



BRADLEY DEPARTMENT  
of ELECTRICAL & COMPUTER ENGINEERING

# **A Game-theoretic Framework to Investigate Conditions for Cooperation between Wind Power Producers and Energy Storage Operators**

Siddharth Bhela  
Dr. Kwa-Sur Tam

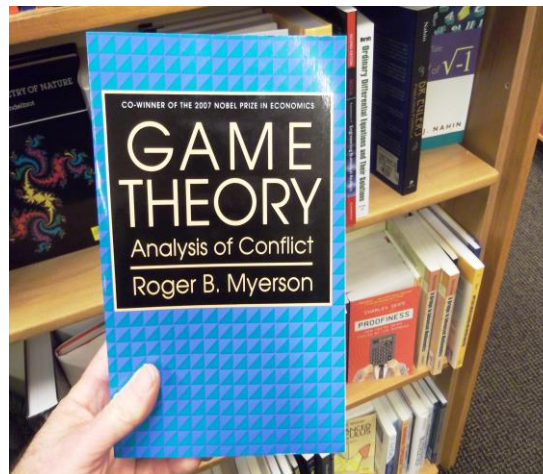
# Objective



Wind Power Producer



Energy Storage Operator



# Problem Definition

- Wind is intermittent
- Generation-load mismatch (Imbalance/Deviation)
  - Energy Storage
  - Demand Response
  - Additional Operating Reserves (Ancillary Services)
- Energy storage (Li-ion batteries)
  - Short-term Imbalances - Regulation Service (min-to-min fluctuations)
  - Larger Imbalances - Capacity Firming/Energy Smoothing (hour-to-hour)

# Problem Definition...Cont'd

- **Current Market**

- Low penetration of renewables (<20%)
- Utility bears cost of procuring expensive generator reserves
- No Imbalance Penalties
- Storage operates independently in energy and reserves markets

- **Future Market**

- Increased penetration (20-35%)
- Utility will offset some cost to wind producers through proposed mechanism of imbalance penalties.
- Energy Storage Operators may enter into agreements with Wind Power Producers to provide what is promised

# Current Approach

- Optimize sizing, placement and scheduling of energy storage to minimize wind power imbalances (collocated)
- Maximize revenues through independent operation in reserve market (arbitrage/regulation etc.)
- Most problem formulations don't take into account imbalance penalties imposed on wind power producers
- Studies that take into account imbalance penalties are solely concerned with the optimal contracting of wind power to decrease these penalties and maximize the revenues of the wind power producer

# Problem Definition...Cont'd

- Should Energy Storage Operators enter into an agreement with Wind Power Producers to balance any wind deviations?

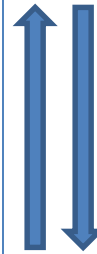
# Network Model



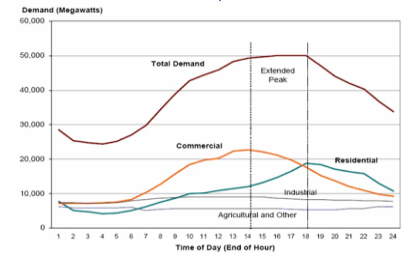
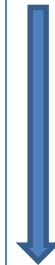
Utility



Wind Power  
Producer



Energy Storage  
Operator



Load Entity

# Model Assumptions and Parameters

Variable Name	Variable Definition	Variable Value
$S$	Storage Size	4 MWh
$SOCC_t, S_t$	State of Charge at time 't'	
$\gamma_c, eff$	Charging/Discharging Efficiency of Storage Device	0.9
$\gamma_s$	Self-Discharge Rate of Storage Device	1
$T$	Time Period	1 hour
$\bar{q}^D, Dlim$	Discharge Limit	1MW
$\bar{q}^R, Clim$	Charge Limit	1MW
$q_t^R$	Quantity purchased through arbitrage at time 't'	
$q_t^D$	Quantity sold through arbitrage at time 't'	
$q_t^{RU}$	Quantity of UP regulation offered into the market at time 't'	
$q_t^{RD}$	Quantity of DOWN regulation offered into the market at time 't'	
$P_t$	Day-Ahead Electricity Market Price (LMP) at time 't' - \$/MWh	
$P_t^{RU}$	Market Clearing Price for UP regulation at time 't' - \$/MWh	
$P_t^{RD}$	Market Clearing Price for DOWN regulation at time 't' - \$/MWh	
$C_d$	Cost of Discharging at time 't' (\$/MWh)	0
$C_r$	Cost of Charging at time 't' (\$/MWh)	0

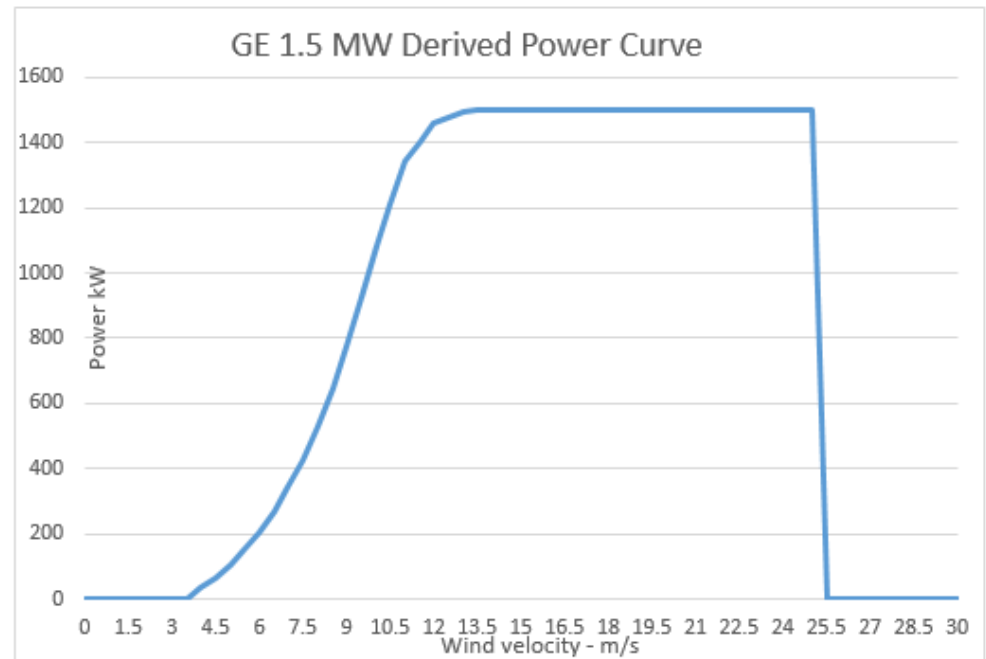


# Game-theoretic Framework

- Wind Model
  - Extrapolation of Data from 50m to 80m

- Wind Power Output
- Persistence Model

- Load Model



# Game-theoretic Framework...Cont'd

- Wind Deviation/Variability

$\Delta \bar{w}_t < 0$  – STORAGE DISCHARGING REQ.

$\Delta \bar{w}_t > 0$  – STORAGE CHARGING REQ.

- Load Deviation/Variability

$\Delta \bar{l}_t < 0$  – STORAGE CHARGING REQ.

$\Delta \bar{l}_t > 0$  – STORAGE DISCHARGING REQ.

- Net Deviation/Variability

$$\Delta \bar{n}_t = \Delta \bar{w}_t - \Delta \bar{l}_t$$

# Game-theoretic Framework...Cont'd

- Energy Storage Model

- Balancing Deviations

$$N_t = \max(\min(x_1, \min(S - x_2, \bar{q}^R)), \max(-x_2, -\bar{q}^D))$$

$x_1 = \text{change in stored energy}, x_2 = \text{stored energy}$

- Maximizing Revenues (Arbitrage + Reg. Service)

$$\min_x f^T x \text{ such that } \begin{cases} Ax \leq b \\ A_{(eq)} x = b_{eq} \\ lb \leq x \leq ub \end{cases}$$

$$x = [q_1^D \quad \dots \quad q_T^D \quad q_1^R \quad \dots \quad q_T^R \quad q_1^{RU} \quad \dots \quad q_T^{RU} \quad q_1^{RD} \quad \dots \quad q_T^{RD}]'$$

# Pay-off Matrix

STORAGE \ WIND	COOPERATION	NON-COOPERATION
COOPERATION	<b>A</b> (Case 1) <b>B</b>	<b>C</b> (Case 2) <b>D</b>
NON-COOPERATION	<b>G</b> (Case 4) <b>F</b>	<b>E</b> (Case 3) <b>D</b>

# Case 1

- Energy storage has four streams of revenue:
  - Balancing Wind deviations ( $\Delta\bar{w}_t$ ).
  - Balancing Load deviations ( $\Delta\bar{l}_t$ )
  - Arbitrage
  - Regulation Service
- Wind Power Producer pays an imbalance fee ( $\partial_1^i, \partial_1^e$ ) to the storage and may also pay penalty ( $\partial_2^i, \partial_2^e$ ) to the utility

# Case 2

- Energy Storage has four streams of revenue:
  - Balancing Load Deviations ( $\Delta \bar{l}_t$ )
  - Balancing Wind Deviations ( $\Delta \bar{w}_t$ )
  - Revenue from Arbitrage
  - Revenue from Regulation Service
- Wind Power Producer pays penalty  $(\partial_2^i, \partial_2^e)$  to the utility

# Case 3

- Energy Storage has three streams of revenue:
  - Balancing Net Deviations ( $\Delta \bar{n}_t$ )
  - Arbitrage
  - Regulation Service
- Wind Power Producer chooses to not cooperate and pays the penalty ( $\partial_2^i, \partial_2^e$ ) to the utility

# Case 4

- Energy Storage has three streams of revenue:
  - Balancing Net Deviations ( $\Delta \bar{n}_t$ )
  - Arbitrage
  - Regulation Service
- Wind Power Producer pays the penalties ( $\partial_2^i, \partial_2^e$ ) to the utility. Penalty is paid only on underproduction. Overproduction is curtailed



# Results – January (Base Case)

STORAGE \ WIND	COOPERATION	NON-COOPERATION
<b>COOPERATION</b>	<b>\$6,988</b>	<b>\$8,514</b>
<b>NON-COOPERATION</b>	<b>\$5,422</b>	<b>\$4,870</b>
	<b>\$707</b>	<b>\$195</b>
	<b>\$2,108</b>	<b>\$195</b>

STORAGE \ WIND	COOPERATION	NON-COOPERATION
<b>COOPERATION</b>	<b>A=\$4,645</b> <b>B=\$2,343</b>	<b>A=\$8,514</b> <b>B=\$0</b>
<b>NON-COOPERATION</b>	<b>A=\$5,422</b> <b>B=\$0</b>	<b>A=\$4,870</b> <b>B=\$0</b>
	<b>A=\$707</b>	<b>A=\$195</b>
	<b>A=\$2,108</b>	<b>A=\$195</b>

# Discussion

- Wind power producer's cooperative strategy dominates its non-cooperative strategy
- Energy storage operator's cooperative strategy dominates its non-cooperative strategy
- There is a unique pure-strategy Nash Equilibrium in all the cases studied and cooperation is self-enforcing.

# Conclusion

- Game-theoretic Framework can be used as an effective tool to study behavior of two independent players, namely wind power producer and energy storage
- Imbalance Penalties are a necessary condition for cooperation
- Game equilibrium does not depend on storage parameters even when stretched to their limits
- Game equilibrium is unchanged across seasons – winter, spring, summer and fall

# Future Work

- Model the other streams of revenue for the storage (spinning /non-spinning reserves, voltage support etc.)
- Allow wind power producers to participate in the ancillary services market
- Model a three player game with the utility as a player

A scenic landscape featuring rolling hills in the foreground and middle ground, covered in trees with vibrant autumn foliage in shades of orange, yellow, and green. In the background, a large, rounded mountain rises against a clear blue sky with a few wispy clouds. The overall atmosphere is peaceful and scenic.

Thank You!