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Citation: Journal of Applied Physics 104, 073910 (2008); doi: 10.1063/1.2992528
View online: http://dx.doi.org/10.1063/1.2992528
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Magnetic properties of self-assembled nanoscale La2/3Ca1/3MnO3 particles in an alumina matrix
The effect of matrix and substrate on the coercivity and blocking temperature of self-assembled Ni nanoparticles

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(Received 31 December 2007; accepted 19 August 2008; published online 15 October 2008)

We have shown that the magnetic properties of nanoparticles may be tuned from superparamagnetic to ferromagnetic by changing the substrate or thin film matrix in which they are embedded. Nickel nanoparticles were embedded into alumina, titanium nitride, and cerium oxide matrices on both silicon and sapphire substrates via pulsed laser deposition. The laser ablation time on the nickel target was kept constant. Only nickel nanoparticles in cerium oxide showed characteristics of ferromagnetism (room temperature coercivity and remanence). Ni nanoparticles, in either alumina or titanium nitride, possessed blocking temperatures below 200 K. Detailed scanning transmission electron microscopy analysis has been conducted on the samples embedded into cerium oxide on both substrates and related to the magnetic data. © 2008 American Institute of Physics. [DOI: 10.1063/1.2992528]

I. INTRODUCTION

Nanostructured magnetic materials display unique properties that are being aggressively researched for a variety of technological applications. Perhaps the best example of an emerging application is the magnetic recording industry in which storage densities $>\text{Tb/in}^2$ are being pursued.1–4 The implementation of nanoparticle based recording media is complicated by the phenomenon of superparamagnetism. Superparamagnetism is a small particle effect that occurs as the nanoparticle diameter is reduced below some critical value.5 Superparamagnetism (SPM) particles are characterized by a lack of remanence and coercivity due to the effect of thermal fluctuations on the direction of the magnetization vector. For SPM samples, a blocking temperature ($T_B$) exists, such that when $T < T_B$ the sample will behave as a ferromagnet. For $T > T_B$, thermal fluctuations are sufficiently energetic to overcome the coercive field, causing random rotation of the nanoparticle spins, which make the particles unsuitable for data storage. High coercivity FePt nanoparticles have been identified as possible solutions to the superparamagnetic limit imposed on nanomagnetic media.5,6 Chemical routes have been predominately used for FePt synthesis.2,6,7 However, after synthesis, additional thermal treatments ($>500{\,}^\circ\text{C}$) are required to achieve magnetic and crystallographic ordering of FePt into its highly anisotropic $L_{10}$ phase that is responsible for the enhanced coercivity.6 Heating above 550 °C results in considerable particle coalescence and loss of particle positional order,6,7 which increases the switching volumes, negating the advantageous aspects of nanoparticle based media.6

Physical vapor deposition techniques such as pulsed laser deposition (PLD) may provide an alternate route to achieve monodispersed, high coercivity magnetic nanoparticles.8 The particles may be formed in the gas phase6,10 or they may be grown directly onto thin film templates.11 For sufficiently controlled growth processes, the nanocluster size can be tailored, providing simultaneous synthesis, deagglomeration, and passivation of nanomaterials in situ. We have used PLD to deposit magnetic nanoparticles in various thin film matrices alumina ($\text{Al}_2\text{O}_3$), titanium nitride (TiN), and cerium oxide ($\text{CeO}_2$). The crystallinity of the thin film matrix has previously been shown to significantly affect the magnetic properties of embedded nanoparticles.12 The Ni particles evolve as three-dimensional (3D) self-assembled clusters because of the tendency of metallic materials to follow the Volmer–Weber growth mode.13 For sufficiently short deposition times, the growing films are not continuous, having the form of discrete islands or clusters. These islands or clusters may be used to mimic the properties of nanoparticles. In this article, we will discuss the effect of thin film matrix ($\text{Al}_2\text{O}_3$, TiN, CeO$_2$) and substrate (Si, sapphire) on the coercivity and blocking temperature of self-assembled Ni nanoparticles. The Ni nanoparticle size can be controlled by tailoring the deposition time (number of laser pulses on the
The depositions were carried out simultaneously on Si and thin films on Si/multitarget carousel and a KrF excimer laser with laser ablation during PLD. The PLD system consists of a 0.73910-2 Abiade deposition temperature. The nominal deposition rate of the Ni layers was 0.073910-2 nm/s. The pulses on the Ni target was constant for all samples. The five alternating nanoparticle/thin film layers. The number of thin film spacer layers was maintained at 4.8 cm. The multilayered structure consisted of an initial thin film layer (50 nm) and alternating layers of nickel nanoparticles and the respective thin film spacer layers (25 nm). Each sample consists of five alternating nanoparticle/thin film layers. The number of pulses on the Ni target was constant for all samples. The nominal deposition rate of the Ni layers was 0.1 nm/s. The depositions were carried out simultaneously on Si and sapphire substrates.

II. EXPERIMENTAL

Nickel nanoparticulates were embedded in alumina (Al2O3), titanium nitride (TiN), and cerium oxide (CeO2) thin films on Si (100) and sapphire (c-plane) substrates by laser ablation during PLD. The PLD system consists of a multitarget carousel and a KrF excimer laser with a wavelength of 248 nm (Lambda Physik). Prior to each deposition, the substrates were cleaned in acetone. The Si substrates were also etched in de-ionized hydrofluoric acid to remove the native oxide layer. After the desired chamber pressure was reached (~10^-7 torr), the substrates were maintained at the deposition temperature (600–650 °C) for 30 min prior to each run. All films were deposited in vacuum. The target to substrate distance was maintained at 4.8 cm. The multilayered structure consisted of an initial thin film layer (~50 nm) and alternating layers of nickel nanoparticles and the respective thin film spacer layers (~25 nm). Each sample consists of five alternating nanoparticle/thin film layers. The number of pulses on the Ni target was constant for all samples. The nominal deposition rate of the Ni layers was ~0.1 nm/s. The depositions were carried out simultaneously on Si and sapphire substrates.

Power x-ray diffraction (XRD) analysis was performed using a Rigaku diffractometer with Cu Ka source. The magnetic properties of the nanocomposites were studied using a physical property measurement system equipped with a vibrating sample magnetometer (VSM) option from Quantum Design and superconducting quantum interference device (SQUID) magnetometer. The VSM and SQUID were used to study the field and temperature dependence of the magnetic moment of Ni particles for the various thin film matrix/substrate combinations. For magnetization versus temperature measurements, the moment was measured in both the zero field cooled (ZFC) and field cooled (FC) modes. During the ZFC measurement, the samples were cooled to 10 K with no applied field. The moment was then measured while warming the samples up to 300 K in a magnetic field of 50 Oe. For FC measurements, the samples were cooled to 10 K in the respective fields and the moment was measured while warming to room temperature. The temperature dependence of the coercivity was obtained from the magnetization versus field loops obtained at different temperatures.

Cross-sectional specimens for electron microscopy analysis were prepared following conventional methods consisting of dimpling and Ar-ion milling to obtain electron transparency. Scanning transmission electron microscopy (STEM) imaging was carried out in a VG HB501UX microscope operated at 100 kV equipped with a Nion aberration corrector. High angle annular dark-field (ADF) and bright-field (BF) images were recorded simultaneously. Spectrum images were acquired by using a Gatan Enfina electron energy loss spectroscopy (EELS) attachment on the STEM. ADF images and EELS spectra were acquired simultaneously in the energy range of 430–966.4 eV with the energy dispersion of 0.4 eV per channel at an acquisition time of 0.5 s. Quantitative elemental mapping after background subtraction was performed using the respective core-loss edges: Ni L2,3 (854 eV), Ce M4,5 (883 eV), and O K (532 eV).

III. RESULTS AND DISCUSSIONS

The three thin film matrices (Al2O3, CeO2, and TiN) in this study have widely varying crystallographic properties depending on growth conditions and substrate. For example, Al2O3 films are generally amorphous regardless of deposition conditions and substrate except at higher deposition temperatures. Epitaxial CeO2 films have previously been obtained on both sapphire and silicon substrates whereas epitaxial TiN films grown in vacuum have been reported on silicon not sapphire. The varying degrees of crystallinity of the thin film matrix permit texturing of the magnetic properties of the embedded particles. Figure 1 shows typical M-H loops recorded at 5 K for the Ni particles embedded in an Al2O3 matrix on a Si substrate [Fig. 1(a)] and a sapphire substrate [Fig. 1(b)]. The coercivity (Hc), saturation magnetization (Ms), remanent magnetization (Mr), and remanence ratio (Mr/Ms) for the various matrix/substrate combinations measured at 5 K are given in Table I. In all cases, the Ni deposition time was kept constant. Ms is ~10^-4 emu for all samples. All of the M-H loops become saturated at fields less than ~3 kOe except for Ni embedded in CeO2 on sapphire, which requires a field in excess of 5 kOe. The coercivity at 5 kOe is ~10^-3 emu.

FIG. 1. Hysteresis loops recorded at 5 K for Ni embedded in an Al2O3 matrix (a) on Si and (b) on a sapphire substrate.
Table I. Coercivity ($H_c$), saturation magnetization ($M_s$), remanent magnetization ($M_r$), and remanence ratio ($M_r/M_s$) for various matrix substrate combinations measured at 5 K. $H_c(0$ K) obtained from fit to data in Fig. 2.

<table>
<thead>
<tr>
<th>Matrix/substrate combination</th>
<th>$H_c$(5 K) Oe</th>
<th>$H_c$(0 K) Oe</th>
<th>$M_s$ (10−4 emu)</th>
<th>$M_r$ (10−4 emu)</th>
<th>$M_r/M_s$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Al$_2$O$_3$/Si</td>
<td>100</td>
<td>130</td>
<td>1.45</td>
<td>0.54</td>
<td>0.37</td>
</tr>
<tr>
<td>Al$_2$O$_3$/Al$_2$O$_3$</td>
<td>135</td>
<td>165</td>
<td>3.30</td>
<td>1.10</td>
<td>0.33</td>
</tr>
<tr>
<td>TiN/Si</td>
<td>265</td>
<td>320</td>
<td>0.92</td>
<td>0.35</td>
<td>0.38</td>
</tr>
<tr>
<td>TiN/Al$_2$O$_3$</td>
<td>190</td>
<td>234</td>
<td>1.30</td>
<td>0.60</td>
<td>0.46</td>
</tr>
<tr>
<td>CeO$_2$/Si</td>
<td>370</td>
<td>400</td>
<td>2.34</td>
<td>1.12</td>
<td>0.48</td>
</tr>
<tr>
<td>CeO$_2$/Al$_2$O$_3$</td>
<td>315</td>
<td>335</td>
<td>6.00</td>
<td>1.59</td>
<td>0.27</td>
</tr>
</tbody>
</table>

K changes dramatically depending on the matrix/substrate combination. Generally, the coercivity is enhanced for matrix substrate combinations in which the matrix layers are more crystalline. The lowest $H_c$ values are observed for Ni particles embedded in an alumina matrix. Ni in CeO$_2$ possessed $H_c$ values of 370 and 315 Oe on Si and sapphire, respectively, at 5 K. Ni particles in TiN matrices on both Si and sapphire possessed intermediate values between that of the alumina and CeO$_2$ matrix (maximum in $H_c$ also on Si). The approximate threefold increase in $H_c$ for Ni embedded in CeO$_2$ in comparison to Ni embedded in Al$_2$O$_3$ is illustrative of the ability to tailor the magnetic properties. The remanence ratio allows insight into interparticle interactions. Generally, $M_r/M_s$ ~ 0.5 is observed for random, noninteracting particles. As shown in Table I, only matrix/substrate combinations of TiN/sapphire and CeO$_2$/Si are suggestive of noninteracting particles.

The Ni nanoparticles are SPM in all matrices except CeO$_2$. Only Ni in CeO$_2$ on Si and sapphire possesses the characteristic features of ferromagnetism (FM) such as room temperature coercivity and remanence. Figure 2 shows the linear dependence of coercivity on the square root of the temperature ($T^{1/2}$) obtained from the relation $H_c(T) = H_c(0 \text{ K})[1-(T/T_B)]^{1/2}$, typical of nanoparticle samples. $H_c(0 \text{ K})$ is the coercivity at 0 K, which is strongly dependent on the intrinsic anisotropy of the system, $T$ is the measurement temperature, and $T_B$ is the blocking temperature, which was previously discussed. The trend lines are linear fits to the data, which were used to obtain $H_c(0 \text{ K})$ and $T_B$. The coercivity was obtained from $M$-$H$ loops measured at different temperatures. From the linear fits, Fig. 2 clearly shows that the $T_B$ for the Ni particles in alumina and TiN is well below 300 K. For Ni in alumina, the estimated $T_B$ is ~117 and 143 K on Si and sapphire, respectively. Similarly, $T_B$ for Ni in TiN is ~199 K on Si and 128 K on sapphire. The estimated $T_B$ for Ni in alumina and TiN agrees well with experimentally determined values represented by irreversibility in the magnetization versus temperature curves in Fig. 3. Except for the TiN sample, the trend lines for the data in Fig. 2 follow a nonmonotonic trend. For example, the curves for Ni in alumina and Ni in CeO$_2$ on the different substrates intersect. This nonmonotonic trend in the slopes of $H_c$ versus $T^{1/2}$ may be attributed to multiple effects: distributions in particles size and/or shape, size dependence of anisotropy constants, and/or particle-particle interactions. The interparticle interactions may be enhanced for tighter packing. Uninfluenced by thermal effects, the low temperature coercivity is directly related to the nanoparticle magnetic anisotropy. Figures 1–3 and Table I clearly demonstrate the ability to texture the magnetic properties by varying the matrix and/or substrate. We will now discuss the samples with Ni particles embedded in a CeO$_2$ matrix in greater detail.

Figure 4 shows the remanence ratio ($M_r/M_s$) versus temperature for Ni embedded in CeO$_2$ on both Si and sapphire substrates. The two curves show quite different temperature dependencies, which suggests the magnetic anisotropy and interparticle interactions may be different for the two samples. An increase in temperature effectively reduces the magnetic properties in part due to randomization of the interparticle interactions and degradation of the magnetic anisotropy. On the Si substrate, the remanence ratio changes ~34% from 5 to 300 K. The temperature dependence is much less pronounced on the sapphire substrate changing ~15% from 5 to 100 K and remaining relatively flat up to room temperature. Several effects may contribute to the observations in Fig. 4. Generally, interparticle interactions lower the remanence, creating flux closure loops. Furthermore, the magnetic anisotropy is also a strong function of the nanoparticle size and temperature. For example, the cubic anisotropy constant for Ni decreases by a factor of 22 from low to room temperature. XRD analysis (not shown) indicates the CeO$_2$ layers are highly crystalline with (111) tex-
ture on both Si and sapphire. Typically, the full width at half maximum of the CeO$_2$ (111) peak is slightly lower on Si than on sapphire because of the similarities in crystal structure and lattice parameter. Based on our XRD data, the relative intensity of the secondary CeO$_2$ orientations such as (200) and (220) with respect to (111) on Si are 10% and <0.1%, respectively. The corresponding values for (200) and (220) on sapphire are both <0.1%. In this study, the crystallinity of the CeO$_2$ matrix layer is better on sapphire. Electron microscopy of the CeO$_2$ layers and Ni particles is required for complete analysis of the magnetometry data.

Figure 5 shows a low magnification STEM image of the Ni particles embedded in CeO$_2$ on Si [Fig. 5(a)] and sapphire [Fig. 5(b)] substrates. The five layers of Ni particles (bright discontinuous regions) are clearly separated by homogeneous regions of CeO$_2$. The composite sample thickness is ~230 nm and each layer of Ni particles is separated by 25 nm CeO$_2$ layers for both substrates. Detailed high resolution STEM imaging has been conducted on the CeO$_2$ layers and the embedded particles. Figure 6 is a STEM image of the sample on the sapphire substrate. Figure 6(a) shows a region of the CeO$_2$ spacer layer with a few Ni particles at the top of the image. Figure 6(a) also indicates that the CeO$_2$/sapphire interface is abrupt whereas the CeO$_2$/Si interface (not shown) consists of native oxide (Si–O) and cerium silicate (Ce–Si–O) layers, which may explain the higher roughness and diminished crystallinity of CeO$_2$ on Si versus sapphire substrates. The boxed region in Fig. 6(a) is shown at a higher magnification in Fig. 6(b). The columnar structure of the

![Image of STEM images](image-url)

**FIG. 4.** Remanence ratio vs temperature for Ni in CeO$_2$ on Si (○) and sapphire (□) substrates.

**FIG. 5.** ADF STEM image of five layers of Ni nanoparticles embedded in CeO$_2$ on (a) Si substrate and (b) sapphire substrate.
CeO₂ layer prominent in Fig. 6(b) was seen on both substrates. In agreement with XRD, the CeO₂ layers are highly (111) oriented. The CeO₂ film grown on sapphire is epitaxial (although the columnar grains are slightly misoriented by a few degrees in plane, as can be seen in Fig. 6(b)). The CeO₂ film grown on the Si substrate also shows (111) textured orientation but its columnar grains do not possess epitaxial relationship with the substrate. This is due to the presence of a thin cerium silicate amorphous layer which results from an interfacial reaction between the growing CeO₂ film and the Si substrate. The bulk CeO₂ matrix on both Si and sapphire substrates is very similar. Perhaps the difference in magnetic properties may be attributed to the Ni/CeO₂ interface or differences in the physical characteristics (size, shape, etc.) of the Ni particles in the two samples.

Figure 7 shows high resolution STEM images of the Ni/CeO₂ interfaces and Ni particles on silicon [Fig. 7(a)] and sapphire [Fig. 7(b)] substrates. EELS (not shown), used for compositional analysis, confirmed the existence of pure metallic Ni nanoparticles on both substrates. The most striking difference in the two samples is the Ni particle size and shape. The Ni particles deposited in CeO₂ on Si substrates are disk shaped with average heights of ∼12–14 nm and widths of ∼25 nm giving a width to height aspect ratio of ∼2. On sapphire, the Ni particles are more spherical with average heights of ∼8 nm and widths of ∼10 nm. Also, the Ni interparticle separation is larger on Si (>5 nm) than on sapphire substrates (∼1–2 nm). The Ni interparticle distance increases as the number Ni layers is increased on the Si substrate because of the increased roughness of the CeO₂ buffer layers. Interparticle separation distances in excess of 3 nm are required to decouple the magnetic particles, as evidenced by the respective remanence ratios given in Table I. On the Si substrate, the $M_r/M_s$ value at 5 K is 0.48 and 0.27 on sapphire. Typically, a $M_r/M_s$ value of 0.5 is observed for random, noninteracting particles. The particles on both substrates are predominantly (111) oriented. The Ni particle interplanar spacing of 0.22 nm highlighted in Fig. 7(b) is close to the bulk value of 0.20, which is indicative of Ni (111). The Ni/CeO₂ interface is also quite different for the two samples. On Si substrates, the crystalline CeO₂ directly contacts Ni particles, establishing local epitaxy whereas the CeO₂ surrounding Ni particles is amorphous on sapphire.

The evolution of the self-assembled Ni nanoparticles is a dynamic process dictated by thermodynamic and kinetic factors during the growth process. In the Ni/CeO₂ system, Ni evolves as 3D clusters or nanoparticles because the Ni surface free energy [∼2.0 J/m² versus 1.06 J/m² for Ni (111) (Ref. 18) and CeO₂ (111) (Ref. 24), respectively] is much larger than that of CeO₂ (i.e., Volmer–Weber growth). This phenomenon is commonly observed for metal on oxide growth. The CeO₂ films possess similar crystallographic texturing on the two different substrates. Hence, the respective Ni/CeO₂ surface and interfacial energies should be similar, which should lead to similar Ni particle size and shape. However, Fig. 7 clearly shows a striking difference exists. This difference in Ni size and shape (Fig. 7) may be attributed to the surface roughness of the CeO₂ buffer layers and the respective Ni/CeO₂ interface. The CeO₂ buffer layers are highly crystalline on both substrates. However, on Si the presence of native oxide and interfacial cerium silicate layers result in CeO₂ layers with higher surface roughness values. The surface roughness affects the mobility of the Ni atoms impinging on the CeO₂ layers.

Upon nucleation, Ni clusters form and their size is increased by capturing other Ni atoms either by diffusional processes or directly from the incident vapor. The Ni nanoparticle size and shape is governed by the number of Ni atoms that can be added to the cluster, which is affected by the characteristics of the CeO₂ surface (surface energy and roughness) and the deposition time. Thurtell and Thurtell determined that diffusing species on rough surfaces scattered by asperities have decreased atomic velocities or mobilities. In our case, the Ni clusters become trapped in “valleys” along the CeO₂ surface. The reduced mobility of the growing cluster results in the bigger, disk shaped Ni particles that we observed on the Si substrate [Fig. 7(a)]. On sapphire, the substrate/buffer layer interface is abrupt resulting in smooth CeO₂ films. Atoms diffusing across the smooth surface are not as effectively scattered, hence this additional diffusion barrier present on rough surfaces does not exist. The amorphous regions at the CeO₂/Ni interface on sapphire also play a role in tailoring the Ni particle shape. An amorphous interface favors a particle with spherical shape whereas crystalline templates usually lead to faceted islands because of surface energy anisotropy. According to STEM analysis [Fig. 7(b)], the Ni particles in contact with amorphous CeO₂ have spherical shapes with a narrow size distribution on sapphire.
The observed narrow size distribution can be attributed to dipolar island edge-edge interactions, which induces a stable island size against coarsening.26

**IV. SUMMARY AND CONCLUSIONS**

We studied the effect of substrate and thin film matrix on the magnetic properties of embedded self-assembled Ni nanoparticles. The nanoparticle/thin film composites were embedded into Al2O3, TiN, and CeO2 matrices on both Si and sapphire. Generally, the magnetic properties vary widely depending on the matrix substrate combination. The Ni nanoparticles in Al2O3 and TiN were superparamagnetism and ferromagnetic in CeO2 on both Si and sapphire. Generally, the Ni nanoparticles size and with increased crystallinity of the thin film matrix. For crystalline CeO2 matrix layers, the Ni nanoparticles size and shape differed on the two substrates. On Si, the particles were larger and disk shaped with larger interparticle separation (>5 nm). On sapphire, the Ni nanoparticles were roughly spherical and smaller with smaller particle-particle separation (1–2 nm). The tighter particle packing on the sapphire substrate resulted in enhanced magnetic interactions between the Ni particles, reducing the coercivity at lower temperatures.

**ACKNOWLEDGMENTS**

This research was support by the following grants from the National Science Foundation NSF-NIRT 4-46109 (NCAT) and NSF-DMR 0213985 (MINT-UA). The research at ORNL was sponsored by the Division of Materials Science and Engineering of the US Department of Energy.

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23Interplanar spacing (d_{ab})=a_0/(h^2+k^2+l^2)^{1/2}, where Ni lattice constant a_0 =0.3524 nm.