

# Appendix F

## Notation

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| $a$        | Reciprocal of the initial shear stiffness of the interface $K_{si}$ under initial loading; reciprocal of the initial tangent modulus $E_i$ of the soil                        |
| $b$        | Reciprocal of the asymptotic shear stress $\tau_{ult}$ for initial loading of the interface; reciprocal of the asymptotic deviator stress $(\sigma_1 - \sigma_3)$ of the soil |
| $B$        | Bulk modulus of the soil  |
| $C_c$      | Coefficient of curvature  |
| $C_k$      | Interface stiffness ratio   |
| $C_N$      | Correction factor for the number of steps in the backside of a rock-founded gravity wall  |
| $C_s$      | Correction factor for a rock-founded gravity retaining wall with an inclined backfill surface   |
| $C_u$      | Uniformity coefficient  |
| $C_{wt}$   | Correction factor for determination of the vertical shear force coefficient during inundation of the backfill   |
| $C_\theta$ | Correction factor for inclination of the backside of a rock-founded gravity wall  |
| $D_r$      | Relative density  |
| $D_1$      | Thickness of the backfill above the hydrostatic water table   |
| $D_2$      | Thickness of the submerged backfill above the heel of the wall  |
| $D_{10}$   | Particle size diameter corresponding to 10 percent passing in the grain size distribution curve   |
| $D_{30}$   | Particle size diameter corresponding to 30 percent passing in the grain size distribution curve   |

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| $D_{60}$           | Particle size diameter corresponding to 60 percent passing in the grain size distribution curve   |
| $d\Delta_s$        | Infinitesimal increment in interface displacement   |
| $d\tau^i$          | Infinitesimal shear stress increment along an inclined stress path  |
| $d\tau^v, d\tau^o$ | Infinitesimal shear stress increments in the orthogonal directions $v'$ and $o'$ , respectively   |
| $E_i$              | Initial tangent (Young's) modulus of the soil   |
| $E_t$              | Tangent modulus of the soil   |
| $E_{ur}$           | Young's modulus for unloading-reloading   |
| $F_v$              | Vertical force or downdrag per unit length of wall  |
| $F_{v,q}$          | Vertical force increment due to surcharge application   |
| $F_{v,soil}$       | Vertical earth force due to the self weight of the backfill   |
| $F_w$              | Hydrostatic force on the wall   |
| $F_x$              | Total horizontal force per unit length of wall  |
| $F_x'$             | Effective horizontal force per unit length of wall  |
| $G_s$              | Specific gravity  |
| $h$                | Height of the horizontal earth force above the base of the wall   |
| $H$                | Height measured along a vertical plane passing through the heel of the wall and extending through the backfill  |
| $H_b$              | Total backfill height as measured in Figure 2-5   |
| $i$                | Generic name for inclined stress paths; as a superscript in Figures 4-40 through 4-44, it denotes the $i^{th}$ load step in a finite element analysis |
| $i'$               | Generic name for the $\sigma_n$ - $\Delta_s$ - $\tau$ response of the interface to an inclined stress path  |
| $i''$              | Generic name for the $\Delta_s$ - $\tau$ response of the interface to an inclined stress path   |
| $I$                | Correction factor for inclination of the stress path  |

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| $[K]$             | Global stiffness matrix  |
| $K$               | Modulus number   |
| $K_b$             | Bulk modulus number  |
| $k_n$             | Normal interface stiffness   |
| $k_s$             | Interface shear stiffness  |
| $K_f\text{-line}$ | Line joining the points in the p'-q plane that correspond to failure   |
| $K_h$             | Earth pressure coefficient for effective horizontal forces   |
| $K_I$             | Dimensionless interface stiffness number for initial loading   |
| $K_n$             | Normal stiffness of an interface element   |
| $K_o$             | At-rest pressure coefficient   |
| $K_{si}$          | Initial shear stiffness of the interface   |
| $K_{sno}$         | Normalized interface shear stiffness at zero-stress level  |
| $K_{sn}$          | Normalized shear stiffness of the interface  |
| $K_{sn}^{ts}$     | Transition stiffness number  |
| $K_{sn}^{ys}$     | Yield stiffness number   |
| $K_{st}$          | Interface tangent stiffness for vertical stress paths (as defined in Clough and Duncan (1971) hyperbolic model for interfaces) |
| $K'_{st}$         | Interface tangent stiffness for stress paths of any orientation  |
| $K'_{st}^I$       | Interface tangent stiffness at point $I$   |
| $K'_{s\ sec}$     | Secant interface shear stiffness   |
| $K_{ur}$          | Unload-reload modulus number for soils   |
| $K_{urj}$         | Unload-reload stiffness number for interfaces  |
| $K_v$             | Vertical shear force coefficient   |
| $K_{v,q}$         | Vertical shear force coefficient for sloping backfill and surcharge  |
| $K_{v,q,ref}$     | Reference value of $K_{v,q}$ obtained for a value of $S = 0$   |

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| $K_{v,soil}$     | Vertical shear force coefficient for self-weight of the backfill  |
| $K_{v,soil,ref}$ | Reference value of $K_{v,soil}$ obtained for an inclination of the back of the wall $\theta$ of 90 degrees                          |
| $m$              | Bulk modulus exponent   |
| $m_k$            | Stiffness degradation parameter   |
| $N$              | Number of steps in the back of a stepped wall   |
| $n$              | Modulus exponent  |
| $n_j$            | Interface stiffness exponent  |
| $o'$             | Generic name for the line of intersection between the initial loading surface and a plane parallel to the $\sigma_n$ - $\tau$ plane |
| $o''$            | Generic name for the projection of $o'$ in the $\Delta_s$ - $\tau$ plane  |
| $p'$             | $(\sigma_1' + \sigma_3')/2$   |
| $p_a$            | Atmospheric pressure = 101.3 kPa  |
| $q$              | Shear direction parameter; $(\sigma_1 - \sigma_3)/2$  |
| $q_s$            | Applied surcharge pressure  |
| $R_f$            | Failure ratio for soils   |
| $R_{ff}$         | Failure ratio for interfaces  |
| $S$              | Horizontal distance from the vertical plane through the wall heel to the top of the backfill slope                                  |
| $SL_o$           | Stress level at the origin of unloading-reloading   |
| $SL^{ts}$        | Transition stress level   |
| $SL^{ys}$        | Stress level for current position of yield surface  |
| $v$              | Generic name for vertical stress paths  |
| $v'$             | Generic name for the $\sigma_n$ - $\Delta_s$ - $\tau$ response of the interface to a vertical stress path                           |
| $v''$            | Generic name for the $\Delta_s$ - $\tau$ response of the interface to a vertical stress path  |

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| $\alpha$                     | Scaling factor for unloading-reloading   |
| $\gamma$                     | Unit weight of the soil  |
| $\gamma_b$                   | Buoyant unit weight of submerged backfill  |
| $\gamma_{max}, \gamma_{min}$ | Maximum and minimum density, respectively  |
| $\gamma_{moist}$             | Moist unit weight of the backfill above the water table                              |
| $\gamma_w$                   | Unit weight of water (9.8 kN/m <sup>3</sup> )  |
| $\delta$                     | Peak interface friction angle  |
| $\delta_r$                   | Residual interface friction angle  |
| $\Delta_{actual}$            | Actual sliding displacement between soil particles and concrete                      |
| $\Delta_{dis}$               | Deformation of the sand mass due to distortion under the applied shear stresses      |
| $\Delta_{meas}$              | Displacement measured between the soil box and concrete specimen                     |
| $\Delta_n$                   | Displacement normal to the interface   |
| $\Delta_s$                   | Displacement along the interface   |
| $\Delta_s^{i-1}, \Delta_s^i$ | Consecutive interface displacement readings  |
| $\Delta_{so}$                | Interface displacement at the origin of unloading-reloading                          |
| $\Delta_{sp}$                | Interface displacement to peak   |
| $\Delta_{sr}$                | Interface displacement to residual   |
| $\Delta_v$                   | Displacement normal to the interface; vertical displacement during interface testing |
| $\Delta P$                   | $H_b - H$  |
| $\{\Delta P\}$               | Vector of nodal forces   |
| $\{\Delta u\}$               | Vector of unknown incremental displacements  |
| $\Delta\gamma_{xy}$          | Shear strain increment   |
| $\Delta\Delta_s$             | Increment of interface displacement  |

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| $\Delta\varepsilon_x, \Delta\varepsilon_y$ | Horizontal and vertical strain increments, respectively  |
| $\Delta\sigma_x, \Delta\sigma_y$           | Horizontal and vertical stress increments, respectively  |
| $\Delta\sigma_n$                           | Normal stress increment  |
| $\Delta\tau^j$                             | Shear stress increment between points $P$ and $Q$  |
| $\Delta\tau', \Delta\tau^o$                | Components of the shear stress increment in the orthogonal directions $v'$ and $o'$ , respectively |
| $\Delta\tau_{xy}$                          | Shear stress increment in soils and backfills  |
| $\Delta\tau$                               | Shear stress increment in interfaces   |
| $\Delta\phi$                               | Reduction in the peak secant friction angle value for a tenfold increase in $\sigma'_3$            |
| $\varepsilon$                              | Axial strain   |
| $\varepsilon_v$                            | Volumetric strain  |
| $\theta$                                   | Angle between the stress path direction and the $\tau$ -axis                                       |
| $\nu$                                      | Poisson's ratio  |
| $\nu_{nom}$                                | Nominal Poisson's ratio  |
| $\sigma_h$                                 | Horizontal pressure  |
| $\sigma_n$                                 | Normal stress acting on the interface  |
| $\sigma_n^{ts}$                            | Normal stress corresponding to point TS where the stress path intersects a transition surface      |
| $\sigma_{no}$                              | Normal stress at the origin  |
| $\sigma_v$                                 | Vertical stress  |
| $\sigma_v'$                                | Effective vertical stress  |
| $\sigma_1$                                 | Major principal total stress   |
| $\sigma_1'$                                | Major principal effective stress   |
| $\sigma_3$                                 | Minor principal total stress   |

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| $\sigma_3'$                   | Minor principal effective stress   |
| $(\sigma_1 - \sigma_3)$       | Deviator stress  |
| $(\sigma_1 - \sigma_3)_f$     | Deviator stress at failure   |
| $(\sigma_1 - \sigma_3)_{ult}$ | Asymptotic deviator stress   |
| $\tau$                        | Interface shear stress   |
| $\tau^{i-1}, \tau^i$          | Consecutive interface shear stress readings                                    |
| $\tau^s$                      | Shear stress at point TS where the stress path intersects a transition surface |
| $\tau_f$                      | Interface shear strength   |
| $\tau_o$                      | Interface shear stress at the origin of unloading-reloading                    |
| $\tau_{ult}$                  | Asymptotic interface shear stress  |
| $\phi$                        | Peak secant internal friction angle of the soil                                |
| $\phi'$                       | Effective peak secant friction angle of the soil                               |
| $\phi_{cv}$                   | Friction angle at a strain of 15 percent                                       |
| $\phi_o$                      | Peak secant friction angle at a confining pressure of 101.3 kPa (1atm)         |