

An evaluation of power performance for a small wind turbine in turbulent wind regimes

**Nicholas J. Ward**

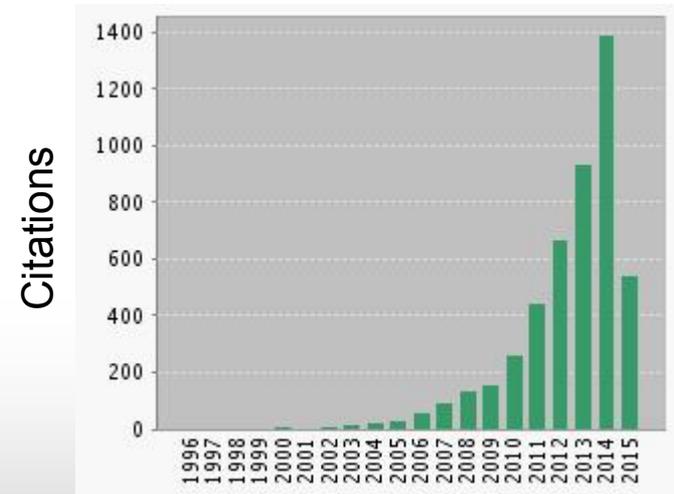
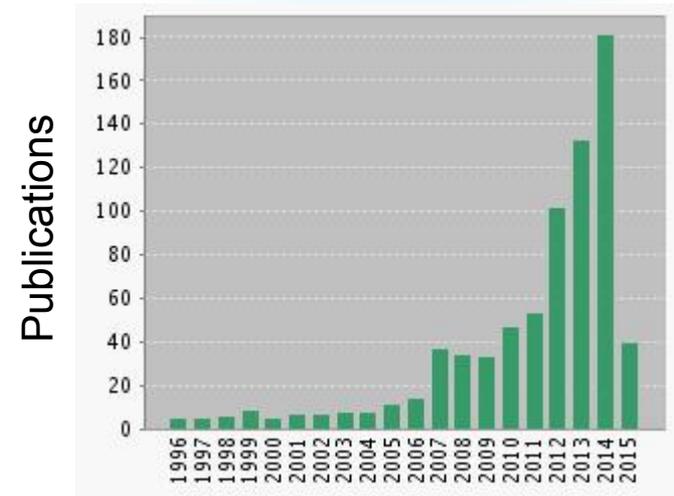
Ph.D. Student, Energy Engineering

Advisor: Dr. Susan W. Stewart

The Pennsylvania State University

# Why study turbulence?

- Increased attention towards engineering and economic feasibility in lower wind speed regimes [Ewing et al (2008)]
- Progressive damage and shortened turbine lifetime via stochastic loads [Saranyasootorn & Manuel (2008)]
- Increased interest in turbulence for future academic study [Web of Science]
  - 180 publications in 2014 (top)
  - 1400 cited articles in 2014 (bottom)



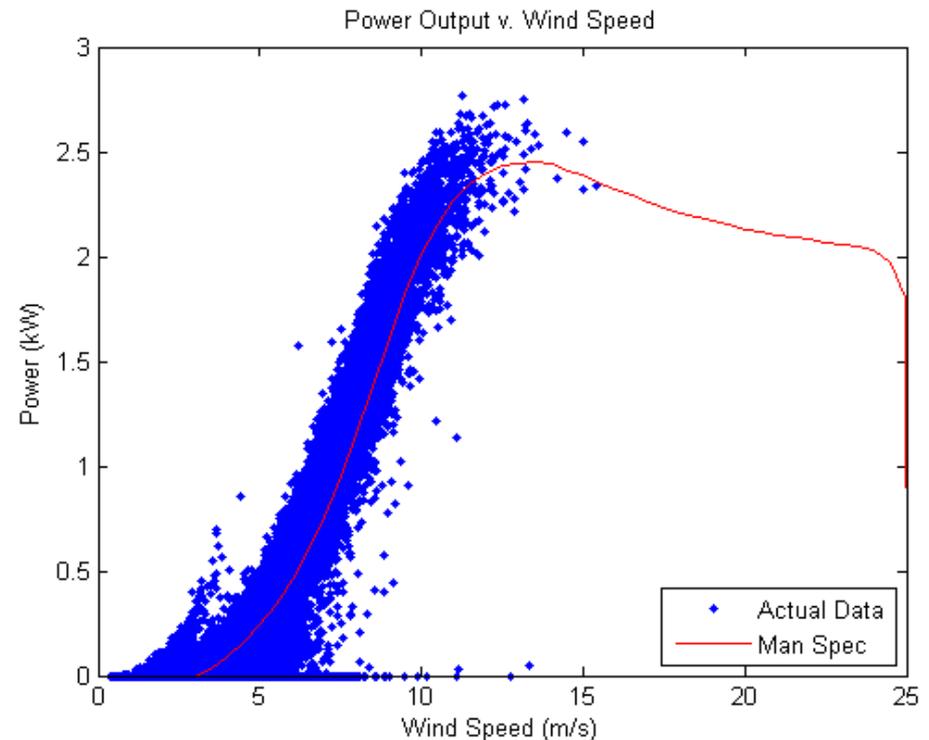
Year

# Wind Turbine & Site

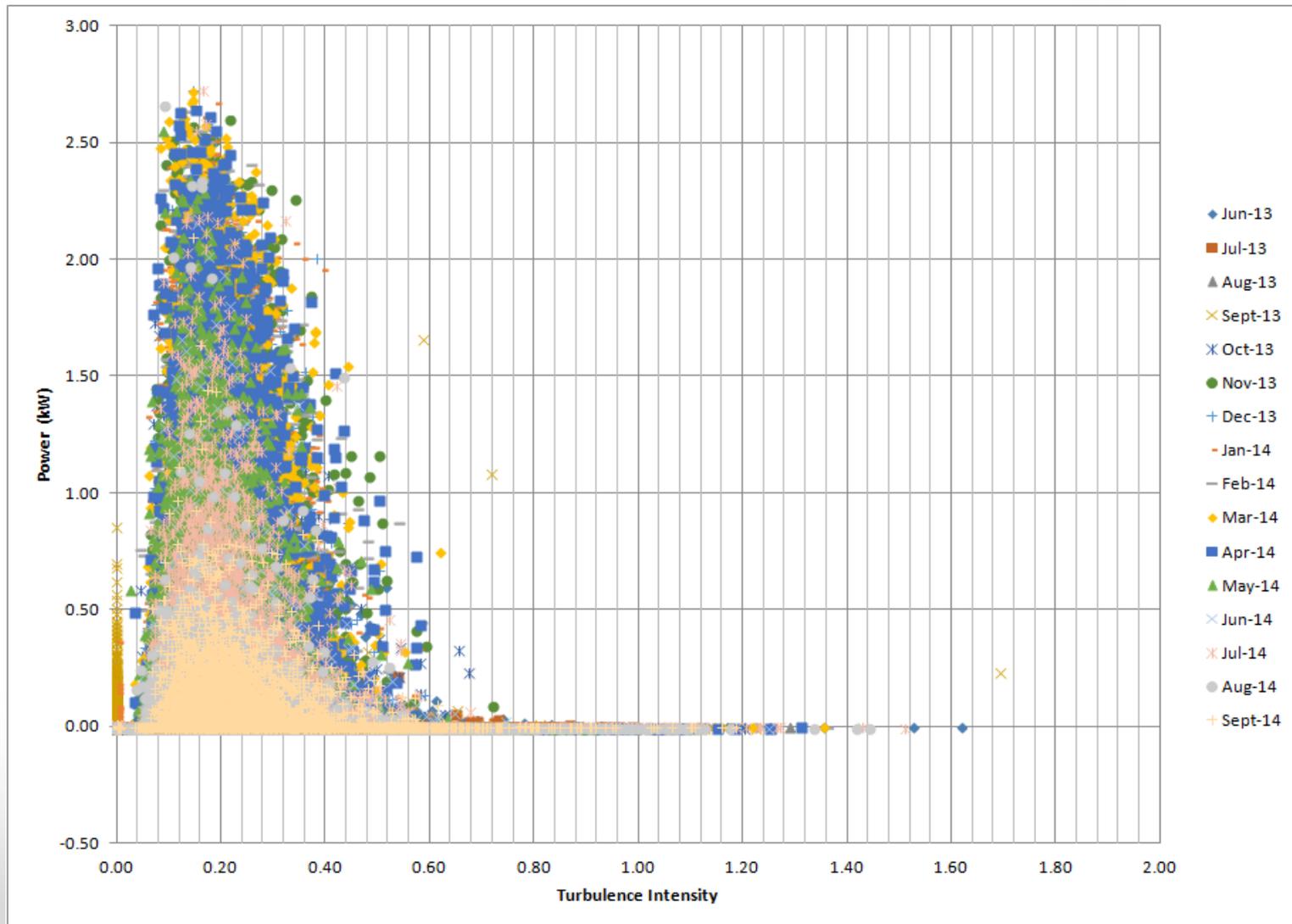


# Methodology

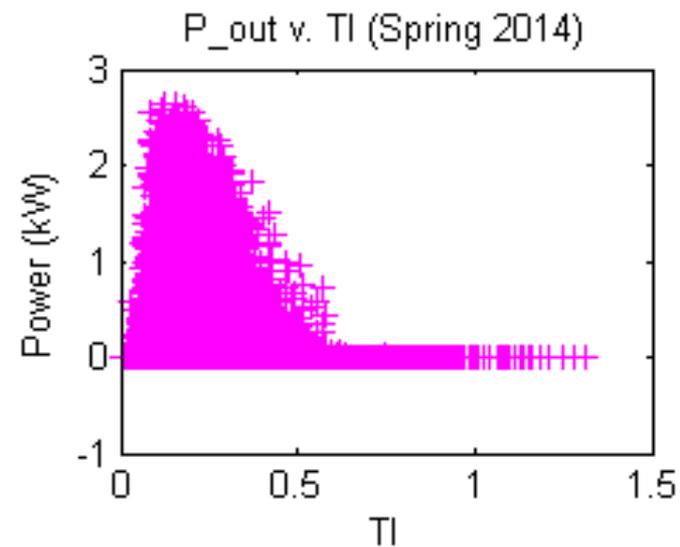
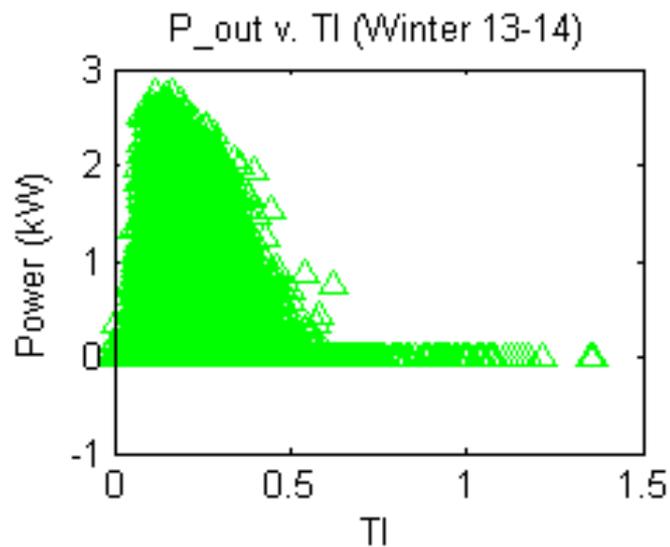
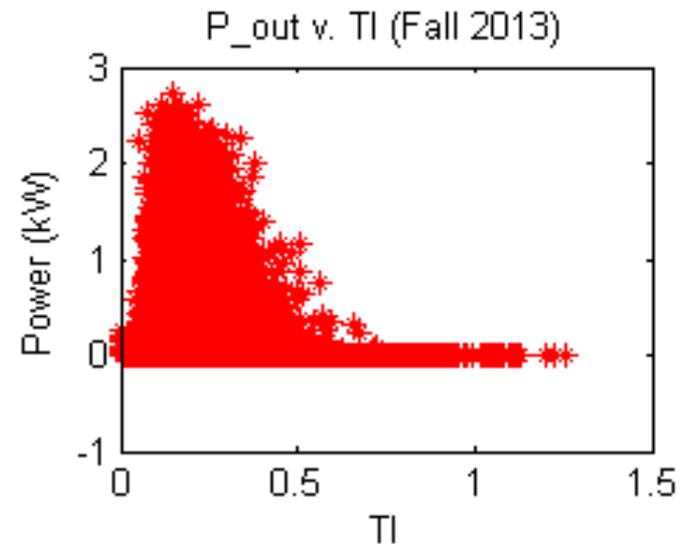
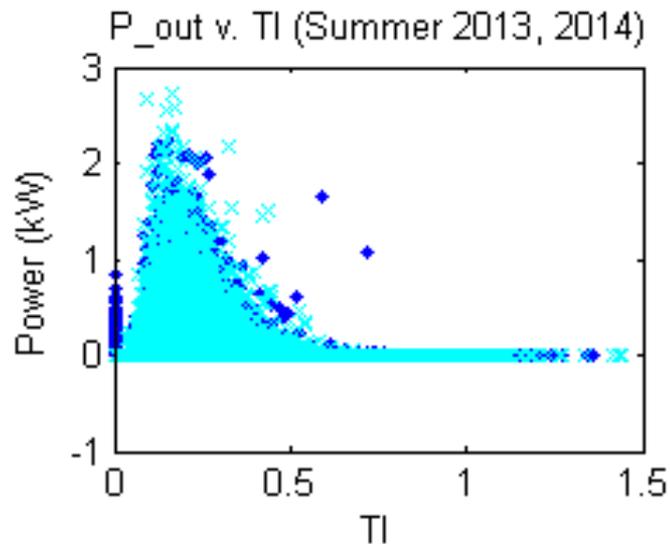
- Collect site characteristics data from wind turbine location
- Determine relationship between  $P$  and  $TI$
- Quantify statistical distribution of in situ  $TI$  frequency
- Verify/compare results with IEC standards, Albers (1997) and Sunderland et al (2013)



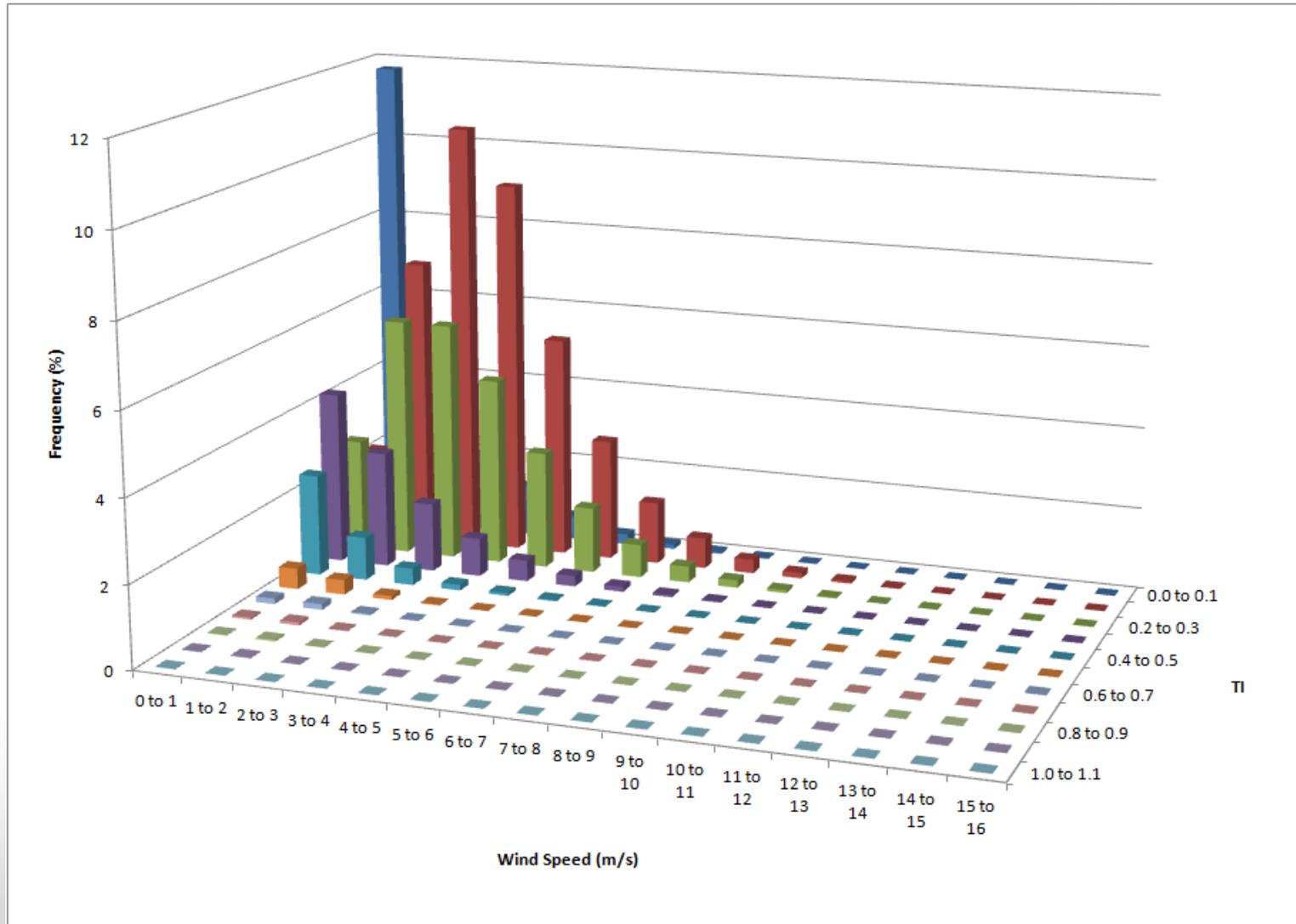
The turbine power and turbulence intensity were quantified over 15 months (6/13-9/14). Excluding anomalies like turbine maintenance, power exhibits strong statistical correlation with turbulence intensity.



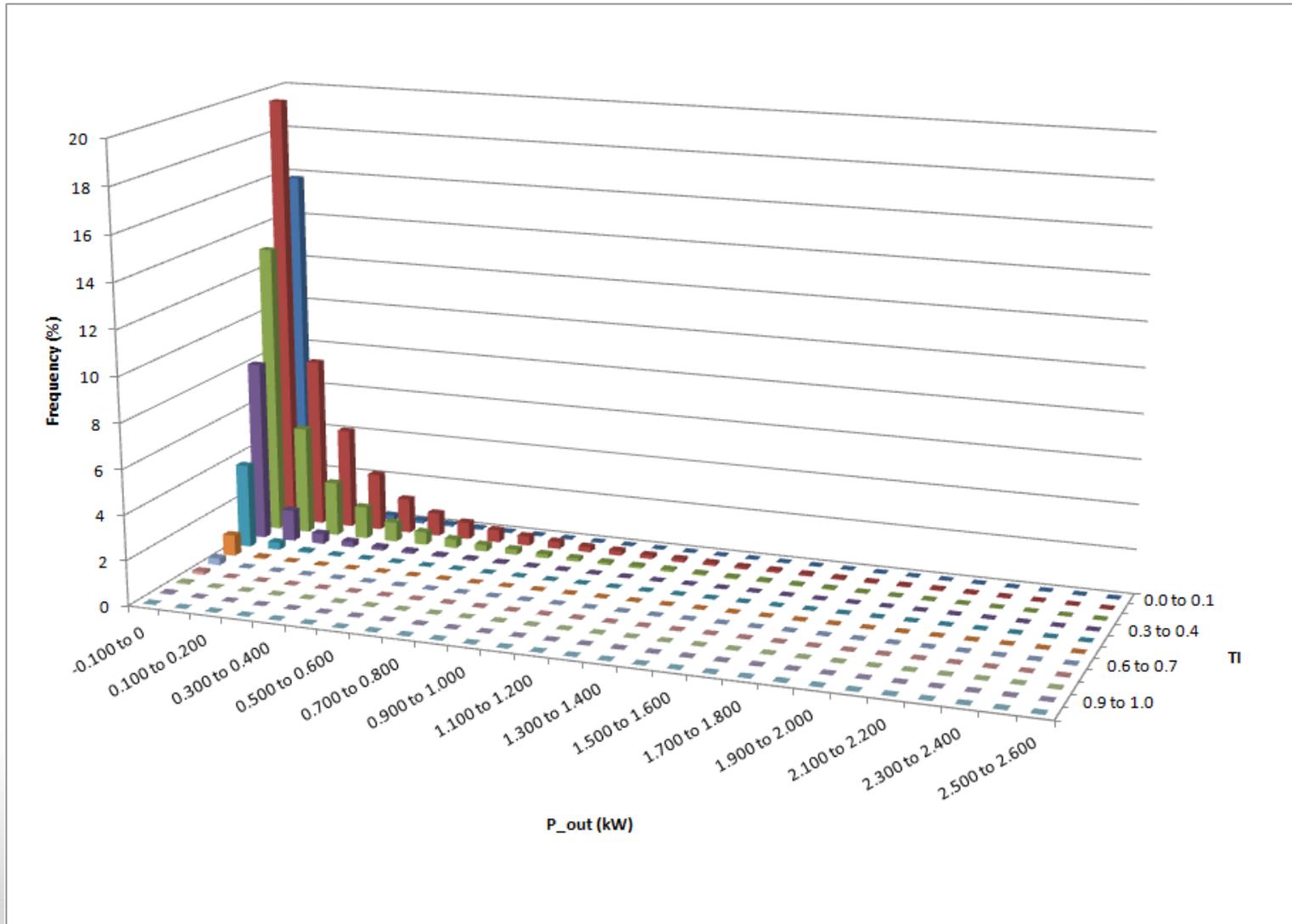
# Seasonal Variation of Power & Turbulence Intensity



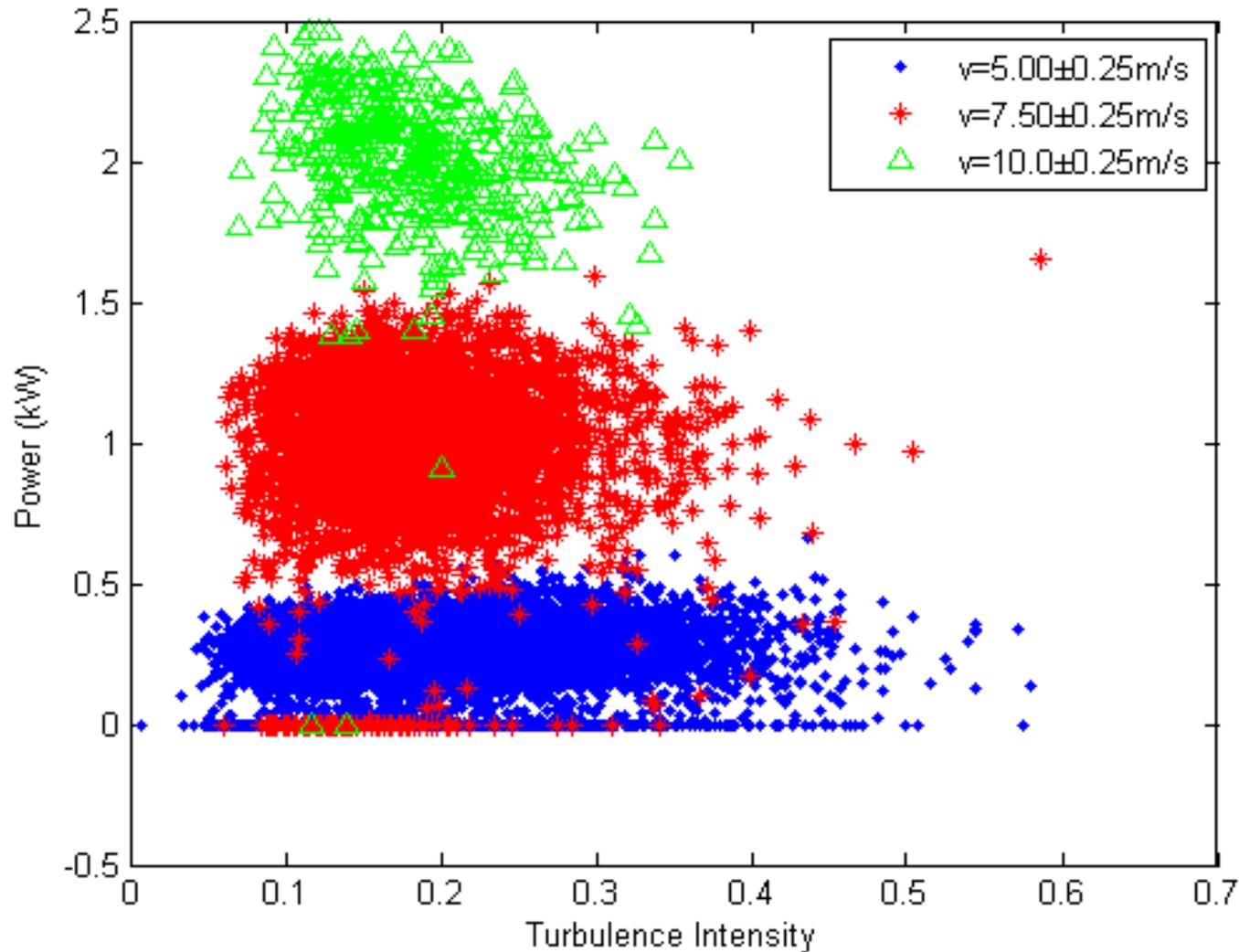
Common industrial practice requires a Weibull distribution for frequency of wind speed [Woolmington et al (2014)]. However, an empirical distribution match for turbulence intensity is more difficult.



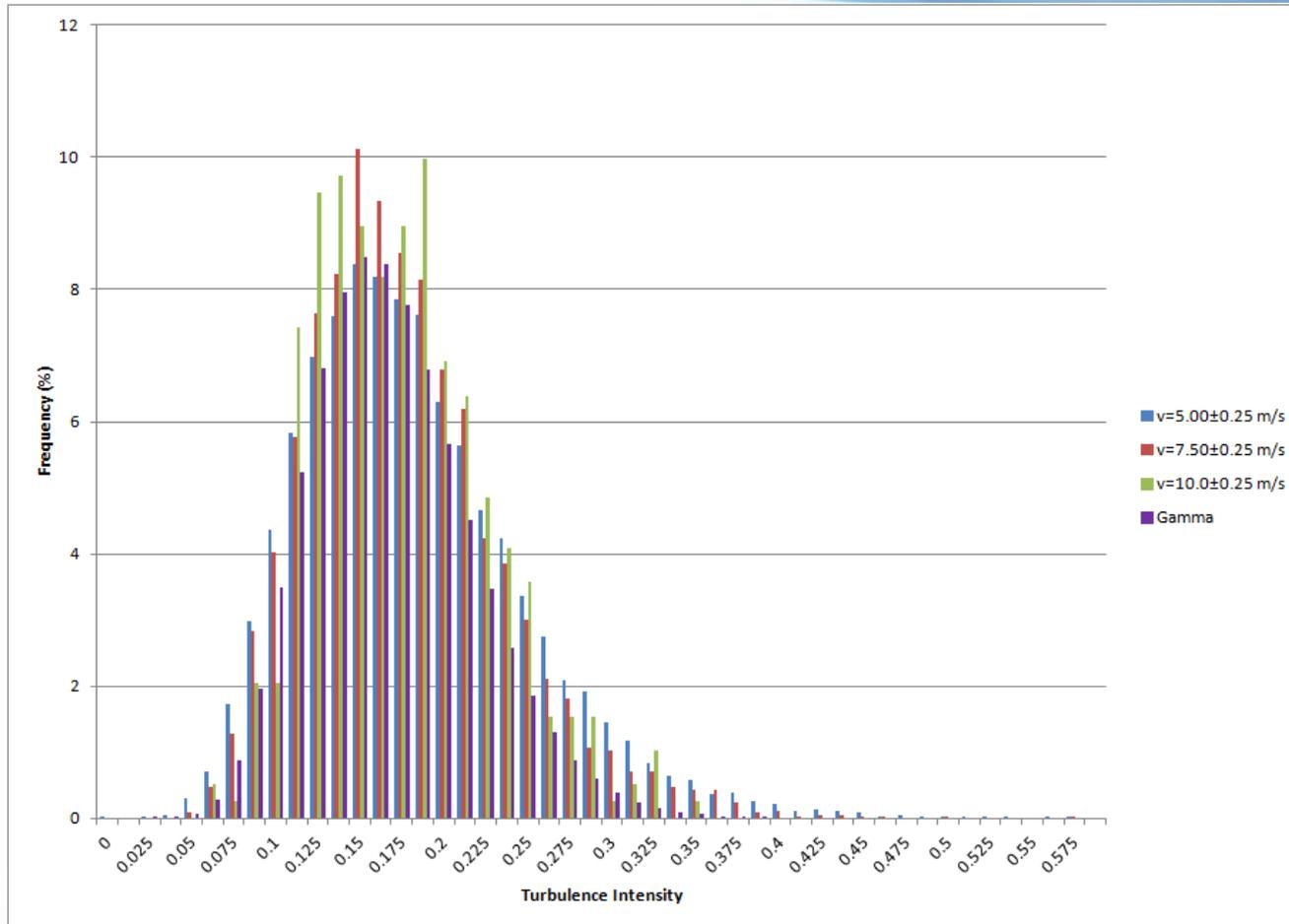
Wind speed dependence for the turbine power curve enables statistical correlation between frequency of occurrence for power and  $Tl$ .



The culmination of these turbulence intensities at constant velocities enable “binning” of turbine power output. With smaller wind speeds, the power output increases for increased  $TI$ , exhibiting periods of overdrive.



Turbulence intensity tends to follow a Gamma distribution ( $k=12$ ,  $\theta=0.014$ ) at constant wind velocity.

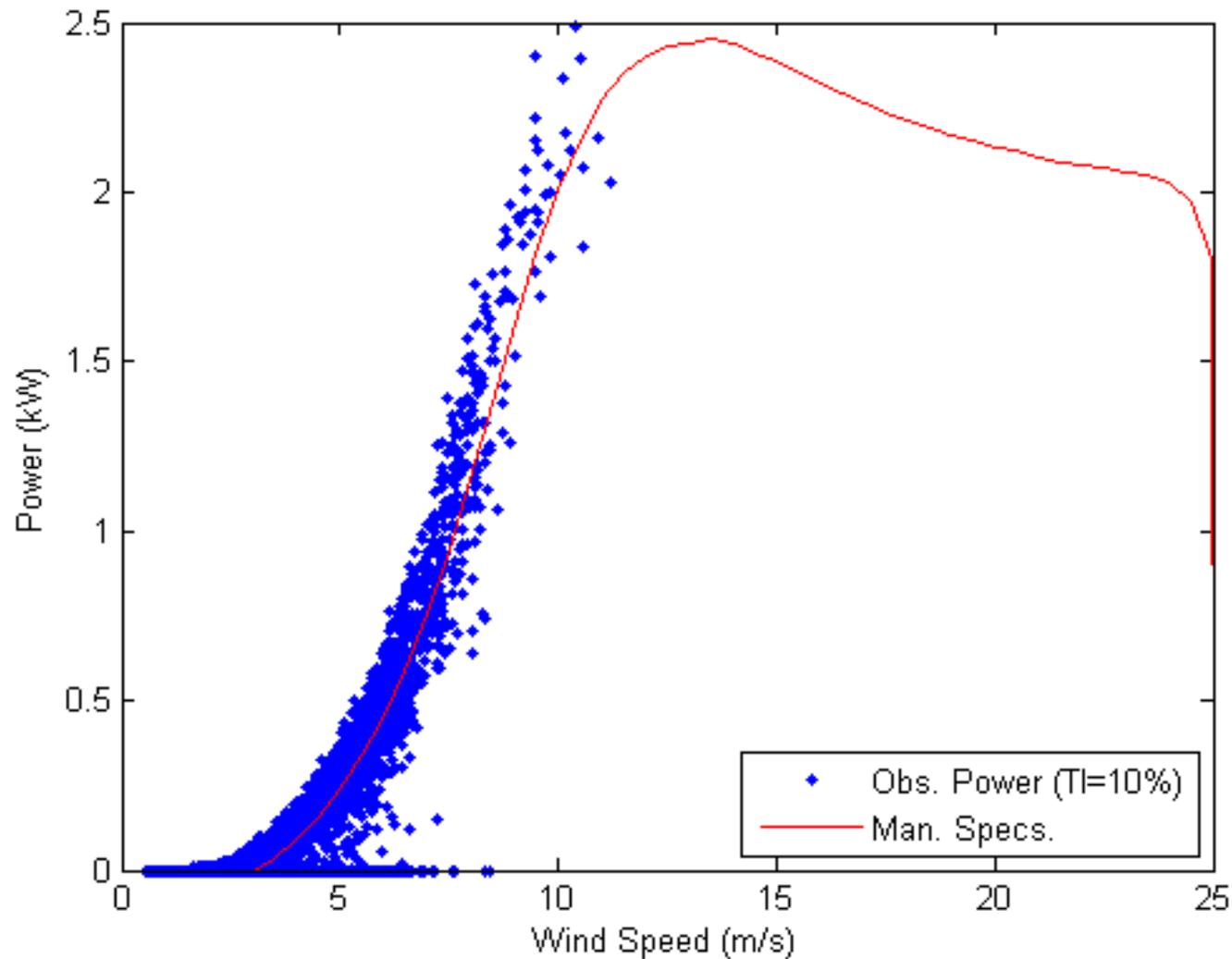


$$f(x; k, \theta) = \frac{x^{k-1} e^{-x/\theta}}{\theta^k \Gamma(k)}; x, k, \theta > 0$$

# Relative Error Between Gamma Function and Observed $Tl$

Wind Speed (m/s)	Min Error (%)	Max Error (%)	Mean Error (%)
5.00±0.25	0.00	1.66	0.45
7.50±0.25	0.00	1.67	0.42
10.0±0.25	0.00	3.18	0.79

# Example of TI Integration into Wind Turbine Power Curve



# Conclusions & Future Work

- The gamma function is a good indicator to estimate power performance incorporating  $TI$
- Power output increased by as much as 60% for lower wind speeds at higher  $TI$ , but decreased power by as much as 17% for high wind speeds and  $TI$
- A more standardized approach for  $TI$  integration into the power curve was tested and correlated well with results from Sunderland et al (2013) and Albers (1997)
- Over-performance is possible for low wind speed regimes with high  $TI$
- This process can be integrated into (or verified by) industry accepted programs like WT\_Perf and FAST for computer simulations predicting stochastic loads due to turbulence and their effects on power production for any turbine size in any location

# Acknowledgments

- Research advisor: Dr. Susan Stewart
- Mr. Brian Wallace
- Aerospace & Energy Engineering  
Departments
- Penn State Center for Sustainability

# References

1. Ewing et al (2008). “Analysis of Time-varying Turbulence in Geographically-dispersed Wind Energy Markets.” doi:10.1080/15567240701232162
2. Saranyasootorn & Manuel (2008). “On the propagation of uncertainty in inflow turbulence to wind turbine loads.” doi:10.1016/j.jweia.2008.01.005
3. Web of Science
4. Manwell et al (2010). “Wind Energy Explained: Theory, Design and Application.” 2<sup>nd</sup> Edition. ISBN: 978-0-470-01500-1
5. Wang et al (2014). “A new turbulence model for offshore wind turbine systems.” DOI: 10.1002/we.1654
6. Woolmington et al (2014). “The progressive development of turbulence statistics and its impact on wind power predictability.” doi: 10.1016/j.energy.2014.03.015
7. Albers (1997). “Turbulence and Shear Normalisation of Wind Turbine Power Curve.”
8. Sunderland et al (2013). “Small wind turbines in turbulent (urban) environments: A consideration of *normal* and *Weibull* distributions for power prediction.” doi:10.1016/j.jweia.2013.08.001



# Questions?

# Quantifying Power and Turbulence

- Turbine power ( $P$ ) is a function of the cube of the velocity ( $v$ ), air density ( $\rho$ ) and rotor area ( $A$ ) [Manwell et al (2010)]

$$P = C_p \frac{1}{2} \rho A v^3$$

- Turbulence intensity ( $TI$ ) is the ratio of the standard deviation ( $\sigma$ ) to the mean wind speed ( $V$ ) [Wang et al (2014)]

$$TI = \frac{\sigma}{V}$$

- It can therefore be quantified that turbine power can related to turbulence intensity

$$P = f(TI)$$

# Sunderland et al (2013) Key Figure

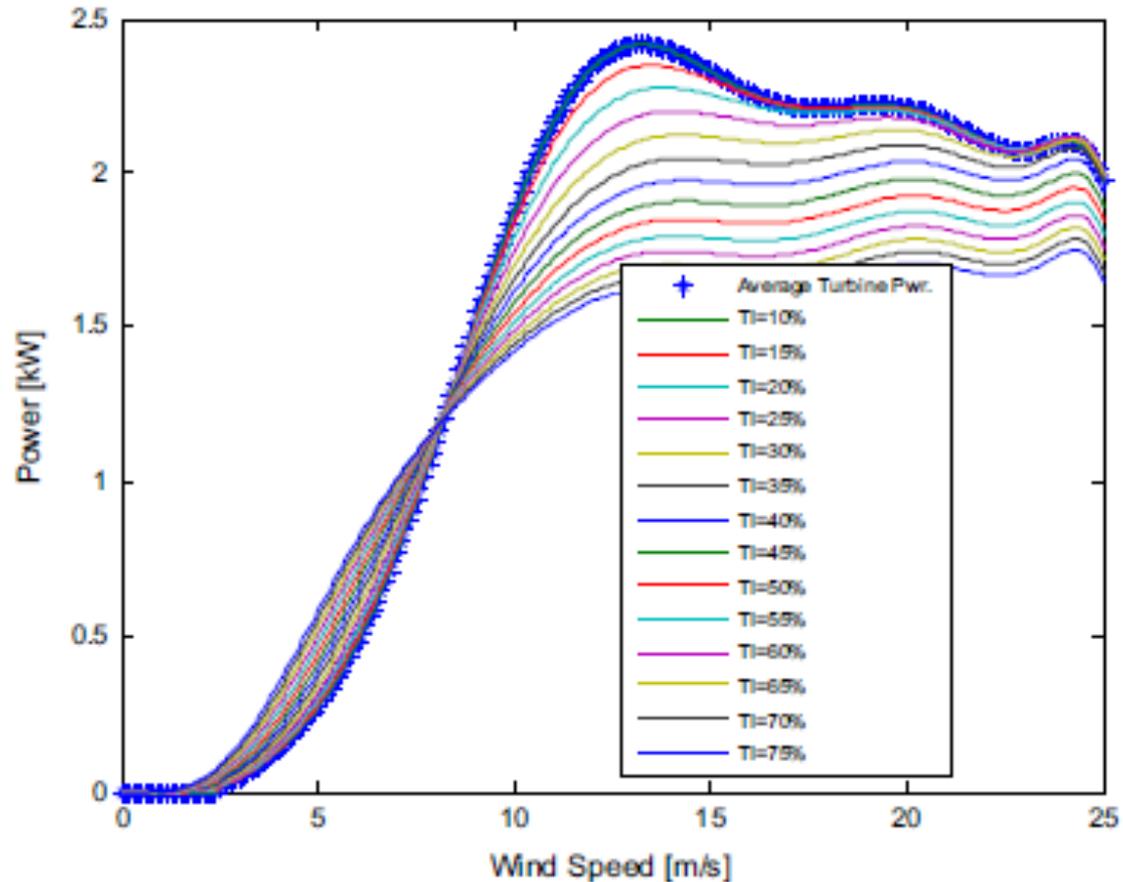


Fig. 5. Albers normalisation of the Skystream 3.7 (2.4 kW) power curve in terms of varying  $TI$  and wind speed.

# Albers (1997) Key Figure

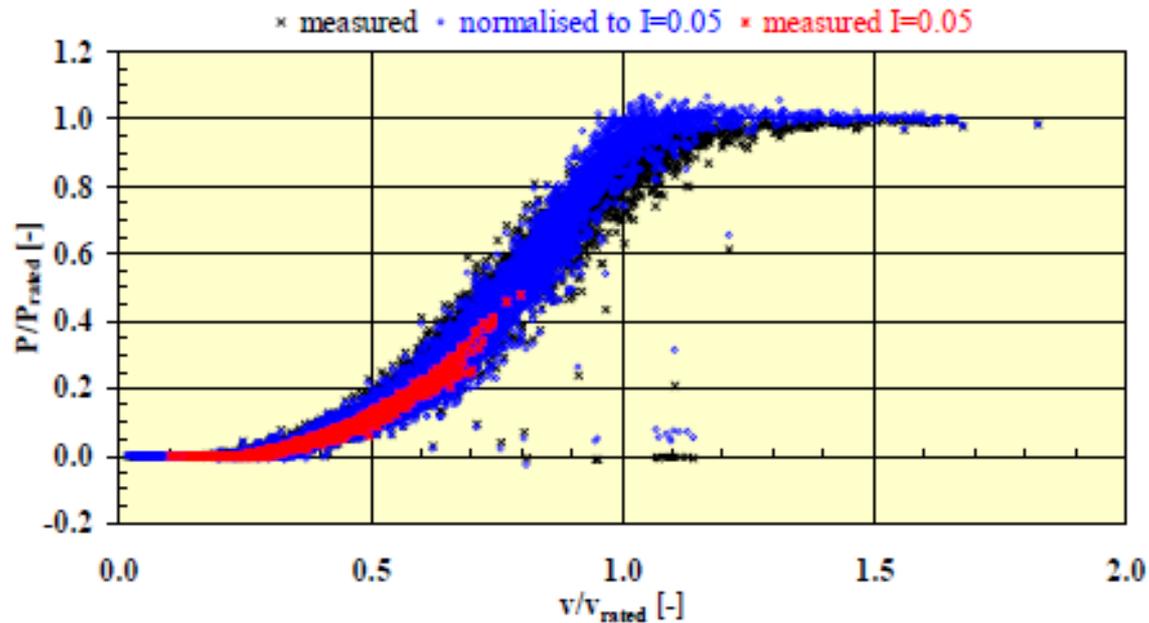


Figure 6: same as Figure 4 but normalisation to 5 % turbulence intensity (blue) and filtering to turbulence range 2.5%-7.5 % (red).