

**Discretization Error Estimation and Exact Solution Generation
Using the 2D Method of Nearby Problems**

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**Thesis submitted to the faculty of the
Virginia Polytechnic Institute and State University
in partial fulfillment of the requirements for the degree of**

**Master of Science
in
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