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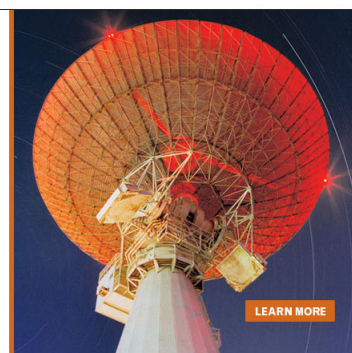
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# Ultrahigh electromechanical response in $(1-x)(\text{Na}_{0.5}\text{Bi}_{0.5})\text{TiO}_3-x\text{BaTiO}_3$ single-crystals via polarization extension

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The dielectric, ferroelectric, and electric field-induced strain response of [001]- and [101]-oriented  $0.944\text{Na}_{0.5}\text{Bi}_{0.5}\text{TiO}_3-0.056\text{BaTiO}_3$  ( $0.944\text{NBT}-0.056\text{BT}$ ) single crystals were investigated as a function of temperature and dc bias ( $E$ ). An ultrahigh electromechanical response with large amplitude longitudinal piezoelectric coefficients as high as  $d_{33} = 2500$  pm/V was found in [001]<sub>PC</sub> oriented  $0.944\text{NBT}-0.056\text{BT}$  single crystals near a depolarization temperature of  $T_d = 130$  °C. *In-situ* XRD revealed that the enhanced piezoelectric properties resulted from a polarization extension between a polar pseudocubic phase with a slight tetragonal ( $P4bm$ ) distortion and a polar tetragonal one with a large tetragonal distortion of  $c/a = 1.02$ . Our findings indicate a potential approach to high performance lead-free piezoelectrics, via polarization extension. © 2012 American Institute of Physics. [<http://dx.doi.org/10.1063/1.4709619>]

## I. INTRODUCTION

Lead zirconium titanate (PZT) ceramics are widely used in transducer, actuator, and other electromechanical applications. Lead has recently been expelled from many commercial applications and materials owing to concerns regarding its toxicity. This concern has stimulated significant research efforts in the search for high-performance lead-free piezoelectrics.<sup>1-7</sup>

In the search for lead-free materials with properties comparable to those of PZT, most efforts have focused on solid solutions having PZT-like morphotropic phase boundary (MPB) between tetragonal (T) and rhombohedral (R) ferroelectric phases.<sup>8</sup> It has been shown that phase transitions near MPBs between R and T phases actually occur by structurally bridging intermediate monoclinic (M) phases.<sup>9</sup> The high electromechanical responses are then believed to relate to symmetry-allowed polarization rotations<sup>10-13</sup> during which the transverse dielectric susceptibility  $\chi_{11}$  and shear piezoelectric coefficient  $d_{15}$  are enhanced as discussed by Damjanovic.<sup>14-19</sup> The large piezoelectric response along non-polar axes is, then, a consequence of the large  $\chi_{11}$  and  $d_{15}$  values.<sup>19,20</sup> Phenomenological calculations have also shown that the piezoelectric response along polar axes can be enhanced due to polarization extension.<sup>19-21</sup>

Solid solutions of  $(1-x)\text{Na}_{0.5}\text{Bi}_{0.5}\text{TiO}_3-x\text{BaTiO}_3$  (abbreviated as  $(1-x)\text{NBT}-x\text{BT}$ ) are potentially important lead-free piezoelectric systems, as their piezoelectric properties are enhanced near  $0.06 < x < 0.08$ .<sup>22,23</sup> Structural investigations revealed that  $(1-x)\text{NBT}-x\text{BT}$  has a coexistence of rhombohedral (R,  $\frac{\Delta P_3}{\Delta E_3}$ ) and tetragonal (T,  $P4bm$ ) phases for  $0.06 < x < 0.08$ .<sup>23</sup> The T ( $P4bm$ ) structure is distorted from cubic by in-phase rotations of the  $\text{TiO}_6$  octahedra about the [001]<sub>PC</sub>: according to the tilt system  $a^0a^0c^+$  (Glazer nota-

tion<sup>24</sup>), combined with antiparallel displacement of the  $\text{Na}^{1+}/\text{Bi}^{3+}$  and  $\text{Ti}^{4+}$  cations along [001]<sub>PC</sub>, where the subscript PC corresponds to the indexing of the directions on the pseudocubic cell setting. A view of the  $P4bm$  structure down the [010]<sub>PC</sub> showing the relative cation displacements are given in Fig. 6(a). The presence of  $a^0a^0c^+$  octahedral tilts gives rise to M-type superstructure reflections<sup>24</sup> such as  $1/2(310)_{\text{PC}}$ . The  $\text{Na}^{1+}/\text{Bi}^{3+}$  and  $\text{Ti}^{4+}$  cations displace almost equally in opposite directions along [001]<sub>PC</sub>, which results in the T ( $P4bm$ ) phase being only weakly polar. The R ( $R3c$ ) structure is characterized by  $a^-a^-a^-$  (Glazer notation<sup>24</sup>) anti-phase octahedral rotations about [111]<sub>PC</sub> combined with parallel displacement of the  $\text{Na}^{1+}/\text{Bi}^{3+}$  and  $\text{Ti}^{4+}$  cations along the [111]<sub>PC</sub> axis.<sup>25</sup> The presence of  $a^-a^-a^-$  octahedral tilts gives rise to R-type superstructure reflections<sup>24</sup> such as  $1/2(311)_{\text{PC}}$ . With increasing temperature from 25 °C to 200 °C, M-type reflections gain intensity, whereas R-type reflections gradually disappear.<sup>25</sup>

More recently, it was found when  $(1-x)\text{NBT}-x\text{BT}$  are co-modified with  $\text{K}_{0.5}\text{Na}_{0.5}\text{NbO}_3$  (or KNN) to form a  $(1-x-y)\text{NBT}-x\text{BT}-y\text{KNN}$  ternary system that the piezoelectric properties can be further enhanced by shifting the T ( $P4bm$ ) phase to room temperature.<sup>26</sup> In this case, the maximum strain can reach values of  $S_{\text{max}} = 0.45\%$  under applied fields of  $E = 80$  kV/cm.<sup>27</sup> The value of  $S_{\text{max}}/E_{\text{max}}$  then reaches 560 pm/V, which is higher than that for PZT ceramics.<sup>1</sup> These large property changes arise due to a field-induced transformation between nonpolar (or weakly polar) and ferroelectric phases.<sup>28</sup> High-resolution neutron diffraction has shown that the initial nonpolar (or weakly polar) phase of  $0.92\text{NBT}-0.06\text{BT}-0.02\text{KNN}$  has a T ( $P4bm$ ) structure with a tetragonal distortion of only 0.0258%.<sup>26</sup> By monitor the M- and R-type superstructure reflection changes under E-field, it was shown that the T ( $P4bm$ ) phase undergoes a reversible transformation to ferroelectric R ( $R3c$ ) phase, giving rise to large induced strains.<sup>26-28</sup> These results indicate that

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$(1-x)$ NBT- $x$ BT- $y$ KNN might be a solid solution whose piezoelectric properties are enhanced by a polarization extension mechanism.<sup>21</sup> However, in polycrystalline materials, only some grains are favorably oriented with respect to the E-field: thus, full advantage of polarization extension cannot be achieved and property enhancement may be limited with respect to its potential.<sup>21</sup>

In the present work,  $(1-x)$ NBT- $x$ BT single crystals were grown by a top-seeded solution growth (TSSG) method. An ultrahigh electromechanical response with large amplitude longitudinal piezoelectric coefficients as high as  $d_{33} = 2500$  pm/V in  $[001]_{PC}$  oriented 0.944NBT-0.056BT single crystals near a depolarization temperature of  $T_d = 130$  °C was obtained. Structural investigations show that this enhancement is due to polarization extension between weakly polar T ( $P4bm$ ) and strongly polar T phases under E applied along  $\langle 001 \rangle_{PC}$ .

## II. EXPERIMENTAL PROCEDURE

Single crystals of  $(1-x)$ NBT- $x$ BT were grown by a TSSG method using high purity (better than 99.99%)  $\text{Na}_2\text{CO}_3$ ,  $\text{Bi}_2\text{O}_3$ ,  $\text{TiO}_2$ , and  $\text{BaCO}_3$  as raw materials. These raw materials were mixed according to a stoichiometric ratio of  $(\text{Na}_{0.5}\text{Bi}_{0.5})_{0.9}\text{Ba}_{0.1}\text{TiO}_3$ , with a 20 wt. % excess of  $\text{Na}_2\text{CO}_3$  and  $\text{Bi}_2\text{O}_3$  as a self-flux. The mixed raw materials were put into a platinum crucible and heated to 1100 °C for 10 h to decompose the carbonates. Then  $(1-x)$ NBT- $x$ BT single crystals were grown using a  $\langle 001 \rangle_{PC}$  oriented NBT crystal seed, which was heated by using a resistance furnace under an air atmosphere. The pulling rate was 1.2–1.5 mm/day and the rotating rate was 10 rpm. After growth, the crystals were removed from the flux-melt surface and cooled to room temperature at a rate of 30 °C/h.

The concentrations of Ba ions in the as-grown condition were determined by inductive coupled plasma atomic emission spectrometry (ICP-AES) to be 5.6 at. %. Pseudocubic  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$  oriented 0.944NBT-0.056BT crystal wafers with dimensions of  $2 \times 2 \times 0.4$  mm<sup>3</sup> were cut from the boule and subsequently electroded on both surfaces with gold. Temperature dependent dielectric constant measurements were performed using a LCR meter (HP 4284 A) under zero-field heating conditions in the temperature range of 30 to 600 °C. Polarization (P-E) and unipolar strain ( $\epsilon$ -E) hysteresis loops were measured at a frequency of 1 Hz, using a modified Sawyer-Tower circuit and a linear variable differential transducer (LVDT) driven by a lock-in amplifier (Stanford Research, SR850) in the temperature range from 25 °C to 180 °C. Longitudinal piezoelectric  $d_{33}$  constants were measured using a quasistatic Berlincourt meter. E-Field dependent  $(200)_{PC}$ ,  $(220)_{PC}$ , and  $(222)_{PC}$   $2\theta$  line scans and reciprocal-space ( $\omega$  versus  $2\theta$ ) maps were taken at various temperatures with increasing E-field between 0 and 20 kV/cm and then decreasing E-field from 20 to 0 kV/cm. These studies were done using a Philips MPD high-resolution x-ray diffraction system, equipped with a two bounce hybrid monochromator, an open three-circle Eulerian cradle, and a domed hot-stage. A Ge (220)-cut crystal was

used as an analyzer, which had an angular resolution of 0.0068°. The x-ray wavelength was that of  $\text{CuK}_\alpha = 1.5406$  Å, and the x-ray generator was operated at 45 kV and 40 mA. During all the *in-situ* x-ray measurements, the E-field was applied along the  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$  directions. The M-type superstructure reflections corresponding to the T ( $P4bm$ ) structure of 0.944NBT-0.056BT were measured with  $[001]_{PC}$  oriented crystals on the synchrotron radiation diffraction beam line 11-ID-C ( $\lambda = 0.10798$  Å and  $E = 114.8$  keV) at the Advanced Photon Sources (Argonne National Laboratory). The beam size was set to be  $0.3 \times 0.3$  mm<sup>2</sup> by tungsten slits. The diffraction images were collected in the forward direction using a Perkin-Elmer large area detector.

## III. RESULTS

### A. Dielectric, ferroelectric, and piezoelectric properties

Figure 1(a) shows the dielectric constant  $\epsilon_r$  and loss factor  $\tan \delta$  as a function of temperature for  $\langle 001 \rangle_{PC}$  oriented 0.944NBT-0.056BT, taken on heating. The results reveal a diffuse phase transformation with a broad dielectric maximum near  $T_m = 285$  °C, near and just below which the dielectric constant was frequency independent. The so-called depolarization temperature ( $T_d$ ) inherent to NBT (Ref. 29) was found to be decreased to  $T_d = 145$  °C, below which notably frequency dispersion was found. The temperature  $T_d$  was frequency dependent and shifted to higher temperature with increasing frequency. Near  $T_d$ , a peak was found in the dielectric loss factor at 130 °C, below which  $\tan \delta$  was notably frequency dispersive. Please note that the dispersion in dielectric constant and loss factor was similar to that of relaxors below  $T_{max}$ ,<sup>30</sup> indicating polar heterogeneities with low frequency fluctuations.

Figure 1(b) shows polarization (P-E) hysteresis loops for  $\langle 001 \rangle_{PC}$  oriented 0.944NBT-0.056BT at various temperatures. At room temperature, the P-E loop saturated for  $E \leq 50$  kV/cm, exhibiting a shape typical of ferroelectrics. The saturation polarization ( $P_s$ ), remnant polarization ( $P_r$ ) and coercive field ( $E_c$ ) were  $49.5$   $\mu\text{C}/\text{cm}^2$ ,  $46.4$   $\mu\text{C}/\text{cm}^2$ , and 28 kV/cm at room temperature. With increasing temperature between 25 °C and 100 °C, the values of  $P_s$ ,  $P_r$ , and  $E_c$  were slightly decreased. On heating above 100 °C,  $P_s$  decreased slightly whereas  $P_r$  and  $E_c$  decreased sharply to  $9.83$   $\mu\text{C}/\text{cm}^2$  and 7 kV/cm. As a consequence, the hysteresis loop became “pinched” near 100 °C, which could indicate the coexistence of ferroelectric (FE) and nonpolar phases. With further increase of temperature towards  $T_d$ , the nonpolar phase became the dominant one, as can be seen from the double P-E loops at 130 °C and 150 °C where  $P_r \approx 0$ . These results in good agreement with previous reported P-E loops for 0.944NBT-0.056BT (Ref. 22) and 0.93NBT-0.06BT-0.01KNN (Ref. 28) ceramics. The temperature dependence of  $P_s$  and  $P_r$  is summarized in Fig. 1(c). The most notable change was a sharp drop in  $P_r$ : from about  $39.3$   $\mu\text{C}/\text{cm}^2$  at 80 °C to  $9.83$   $\mu\text{C}/\text{cm}^2$  at 100 °C, which then asymptotically converged to zero on heating to  $T_d$ , whereas,  $P_s$  slowly decreased from  $49.5$   $\mu\text{C}/\text{cm}^2$  to  $24.9$   $\mu\text{C}/\text{cm}^2$  with increasing temperature between 25 °C and 150 °C.

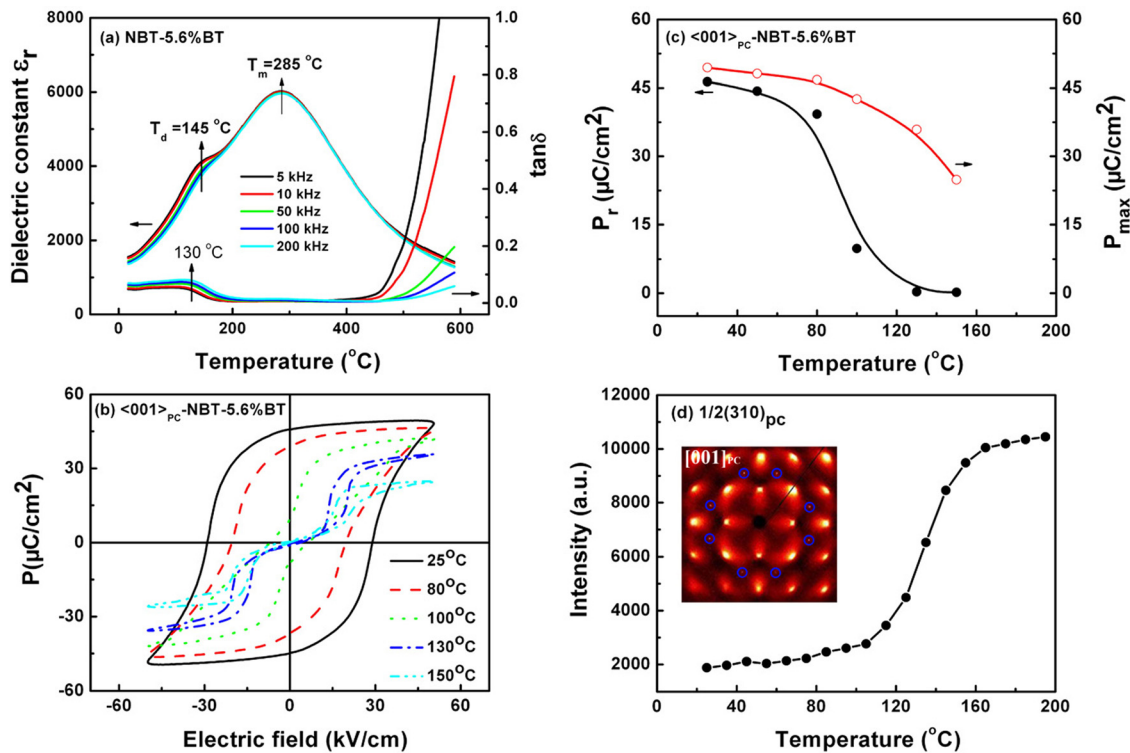


FIG. 1. (a) Temperature dependence of the dielectric constant  $\epsilon_r$  and loss factor  $\tan \delta$ ; (b) polarization (P-E) hysteresis loops at various temperatures; (c) temperature dependence of the remnant polarization ( $P_r$ ) and induced maximum polarization ( $P_{max}$ ) under  $E_{max} = 50$  kV/cm; and (d) diffraction intensity of the  $1/2(310)_{PC}$  peak as a function of temperature for  $(001)_{PC}$  oriented 0.944NBT-0.056BT crystal taken on heating. The inset in (d) shows the x-ray scattering imaging pattern at  $150^\circ\text{C}$ . Circled spots indicate the presence of  $1/2(310)$  super-lattice reflections corresponding with the  $a^0a^0c^+$  ( $P4bm$ ) octahedra tilting system.

The true nature of  $T_d$  is not yet fully understood.<sup>29,31–33</sup> Previously structural studies indicated that  $(1-x)\text{NBT}-x\text{BT}$  near the MPB does not have a notable deviation from cubic symmetry in the temperature range of 25 and  $350^\circ\text{C}$ .<sup>23,27,34–36</sup> We conjecture that  $T_d$  is related to an  $a^-a^-a^- \rightarrow a^0a^0c^+$  octahedral tilting transition. Figure 1(d) shows the temperature dependence of the  $1/2(310)_{PC}$  super-lattice reflection in the temperature range between  $25^\circ\text{C}$  and  $200^\circ\text{C}$ . The inset of this figure shows a synchrotron x-ray scattering imaging pattern along  $[001]_{PC}$  at  $130^\circ\text{C}$ . The circled spots show the presence of  $1/2(310)_{PC}$  super-lattice reflections, which indicate the existence of  $T$  ( $P4bm$ ) structural regions having  $a^0a^0c^+$  octahedral tilts. From Fig. 1(d), it can be seen that the intensities of these  $1/2(310)_{PC}$  super-lattice reflections remained measurable at room temperature. This is consistent with previous transmission electron microscopy (TEM)<sup>37,38</sup> and neutron diffraction<sup>36</sup> studies which revealed the coexistence of dominant  $a^-a^-a^-$ -tilted ( $R3c$ ) and small volume fractions of  $a^0a^0c^+$ -tilted ( $P4bm$ ) structures for MPB  $(1-x)\text{NBT}-x\text{BT}$ . At room temperature, the dominant phase of 0.944NBT-0.056BT was  $R3c$ , with  $P_r = 46.4 \mu\text{C}/\text{cm}^2$ . The volume fraction of the  $R3c$  phase was decreased with increasing temperature, whereas that of the weakly polar  $P4bm$  one increased. With increasing temperature between  $100^\circ\text{C}$  and  $T_d$ , the intensity of the  $1/2(310)_{PC}$  super-lattice reflection increased significantly (see Fig. 1(d)), indicating a transition from the polar  $R3c$  phase to a weakly polar  $P4bm$  one. This  $R3c \rightarrow P4bm$  transition is consistent with changes in  $P_r$  which sharply decreased to zero at  $130^\circ\text{C}$  (see Fig. 1(c)). Even though the  $P4bm$  phase is weakly polar

at  $130^\circ\text{C}$ , it could be fully saturated with  $P_s = 35.9 \mu\text{C}/\text{cm}^2$  under  $E = 50$  kV/cm.

Figures 2(a) and 2(b) show  $\epsilon$ -E curves for 0.944NBT-0.056BT measured along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$  at various temperatures under a maximum ac electric field of  $E_{max} = 20$  kV/cm. Below  $100^\circ\text{C}$ , the  $\epsilon$ -E curves were nearly linear and anhysteretic. The maximum strains at  $25^\circ\text{C}$  was  $S_{max} = 0.08\%$  and  $0.04\%$  along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$ , respectively. An approximation of the large signal value of  $d_{33}$  was derived from the slope of the  $\epsilon$ -E curves: which were about  $400$  pm/V and  $200$  pm/V along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$ , which are close to the values of  $380$  pC/N and  $190$  pC/N measured by a Berlincourt meter. At  $100^\circ\text{C}$ , the value of  $S_{max}$  increased modestly to  $0.17\%$  and  $0.06\%$  along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$ . On heating to  $130^\circ\text{C}$  and  $120^\circ\text{C}$ , the value of  $S_{max}$  increased significantly, reaching values of  $0.60\%$  and  $0.20\%$  along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$  under  $E = 20$  kV/cm. With further increase of temperature,  $S_{max}$  decreased along both directions: in fact, no induced strain was apparent at  $180^\circ\text{C}$  even for  $E = 20$  kV/cm.

The temperature dependent ratio of  $S_{max}/E_{max}$  is shown in Figure 2(c). The value of  $S_{max}/E_{max}$  along  $\langle 001 \rangle_{PC}$  was higher than that along  $\langle 101 \rangle_{PC}$  in the temperature range of  $25^\circ\text{C}$  to  $170^\circ\text{C}$ . Below  $110^\circ\text{C}$ ,  $S_{max}/E_{max}$  along  $\langle 101 \rangle_{PC}$  varied in the range of  $200$ – $310$  pm/V, whereas along  $\langle 001 \rangle_{PC}$ , it ranged between  $400$  and  $1000$  pm/V. A sharp increase in  $S_{max}/E_{max}$  was observed along both directions near  $120^\circ\text{C}$  to  $130^\circ\text{C}$ : values as high as  $3000$  pm/V ( $130^\circ\text{C}$ ) and  $1000$  pm/V ( $120^\circ\text{C}$ ) were found along  $\langle 001 \rangle_{PC}$  and  $\langle 101 \rangle_{PC}$ , respectively. These values are higher than those

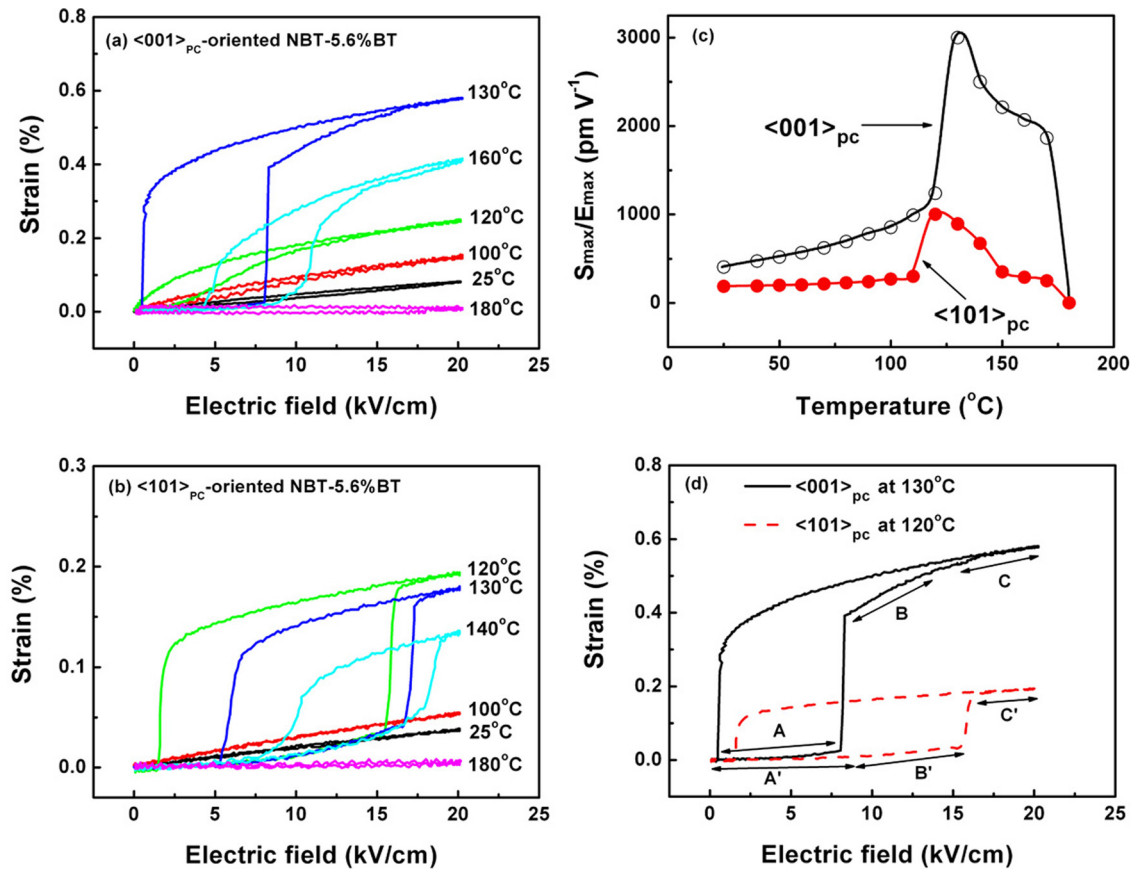


FIG. 2. Unipolar strain ( $\epsilon$ - $E$ ) hysteresis loops of 0.944NBT-0.056BT measured along (a)  $\langle 001 \rangle_{PC}$  and (b)  $\langle 101 \rangle_{PC}$  at various temperatures; (c)  $S_{max}/E_{max}$  as determined from the unipolar strain curves; and (d) a comparison of the  $\epsilon$ - $E$  curves measured along  $\langle 001 \rangle_{PC}$  with that measured along  $\langle 101 \rangle_{PC}$  at 130°C and 120°C, respectively. The longitudinal piezoelectric coefficient  $d_{33}$  derived from the slope of steps A, B, C and A', B', and C' are summarized in Table I.

previously reported for other Pb-free and Pb-containing piezo-ceramics and are comparable to those of Pb-containing relaxor-based single crystals.<sup>1,27,39-45</sup>

A comparison of the  $\epsilon$ - $E$  curves along  $\langle 001 \rangle_{PC}$  (solid line) and  $\langle 101 \rangle_{PC}$  (dashed line) (at 130°C and 120°C, respectively) is given in Figure 2(d). Three steps are identified in this figure that has notably different slopes in the  $\epsilon$ - $E$  curves with increasing  $E$  along both directions. Large amplitude values for  $d_{33}$  derived from the  $\epsilon$ - $E$  slope for these steps are summarized in Table I. Along  $\langle 001 \rangle_{PC}$ , the value of  $d_{33}$  was 350 pm/V, 2500 pm/V, and 720 pm/V for regions A (0–8 kV/cm), B (9–16 kV/cm), and C (16–20 kV/cm); whereas, along  $\langle 101 \rangle_{PC}$ , the values were 75 pm/V, 485 pm/V, and 420 pm/V for regions A' (0–9 kV/cm), B' (10–15 kV/cm) and C' (16–20 kV/cm). Clearly, there is the potential for giant  $d_{33}$  values in the vicinity of steps B and C: which might exceed that of conventional PZT ceramics<sup>46</sup> and which might be comparable to that of Pb-containing relaxor-based piezo-crystals.<sup>44,45</sup> However, the question must be asked: what is the mechanism of this large response?

## B. Structural studies

To better understand the mechanism of this giant induced strain and large amplitude  $d_{33}$  value at 130°C, *in-situ* high resolution x-ray diffraction (XRD) studies under  $E//\langle 001 \rangle_{PC}$  and  $E//\langle 101 \rangle_{PC}$  were performed for

$0 \leq E \leq 20$  kV/cm. Figures 3(a)–3(c) show  $(002)_{PC}$ ,  $(202)_{PC}$ , and  $(111)_{PC}$  line scans taken at 130°C for  $E//\langle 001 \rangle_{PC}$ . The intensity is plotted on a sqrt scale, so that small peaks with low intensity can be more clearly seen. Under  $E = 0$  kV/cm, only a single sharp  $2\theta$  peak was observed along the  $(002)_{PC}$ ,  $(202)_{PC}$ , and  $(111)_{PC}$  zones: which was also evident in  $\omega$ - $2\theta$  area scans (see Figs. 5(a), 5(d), and 5(g)). The peak positions occurred  $2\theta = 46.423^\circ$ ,  $67.769^\circ$ , and  $39.930^\circ$  for  $(002)_{PC}$ ,  $(202)_{PC}$ , and  $(111)_{PC}$ . The calculated d-spacing for these diffraction planes are consistent with a cubic structure having a lattice parameter of  $a = 3.909 \pm 0.002$  Å. However, the  $\frac{1}{2}(310)_{PC}$  super-lattice reflection in the synchrotron x-ray scattering imaging pattern at 130°C (see inset of Fig. 1(d)) reveals that  $a^0_0c^+$  tilts exist in 0.944NBT-0.056BT, indicating slight tetragonal ( $P4bm$ ) distortions which are too small to be detected within the resolution limit of our XRD system.

In Figure 3(a), it can be seen that the  $(002)_{PC}$  peak was shifted slightly towards lower angles with increasing  $E$  between  $0 \leq E \leq 8$  kV/cm. For  $E = 9$  kV/cm, the  $(002)_{PC}$  peak became much weaker and a new peak with a stronger intensity appeared at  $2\theta = 46.065^\circ$ , indicating an E-field induced transformation. The E-field induced transformation was also reflected by changes in the  $(202)_{PC}$  and  $(111)_{PC}$  peak positions, as shown in Figures 3(b) and 3(c). Under 20 kV/cm, the dominant peaks were at  $2\theta = 46.016^\circ$ ,  $67.568^\circ$ , and  $39.899^\circ$  which were along the  $(002)_{PC}$ ,  $(202)_{PC}$ ,

TABLE I. Longitudinal piezoelectric coefficient  $d_{33}$  derived from the slope of steps A, B, and C of the  $\epsilon$ -E curve along  $\langle 001 \rangle_{\text{PC}}$  (at  $130^\circ\text{C}$ ) and A', B', and C' of the  $\epsilon$ -E curve along  $\langle 101 \rangle_{\text{PC}}$  (at  $120^\circ\text{C}$ ) directions at  $130^\circ\text{C}$  (see Fig. 2(d)).

	$d_{33}$ (pm/V) along $\langle 001 \rangle_{\text{PC}}$	$d_{33}$ (pm/V) along $\langle 101 \rangle_{\text{PC}}$
Step A	350 (PC phase)	75 (PC phase)
Step B	2500 (PC+T)	485 (PC+T+R)
Step C	720 (T)	420 (T+R)

and  $(111)_{\text{PC}}$  zones, respectively. The calculated d-spacing for the  $(002)_{\text{PC}}$ ,  $(202)_{\text{PC}}$ , and  $(111)_{\text{PC}}$  diffraction planes were consistent with a tetragonal structure having lattice parameters of  $(a_t, c_t) = (3.895, 3.942)\text{\AA}$ . Figures 5(b), 5(e), and 5(h) show  $\omega$ - $2\theta$  area scans at  $130^\circ\text{C}$  under  $E_{\parallel[001]_{\text{PC}}} = 20\text{ kV/cm}$  taken about  $(002)_{\text{PC}}$ ,  $(202)_{\text{PC}}$ , and  $(111)_{\text{PC}}$ , respectively. Only a single domain was observed in each of these scans, indicating the presence of a well-developed tetragonal c-domain state. The tetragonal distortion  $(c_t/a_t - 1)$  was 0.012.

The evolution of the  $(002)_{\text{PC}}$  peak profiles under E is shown in Figure 3(a). This data clearly reveal a transformation from a pseudo-cubic phase with a small tetragonal distortion to a T phase with a strong tetragonal distortion with increasing  $E_{\parallel[001]_{\text{PC}}}$ . For  $0 < E < 8\text{ kV/cm}$ , the peak position of  $2\theta$  value for  $(001)_{\text{PC}}$  was slightly shifted towards lower angle, indicating a slight extension of the crystal lattice along  $[001]_{\text{PC}}$ . This is consistent with the induced strain

for step A in the  $\epsilon$ -E curve along  $[001]_{\text{PC}}$  at  $130^\circ\text{C}$  (see Figure 2(d)). With increasing E to  $9\text{ kV/cm}$ , an intense  $(002)_{\text{T}}$  peak became apparent, whereas the  $(002)_{\text{PC}}$  became weaker. Clearly, a transformation to a T phase with a large c/a occurred. The intensity of  $(002)_{\text{PC}}$  became increasingly weak for  $E > 9\text{ kV/cm}$  and was undetectable for  $E \geq 16\text{ kV/cm}$ . These results indicate that the pseudo-cubic and T phases coexist for  $9\text{ kV/cm} < E < 16\text{ kV/cm}$  and that the volume fraction of the T phase is gradually increased. Above  $E = 16\text{ kV/cm}$ , the entire crystal is transformed to a single domain T state. The ultrahigh value of the large signal  $d_{33}$  value of step B in the  $\epsilon$ -E curve (see Fig. 2(d)) may then be a consequence of this coexistence and reflected in an E-field induced change in the volume fraction, via length extension polarization mode. The large signal  $d_{33}$  value of  $720\text{ pm/V}$  for  $E \geq 16\text{ kV/cm}$  for single c-domain state of step C (see Fig. 2(d)) is quite high, again indicating a polarization extension mode.

Figures 4(a)–4(c) show *in-situ* XRD line scans for  $(202)_{\text{PC}}$ ,  $(002)_{\text{PC}}$ , and  $(111)_{\text{PC}}$  reflections under  $E_{\parallel[101]_{\text{PC}}}$  at  $120^\circ\text{C}$  with increasing field for  $0 \leq E \leq 20\text{ kV/cm}$ . Under  $E = 0\text{ kV/cm}$ , only a single sharp peak was observed along each zone at  $120^\circ\text{C}$ . The peak positions were determined to be  $2\theta = 46.494^\circ$ ,  $67.853^\circ$ , and  $39.975^\circ$ , respectively, and the lattice parameters of this pseudo-cubic structure were  $a = 3.903 \pm 0.002\text{ \AA}$ . With increasing E in the range of 0 to  $8\text{ kV/cm}$ , the  $2\theta$  position of  $(202)_{\text{PC}}$  peak was slightly shifted

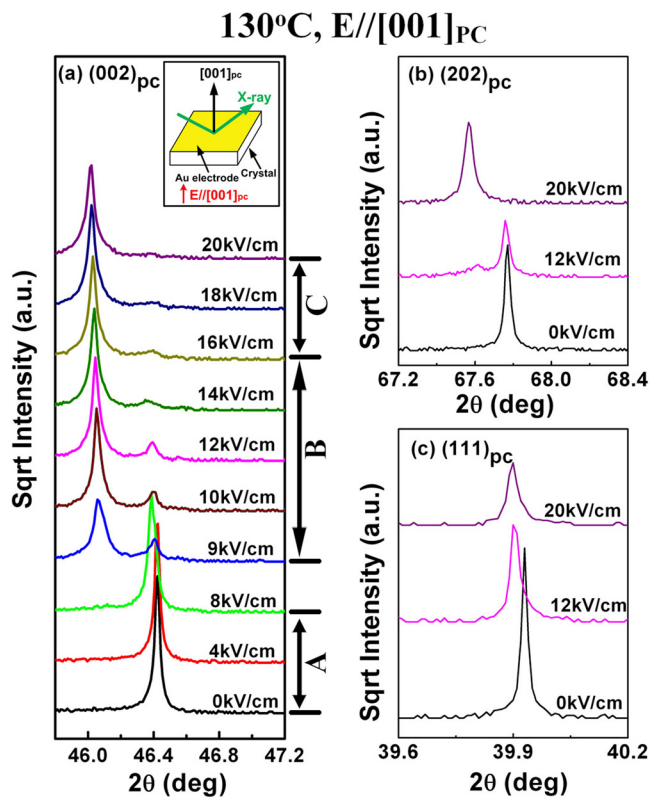


FIG. 3. *In-situ* x-ray line scans of (a)  $(002)_{\text{PC}}$ , (b)  $(202)_{\text{PC}}$ , and (c)  $(111)_{\text{PC}}$  with increasing E-field under  $E_{\parallel[001]_{\text{PC}}}$  for 0.944NBT-0.056BT crystals at  $130^\circ\text{C}$ . The E-field configuration during XRD measurements is shown in the inset of (a). Steps A, B, and C correspond to the steps on  $\epsilon$ -E curves along  $[001]_{\text{PC}}$  shown in Fig. 2(d).

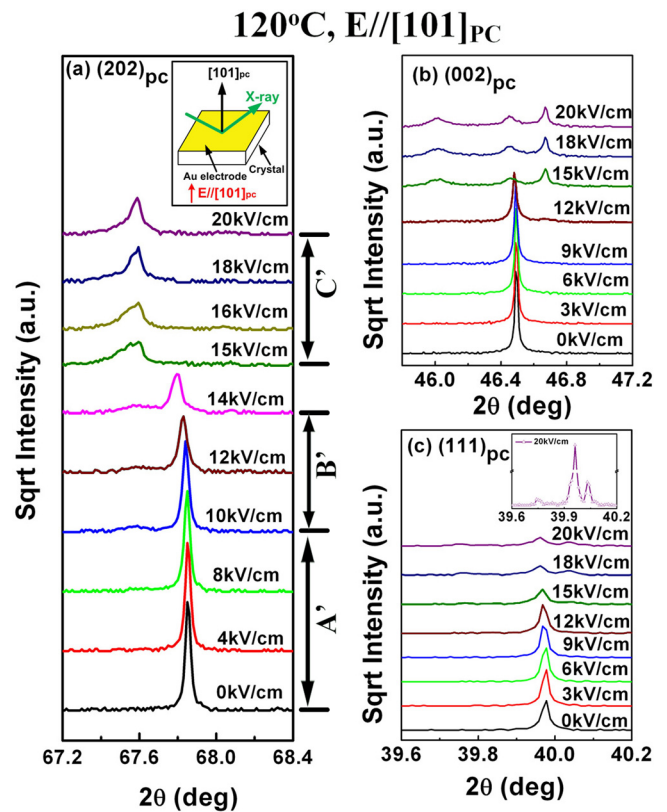


FIG. 4. *In-situ* x-ray line scans of (a)  $(202)_{\text{PC}}$ , (b)  $(002)_{\text{PC}}$ , and (c)  $(111)_{\text{PC}}$  with increasing E-field under  $E_{\parallel[101]_{\text{PC}}}$  for 0.944NBT-0.056BT crystals at  $120^\circ\text{C}$ . The E-field configuration during XRD measurements is shown in the inset of (a). Steps A', B', and C' correspond to the steps on  $\epsilon$ -E curves along  $[101]_{\text{PC}}$  shown in Fig. 2(d).

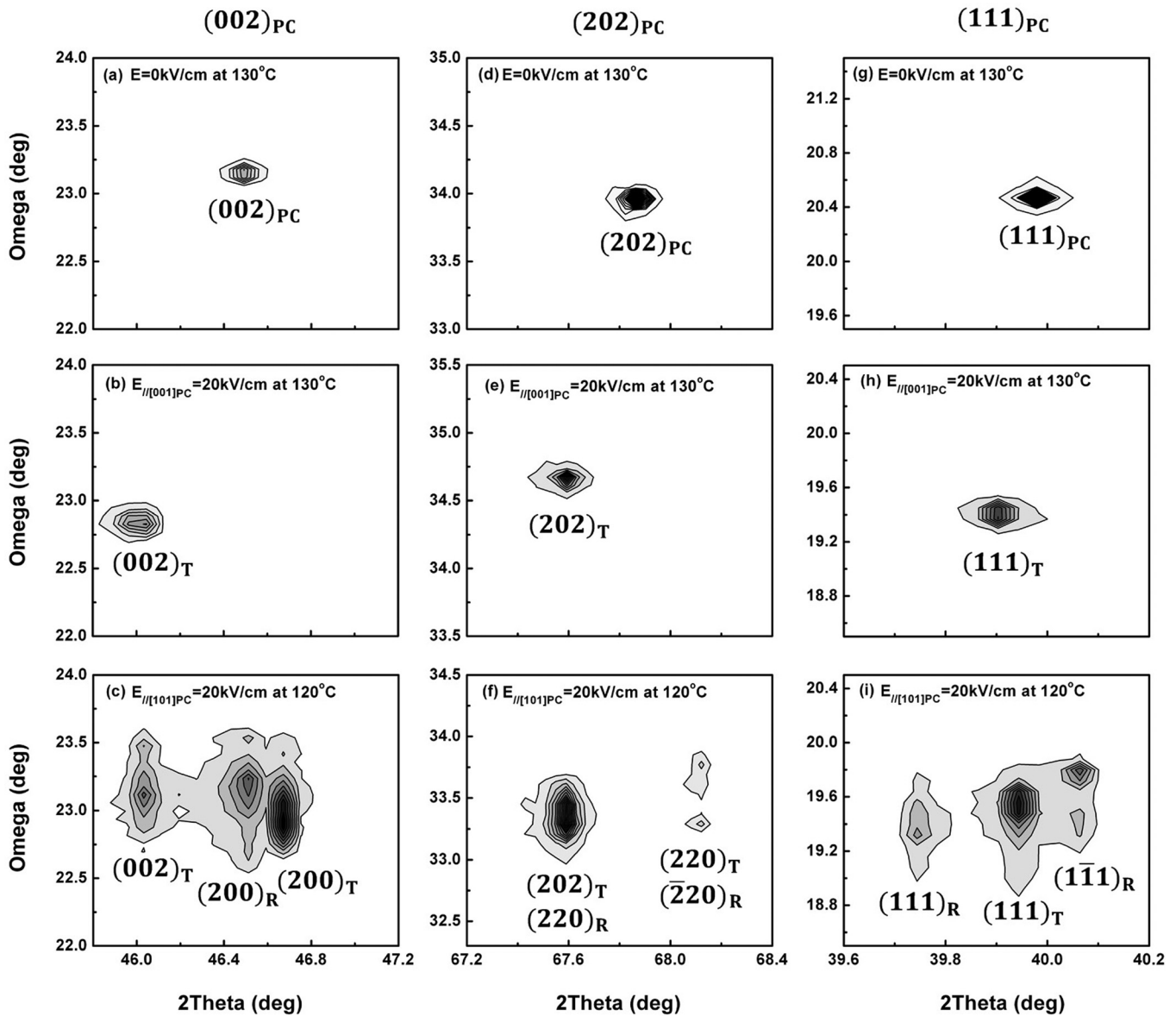


FIG. 5.  $\omega$ - $2\theta$  maps for  $(002)_{PC}$ ,  $(202)_{PC}$ , and  $(111)_{PC}$  collected [(a), (d), and (g) at  $130^\circ\text{C}$ ] under  $E=0\text{ kV/cm}$ , [(b), (e), and (h) at  $130^\circ\text{C}$ ] under  $E_{//[001]_{PC}}=20\text{ kV/cm}$ , and [(c), (f), and (i) at  $120^\circ\text{C}$ ] under  $E_{//[101]_{PC}}=20\text{ kV/cm}$ .

towards lower angle values. This shift became more pronounced at  $E=10\text{ kV/cm}$ , and a 2nd weaker peak at  $2\theta=67.557^\circ$  became noticeable. With further increasing  $E$ , the  $(202)_{PC}$  peak continually shifted to lower  $2\theta$  values and became weaker. For  $E \geq 15\text{ kV/cm}$ , the  $(202)_{PC}$  peak at  $67.853^\circ$  was nearly undetectable, and only a single asymmetry peak at  $2\theta=67.557^\circ$  was observable (see Fig. 4(a)). However, for  $E \geq 15\text{ kV/cm}$ , the  $(002)_{PC}$  peak exhibited a triplet splitting with peaks near  $2\theta=46.013^\circ$ ,  $46.453^\circ$ , and  $46.666^\circ$  (see Fig. 4(b)). And, for  $E=20\text{ kV/cm}$ , the  $(111)_{PC}$  peak exhibited a triplet splitting with  $2\theta=39.739^\circ$ ,  $39.957^\circ$ , and  $40.026^\circ$  (see Fig. 4(c)). The calculated d-spacing for  $(002)_{PC}$ ,  $(202)_{PC}$ , and  $(111)_{PC}$  diffraction plane under  $E=20\text{ kV/cm}$  reveals a coexistence of T ( $a_t, c_t$ ) =  $(3.890 \pm 0.002, 3.942 \pm 0.002)\text{ \AA}$  and R ( $a_r, c_r$ ) =  $(3.907 \pm 0.002\text{ \AA}, 89.644^\circ)$  phases.

Figures 5(c), 5(f), and 5(i) show  $\omega$ - $2\theta$  area scans at  $120^\circ\text{C}$  for  $E_{//[101]_{PC}}=20\text{ kV/cm}$  taken about  $(002)_{PC}$ ,

$(202)_{PC}$ , and  $(111)_{PC}$ . Multi-domain states can be seen in each of these scans. For the  $\omega$ - $2\theta$  area scan around  $(002)_{PC}$ , the three domain states with peaks at  $2\theta=46.013^\circ$ ,  $46.453^\circ$ , and  $46.666^\circ$  correspond to  $(002)_T$ ,  $(200)_R$ , and  $(200)_T$  reflections. Along  $(111)_{PC}$ , area scans show three domain states at  $2\theta=39.739^\circ$ ,  $39.957^\circ$ , and  $40.026^\circ$  that correspond to  $(111)_R$ ,  $(111)_T$ , and  $(\bar{1}\bar{1}\bar{1})_R$  reflections. And, along  $(202)_{PC}$ , two domains were found at  $2\theta=67.557^\circ$  and  $68.122^\circ$ , corresponding to  $(202)_T$  overlapped with  $(220)_R$  and to  $(220)_T$  overlapped with  $(\bar{2}\bar{2}\bar{0})_R$  reflections: the d-spacing of  $(202)_T$  and  $(220)_T$  is too close to those of  $(220)_R$  and  $(\bar{2}\bar{2}\bar{0})_R$  to be resolved. This overlap resulted in peak asymmetry ( $2\theta=67.557^\circ$ ) in the linear scan for  $E_{//[101]_{PC}} \geq 15\text{ kV/cm}$  (see Fig. 4(a)).

These results indicate two E-field induced phase transformation for  $E_{//[101]_{PC}} \geq 15\text{ kV/cm}$ : (i) pseudo-cubic (slightly T distortion)  $\rightarrow$  T (with strong T distortion) and (ii) pseudo-cubic  $\rightarrow$  R. Accordingly, the three steps in the  $\varepsilon$ -E

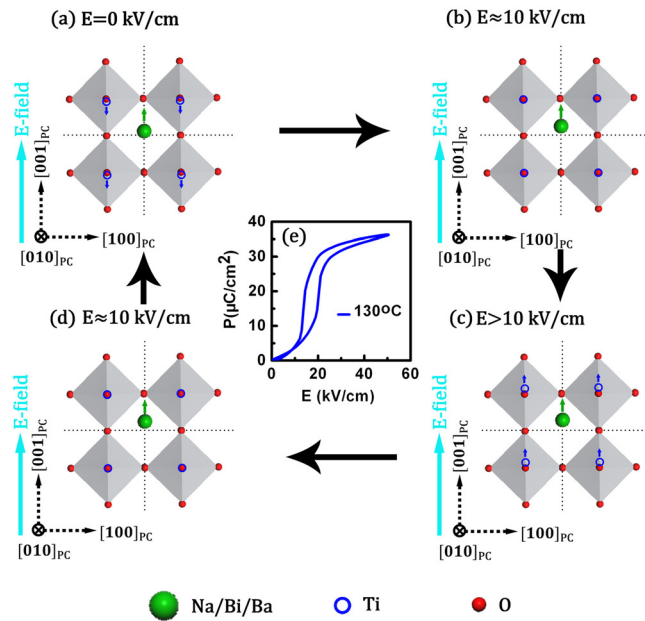


FIG. 6. Schematic illustrating the possible mechanism of polarization extension between weakly polar and strongly polar tetragonal phases, which is responsible for the ultrahigh electromechanical response in 0.944NBT-0.056BT single crystals along  $[001]_{PC}$  at  $130^\circ\text{C}$ : (a) Projection of the weakly polar tetragonal ( $P4bm$ ) structure along  $[010]_{PC}$ , showing the relative cation displacements. The large closed circles represent the Na/Bi sites, the small closed ones represent O sites, and the open circles represent Ti sites in the  $\text{TiO}_6$  octahedra; (b)  $\text{Ti}^{4+}$  cations go back to the center along  $[001]_{PC}$  direction under  $E \approx 10$  kV/cm; (c) E-field induced polar T phase with strong tetragonal distortion by moving  $\text{Ti}^{4+}$  cations away center along  $[001]_{PC}$  under  $E > 10$  kV/cm; and (d)  $\text{Ti}^{4+}$  cations go back to the center along  $[001]_{PC}$  direction under  $E \approx 10$  kV/cm during subsequent E-field decreasing cycle. After E-field removal, the sample was brought back to the initial weak polar  $P4bm$  phase (a).

curves (see Fig. 2(d)) can be identified from the structural data to be (i)  $E < 10$  kV/cm, stable pseudo-cubic or step A' where  $d_{33} = 75$  pm/V; (ii)  $10$  kV/cm  $\leq E \leq 14$  kV/cm, E-field induced T and R phases coexisting with a pseudo-cubic one, or step B' where  $d_{33} = 485$  pm/V; and (iii)  $E \geq 15$  kV/cm, complete transformation into a mixture phase of T and R phases or step C' where  $d_{33} = 420$  pm/V. Interestingly, the E-field induced R and T phases were distinct and individually identifiable by XRD, with no evidence of low symmetry structurally bridging phases (i.e., monoclinic).<sup>9</sup> This is in sharp contrast to lead-based MPBs between polar phases, where enhanced piezoelectricity results from polarization rotation via M phase. Clearly, a mechanism of piezoelectric enhancement for MPB in  $(1-x)\text{NBT}-x\text{BT}$  crystals is different from that in Pb-based systems.

#### IV. DISCUSSION AND SUMMARY

*Ab-initio* and phenomenological calculations have both shown a flattening of the free energy profile near MPB regions.<sup>10,13,16,17</sup> It has also previously been pointed out that polarization rotation is not the only mechanism for property enhancement, but rather polarization extension contributions can also contribute.<sup>19</sup> The ultrahigh electromechanical response of 0.944NBT-0.056BT in step B (see Fig. 2(d)) can be explained by such a polarization extension, between weakly T and strongly T phases, as schematically illustrated

in Figure 6. The initial structure near  $130^\circ\text{C}$  is pseudocubic, with only weak T distortions ( $P4bm$ ) where the  $\text{Na}^{1+}/\text{Bi}^{3+}/\text{Ba}^{2+}$  and  $\text{Ti}^{4+}$  cations are near equally displaced in opposite directions along  $[001]_{PC}$  (see Fig. 6(a)). With increasing  $E//[001]_{PC}$ , the  $\text{Ti}^{4+}$  cations are shifted to the center along  $[001]_{PC}$  (see Fig. 6(b)), during which process the polarization is slightly increased (without hysteresis) for  $E < 10$  kV/cm (see Fig. 6(e)). For  $E \geq 10$  kV/cm, the  $\text{Ti}^{4+}$  cations move off-center along  $[001]_{PC}$  (see Fig. 6(c)), resulting in a significantly enhanced T distortion and an induced transformation. Polarization extension along  $[001]_{PC}$  increases rapidly near this induced transition for  $10$  kV/cm  $< E < 16$  kV/cm. For  $E > 16$  kV/cm, the entire crystal transforms into a T phase single c-domain state. After removal of  $E$ , the initial weakly polar phase is recovered (see Fig. 6(a)). The slim P-E loop in Fig. 6(e) indicates that the hysteresis between weakly polar and strongly polar T phases is small: i.e., polarization extension is reversible.

Following Landau-Devonshire theory, the value of  $d_{33}$  can be given as<sup>47</sup>

$$d_{33} = 2 \cdot Q_{33} \cdot \epsilon_{33} \cdot P_3, \quad (1)$$

where  $Q_{33}$ ,  $\epsilon_{33}$ , and  $P_3$  are the electrostriction coefficient, dielectric constant, and polarization. The standard definition of the dielectric constant is<sup>47</sup>

$$\epsilon_{33} = 1 + \frac{4\pi \cdot \Delta P_3}{\Delta E_3} \approx \frac{4\pi \cdot \Delta P_3}{\Delta E_3}, \quad (2)$$

where  $E_3$  is external electric field. Thus,  $d_{33}$  can be given as

$$d_{33} = 8\pi \cdot Q_{33} \cdot \frac{\Delta P_3}{\Delta E_3} \cdot P_3 \quad (3)$$

This equation shows that  $d_{33}$  is proportional to the polarization change  $\frac{\Delta P_3}{\Delta E_3}$  multiplied by the total polarization  $P_3$ . For  $E < 10$  kV/cm, both  $\frac{\Delta P_3}{\Delta E_3}$  and  $P_3$  of 0.944NBT-0.056BT are small, thus a relative small  $d_{33} \sim 350$  pm/V was obtained for step A. With increasing  $E$  between 10 kV/cm and 16 kV/cm, both  $\frac{\Delta P_3}{\Delta E_3}$  and  $P_3$  sharply increased due to polarization extension, thus  $d_{33}$  increased significantly to values as high as 2500 pm/V. For  $E > 20$  kV/cm, the polarization is saturated, and  $\frac{\Delta P_3}{\Delta E_3}$  becomes smaller: thus,  $d_{33}$  is decreased for step C but remained relatively high at 700 pm/V.

For  $E//[101]_{PC}$ , coexisting T (strongly T distorted) and R phases were identified by XRD; however, no evidence of low symmetry structurally bridging M phases was found as for PMN-PT or PZN-PT.<sup>9</sup> This indicates that the polarization rotation between T and R phase does not occur near the MPB of  $(1-x)\text{NBT}-x\text{BT}$ . Rather, polarization extension from pseudo-cubic (slightly T distorted)  $\rightarrow$  T (strongly T distorted) or R phases resulted in enhanced piezoelectricity. But the polarization extension direction is  $[001]_{PC}$  for the T phase. Thus, the value of  $d_{33}$  along  $[101]_{PC}$  is significantly smaller than that along  $[001]_{PC}$ . These results indicate that the enhancement of piezoelectric properties via polarization extension is strongly crystallographically dependent. In polycrystalline materials, only a few grains are favorably oriented with respect to  $E$ : thus, full advantage of polarization



extension can not be achieved and property enhancement limited with respect to its potential.<sup>21</sup> Thus, the possibility to get high performance lead-free piezoelectric, via polarization extension, lies within properly oriented single crystals.

In summary, an ultrahigh electromechanical response with longitudinal piezoelectric coefficients as high as  $d_{33} = 2500$  pm/V was found in [001]<sub>PC</sub> oriented 0.944NBT-0.056BT single crystals near a depolarization temperature of  $T_d = 130$  °C. *In-situ* XRD revealed that the enhanced piezoelectric properties resulted from a polarization extension between a polar pseudocubic phase with a slightly tetragonal (*P4bm*) distortion and a polar tetragonal phase with a large tetragonal distortion of  $c/a = 1.02$ . Our findings demonstrate a potential approach to high performance lead-free piezoelectrics in single crystals, via polarization extension.

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