 4σ statistical significance over an area of 0.3 deg^2 . None of these correspond to red SPIRE sources cataloged in Table 2. However, all 17 of the AzTEC sources with greater than 5σ statistical significance are associated with clear SPIRE sources and positive peaks in the difference image D . These sources range in 1.1 mm brightness from 3.6 to 6.6 mJy (deboosted), with a mean of 4.6 mJy. We stacked the SPIRE $50''$ -resolution images at the positions of the 17 AzTEC sources. The stacked mean values of $S_{250 \mu\text{m}}$, $S_{350 \mu\text{m}}$, $S_{500 \mu\text{m}}$ and D are 30.1, 34.1, 25.7, and 11.4 mJy, respectively. Collectively, then, these millimeter-selected sources peak at shorter far-IR wavelengths than the red sample in this paper, and they are a factor of ~ 1.3 fainter in the far-IR.

Only one source—no. 13—among the 17 AzTEC 5σ sources has a SPIRE counterpart which meets our redness criterion, but not our brightness criterion. In matched $50''$ beams, it has flux densities $S_{250 \mu\text{m}}$, $S_{350 \mu\text{m}}$, $S_{500 \mu\text{m}}$ of 12.4, 25.8, 29.0 mJy, respectively. A tentative photometric redshift of 2.1—ironically below the median for the sample—was assigned to source 13 by the AzTEC team (Michałowski et al. 2012) based on a radio and $24 \mu\text{m}$ counterpart. However, the radio and $24 \mu\text{m}$ source appear to be offset by similar distance and direction from both the AzTEC and SPIRE source, so may not be physically associated.

7.3. Contribution of Red Sources to Far-IR Background

Using our completeness and purity simulations, it is simple to estimate the contribution of sources selected by our method to the cosmic far-infrared background (CIB) at $500 \mu\text{m}$ by weighting the number density calculation by $S_{500 \mu\text{m}}$. Carrying out this procedure, we find for the FLS field a value of $0.66 \pm 0.20 \text{ kJy sr}^{-1}$, and for Lockman-SWIRE $0.38 \pm 0.10 \text{ kJy sr}^{-1}$, where the uncertainty in the observed fluxes and Poisson fluctuations (which account for $\sim 2/3$ of the error budget) are included, but not the uncertainty in the SPIRE calibration. These differ by 1.3 σ , and hence are consistent. Compared with the FIRAS measurement of $0.39 \pm 0.10 \text{ MJy sr}^{-1}$ (Fixsen et al. 1998), the red sources with $S_{500 \mu\text{m}} > 30$ mJy account for only 0.1%–0.2% of the background. Note that these only represent

⁴² The South Pole Telescope (Mocanu et al. 2013) and Atacama Cosmology Telescope (Marsden et al. 2013) surveys; due to their large areas, however, these are effectively much shallower than the HerMES survey.

the intrinsically most luminous high- z DSFGs, and non-red sources at these redshifts are not included, but, assuming that the luminosity function for DSFGs has a similar shape at $z > 3$ as it does at $z \sim 2$, 500 μm risers probably do not account for more than a few percent of the CIB at 500 μm .

7.4. Photometric Redshifts

Up until this point in the paper, we have tried to avoid any analysis which requires photometric redshifts, but they are required in order to estimate the contribution of our sources to the star formation history of the universe. We have firm spectroscopic redshifts for only five of the galaxies in our sample. Without precise interferometric positions, we are limited to the properties of the thermal dust SEDs to derive photo- z 's. Because modified blackbody models are perfectly degenerate in $T_d/(1+z)$ and $\lambda_0(1+z)$, deriving photo- z 's from these data essentially requires assuming a prior on the rest frame values of these parameters. Here we attempt to derive a crude estimate of the redshift distribution of our population using such a prior. Note that here we are not making use of the priors discussed in Section 3 in any way.

Instead of working with the dust temperature T_d , which is rather indirectly constrained by the data, we use the wavelength at which S_ν peaks, λ_{max} , for each source. We construct a prior for the rest-frame λ_{max} by following the approach of Greve et al. (2012): collect a comparison sample of DSFGs (with precise spectroscopic redshifts and well constrained thermal SEDs), and analyze them using the same modified blackbody model. If the (observer frame) peak wavelength of each red source is λ_{max}^S , and the (rest frame) peak wavelength of each comparison source is λ_{max}^C , then the photometric redshift estimate z_p for that red source from that comparison is $1+z_p = \lambda_{\text{max}}^S/\lambda_{\text{max}}^C$. Because our SED analysis is based on MCMC methods, we can also easily include measurement uncertainties in each $\lambda_{\text{max}}^{(C,S)}$.

The results depend sensitively on the comparison sample. Ideally, this sample would be selected in exactly the same manner (adjusting for redshift) as our red sources—but no such sample is currently available. We considered several possible compilations, evaluating them based on how well they predict the redshifts of a test sample consisting of our five red sources with spectroscopic redshifts as well as the red sources from Combes et al. (2012) and Cox et al. (2011), both of which were discovered in *Herschel*/SPIRE observations and which would clearly be selected using our method. We do not include the SPT red sources in our test sample because it is not clear how the 1.4 mm selection will bias the selection relative to ours. Magnelli et al. (2012) present a detailed study of “classic SMGs” at $z \sim 2.4$ selected based on longer wavelength (850 μm –1.2 mm) observations, and with redshifts generally determined on the basis of radio cross-identifications, using the same SED model. The longer wavelength selection is expected to bias this sample relative to ours toward colder sources, and hence toward lower redshifts for fixed SPIRE colors. Indeed, analysis of this sample gives $z_p \sim 2$ for our seven test sources ($z_p \sim 3$ for FLS 3), which can be ruled out at very high significance, as 6/7 are at $z > 4$. Therefore, as a comparison sample this does a very poor job predicting the redshifts of our sources—so poorly, in fact, that it is not possible to re-weight it to provide a good estimate. The same is true, but to a lesser extent, for the SPT sample of Vieira et al. (2013): the sources are colder, and hence under-predict the redshifts of our test sample.

The Casey et al. (2012) study discussed in Section 6 presents redshifts for a large sample of *Herschel*-selected DSFGs, with the additional requirement that they be detected in *Spitzer* 24 μm or radio observations. While that paper uses a somewhat different SED model, they also present λ_{max} measurements. At the typical L_{IR} of our sources ($\sim 10^{13} L_\odot$), this predicts $\langle z_p \rangle \sim 9$, which is again strongly ruled out. This may be the result of selection biases in the λ_{max} – L_{IR} relation of the Casey et al. (2012) sample. If we instead select $S_{500\mu\text{m}} > S_{350\mu\text{m}} > S_{250\mu\text{m}}$ sources—now dropping the minimum flux requirements to $S_{500\mu\text{m}} > 10$ mJy in order to increase the comparison sample size (to 19 sources)—we find $\langle z_p \rangle = 6.3$ for the comparison sample (excluding FLS 3), an improvement, but again strongly ruled out. These sources have similar colors as those of our red sample, so this is somewhat surprising—the 24 μm /radio and optical spectroscopic success requirements are expected to bias this sample toward lower z , increasing the rest-frame λ_{max} values, which would lead to an under-prediction of z_p for our test sources rather than the observed over-prediction. In any case, this does not seem to be a good comparison sample for our purposes.

Finally, we consider the compilation of well-observed *Herschel*-selected lensed sources of Greve et al. (2012), also at $z \sim 2$ (which these authors used to make photo- z estimates for 1.4 mm selected SPT sources). They fit the photometry of the lensed sources using a similar SED model, but holding β and $\lambda_0(1+z)$ fixed. Because these sources are generally quite well observed, we re-fit this sample using our model but without fixing these parameters (or using priors), excluding the few sources where the data quality was insufficient to constrain such a fit. Comparison with our test sample gives $(1+z_p)/(1+z_{\text{spec}}) = 0.93 \pm 0.08$, much better than the other comparison samples. These highly magnified sources almost certainly probe a different (fainter) luminosity range than our red sources. This may result in some bias in the photo- z 's; for example, if dust temperature increases with luminosity, we would expect the lower- z lensed galaxies to peak at longer rest-frame wavelengths than our red sources, and hence under-predict the redshifts. However, we do not apply any correction, since the derived photo- z values are consistent overall with the spectroscopic redshifts of our test sample. We further supplement this collection by including the fits to FLS 1, FLS 3, FLS 5, and LSW 20 as in Section 4.7, resulting in a final comparison sample of 19 DSFGs.

Applying this effective prior to the λ_{max} values derived in Section 3 results in the population distribution given in Figure 14. This gives $\langle z_p \rangle = 4.7$ with a one sigma range of ± 0.9 , and with 20% of the population at $z < 4$ —consistent with the existence of LSW 20 at $z = 3.4$ in our test sample. The tail to higher redshift is due to the fact that, for the redder sources in our sample, the upper limit on λ_{max} is not as well constrained as the lower limit, although the existence of FLS 3 at $z = 6.34$ demonstrates that there are at least some $z > 6$ DSFGs. Adding more longer- λ observations would help constrain this tail.

7.5. Contribution of These Sources to High- z Star Formation

At this time, the paucity of spectroscopic redshifts of our sources prevents a precise calculation of their contribution to the star formation history of the universe. However, we can extend the photometric redshift model discussed in Section 7.4 to form a rough estimate. Each of the comparison sample sources has a well determined thermal SED, so in addition to using randomly

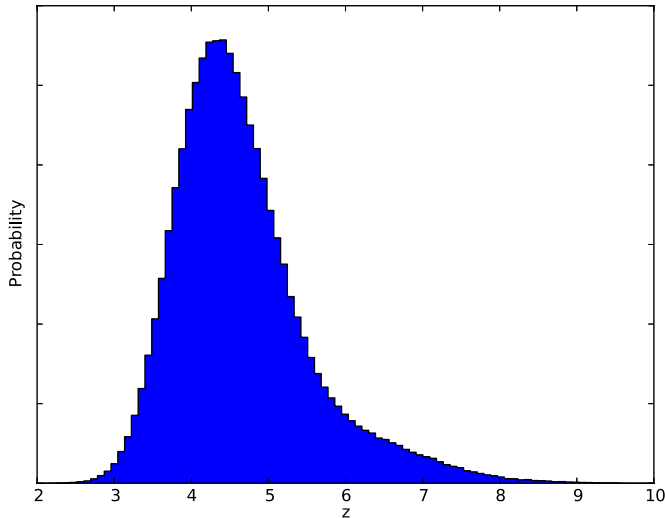


Figure 14. Photo- z distribution of our sample using the SED prior discussed in the text.

(A color version of this figure is available in the online journal.)

sampled λ_{\max}^C values, we also take the corresponding values of the SED parameters (T_d , β , etc.), redshifting that SED to the corresponding z_p of the catalog source, and scaling it to match the observed $500 \mu\text{m}$ flux density. For this calculation we must also correct for the selection efficiency and purity, as discussed in Section 5, so for each z_p , L_{IR} pair we also associate a randomly drawn ϵ and p appropriate to that source. Doing this once for each source in our catalog provides a single simulation of our red source sample. We then bin the simulated sources by z_p into two broad bins ($z_p = 4\text{--}5$ and $z_p = 5\text{--}6$), add up the total L_{IR} in each bin, counting each catalog source as $p/\epsilon A$ sources per deg^2 , where A is the area of the field that that source comes from. For those sources in our main survey area with spectroscopic redshifts (FLS 1, FLS 3, FLS 5, and LSW 20) we instead sample L_{IR} directly from their SED fits (Section 4.7), hence excluding both FLS 3 and LSW 20 from our calculation as they lie outside both redshift bins.

We then divide the total L_{IR} in each bin by the comoving volume per deg^2 , and convert to a star formation rate density (SFRD) using the Kennicutt (1998) conversion. By repeating this procedure 5000 times, and folding in Poisson noise due to the limited sample size, we can estimate the uncertainty in the SFRD from these sources, deriving values of $(1.5 \pm 0.5) \times 10^{-3}$ and $(8.6 \pm 4.9) \times 10^{-4} M_{\odot} \text{yr}^{-1} \text{Mpc}^{-3}$ at $4 \leq z < 5$ and $5 \leq z < 6$, respectively (Figure 15). About half of the uncertainty budget in the lower bin and the majority in the higher bin arises from Poisson noise. Note that we make no attempt to correct for non-red DSFGs at these redshifts, nor for sources fainter than our detection limit. These values thus represent only the contribution to the SFRD from the most luminous, heavily obscured far-IR galaxies.

This discussion assumes that AGN activity is not a major contributor to the far-IR luminosity of our sources, as is thought to be the case for lower- z DSFGs (Alexander et al. 2005). Unfortunately, given the high redshift, extreme obscuration, and modest source density of our sources, obtaining sufficiently deep X-ray data for even a small fraction of our catalog would be prohibitively expensive. However, we note that the closest X-ray source to GOODS-N 8 in the 2 Ms *Chandra* Deep Field North catalog (Alexander et al. 2003) is $18''$ away, which, given our positional uncertainties, is unlikely to be related.

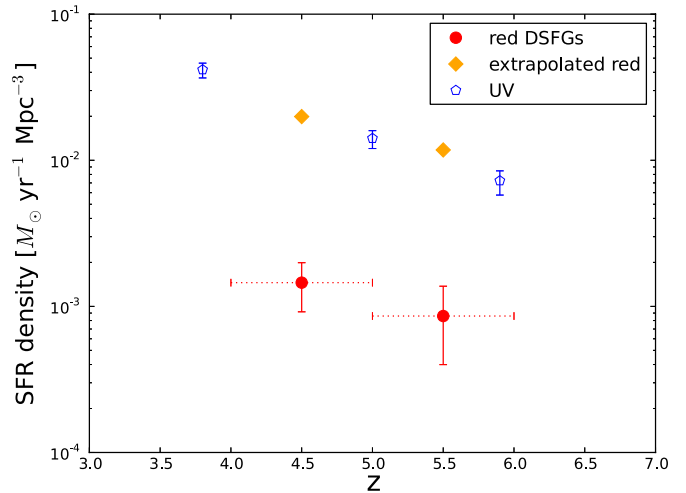


Figure 15. Estimated contribution of our $500 \mu\text{m}$ riser selected DSFGs to the star formation rate density at $z = 4\text{--}6$ (red circles). No correction is made for fainter sources, or for DSFGs in this redshift range that are not red in the SPIRE bands. The horizontal bars reflect the bin size, and are not uncertainties. The orange diamonds show the red points corrected for fainter sources using the B11 luminosity function. For comparison, the blue pentagons are the extinction corrected values derived from rest-frame UV *HST* surveys for sources brighter than $0.3 L_{\star}$ (Bouwens et al. 2007); these include significantly lower luminosity sources than the red points.

(A color version of this figure is available in the online journal.)

If we assume that the *shape* of the DSFG luminosity function does not evolve from $z \sim 2$ to $z \sim 5$ (which is almost certainly not true in detail, and may not even be a good approximation), then we can correct for the presence of fainter starbursts. Further assuming that our $z > 4$ targets have $L_{\text{IR}} > 10^{13} L_{\odot}$, based on the results of Section 4.7, and using the B11 luminosity function,⁴³ the contribution to the SFRD from red, $z > 4$ DSFGs is similar to the extinction-corrected, UV-inferred SFRD at the same redshifts of Bouwens et al. (2007), as shown in Figure 15. Using the B12 luminosity function increases this by a further factor of three. Again, we have not made any attempt to include non-red $z > 4$ DSFGs. Furthermore, the overall SFRD for these luminosity functions is dominated by sources with $L_{\text{IR}} \sim 10^{12} L_{\odot}$, which are too obscured to be detected in the rest-frame UV even in deep *Hubble Space Telescope* (*HST*) observations. Clearly, the exact values should not be taken too seriously, but they do suggest that rest-frame UV based estimates of the star formation history of the universe may be missing a significant component of the SFRD, even after corrections for extinction. Determining whether or not this is the case will require further observations—with the goals of both increasing the number of red sources with spectroscopic redshifts, and extending the search to fainter sources.

8. CONCLUSIONS

We have presented a method for selecting candidate high- z DSFGs using *Herschel*/SPIRE colors, and provided a catalog of such sources selected from the first 21.4 deg^2 of data from the HerMES project.

1. The number density of red $S_{500 \mu\text{m}} \geq 30$, $D = 0.92 S_{500 \mu\text{m}} - 0.39 S_{250 \mu\text{m}} \geq 23.9 \text{ mJy}$ sources in confusion limited SPIRE maps is $\sim 2 \text{ deg}^{-2}$. After modeling for

⁴³ See Figure 11 of B11, noting that the only change in the shape from $z = 3$ to 5 is an increase in L_{\star} by 6%.

- selection efficiency and contamination, this implies an underlying number density of $3.3_{-0.8}^{+0.7} \text{ deg}^{-2}$. The 95% lower limit is 2.0 deg^{-2} .
2. We have obtained redshifts for five targets selected using our method. They range from $z = 3.4$ to 6.3 , with $4/5$ at $z > 4$.
 3. SED modeling of the sources with redshifts shows that they correspond to the luminous tip of the lower- z DSFG luminosity function, with typical $L_{\text{IR}} > 10^{13} L_{\odot}$.
 4. Combining the measured redshifts with the source density, we estimate the number of red, luminous $z > 4$ DSFGs to be $2.4 \pm 0.8 \text{ deg}^{-2}$; the largest uncertainty is due to the small number of sources with secure spectroscopic redshifts.
 5. The number of such high- z DSFGs is significantly higher than the predictions of existing population models. While gravitational lensing clearly has a role to play in understanding this population, the amount required to reproduce observations with current population models appears to be unrealistic.
 6. Using a photo- z model based on the properties of lower- z , lensed, *Herschel*-selected DSFGs, we estimate $\langle z \rangle \sim 4.7$ for our population.
 7. Extending this model to predict the contribution of red sources satisfying our selection criteria to the SFRD, we find $\sim 10^{-3} M_{\odot} \text{ yr}^{-1} \text{ Mpc}^{-3}$ at $z \sim 5$. This is significantly lower than the total inferred SFRD at these redshifts—which these represent only the tip of the luminosity function.
 8. If the ratio between the most luminous sources and the rest of the population is similar at $z > 4$ to that for lower- z DSFGs, then DSFGs may contribute a similar amount to the overall star formation density at these redshifts as the extinction corrected, rest-frame UV measurements—which do not account for such highly extinguished systems.

This sample represents less than $1/5$ of the 110 deg^2 of the main HerMES survey, which reaches similar depths, and an even smaller fraction of the 300 deg^2 of the shallower HeLMS companion survey (Oliver et al. 2012). The number density of sources selected by our method should be a good description of all but the deepest (e.g., GOODS-N) confusion limited SPIRE maps, although we are working to improve this by using more optimal filtering. In shallower surveys, such as HeLMS or H-ATLAS (Eales et al. 2010), the number density will be lower. For example, to a depth of 50 mJy at $500 \mu\text{m}$, the number density (without purity or completeness corrections) is $\sim 0.5 \text{ deg}^{-2}$, about $4\times$ less, based on our catalogs. Follow-up of our sources is ongoing at a wide range of facilities. Obtaining more redshifts is the highest priority for future studies.

This material is based upon work supported by the National Aeronautics and Space Administration under grant No. 12-ADAP12-0139 issued through the ADAP program. Part of this work was performed at the Jet Propulsion Laboratory, California Institute of Technology, under a contract with NASA. SPIRE has been developed by a consortium of institutes led by Cardiff Univ. (UK) and including Univ. Lethbridge (Canada); NAOC (China); CEA, LAM (France); IFSI, Univ. Padua (Italy); IAC (Spain); Stockholm Observatory (Sweden); Imperial College London, RAL, UCL-MSSL, UKATC, Univ. Sussex (UK); Caltech, JPL, NHSC, Univ. Colorado (USA). This development has been supported by national funding agencies: CSA (Canada); NAOC (China); CEA, CNES, CNRS (France); ASI (Italy); MCINN (Spain); SNSB (Sweden); STFC (UK); and NASA

(USA). The SPIRE data presented in paper this have been released through the *Herschel* Database in Marseille, HeDAM (<http://hedam.oamp.fr/HerMES>). Some of this material is based upon work at the Caltech Submillimeter Observatory, which was operated by the California Institute of Technology under cooperative agreement with the National Science Foundation (AST-0838261). The Submillimeter Array is a joint project between the Smithsonian Astrophysical Observatory and the Academia Sinica Institute of Astronomy and Astrophysics and is funded by the Smithsonian Institution and the Academia Sinica. Based in part on observations carried out with the IRAM Plateau de Bure Interferometer. IRAM is supported by INSU/CNRS (France), MPG (Germany) and IGN (Spain). Support for CARMA construction was derived from the Gordon and Betty Moore Foundation, the Kenneth T. and Eileen L. Norris Foundation, the James S. McDonnell Foundation, the Associates of the California Institute of Technology, the University of Chicago, the states of California, Illinois and Maryland, and the National Science Foundation. Ongoing CARMA development and operations are supported by the National Science Foundation under a cooperative agreement and the CARMA partner universities. Some of the data presented herein were obtained at the W. M. Keck Observatory, which is operated as a scientific partnership among the California Institute of Technology, the University of California and the National Aeronautics and Space Administration. The Observatory was made possible by the generous financial support of the W. M. Keck Foundation. Based in part on observations made with the Gran Telescopio Canarias (GTC), installed in the Spanish Observatorio del Roque de los Muchachos of the Instituto de Astrofísica de Canarias, in the island of La Palma. This research made use of Astropy (<http://www.astropy.org>), a community-developed core Python package for Astronomy (Astropy Collaboration 2013). This research has made use of NASA’s Astrophysics Data System Bibliographic Services. This research has made use of the NASA/IPAC Extragalactic Database (NED) which is operated by the Jet Propulsion Laboratory, California Institute of Technology, under contract with the National Aeronautics and Space Administration.

Facilities: Herschel (SPIRE), CSO (Bolocam, Z-Spec), CARMA, SMA, IRAM:Interferometer, Keck:I (LRIS), GTC (OSIRIS), MERLIN

APPENDIX

MODIFIED BLACKBODY SED FITS

Here we discuss the details of our modified blackbody fits to the thermal SEDs of our sources. The basic model is given by Equation (3), and is written in terms of the blackbody function (through the dust temperature T_d), the dust properties (β and λ_0), and the overall normalization (Ω). Note that using Ω directly is a poor choice for fitting purposes because it is extremely degenerate with T_d , so instead we use the observer frame flux density at $500 \mu\text{m}$ as the normalization parameter. Tests show that this parameterization is much better behaved. We use flat priors over all model parameters.

We have developed code to fit this model to SED data using an Markov Chain Monte Carlo (MCMC) method. An earlier version of this code was also used by Riechers et al. (2013) to analyze the photometry of FLS 3, and we have made it freely available.⁴⁴ We make use of the parallelized affine-invariant

⁴⁴ https://github.com/aconley/mbb_emcee

MCMC python module `emcee` (Foreman-Mackey et al. 2013), which in practice has better convergence properties than the more commonly used Metropolis–Hastings method. We check convergence of our chains by requiring that the autocorrelation length for each model parameter is several times less than the number of steps taken during an initial burn-in stage (which are then discarded).

Compared with the version of this code used by Riechers et al. (2013), several improvements have been made. First, we have added the ability to impose upper and lower limits as well as Gaussian priors on the model parameters. These additions are useful for analyzing poorly constrained data, such as when we consider fits to only the SPIRE photometry in Section 3. Second, instead of treating the instrument response as a delta function in wavelength, we now fully model the wavelength response of each instrument. We have applied this improved code to FLS 3, and find that the resulting changes in the model parameters are well within the quoted uncertainties.

REFERENCES

- Alexander, D. M., Bauer, F. E., Brandt, W. N., et al. 2003, *AJ*, 126, 539
- Alexander, D. M., Bauer, F. E., Chapman, S. C., et al. 2005, *ApJ*, 632, 736
- Amblard, A., Cooray, A., Serra, P., et al. 2011, *Natur*, 470, 510
- Aretxaga, I., Wilson, G. W., Aguilar, E., et al. 2011, *MNRAS*, 415, 3831
- Austermann, J. E., Dunlop, J. S., Perera, T. A., et al. 2010, *MNRAS*, 401, 160
- Barger, A. J., Cowie, L. L., Sanders, D. B., et al. 1998, *Natur*, 394, 248
- Baugh, C. M., Lacey, C. G., Frenk, C. S., et al. 2005, *MNRAS*, 356, 1191
- Becker, R. H., White, R. L., & Helfand, D. J. 1995, *ApJ*, 450, 559
- Bendo, G. J., Griffin, M. J., Bock, J. J., et al. 2013, *MNRAS*, 433, 3062
- Bertoldi, F., Carilli, C., Aravena, M., et al. 2007, *ApJS*, 172, 132
- Béthermin, M., Daddi, E., Magdis, G., et al. 2012, *ApJL*, 757, L23
- Béthermin, M., Dole, H., Lagache, G., Le Borgne, D., & Penin, A. 2011, *A&A*, 529, A4
- Blain, A. W., Barnard, V. E., & Chapman, S. C. 2003, *MNRAS*, 338, 733
- Blain, A. W., & Longair, M. S. 1993, *MNRAS*, 264, 509
- Blain, A. W., Smail, I., Ivison, R. J., Kneib, J.-P., & Frayer, D. T. 2002, *PhR*, 369, 111
- Borys, C., Chapman, S., Halpern, M., & Scott, D. 2003, *MNRAS*, 344, 385
- Bouwens, R. J., Illingworth, G. D., Franx, M., & Ford, H. 2007, *ApJ*, 670, 928
- Capak, P. L., Riechers, D., Scoville, N. Z., et al. 2011, *Natur*, 470, 233
- Capozzi, D., Collins, C. A., Stott, J. P., Hilton, M., et al. 2012, *MNRAS*, 419, 2821
- Casey, C. M., Berta, S., Béthermin, M., et al. 2012, *ApJ*, 761, 140
- Chapin, E. L., Chapman, S. C., Coppin, K. E., et al. 2011, *MNRAS*, 411, 505
- Chapman, S. C., Blain, A. W., Smail, I., & Ivison, R. J. 2005, *ApJ*, 622, 772
- Clements, D. L., Rigby, E., Maddox, S., et al. 2010, *A&A*, 518, L8
- Combes, F., Rex, M., Rawle, T. D., et al. 2012, *A&A*, 538, L4
- Condon, J. J., Cotton, W. D., Greisen, E. W., et al. 1998, *AJ*, 115, 1693
- Conley, A., Cooray, A., Vieira, J. D., et al. 2011, *ApJL*, 732, L35
- Coppin, K. E. K., Chapin, E. L., Mortier, A. M. J., et al. 2006, *MNRAS*, 372, 1621
- Coppin, K. E. K., Smail, I., Alexander, D. M., et al. 2009, *MNRAS*, 395, 1905
- Cox, P., Krips, M., Neri, R., et al. 2011, *ApJ*, 740, 63
- Daddi, E., Dannerbauer, H., Krips, M., et al. 2009, *ApJL*, 695, L176
- Dannerbauer, H., Lehnert, M. D., Lutz, D., et al. 2002, *ApJ*, 573, 473
- Diolaiti, E., Bendinelli, O., Bonaccini, D., et al. 2000, *A&AS*, 147, 335
- Draine, B. T. 2006, *ApJ*, 636, 1114
- Dunne, L., Eales, S. A., & Edmunds, M. G. 2003, *MNRAS*, 341, 589
- Eales, S., Dunne, L., Clements, D., et al. 2010, *PASP*, 122, 499
- Eales, S., Lilly, S., Webb, T., et al. 2000, *AJ*, 120, 2244
- Earle, L., Ade, P., Aguirre, J., et al. 2006, *Proc. SPIE*, 6275, 627510
- Fernandez-Conde, N., Lagache, G., Puget, J.-L., & Dole, H. 2008, *A&A*, 481, 885
- Fixsen, D. J., Dwek, E., Mather, J. C., Bennett, C. L., & Shafer, R. A. 1998, *ApJ*, 508, 123
- Foreman-Mackey, D., Hogg, D. W., Lang, D., & Goodman, J. 2013, *PASP*, 125, 306
- Franceschini, A., Rodighiero, G., Vaccari, M., et al. 2010, *A&A*, 517, A74
- Fu, H., Cooray, A., Feruglio, C., et al. 2013, *Natur*, 498, 338
- Glenn, J., Ade, P. A. R., Amarie, M., et al. 2003, *Proc. SPIE*, 4855, 30
- Glenn, J., Conley, A., Béthermin, M., et al. 2010, *MNRAS*, 409, 109
- Greve, T. R., Ivison, R. J., Bertoldi, F., et al. 2004, *MNRAS*, 354, 779
- Greve, T. R., Vieira, J. D., Weiß, A., et al. 2012, *ApJ*, 756, 101
- Griffin, M. J., Abergel, A., Abreu, A., et al. 2010, *A&A*, 518, L3
- Hayward, C. C., Narayanan, D., Kereš, D., et al. 2013, *MNRAS*, 428, 2529
- Hodge, J. A., Karim, A., Smail, I., et al. 2013, *ApJ*, 768, 91
- Hughes, D. H., Serjeant, S., Dunlop, J., et al. 1998, *Natur*, 394, 241
- Ivison, R. J., Greve, T. R., Dunlop, J. S., et al. 2007, *MNRAS*, 380, 199
- Ivison, R. J., Magnelli, B., Ibar, E., et al. 2010, *A&A*, 518, L31
- Kaviraj, S., Cohen, S., Ellis, R. S., et al. 2013, *MNRAS*, 428, 925
- Kennicutt, R. C., Jr. 1998, *ApJ*, 498, 541
- Kovács, A., Chapman, S. C., Dowell, C. D., et al. 2006, *ApJ*, 650, 592
- Lagache, G., Dole, H., Puget, J.-L., et al. 2004, *ApJS*, 154, 112
- Lagache, G., Puget, J.-L., & Dole, H. 2005, *ARA&A*, 43, 727
- Laurent, G. T., Aguirre, J. E., Glenn, J., et al. 2005, *ApJ*, 623, 742
- Le Borgne, D., Elbaz, D., Ocvirk, P., & Pichon, C. 2009, *A&A*, 504, 727
- Levenson, L., Marsden, G., Zemcov, M., et al. 2010, *MNRAS*, 409, 83
- Lupu, R. E., Scott, K. S., Aguirre, J. E., et al. 2012, *ApJ*, 757, 135
- Magnelli, B., Lutz, D., Santini, P., et al. 2012, *A&A*, 539, A155
- Marsden, D., Gralla, M., Marriage, T. A., et al. 2013, arXiv:1306.2288
- Michałowski, M. J., Dunlop, J. S., Ivison, R. J., et al. 2012, *MNRAS*, 426, 1845
- Mocanu, L. M., Crawford, T. M., Vieira, J. D., et al. 2013, *ApJ*, 779, 61
- Morrison, G. E., Owen, F. N., Dickinson, M., Ivison, R. J., & Ibar, E. 2010, *ApJS*, 188, 178
- Negrello, M., Perrotta, F., González-Nuevo, J., et al. 2007, *MNRAS*, 377, 1557
- Nguyen, H. T., Schulz, B., Levenson, L., et al. 2010, *A&A*, 518, L5
- Oke, J. B., Cohen, J. G., Carr, M., et al. 1995, *PASP*, 107, 375
- Oliver, S. J., Bock, J., Altieri, B., et al. 2012, *MNRAS*, 424, 1614
- Oliver, S. J., Wang, L., Smith, A. J., et al. 2010, *A&A*, 518, L21
- Owen, F. N., & Morrison, G. E. 2008, *AJ*, 136, 1889
- Perera, T. A., Chapin, E. L., Austermann, J. E., et al. 2008, *MNRAS*, 391, 1227
- Pilbratt, G. L., Riedinger, J. R., Passvogel, T., et al. 2010, *A&A*, 518, 1
- Pope, A., Borys, C., Scott, D., et al. 2005, *MNRAS*, 358, 149
- Rangwala, N., Maloney, P. R., Glenn, J., et al. 2011, *ApJ*, 743, 94
- Richards, G. T., Deo, R. P., Lacy, M., et al. 2009, *AJ*, 137, 3884
- Riechers, D. A., Bradford, C. M., Clements, D. L., et al. 2013, *Natur*, 496, 329
- Riechers, D. A., Capak, P. L., Carilli, C. L., et al. 2010, *ApJL*, 720, L131
- Robitaille, T. P., Tollerud, E. J., Greenfield, P., et al. 2013, *A&A*, 558, A33
- Roseboom, I. G., Oliver, S. J., Kunz, M., et al. 2010, *MNRAS*, 409, 48
- Schwartz, P. R. 1982, *ApJ*, 252, 589
- Scott, K. S., Austermann, J. E., Perera, T. A., et al. 2008, *MNRAS*, 385, 2225
- Scott, S. E., Fox, M. J., Dunlop, J. S., et al. 2002, *MNRAS*, 331, 817
- Smail, I., Ivison, R. J., & Blain, A. W. 1997, *ApJL*, 490, L5
- Smith, A. J., Wang, L., Oliver, S. J., et al. 2012, *MNRAS*, 419, 377
- Sobral, D., Best, P. N., Matsuda, Y., et al. 2012, *MNRAS*, 420, 1926
- Stott, J. P., Collins, C. A., Burke, C., Hamilton-Morris, V., & Smith, G. P. 2011, *MNRAS*, 414, 445
- Swinbank, A. M., Karim, A., Smail, I., et al. 2012, *MNRAS*, 427, 1066
- Swinbank, A. M., Smail, I., Longmore, S., et al. 2010, *Natur*, 464, 733
- Valiante, E., Lutz, D., Sturm, E., Genzel, R., & Chapin, E. L. 2009, *ApJ*, 701, 1814
- Vieira, J. D., Marrone, D. P., Chapman, S. C., et al. 2013, *Natur*, 495, 344
- Viero, M. P., Wang, L., Zemcov, M., et al. 2013, *ApJ*, 772, 77
- Walter, F., Decarli, R., Carilli, C., et al. 2012, *Natur*, 486, 233
- Wardlow, J. L., Cooray, A., De Bernardis, F., et al. 2013, *ApJ*, 762, 59
- Weiß, A., De Breuck, C., Marrone, D. P., et al. 2013, *ApJ*, 767, 88
- Weiß, A., Kovács, A., Coppin, K., et al. 2009, *ApJ*, 707, 1201
- Wu, J., Tsai, C.-W., Sayers, J., et al. 2012, *ApJ*, 756, 96
- Xu, C., Lonsdale, C. J., Shupe, D. L., O’Linger, J., & Masci, F. 2001, *ApJ*, 562, 179
- Younger, J. D., Fazio, G. G., Huang, J.-S., et al. 2007, *ApJ*, 671, 1531
- Younger, J. D., Fazio, G. G., Huang, J.-S., et al. 2009, *ApJ*, 704, 803