

# **Pavement Friction Management (PFM) – A Step towards Zero Fatalities**

Dissertation submitted to the faculty of the Virginia Polytechnic Institute and State University in  
partial fulfillment of the requirements for the degree of

Doctor of Philosophy

in

Civil Engineering

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December 2, 2015

Blacksburg, Virginia

Keywords: Friction, pavement, safety, management.

# **Pavement Friction Management (PFM) – A Step towards Zero Fatalities**

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## **ABSTRACT**

It is important for highway agencies to monitor the pavement friction periodically and systematically to support their safety management programs. The collected data can help implement preservation policies that improve the safety of the roadway network and decrease the number of skidding-related crashes. This dissertation introduces new approaches to effectively use tire-pavement friction data for supporting asset management decisions. It follows a manuscript format and is composed of five papers. The first chapter of the dissertation discusses the principles of tire pavement friction and surface texture. Methods for measuring friction and texture are further discussed in this chapter. The importance of friction in safety design of highways is also highlighted. The second chapter discusses a case study on developing pavement friction management program. The proposed approach in this chapter can be used by highways agencies to develop pavement friction management program. Contrary to general perception, that friction is only influencing wet condition crashes, this study indicated that friction is associated with both wet and dry condition crashes.

The third and fourth chapters of the dissertation introduce a soft-computing approach for pavement friction management. Artificial Neural Network and Fuzzy Logic approach are presented. The learning ability of Neural Network makes it appealing as it can learn from examples; however, Neural Network is generally complicated and hard to understand for practical purposes. The Fuzzy system on the other hand is easy to understand. The advantage of Fuzzy system over Artificial Neural Network is that it uses linguistic and human like rules. Sugeno Neuro-Fuzzy approach is used to tune the proposed Fuzzy Logic model. Neuro-Fuzzy approach has the benefit of incorporating both “learning ability” of neural network and human ruled based decision making aspect of fuzzy logics. The application of the fuzzy system in real-time slippery spot warning system is demonstrated in chapter five.

Finally, the sixth chapter of the dissertation evaluates the potential of grinding and grooving technique to restore friction properties of the pavement. Once sleek spots are identified through pavement friction management program, this technique can be used to restore the friction without compromising the roadway smoothness.

## **ACKNOWLEDGEMENTS**

I would like to express my sincerest gratitude to my supervisor, Dr. Gerardo Flintsch, who supported me throughout my dissertation with his patience and knowledge. Without him, this dissertation would not have been completed.

I would like to thank the rest of my committee members: Dr. Taheri, Dr. Trani, and Dr. Guo for their valuable help throughout my studies.

I would like to thank all of my friends and fellows at the Center for Sustainable Transportation Infrastructures (CSTI) group: Ryland, Billy, Edgar, Samer, Saeid, James, Lijie, Akiyaa, Flippo, Chris, Daniel and Paul for all the fun we had together in the last several years.

I would like to thank my colleagues at the Virginia Department of Transportation (VDOT): Allen, Ray, Ruth, Pat, James, Tammy, Robin, David, Travis, Kevin, Brian, Affan, Tanveer and Raja for their help and support throughout my studies.

Lastly, and most importantly, I would like to thank my parents for supporting me throughout all my studies. To them I dedicate this dissertation.

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## **CHAPTER 1 - INTRODUCTION**

Frictional properties of the pavements play a significant role in road safety as the friction between tire and pavement is a critical contributing factor in reducing potential crashes. When a tire is free rolling in a straight line, the tire contact patch is instantaneously stationary and there is little or no friction developed at the tire/road interface, although there may be some interactions that contribute to rolling resistance. However, when a driver begins to execute a maneuver that involves a change of speed or direction, forces develop at the interface in response to acceleration, braking, or steering that cause a reaction between the tire and the road (called friction) which enables the vehicle to speed up, slow down, or track around a curve. To reduce the number of fatalities, injuries, and properties damage due to car crashes, the Federal Highway Administration (FHWA) recommends that highway agencies implement safety management programs that include pavement friction (FHWA 2010).

Car crashes can be due to several factors related with the driver, the vehicle, the environment, and the roadway infrastructure. As lack of sufficient friction between the tire and pavement is one of the factors that can increase the risk of car crashes, it is important for Departments of Transportation (DOTs) to monitor the friction of their pavement networks frequently and systematically and take pro-active measures to reduce skidding crashes.

### **PROBLEM STATEMENT**

FHWA policies recommend highways agencies to develop a Pavement Friction Management (PFM) program to reduce the risk of fatal and injury causing crashes and take corrective actions to address friction deficiencies. This requires an in-depth understanding of the tire-pavement friction and its relationship to vehicle crashes as well as developing appropriate methods to correct friction deficiencies.

FHWA technical advisory T5040.36 and the American Association of State Highway and Transportation Officials (AASHTO) Guide for Pavement Friction Management have presented several approaches to define minimum and desirable friction levels. Most approaches require historical friction and accident data which may not be available. This necessitates alternative

methods to model the relationship between vehicle crashes and friction and use the model to manage desirable network level of friction.

## **OBJECTIVE**

The objective of this dissertation is to develop a framework for PFM program to minimize fatal and injury causing vehicle crashes. Specifically, the research aims to answer the following questions:

1. Is there a relationship between the rate of vehicle crashes and tire-pavement friction?
2. Can soft-computing techniques being used to develop a PFM program?
3. What is the best approach to incorporate PFM in real-time application and connected vehicles framework?
4. How to achieve an optimal surface texture level that improves tire-pavement friction without compromising ride quality?

## **ORGANIZATION OF THE DISSERTATION**

This dissertation follows a manuscript format and is composed of five papers. The first chapter provides background information on the principles of tire-pavement friction and surface texture. Methods for measuring friction and texture are further discussed in this chapter. The importance of friction in safety design of highways is also highlighted.

The second chapter of the dissertation discusses a case study on developing pavement friction management program. The study suggests that both wet and dry crashes have to be considered when developing a PFM. Contrary to general perception, that friction is only influencing wet condition crashes, this study indicated that friction is associated with both wet and dry condition crashes.

The third and fourth chapters of the dissertation introduce a soft-computing approach for pavement friction management. Chapter three presents the Artificial Neural Network approach. The current methods of developing PFM suggested by the AASHTO guide for pavement friction

were examined and their limitations were discussed. The results suggest that Neural Network model can reliably predict the rate of crashes.

The learning ability of Neural Network makes it appealing as it can learn from examples; however, Neural Network is generally complicated and hard to understand for practical purposes. The Fuzzy system on the other hand is easy to understand. The advantage of Fuzzy system over Neural Network is that it uses linguistic and human like rules. The application of the Fuzzy system in PFM is presented in chapter four. Sugeno Neuro-Fuzzy approach is used to tune the proposed Fuzzy Logic-based model. Neuro-Fuzzy approach has the benefit of incorporating both “learning ability” of neural network and human ruled based decision making aspect of fuzzy logics. The application of the Fuzzy system in a real-time slippery spot warning system is demonstrated as a proof of concept in chapter five.

Finally, the sixth chapter of the dissertation evaluates the potential of grinding and grooving technique to restore friction properties of the pavement. Once sleek spots are identified through pavement friction management program, this technique can be used to restore the friction without compromising the roadway smoothness.

## **SIGNIFICANCE**

This dissertation introduces a new approach for developing PFM based on soft-computing. Furthermore, it introduces the concept of real-time slippery spot road warning system to be utilized in connected vehicle studies.

Several researchers have studied the association between wet condition car crashes and friction. This dissertation evaluates the effect of friction on both wet and dry car crashes. Finally, it introduces a methodology to achieve an optimal pavement surface with high friction and low roughness.

## **BACKGROUND<sup>1</sup>**

The principles of friction and texture are explained in this section. Methods for measuring pavement surface friction and texture and the factors that can affect these measurement are further discussed. The importance of friction in safety design of highways is also highlighted in the proceeding.

### **Effect of Tire Pavement Friction on Roadway Safety**

Each year many people around the world lose their lives in vehicle crashes, which are one of the leading causes of death in the United States (U.S.) (Roa 2008). This has led Federal Highway Administration (FHWA) to implement new policies that require the state Departments of Transportation (DOTs) to implement highway safety programs with the purpose of reducing car crashes.

The friction between tire and pavement is a critical factor in reducing crashes (Hall et al. 2009; Henry 2000; Ivey et al. 1992). Most of the skidding problems occur when the road surface is wet due to friction deficiencies. The study performed in Kentucky in 1972 revealed that the rate of wet crashes increases as the surface friction drops below a certain value. The data for the study were collected on rural interstates and parkways. The study also confirmed the relationship between the rate of wet to dry crashes and pavement friction (Hall et al. 2009). In the study that was performed in Texas, it was found that higher percentage of crashes happen on roads with low friction while a few crashes happen on roads with high friction (Hall et al. 2009). Many researchers have developed models to predict the association between car crashes and friction. Most studies confirm the association between high rate of car crashes and low level of pavement friction.

Rizenbergs et al. (1972) did a friction study on rural interstate routes in Kentucky using a ribbed-tire locked-wheel friction tester. They found that wet crash rates as well as wet-to-dry crash ratios increased once the friction numbers dropped below 40 (Rizenbergs et al. 1972). McCullough and Hankins (1996) studied the relationship between friction and crashes for 571

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<sup>1</sup> Part of this chapter has been published under “The Little Book of Tire-Pavement Friction”. Co-authors include: Gerardo Flintsch, Edgar de Leon, and Kevin McGhee.

sites in Texas. The result of the study revealed that the majority of crashes happened on the sites with low friction, while a few crashes happened on the sites with high friction values. They proposed a minimum desirable friction threshold of 0.4 measured at 30 mph (McCullough and Hankins 1966).

Xiao et al. used fuzzy-logic to predict the risk of wet pavement crashes (2000). They used the accident and traffic data from 123 sections of highways in Pennsylvania. The data were collected from 1984 to 1986. The inputs to the model were skid number, posted speed, average daily traffic, percentage wet time and driving difficulty and the output was the number of wet crashes. The researchers found that fuzzy-logic can be used to predict the rate crashes. Furthermore, it can be used to determine the corrective action to be taken to improve the safety (Xiao et al. 2000).

## Friction and Surface Texture

### *Basic Concepts of Friction*

According to the AASHTO Guide for Pavement Friction; “pavement friction is the force that resists the relative motion between a vehicle tire and a pavement surface” (FHWA 2010). The friction force between tire and pavement is generally characterized by a dimensionless coefficient known as coefficient of friction ( $\mu$ ), which is the ratio of tangential force at the contact interface to the longitudinal force on the wheel. These forces are demonstrated in Figure 1.

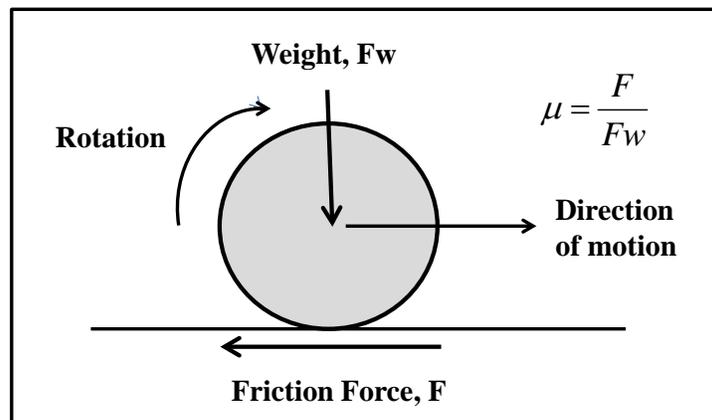


Figure 1 Force body diagram for rotating wheel.



rubber on a molecular scale and provide adhesion. This component of the texture is especially important at low speeds but needs to be present at any speed.

On wet pavements, as speed increases skid resistance decreases and the extent to which this occurs depends on the macrotexture, typically formed by shape and size of the aggregate particles in the surface or by grooves cut into some surfaces. Generally, surfaces with greater macrotexture have better friction at high speeds for the same low-speed friction (Roe and Sinhal 1998) but this is not always the case. Since all friction test methods can be insensitive to macrotexture under specific circumstances, it is recommended that friction testing be complemented by macro-texture measurement (ASTM E-1845). It has been found that at speeds above 56 mph on wet pavements, macrotexture is responsible for a large portion of the friction, regardless of the slip speed (Hall et al. 2009).

### ***Components of Tire Pavement Friction***

Tire pavement friction is the result of two main forces, adhesion and hysteresis. Adhesion is due to the molecular bonding between the tire and the pavement surface while hysteresis is the result of energy loss due to tire deformation. As the tire passes through pavement, surface texture causes deformation in the tire rubber. This deformation is the potential energy stored in the tire. As the tire relaxes part of this energy will be recovered and part of it will be dissipated in form of heat. The generated heat (energy loss) is known as hysteresis. Both hysteresis and adhesion are related to surface characteristics and tire properties (Hall et al. 2009). The key components of tire pavement friction are illustrated in Figure 3.

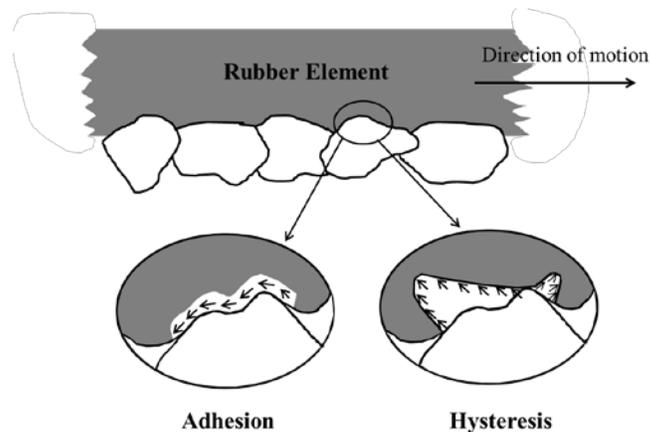


Figure 3 Key components of tire pavement friction (after Hall et al. (2009)).

### ***Braking, Accelerating, and Cornering***

When a tire is free rolling in a straight line, the tire contact patch is instantaneously stationary and there is little or no friction developed at the tire/road interface, although there may be some interactions that contribute to rolling resistance. However, when a driver begins to execute a maneuver that involves a change of speed or direction, forces develop at the interface in response to acceleration, braking, or steering that cause a reaction between the tire and the road which enables the vehicle to speed up, slow down, or track around a curve.

During braking, as the braking force increases, the reacting force increases until it approaches a point at which the peak coefficient of friction available between the tire and the road is exceeded (this normally occurs between 18 and 30 percent slip). At this point (commonly known as “peak friction”), the tire continues to slow down relative to the vehicle speed and to slip over the road surface, even though the wheel is still rotating. If the braking force continues, the tire slips even more. Eventually complete locking of the wheel occurs, at which time the wheel stops rotating and the tire contact patch skids over the road surface.

On a dry road surface, there is often little difference between peak and sliding friction and relatively little effect of speed. However, on a wet road, peak friction is often lower than in dry conditions, the sliding friction is typically lower than peak friction, and both usually (but not always) decrease with increasing speed. The differences between wet and dry and peak and sliding friction depend not only on vehicle speed and tire properties (including tread depth and pattern), but also to a large extent on the characteristics of the road surface, particularly its state of microtexture, the form and magnitude of the macrotexture, and the amount of water and other contaminants on the pavement (the importance of which is discussed further below).

An analogous situation occurs during acceleration: although in normal circumstances the tire contact patch remains instantaneously stationary, too great a demand for acceleration can overcome the peak friction available and the wheel will start to slip, or in the extreme, to spin with little or no vehicle acceleration (as on ice).

Similarly, in cornering, the side forces generated make the vehicle follow a curved path. If the combination of forward speed and the effective radius of curvature (influenced by the

geometry of the road and steering angle) result in a demand for friction that exceeds what the road can provide, the wheel may slip sideways. If the demand is high enough to overcome peak friction, the wheel may slide sideways causing the vehicle to yaw. In this situation, a marked difference between peak and sliding friction could lead to a rapid loss of control.

The situation is exacerbated when braking and cornering occur simultaneously, because the available friction has to be shared between the two mechanisms. If the peak is exceeded, the side-force goes down to near zero and the operator loses all control of steering. This is why anti-lock braking systems (ABS) are important. They detect the onset of wheel slip and momentarily release and then re-apply the brakes to make sure the peak friction is not exceeded and to reduce the likelihood of side-slip occurring, thus helping the driver to maintain control. Similar ideas are used in some modern vehicle control systems to reduce the risk of side-slip occurring under simultaneous acceleration and cornering.

However, it is important to appreciate that while the instantaneous deceleration rates (and inversely stopping distances) with ABS functioning may be greater than for a vehicle skidding with locked wheels, there can be situations (particularly when the road is wet and the friction level is low) when the average friction (including the times when the wheel is released as well as those when it is slipping) will be less than in the locked-wheel condition.

### **Measuring tire-pavement friction**

Since the friction depends on the interaction between the tire and the pavement, different measurements are obtained for different testing conditions. This has led to the development of different testing devices, which operate under different conditions. As the tire freely rolls on the pavement surface, longitudinal frictional forces generate at the tire and the pavement interface. The relative speed between the tire circumference and the pavement surface (slip speed) is zero (or very low) during free rolling (no braking) condition. Applying a constant brake to the tire will increase the slip speed to the potential maximum equivalent of the vehicle speed. This relationship can be mathematically expressed as follow (Hall et al. 2009):

$$S = V - V_p = V - (0.68 \times \omega \times r) \quad (1)$$

Where: S = Slip speed (mph)

$V$  = Vehicle directional speed (mph)  
 $V_p$  = Average peripheral speed of tire (mph)  
 $\omega$  = Angular velocity of the tire (radians/Second)  
 $r$  = Average radius of the tire (ft)

If the average peripheral speed of tire ( $V_p$ ) is equal to the vehicle speed therefore the slip speed ( $S$ ) will be zero. During the fully locked wheel braking condition  $V_p$  is zero. This makes the slip speed to be equal to vehicle speed. Most literature referred to locked wheel condition as 100 percent slip ratio and the free rolling condition as the zero slip ratio (fully locked condition). The slip ratio can be mathematically expressed as follow (Hall et al. 2009):

$$SR = \frac{V - V_p}{V} \times 100 = \frac{S}{V} \times 100 \quad (2)$$

Where: SR = slip ratio.

When the vehicle steers around a curve or changes lanes another type of friction force generates at the tire pavement interface. This type of friction is called lateral (side-force) friction (Hall et al. 2009; Shahin 2005). The angle between test wheel and direction of travel is known as “yaw angle”. The force-body diagram of a vehicle steering on a curve is shown in Figure 4. According to the diagram the side force friction can be defined as (Shahin 2005).

$$SFC = \frac{\textit{sideways \cdot force}}{\textit{vertical \cdot reaction \cdot between \cdot tire \cdot and \cdot road \cdot surface}}, \quad (3)$$

Where: SFC = sideways friction coefficient.

The slip ratio of the test wheel is related to the yaw angle of the wheel and it can be calculated as follow:

$$\textit{Slip \cdot Angle} = \textit{Sin}(\alpha) \quad (4)$$

Where:  $\alpha$  = Yaw angle.

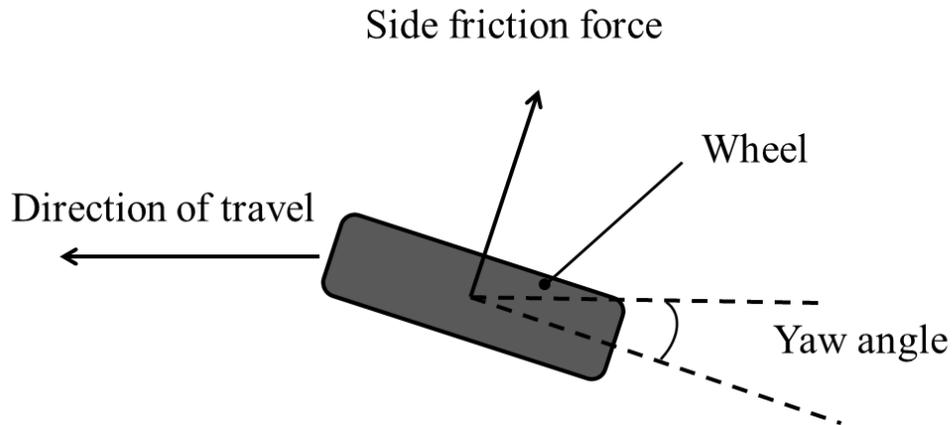


Figure 4 Force-body diagram for a wheel traveling round a curve with constant speed (after Hall et al. (2009)).

Similar to slip speed, the slip ratio is zero during free rolling and it is maximum (100 percent) during fully locked condition. When a tire is free rolling in a straight line, the tire contact patch is instantaneously stationary and there is little or no friction developed at the tire/road interface, although there may be some interactions that contribute to rolling resistance. However, when a driver begins to execute a maneuver that involves a change of speed or direction, forces develop at the interface in response to acceleration, braking, or steering that cause a reaction between the tire and the road which enables the vehicle to speed up, slow down, or track around a curve.

### ***Principles of Friction Measuring Equipment***

Several different friction measuring devices have been developed over the years. They all rely on the broad principle of sliding rubber over a road surface and measuring the reaction forces developed in some way. There are essentially four general principles.

- (i) Sliders, attached either to the foot of a pendulum arm or to a rotating head, which slow down on contact with the road surface. The rate of deceleration is used to derive a value representing the skid resistance of the road. A variant of this approach, still used by police forces in some parts of the world, is to measure the reaction force when a sled (with sliders representing car tires) is dragged over the road surface.
- (ii) Sideway Force Coefficient (SFC) measurement uses an instrumented measuring wheel set at an angle to the direction of travel of the vehicle. Although normally freely rotating

because it is set at an angle, the tire is made to slip over the road surface and the resulting force along the wheel axle (the “side force”) is measured. The ratio of vertical and side forces averaged over a defined measuring length provides the value that is recorded to represent skid resistance. The wheel angle determines the slip ratio and the vehicle speed determines the slip speed.

- (iii) Longitudinal Friction Coefficient (LFC) measurement uses an instrumented measuring wheel aligned with the direction of travel. A fixed gear or braking system forces the test wheel to rotate slower than the forward speed. Consequently, the tire contact patch slips over the road surface and a frictional force is developed that can be measured. Typically, the ratio of vertical and drag forces is calculated (averaged over a fixed measuring length) to provide a value representing the LFC that is recorded. Within this category there is a wide range of slip ratios that may be used by individual devices. The slip ratio is usually governed by the control system to a fixed proportion of the forward speed which, in turn, determines the slip speed. Locked wheels (Figure 5) measure the longitudinal friction by completely locking the brake of the measuring wheel, regardless of the test vehicle speed. This simulates emergency braking without anti-lock brakes system (ABS). Locked wheels can either use ribbed tire or smooth tire. Ribbed tires are known to be less sensitive to pavement macrotexture and water film depth than smooth tires. Figure 6 shows an example of a fixed-slip friction tester.



Figure 5 Locked-wheel friction tester.



Figure 6 GripTester.

- (iv) Decelerometers are typically custom-made units mounted in a test vehicle, used to measure the deceleration of a vehicle under emergency braking. Widely used by police forces to assess road surface friction for collision investigations, and more recently in experimental naturalistic driving studies, these devices are not suitable for road network assessment or quality control purposes. They are further discussed later in this chapter.

Over the last several years, agencies around the world have started using Continuous Friction Measuring Equipment (CFME) for highway friction management (mainly fixed-slip technology). CFME has the advantage of operating under conditions similar to those of vehicles equipped with ABS. They are designed to test the friction at a slip ratio between 10 to 30 percent, which is around the critical slip of most ABSs. Another advantage of these systems over locked-wheels is that they continuously measure the friction across the entire stretch of a road, providing greater detail about spatial variability of the tire-pavement frictional properties. Furthermore, the locked-wheel testers and fixed slip devices like the GripTester cannot measure the lateral friction at curves as side force equipment does (Najafi et al. 2011).

To better understand the function of ABSs, the interaction between friction and the slip ratio is illustrated in Figure 7. At zero slip (free rolling) there is no friction. Friction starts to increase as the slip increases and reaches a peak friction value. Peak friction happens around critical slip (typically between 10 to 30 percent). ABSs are designed to maintain the slip near the

peak by turning the brakes on and off. After the peak, friction starts to decrease until it reaches the full sliding, which corresponds to a 100 percent slip (fully locked) condition. The coefficient of friction values around this point is lower than at the peak friction. Locked-wheel skid testers test the friction with 100 percent slip ratio. In general, the friction before the peak is affected mainly by tire properties, while surface properties have the main effect after the peak (Henry 2000).

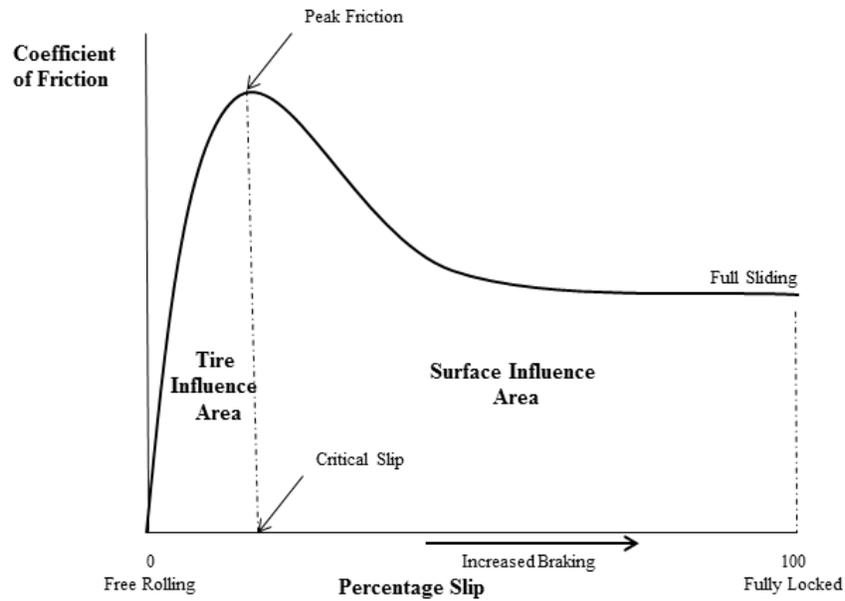


Figure 7 Friction versus slip (after Henry (2000)).

### ***Real-time friction estimation from regular fleet vehicles***

Due to the importance of tire-pavement friction in vehicle dynamics and stability control, several researchers have investigated various methods to estimate the tire-pavement friction in real time. For highway agencies, a real-time estimate of the tire-pavement friction can be used to detect sleek spots which can then be treated to reduce the risk of friction related crashes. It can also be used for winter maintenance operations so the operator can adjust the amount of chemical/abrasives based on the available friction (Erdogan et al. 2009). Real-time friction estimation can be categorized into two categories; 1- sensor-based estimation, and, 2- vehicle dynamic-based estimation (Rajamani et al. 2010).

### ***Sensor-based Friction Estimation***

Special sensors can be installed in the vehicle chassis or in the tire carcass to measure the friction in real time. Varieties of sensors capable of measuring tire-pavement friction are documented in the literature (Rajamani et al. 2010).

Acoustical sensors can be mounted in the car to record the sound made by the tire at the interface and use that to estimate the friction at the tire-pavement interface (Rajamani et al. 2010). The correlation between tire noise levels and friction has been documented (Eichhorn and Roth 1992). Correlation model between tire noise and friction can be used to estimate the friction at the interface in real-time (Breuer et al. 1992; Eichhorn and Roth 1992).

Stresses and strains in the tire can also be used to estimate the tire-pavement friction (Breuer, et al. 1992; Eichhorn and Roth 1992; Rajamani et al. 2010). Strain sensors can measure the deformation in the tire at the contact patch in various directions and use that to estimate the forces interfering at the tire-pavement interface. Using the magnitude and direction of these forces will allow the estimation of friction at the contact patch possible (Rajamani et al. 2010).

Various types of optical sensors have also been implemented to estimate the road friction. Optical sensors can detect surface type based on the ground reflection (Rajamani et al. 2010). Several commercial systems are available that use the same concept to detect the snow and ice on the road surface (SENSICE ; VAISALA). These systems are mostly used for winter maintenance monitoring purposes. Some laser-based optical sensor cannot operate during wet condition as the water on the pavement refracts the laser beam.

The main drawback of sensor-based estimation of tire-pavement friction is the cost associated with acquiring the sensors. Sensors also have a limited service life which makes them less desirable for frequent test applications. Frequent calibration requirements can also cause user-time delays and it can increase the maintenance costs. Installing the sensors in the tire carcass can also raise liability issues. Optical laser also have limited application during wet weather condition. So for the above reasons this method was not implemented in this dissertation.

### **Vehicle Dynamic Control-based Friction Estimation**

In this approach tire-pavement friction is estimated based on the vehicle motion. This method uses the measurements from the sensors already installed in the vehicle which gives it leverage over sensor-based approach that requires additional sensors being installed in the car.

As the tire freely rolls on the pavement surface, longitudinal frictional forces generate at the tire and the pavement interface. The relative speed between the tire circumference and the pavement surface (slip speed) is very low during free rolling (no braking) condition. Applying a constant brake to the tire will increase the slip speed to the potential maximum equivalent of the vehicle speed. The coefficient of friction can be determined based on the relationship between normalized forces on the tire and the slip ratio (Rajamani et al. 2010). This relationship can be explained by the “magic formula” tire model (Bakker et al. 1989; Pacejka and Bakker 1992). The relationship between normalized tire forces versus slip ratio for various road surfaces with different friction levels is presented in Figure 8.

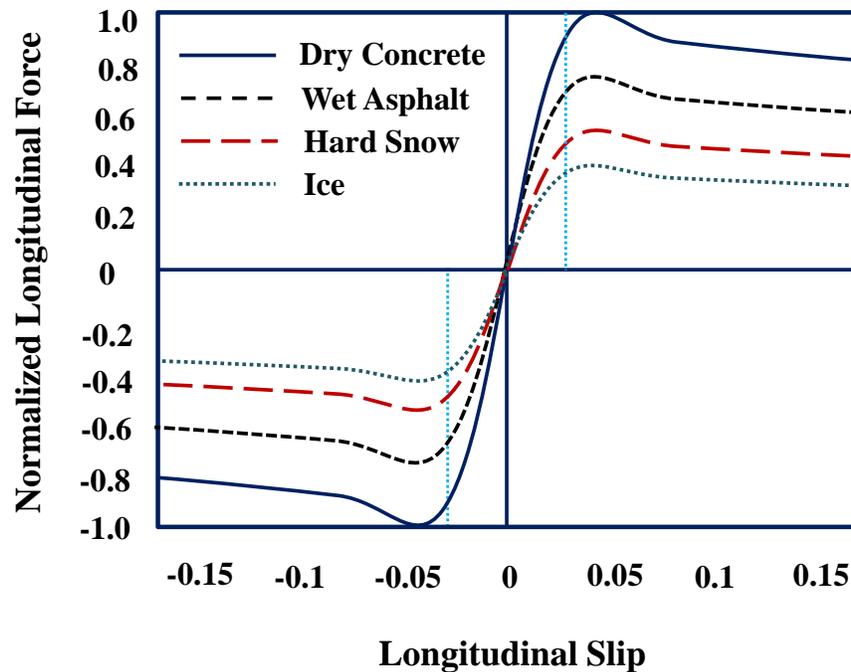


Figure 8 Normalized longitudinal tire forces versus slip ratio (after Rajamani et al. (2010)).

For small slip ratios, the normalized tire forces are “proportional” to slip ratio (Rajamani et al. 2010). The coefficient of friction can be determined based on the slope at the low slip region – commonly known as “slip-slope” (Rajamani et al. 2010). The low slip/force data can be measured from traction which usually happens during acceleration condition (Uchanski et al. 2003). Some references argue that tire properties influence the “shape” of the low slip region versus the road surface properties (Henry 2000; Uchanski et al. 2003). It is cited that for slip ratios greater than 0.005, the slip-slope method can reliably estimate the coefficient of friction (Rajamani, Piyabongkarn et al. 2010). References (Dieckmann 1992; Germann et al. 1994; Gustafsson 1997; Yi et al. 1999; Hwang and Song 2000) have used this method to estimate the tire-pavement friction.

Another approach to finding the coefficient of friction is based upon the “saturated” normal tire force (the peak force). As can be seen from Figure 2, normalized forces on the tire “saturate” at high slip ratios and begin to decrease as the longitudinal slip increases. The “saturated” normalized forces on the tire are proportional to the coefficient of friction and can be used to estimate the coefficient of friction (Rajamani et al. 2010). Medium to high slip/force data can be measured from braking (Uchanski et al. 2003). This method is demonstrated in Müller et al. (2001) and Ray (1997).

### ***Macrotexture Measuring Techniques***

Macrotexture can be measured using both highway speed profilers and static methods. While static devices can be used for project level measurements, the high speed devices are more appropriate for network level data collection. There are two basic measurement techniques. The oldest of these is the volumetric “patch” test in which a known volume of sand or glass beads (or grease) is placed on the road surface and spread into a circular patch, filling the voids. The area of the circle is measured and thus the average depth below the peaks in the surface is calculated to give a value known as Mean Texture Depth (MTD).

In more recent years, laser displacement sensors, which measures along a narrow line traversed by the laser (rather than across the area of a patch of sand or glass beads), have been used to determine a surface profile from which a number of different parameters may be calculated to represent the texture depth. Of these, root mean square (RMS) texture depth has

been used extensively both in research and as part of friction management in other countries. However, the most widely used parameter internationally, and defined in the ASTM E-1845 standard, is the Mean Profile Depth (MPD), which also attempts to estimate the average depth below the peaks in the surface. The standard device for measuring macrotexture is Circular Track Meter (CTMeter) (ASTM E 2157). This static texture measuring device (Figure 9) has a displacement sensor mounted on an arm at which rotates at a fixed elevation from the surface collecting a high-resolution profile. The device is controlled by a computer that records the data and reports the processed data as MPD and RMS. This device was found to have good correlation with mean texture depth (MTD), which has been found highly correlated to speed constant in the PIARC experiment described in the next section (Wambold et al. 1995).

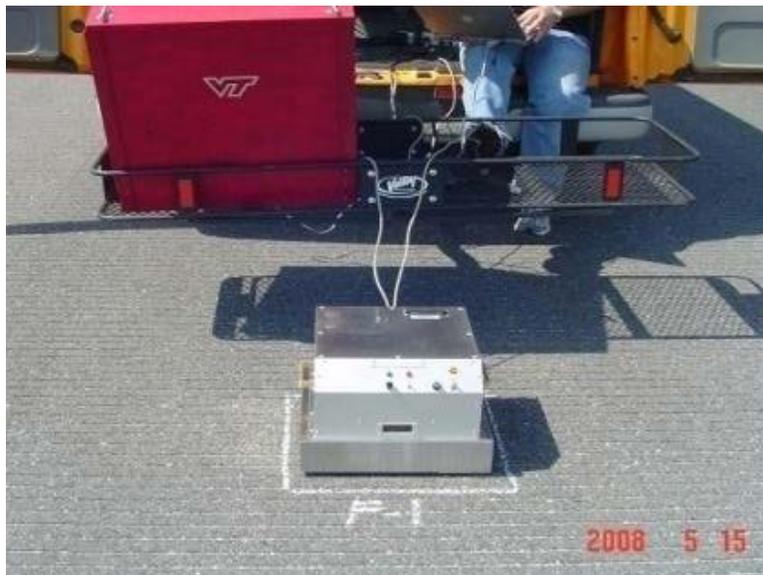


Figure 9 Circular Track Meter (CTMeter).

Research is showing that although both are useful in some situations, an alternative to RMS or MPD measures will likely be necessary to fully characterize road surface behavior. What that index should be is not clear at the moment. A device that measures both, friction and macrotexture, concurrently is needed to determine both low-speed and high-speed friction performance (and their relative relevance in different situations) from a single measurement pass. On dry pavement with good texture, the tire envelopes the texture and the depth of the penetration in the footprint is a tire property; however, when wet, water can partially prevent the penetration if the macrotexture is not deep enough. Tire tread and macrotexture sometimes are

not enough to allow the water to escape and thus causes the water to be present in the tire pavement interface. MPD accounts for some of this, but not all and this needs to be taken into consideration.

### ***Operational Factors Affecting Friction Measurements***

There are several operational factors that can affect the friction measurement. Better understanding of these factors can help highway agencies to establish standard testing condition and approaches for correcting measurement taken under other conditions.

Water film thickness is one of the factors that have been proven to affect the friction measurements. The water on the pavement surface decreases the tire-pavement contact area which results in reduction in friction. This effect is known to be more noticeable at higher speeds (>40 mph) compared to lower speeds (Hall et al. 2009). Worn tires are known to be more sensitive to water film thickness. Pavement macrotexture and tires threads can provide channels for water to escape through the tire-pavement contact area which result in increasing the traction between tire and the pavement surface. The effect of water film thickness on locked wheel skid trailer measurements is illustrated in Figure 10. The friction measurements (skid numbers) are collected at 40 mph. Figure 10 suggests that smooth tires are more sensitive to the changes of water film thickness. Due to the less sensitivity of ribbed tires to operational test conditions and water film thickness some recommends them as the preferred choice for friction measurements (Henry 2000). However, since ribbed tires are less sensitive to the pavement macrotexture is it recommended that their measurements be accompanied by macrotexture measurements. Recent studies have also confirmed the sensitivity of Continuous Friction Measuring Equipment (CFME) to water film thickness and other operational test conditions (Najafi et al. 2012).

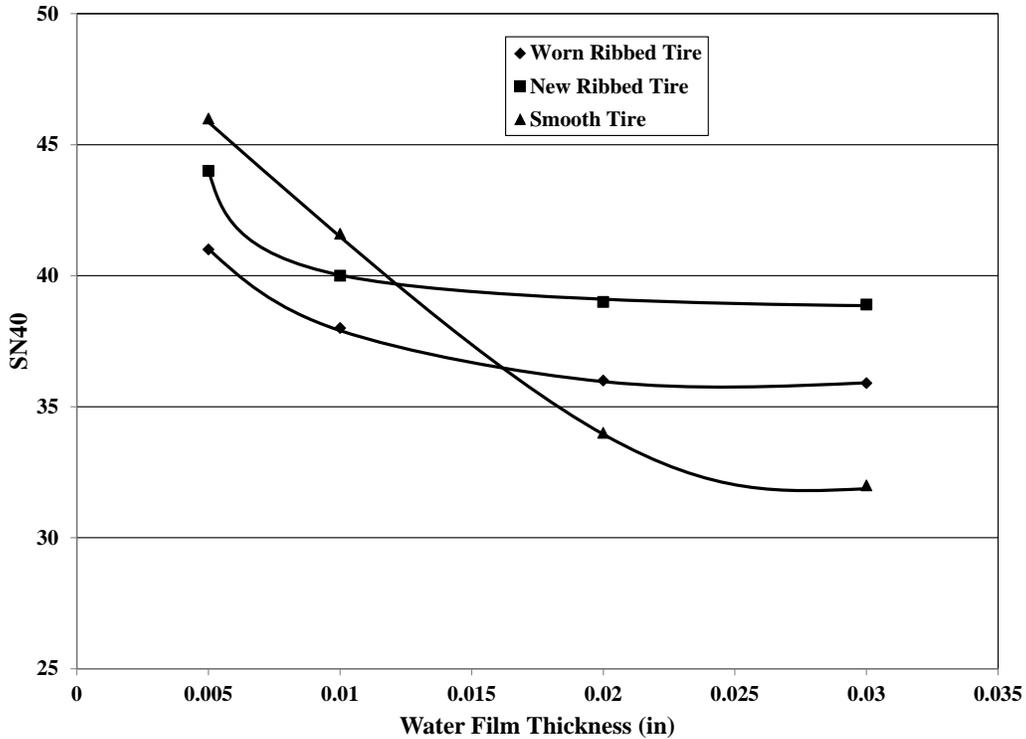


Figure 10 Effect of water film thickness on skid measurements (after Henry (2000)).

Since both hot mix asphalt surface and tires are viscoelastic materials, temperature can also affect their properties. Research has indicated that tire-pavement friction decreases if the tire temperature increases (Hall et al. 2009).

Jayawickrama and Thomas (1998) found that variation in skid numbers measurements can be as significant as 10 to 12 skid numbers from one day to another. These variations are due to changes in temperature and precipitation (Jayawickrama and Thomas 1998). Colony (1992) also reported that fluctuation of friction trough out the year has the highest values in the winter and the lowest friction is experienced at the end of the summer. Similarly, Faung and Hughes (2007) detected that skid measurement on Surepave mixes (SM), follows a cyclic pattern with the higher values in winter and low values in fall and summer. Changes in temperature do not have a direct effect on the friction of pavement surface. However, they can affect the properties of the skid tester's tire (Jayawickrama and Thomas 1998). As it was explained before, tire-pavement friction is composed of adhesion and hysteresis. Adhesion is the shear force generated at the interface of the contact area and hysteresis is due to the damping losses in the tire rubber

(Li et al. 2004). Higher temperature makes the tire more flexible. This reduces the energy loss of the tire (hysteresis) and decreases the measured skid number. Nevertheless there is no proof available for this mechanism in the literature. While some studies stated that the effect of temperature is a very insignificant; many others indicate that temperature is a significant factor (Jayawickrama and Thomas 1998). Bazlamit and Reza (2005) indicated that regardless of the surface texture, increasing the temperature decreases the hysteresis component of surface friction while for adhesion component, surface texture affects this behavior (Bazlamit and Reza 2005). Since hysteresis accounts for greater part of total friction, the combined friction of the surface decreases with increasing temperature (Bazlamit and Reza 2005).

Hill and Henry (1982) proposed a model that predicts the seasonal variation in the skid number intercept (SN0). The analysis was based on the data collected on test sites in Pennsylvania from 1978 to 1980.

### **Pavement Friction Management**

Pavement friction management includes both engineering practices to provide a pavement surface with adequate and durable friction and also periodic data collection and analysis to ensure the effectiveness of these practices.

If the reason that the road is slippery is due to some external factor, such as ice on the surface or a local oil spillage, there is little that the road engineer can do, apart from taking measures to prevent ice from forming or having procedures in place to clean up spills. If, however, the road has inherently poor skid resistance because of the materials of which it is made and how those materials have reacted to the passage of traffic over time, then it can be said that the road may contribute to crashes and road engineers should be able to detect such situations and take appropriate action. Inadequate cross slope and/or grade can also contribute to crashes by contributing to flooding the road.

### ***Friction demand***

Friction demand is the level of friction needed to safely perform braking, steering, and acceleration maneuvers. Factors such as traffic volume, geometrics (curves, grades, sight distance, etc.), potential for conflicting vehicle movements, and intersections should be

considered for determining friction demand. Curves and intersections also tend to lose friction at a faster rate than other roadway locations and thus justify a higher friction demand. Highway agencies can establish Investigatory Level (desirable) and Intervention Level (minimum) values for pavement friction and texture in accordance with AASHTO Guide for Pavement Friction.

AASHTO “Guide for Pavement Friction” has defined three methods to establish two distinctive friction threshold levels – investigatory and intervention. The sites with the friction values below investigatory level will be selected for detailed investigation to determine if there is a need for posting warning signs. The sites with friction values below intervention level are typically selected for corrective action such as resurfacing or other programmatic maintenance treatment. The first method uses the friction deterioration curve by plotting friction loss versus pavement age. The friction value at which significant loss rapidly begins is selected as investigatory level as shown in Figure 17. An intervention level can be defined at a fixed percentage below the investigatory level (Hall et al. 2009).

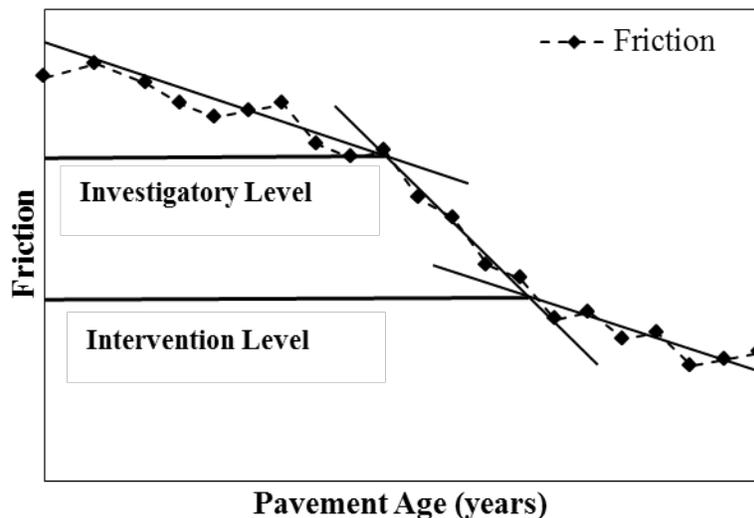


Figure 11 Friction deterioration curve (after Hall et al. (2009)).

The second method uses both friction deterioration curve as well as the historical crash data. The investigatory level is set where there is a significant drop in friction level and the intervention method is set where there is significant increase in crashes (Figure 18) (Hall et al. 2009).

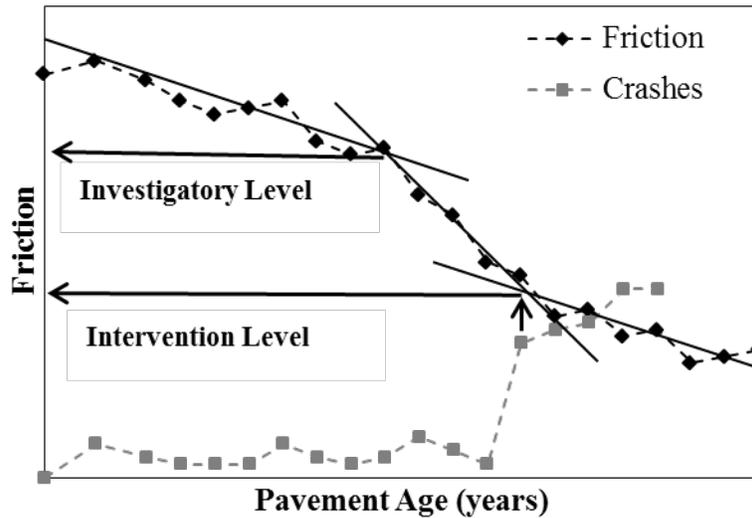


Figure 12 Investigatory and Intervention friction level based on friction deterioration and crash rate (after Hall et al. (2009)).

Finally, the third method uses the friction distribution and crash rate for each roadway category to determine the investigatory and intervention level of friction. The histogram of pavement friction and wet-to-dry crash ratio is plotted first (Figure 19). The mean and standard deviation of friction distribution are then calculated. The investigatory level is set as the mean friction minus “X” (e.g. 1.5 or 2.0) standard deviation and it is adjusted to where wet-to-dry crashes begin to increase considerably. The intervention level is set as the mean friction minus “Y” (e.g. 2.5 or 3.0) standard deviation and it is adjusted to minimum satisfactory wet-to-dry crash rate or by the point where enough funding is available to address the friction deficiencies (Hall et al. 2009). This method is more practical than other two approaches since agency can adjust the intervention friction level based on available funding.

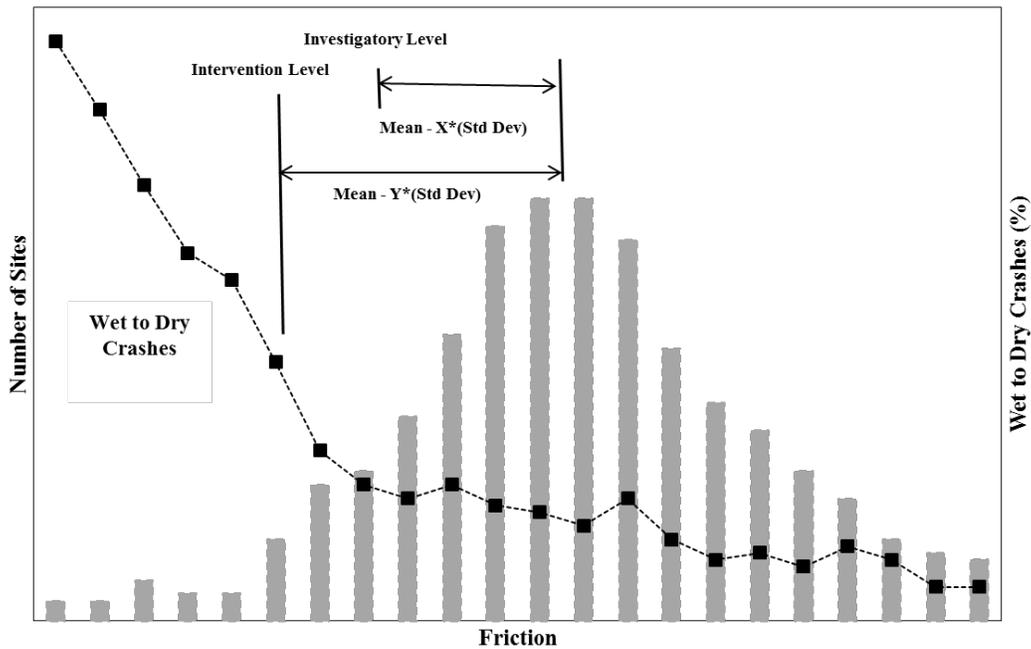


Figure 13 Investigatory and intervention level of friction based on friction distribution and wet-to-dry crash ratio (after Hall et al. (2009)).

***Pavement Friction Management (PFM) program***

The role of a Pavement Friction Management (PFM) program or policy is to provide a framework by which road engineers can monitor the condition of their networks and, based on objective evidence, make appropriate judgments regarding treating or resurfacing the road in those situations that require it. This involves balancing the risk of a crash occurring with the costs and practicalities of providing adequate friction. By enabling vehicles to reduce speeds more rapidly or allowing control to be retained for longer, the consequences of a crash in terms of death or severity of injury may be improved. Although crashes will probably never be completely eliminated, an effective policy can reduce collision risk and reduce the severity level of those crashes that do happen.

Through appropriate pavement design, construction, and maintenance practices; highway agencies can ensure their pavement surfaces provide adequate friction. FHWA Technical Advisory TA 5040.36 "Surface Texture for Asphalt and Concrete Pavements" provides guidelines on state-of-the-practice techniques for providing adequate surface texture and friction (FHWA 2010).

Locations with high rate of wet-weather crashes need to be identified and investigated for the purposes of minimizing friction-related crash rates. The procedure is commonly done by calculating the ratio between wet weather crashes and total crashes (wet + dry) and then following one of the subsequent approaches (FHWA 2010):

- Agencies may use a specific value for the wet crash ratio above which a location will be identified as an elevated wet-weather crash location. Depending on geographical and climate circumstances this ratio can vary between 0.25 and 0.5.
- Agencies may compare the wet crash ratio with the average ratio for that functional class of highway in that area. If the computed ratio is above the average by a specified percentage that location is identified as an elevated wet-weather crash location.
- A minimum number of wet-weather or total crashes within a segment is another criterion that some agencies use in order for a segment to be identified as an elevated wet-weather crash location.

### ***Frequency of friction testing***

The facilities with the highest traffic volumes, the highest likelihood of changes in friction over time, and the highest friction demand justify the most frequent monitoring of friction. A risk-based approach can be implemented to determine the frequency of the friction test for roadway networks. Facilities with higher friction demand require more frequent friction monitoring. Many agencies monitor the friction of their important roadway network on an annual basis. While a 2 to 3 year cycle may be appropriate for the part of network with lower-risk (FHWA 2010).

### **Achieving and Maintaining Adequate Tire-pavement Friction**

#### ***Designing for Friction***

Pavement friction design involves utilizing proper materials and construction techniques to achieve high level of microtexture and microtexture in the pavement surface. Type of the aggregates used in the surface mix directly affects the microtexture while gradation and size of aggregates governs the macrotexture properties of pavement surface. In asphalt mixtures, large

aggregates govern the frictional properties of the surface while for concrete mixes, fine aggregates control the frictional properties (Hall et al. 2009).

The wear characteristics of aggregates are also important in maintaining proper friction level. Aggregates mineralogy and hardness directly affect the durability and polish ability of the aggregates. It is generally better to have aggregates with different size and wear characteristics in the mix so they can constantly renew the surface (Hall et al. 2009).

### ***Restoring Friction***

There are several methods that can be used to restore the frictional properties of old pavements. Diamond grooving is a technique that is used in order to improve the frictional properties of the pavement surfaces (Martinez 1977). This method is mostly used for concrete pavements. The method uses diamond infused steel cutting blades for grinding and grooving concrete pavement. For grinding, the blades are spaced close together so that they can cut the pavement's unevenness (megatexture) and leave a rough pavement surface (high microtexture). For grinding, the blades are further spaced out so they create channels on the pavement surface (high macrotexture). Diamond grooving is mainly used for new concrete pavement to texture the pavement which increases the friction by improving water drainage (Wulf et al. 2008). More discussion on the effect of diamond grinding and grooving on restoring pavement friction is provided in the chapter 5 of the dissertation.

Using High Friction Surfaces (HFS) and epoxy overlays is another option to increase the surface friction. This method can increase the surface friction without jeopardizing other surface characteristics including noise and durability. HFS treatments utilize a durable aggregate and some type of resin (binder) to hold the aggregate particles together and glued to the road surface. There are several types of HFS commercially available in the market including: Cargill, Tyregrip, Italgrip, Crafcro, and Flexogrid (Roa 2008).

### **SUMMARY**

The principles of friction and texture and the factors affecting these measurements were discussed in this chapter. The importance of friction in safety was also highlighted. Most of the

past literature is focused on the effect of friction on wet crashes. Chapter two of the dissertation investigates the effect of friction on dry crashes as well.

Several methods for defining minimum acceptable friction threshold were demonstrated. Most of these methods require historical friction data which is not readily available. Chapter three and four introduce an alternative method based on soft-computing to define an allowable friction threshold.

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## **CHAPTER 2 - LINKING ROADWAY CRASHES AND TIRE-PAVEMENT FRICTION: A CASE STUDY<sup>2</sup>**

### **ABSTRACT**

Tire-pavement friction is a factor that can affect the rate of car crashes. Several studies have suggested that reduced friction during wet weather conditions, due to water on the pavement surface reducing the contact area between the tire and the pavement, increases vehicle crashes. This study evaluates the effect of friction on both wet- and dry-condition crashes. The data for the study were provided by the New Jersey Department of Transportation. Regression analysis was performed to verify the effect of friction on the rate of wet- and dry-condition car crashes for various types of urban roads. It was found that friction is not only associated with the rate of wet-condition car crashes, but it also impacts the rate of dry-condition car crashes. The analysis also suggested that the developed regression models could be used to define the friction demand for different road categories.

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<sup>2</sup> This manuscript has been published in the International Journal of Pavement Engineering (IJPE). DOI:10.1080/10298436.2015.1039005. Co-authors include: Gerardo Flintsch, and Alejandra Medina.

## INTRODUCTION

Each year many people around the world lose their lives in vehicle crashes, which are one of the leading causes of death in the United States. According to a National Transportation Safety (N.T.S.) report, car crashes injure or disable more than 3.2 million people each year in the United States. Every twelve minutes, one person dies in a motor vehicle crash in the United States. These accidents have a great influence on economics and health services (Roa 2013). This has led the Federal Highway Administration (FHWA) to implement new policies that require the state Departments of Transportation (DOTs) to implement highway safety programs with the purpose of reducing car crashes. Several factors, including the driver, the vehicle, the environment, and the roadway infrastructure, can influence the rate of car crashes. Of all these factors, transportation engineers can control only the roadway design factor, which includes road geometry, grade, and surface friction (Flintsch et al. 2012). Highway agencies generally monitor pavement friction as part of their asset management efforts due to its importance in reducing car crashes.

The relationship between friction and car crashes has been well studied by several researchers. Kuttesch developed a model to quantify the effect of friction on wet-weather crashes for the state of Virginia (Kuttesch 2013). Larson et al. studied the effect of friction on wet-condition crashes for the Ohio Department of Transportation (ODOT). The result of the study was a comprehensive list of recommendations for ODOT to improve their roadway network safety (Larson et al. 2013). Schram performed a correlation analysis between the ratio of wet-condition to dry-condition crashes and friction using Iowa DOT data. He further used the model to define the minimum desirable friction level and a specification for aggregate frictional qualities (Schram 2011). Davies et al. studied the effect of friction and texture depth on crash risk for New Zealand's state highway network. They also incorporated the effect of geometry (e.g., curvature, gradient), surface condition (e.g., roughness, rut depth), and roadway characteristics (e.g., region, urban versus rural, traffic flow) into the study (Davies et al. 2005). Viner et al. investigated the link between friction and accidents for the United Kingdom (U.K.) highway network. They found that although skid resistance is an important factor affecting the rate of accidents, the "nature" of this effect is "site specific" (Viner et al. 2004). They later developed a new investigatory friction level for various site categories (Viner et al. 2005).

## **BACKGROUND**

Friction is an important performance parameter of the road surface. It is defined as the force that provides resistance to slipping when the tires are prevented from rolling (Shahin 2005). The friction between tire and pavement is a critical factor in reducing crashes (Henry 2000, Ivey 1992). Most skidding problems occur when the road surface has friction deficiencies due to wetness (Flintsch et al. 2012). According to some sources, one third of all wet-condition crashes are related to surface characteristics of roadways (Fwa 2005). Traditionally, it has been found that pavement friction is high during dry conditions. Data collected with a Sideway-force Coefficient Routine Investigation Machine (SCRIM) device has proven that dry friction is very similar for various surfaces (Fwa 2005). Once the pavement gets wet, surface friction drops significantly. Pavement surface friction gradually drops as the water film thickness increases; however, the changes in pavement surface friction are not substantial (Fwa 2005). Several studies have quantified the effect of water film thickness on surface friction (Najafi et al. 2013, Kulakowski et al. 1990, Rose et al. 1997).

Several factors can affect pavement friction. According to Hall et al. (2009) these factors can be classified into four groups: (1) pavement surface characteristics (i.e., microtexture, macrotexture, material properties, and temperature), (2) vehicle operating parameters (i.e., slip speed, driving maneuver), (3) tire properties (i.e., footprint, tread design, inflation pressure, rubber composition, and temperature), and (4) environment (i.e., climate, temperature, water, snow and ice, and contamination) (Hall et al. 2009). Seasonal variations can have a significant effect on pavement friction (Fwa 2005). This effect can be explained by changes in temperature and precipitation (Jayawickrama 1998). Overall friction is lower in summer months compared to other times of the year. This is mainly due to accumulation of polished particles from pavement or contamination from vehicles (Flintsch et al. 2012). Since both hot-mix asphalt surface and tires are viscoelastic materials, temperature can affect their properties. Several researchers have studied the effect of temperature on pavement friction measurements (Bianchini et al. 2011, Bazlamit et al. 2005). Although several attempts have been made to quantify the effect of seasonal variation on friction measurement (Jayawickrama 1998, Hill et al. 1981, Flintsch et al. 2009, FHWA 2010), there is no practical model currently available for this purpose.

Friction measurements are typically collected as part of the state’s wet accident reduction program (WARP) on areas with a high rate of car crashes. This means that data collection is mostly being done at the project level on specific areas. Statistics show that 55.4% of agencies collect friction measurements at the project level. Only 33.9% of agencies collect network-level friction data (Flintsch et al. 2009). To be able to collect network-level friction data, agencies need to implement equipment with high daily output. In the United States, locked-wheel trailers are the most predominant friction tester used by state DOTs. They measure the steady state friction—also called Skid Number (SN)—on a fully locked wheel at a certain speed 64 kph (40 mph) based on the ASTM standard). The locked wheels use two types of test tires; Smooth (ASTM E-524) and Ribbed (ASTM E-501). Figure 14 shows a locked-wheel skid trailer. The SCRIM is the most commonly used friction tester in Europe. SCRIM devices can measure friction continuously. The device has a bigger water tank compared to locked-wheel trailers, so it can test a longer length of roadway network, on average, 200 km (125 miles) of roadway every day (Fwa 2005).



Figure 14 Locked-wheel trailer.

Friction data can be used in developing Pavement Friction Management (PFM) programs. PFM includes engineering practices and periodic data collection to ensure an adequate friction level for the riding surface. This can be achieved by using appropriate pavement design,

construction, and maintenance techniques. Guidelines and techniques for providing adequate surface texture and friction levels can be found in FHWA Technical Advisory TA 5040.36, “Surface Texture for Asphalt and Concrete Pavements” (FHWA 2013). Locations with high rates of wet-condition crashes need to be identified and further investigated. This can be done by computing the ratio between wet-condition crashes and total crashes (wet- and dry-condition) and then using one of the following procedures (FHWA 2013):

- Set a specific threshold for the wet-condition crash ratio, above which a location will be identified as an elevated wet-condition crash location. This ratio can vary between 0.25 and 0.5, depending on geographical and climate conditions.
- Compare the wet-condition crash ratio with the average crash ratio for a specific highway functional class in that area. The location will be identified as an elevated wet-condition crash location if the computed ratio is above the average by a specified percentage.
- Set the threshold at the minimum of the total number of crashes within a segment.

The American Association of State Highway and Transportation Officials (AASHTO) Guide for Pavement Friction Management outlines several methods for highway agencies to establish Investigatory Level (desirable) and Intervention Level (minimum) thresholds for pavement friction and texture (Hall et al. 2009). Most of these methods require historical data for pavement friction, which are not readily available for most states.

## **OBJECTIVE**

This paper investigates the effect of friction on the rate of fatal and injury-causing car crashes on urban roads. The effect of friction on the rate of both wet-condition and dry-condition crashes is evaluated. The data for this study were provided by New Jersey Department of Transportation.

## **DATA COLLECTION**

The friction database includes the network-level friction measurements collected by a ribbed-tire, locked-wheel skid trailer. The friction database also includes traffic (Annual Average Daily Traffic (AADT)), speed limit, road functional class (Urban Interstate, Urban Principle Arterial, etc.), and the location (route name and the milepost) of the collected data.

The crash database includes the location information of the crashes (route and milepost), type of accident (fatal, injury-causing, etc.), road surface condition at the time of accident (wet, dry, etc.), and the date of the accident. The analysis of this project considered only the crashes that had at least one injury or fatality. For practicality, only the data for one year (2007) were analyzed.

## DATA ANALYSIS

The first step for analyzing the data was to match up the friction measurements with corresponding crash location. This was done by comparing the route and milepost information. If the difference between the milepost of the crash location and the friction measurement that were on the same route was less than 0.1 miles they were matched. The summary of the crashes that were successfully matched with friction locations are provided in Table 1. Since urban collector, urban local, and all rural roads had very few matched locations compared to other types of roads, they were not included in further analysis.

Table 1 Fatal and Injury-Causing Accident Counts

Functional Class	# of sites with accidents	
	Surface Condition	
	<i>Dry</i>	<i>Wet</i>
Urban Principal Arterial	20308	5010
Urban Interstate	3963	1251
Urban Minor Arterial	2979	714
Urban Freeway Expressway	2409	665
Urban Collector	20	11
Urban Local	12	4
Rural Principal Arterial	758	166
Rural Interstate	510	170
Rural Major Collector	687	158

Friction measurements were divided into intervals (bins) with increments of two friction units (20: SN below 20, 22:  $20 < SN \leq 22$ , etc.) and the numbers of crashes for each friction

interval were determined for different road classes. This number was then used to find the rate of car crashes in Million Vehicles per Mile (MVM) using the following formula<sup>3</sup> (Gan et al. 2012):

(5)

$$\text{Crash Rate} = \frac{\text{Number of crashes} \times 1,000,000}{\text{Exposure}} = \frac{\text{Number of crashes} \times 1,000,000}{\text{AADT} \times 365 \times Y \times L}$$

Where,

AADT: total Annual Average Daily Traffic

Y: study duration in years (1 year in this study)

L: length of the roadway segments

### Regression Analysis

To determine the significance of the effect of friction (regressor) on the rate of car crashes (independent variable), an Analysis of Variance (ANOVA) was performed using SAS software. The summary of ANOVA statistics for Urban Principal Arterial roads is provided in Table 2. According to the P-values provided in Table 2, friction (SN) is a significant factor in the model, with a confidence level greater than 95% (P-value < 0.05).

Table 2 SAS Outputs for Analysis of Variance (ANOVA) for Urban Principle Arterial Roads

Analysis of Variance					
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F
Model	1	5.50876	5.50876	87.97	<.0001
Error	21	1.31501	0.06262		
Corrected Total	22	6.82377			
Root MSE	Dependent Mean	Coeff Var	R-Square	Adj R-Sq	
0.25024	1.71191	14.61751	0.8073	0.7981	

Parameter Estimates						
Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t	95% Confidence Limits
Intercept	1	3.26129	0.17323	18.83	<.0001	2.90102 3.62155
SN	1	-0.03689	0.00393	-9.38	<.0001	-0.04507 -0.02871

<sup>3</sup> Note: The crash rates defined in this chapter were normalized using 365 days per year, without discriminating on rainy and dry days as in chapters 3 and 4.

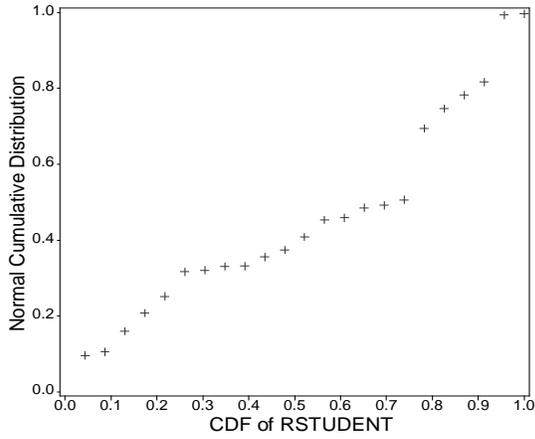
To verify the adequacy of the linear model, residual analysis was performed. Residual analysis is a diagnostic method for examining the adequacy of the fit of a regression model. There are several assumptions that we make in any regression analysis. According to Montgomery et al. 2001, these assumptions are as follow (Montgomery et al. 2001):

- 1- The relationship between response and regressors is linear.
- 2- The error term has a zero mean and constant variance.
- 3- The errors are uncorrelated and normally distributed.

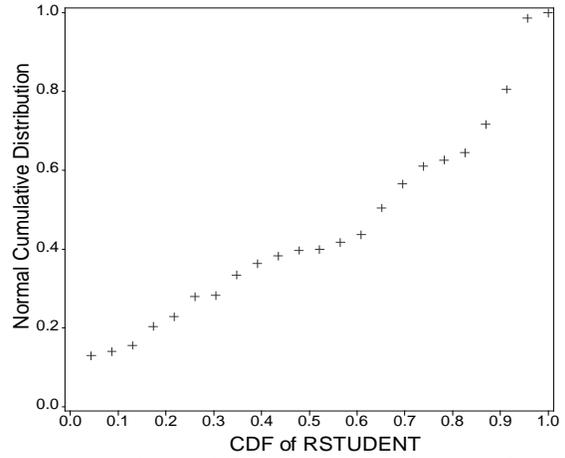
The violation of these assumptions can create an unstable model in which different samples can result in totally different models with contradictory conclusions (Montgomery et al. 2001). Graphical analysis of the residuals is a common way of examining the adequacy of a regression model (26). This method was used to examine the adequacy of the model proposed for Urban Principal Arterial roads. First, to check the normality assumption, a normal probability plot of residuals was constructed using the SAS software (Figure 15 (a)). Ideally, the points should lie along a straight line in the normal probability plot. The plot in Figure 15 (a) seems to have a light tail. Transformation can be applied to data to deal with this problem. Plot of residuals versus the predicted values (fitted values) and versus the regressors are other useful methods for identifying model inadequacies (26). These plots are provided in Figure 15 (b) and (c). Ideally, the points should be randomly scattered around zero in these plots; however, they seem to have a slight nonlinear behavior. Residuals greater than 3 are potential outliers. These points are highlighted in Figure 15 (c). Further investigation on these points revealed that there are several accidents happening in these locations. These accidents can be due to several factors other than friction, and they should be reported to the appropriate roadway agency for further investigation.

To eliminate the nonlinear behavior of the residuals, transformation was applied to the regressor (friction). Common transformations, including logarithmic, reciprocal, and square root, were applied and the residual plots were examined after transformation. Logarithmic transformation for the regressor produced the most satisfactory residual plots, provided in Figure 15 (a'), (b'), and (c'). No systematic pattern can be observed in residual plots for predicted value and regressor after transformation (Figure 15 (b') and (c')). Normal probability plot after transformation still seems to have a very light tail, which indicates that error may come from a

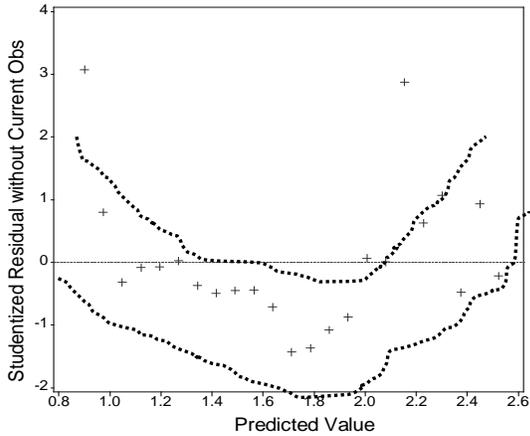
distribution that has a slightly lighter tail than a normal distribution. Because there is no evidence of model inadequacy, we can conclude that the transformation was satisfactory.



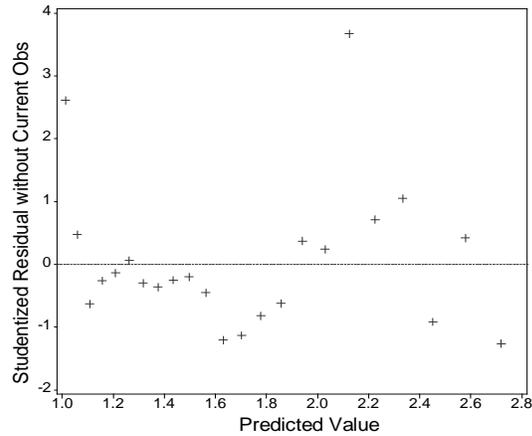
(a) Normal probability plot (NPP) before transformation



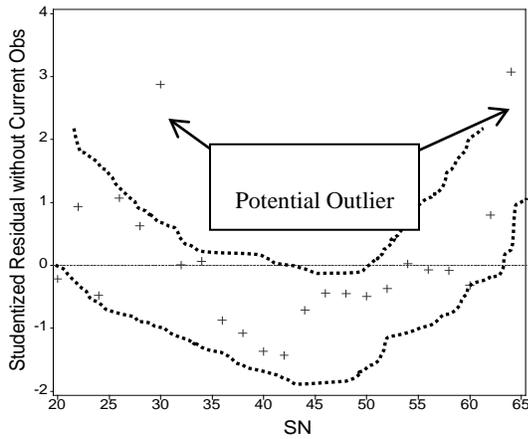
(a') Normal probability plot (NPP) after transformation



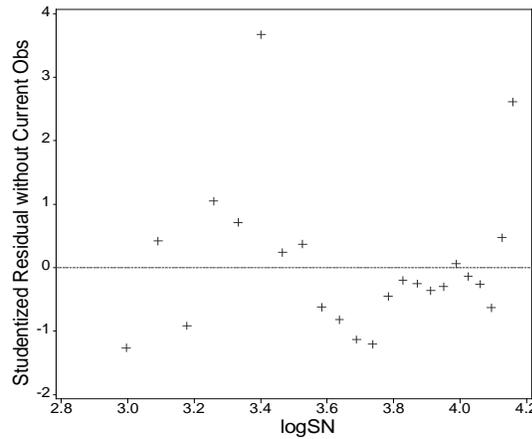
(b) Residual plot for predicted values



(b') Residual plot for predicted values after transformation ( $x \rightarrow \ln(x)$ )



(c) Residual plot for regressor



(c') Residual plot for regressor after transformation ( $x \rightarrow \ln(x)$ )

Figure 15 Residual plots.

Once the transformations were verified, ANOVA was conducted on the transformed model. ANOVA results are provided in Table 3. It can be seen from the table that transformation has improved the model's coefficient of determination (R-square). The regressor in the model is still satisfactory (P-value < 0.0001).

Table 3 Analysis of Variance (ANOVA) on Transformed Model for Urban Principle Arterial Roads

<b>Analysis of Variance</b>							
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F		
Model	1	5.77753	5.77753	115.97	<.0001		
Error	21	1.04624	0.04982				
Corrected Total	22	6.82377					
Root MSE	Dependent Mean	Coeff Var	R-Square	Adj R-Sq			
0.22321	1.71191	13.0384	0.8467	0.8394			

<b>Parameter Estimates</b>							
Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t	95% Confidence Limits	
Intercept	1	7.11387	0.50379	14.12	<.0001	6.06619	8.16155
Ln(SN)	1	-1.46691	0.13622	-10.77	<.0001	-1.75019	-1.18363

Similar analysis was performed for other road classes. Proper transformation was applied for each model.

Table 4 summarizes the model's parameters. According to P-values, friction is a significant factor in all the models except for Urban Freeway Expressway wet-condition crashes (in which P-value > 0.05). The slope of the regression line is negative for all cases except for Urban Freeway Expressway dry-condition crashes. It is noted that the coefficient of determination for this type of roadway is very low. This supports the hypothesis that increasing the friction level decreases the rate of both dry- and wet-condition car crashes.

Table 4 Summary Statistics of the Models

Road Functional Class	Surface Condition at Time of Crash	Regression Model	R-square	P-value
Urban Principal Arterial	Dry	$Y = 7.11 - 1.47 \times \text{Ln}(X)$	0.84	<0.0001
	Wet	$Y = 1.79 - 0.37 \times \text{Ln}(X)$	0.73	<0.0001
Urban Interstate	Dry	$Y = 2.33 - 0.47 \times \text{Ln}(X)$	0.36	0.0144
	Wet	$Y = 0.96 - 0.21 \times \text{Ln}(X)$	0.73	<0.0001
Urban Minor Arterial	Dry	$Y = 11.78 - 2.58 \times \text{Ln}(X)$	0.65	<0.0001
	Wet	$Y = 3.09 - 0.69 \times \text{Ln}(X)$	0.35	0.0009
Urban Freeway Expressway	Dry	$Y = -0.88 + 0.43 \times \text{Ln}(X)$	0.24	0.01
	Wet	$Y = 0.49 - 0.08 \times \text{Ln}(X)$	0.10	0.15

Note: Y = rate of fatal and injury-causing crashes (MVM), and X = Ribbed Tire Skid Number (SNr)

The regression models can be used to define the minimum allowable friction level for various types of roads. The relationship between crash rate and friction is illustrated in Figure 16. Highway agencies should first define the minimum allowable crash rate for various road networks. Suppose that their goal is to decrease the rate of wet-condition car crashes for Urban Principal Arterials to 0.5. This requires that the friction be at least 33 [ $1.79 - 0.37 \times \text{Ln}(33) \approx 0.5$ ]. This has been demonstrated in Figure 16 (b). Similar friction threshold can be defined for other road classes.

## CONCLUSION

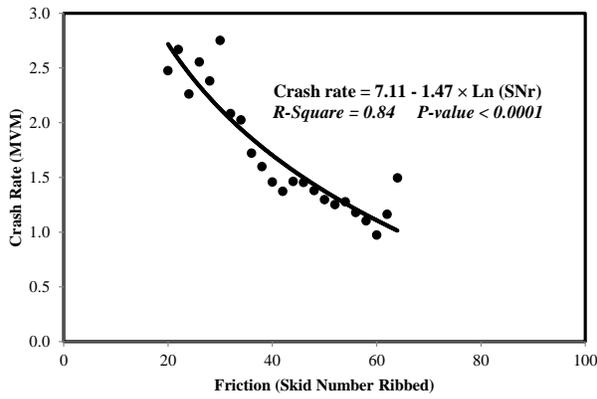
The paper evaluated the effect of friction on car crashes and resulted in the following conclusions:

- Friction was found to be a significant factor affecting the ratios of both wet- and dry-condition car crashes on urban roads. Contrary to other studies that only emphasize the effect of friction on wet-condition crashes; this study revealed that friction impacts the rate of dry-condition crashes as well.
- The normal probability plot of residuals and residual plots for predicted values and regressors suggested, as expected, that the relation is not linear and that a logarithmic transformation was necessary for the data. Transformation improved the coefficient of determination (R-square) of the models.

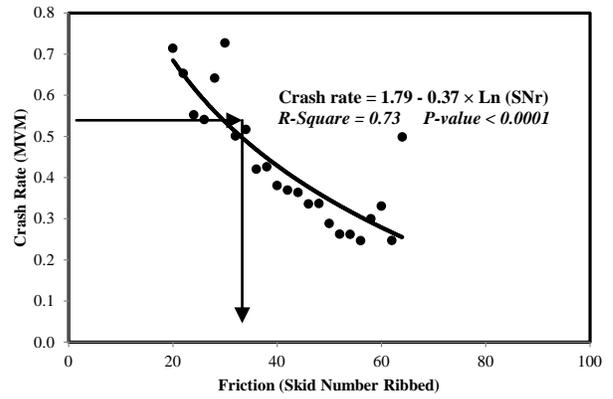
Factors such as seasonal variation and temperature changes can also affect the friction measurement. This effect needs to be further investigated and incorporated into the pavement friction management program. Furthermore, the relationship between friction and crash rates can be used by DOTs and highway agencies to define acceptable levels of friction for various types of roadways in their networks.

#### **ACKNOWLEDGEMENT**

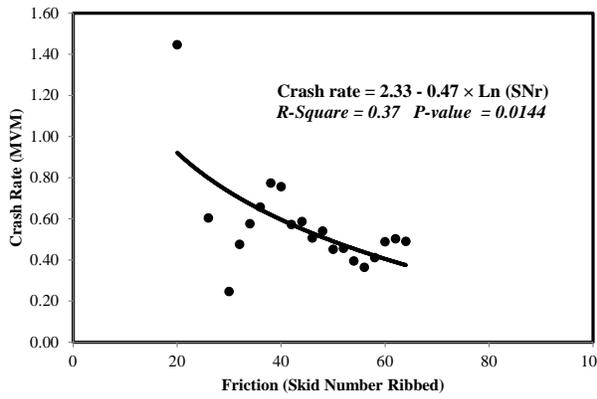
The authors would like to acknowledge the New Jersey Department of Transportation and, in particular, Susan Gresavage for their contribution and support in providing the data for this study, as well as Dr. Feng Guo for his guidance in the statistical analysis.



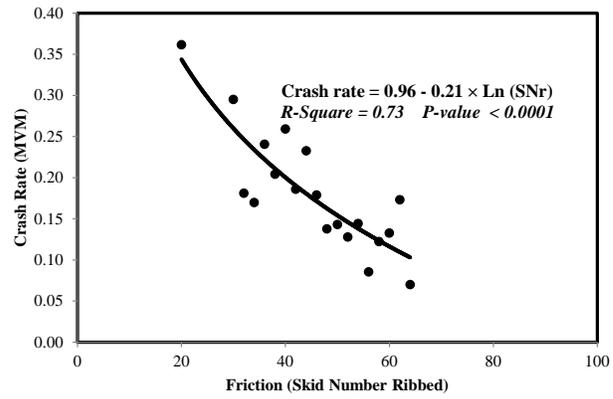
(a) Urban Principal Arterial - dry



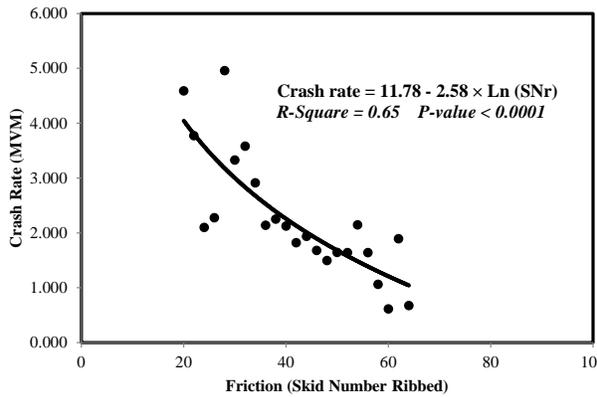
(a') Urban Principal Arterial - wet



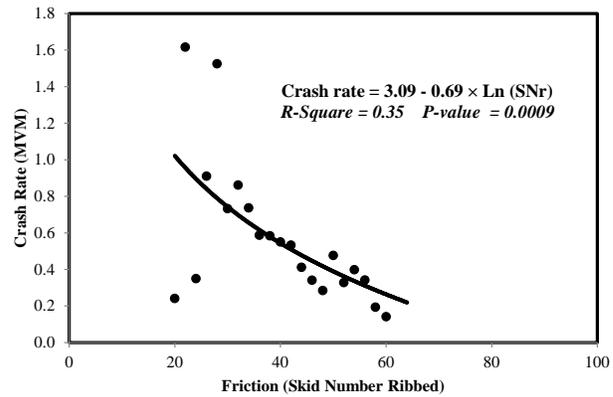
(b) Urban Interstate - dry



(b') Urban Interstate - wet



(c) Urban Minor Arterial - dry



(c') Urban Minor Arterial - wet

Figure 16 Crash rate vs. friction.

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## **CHAPTER 3 - PAVEMENT FRICTION MANAGEMENT – ARTIFICIAL NEURAL NETWORK APPROACH<sup>4</sup>**

### **Abstract**

The Highway Safety Improvement Program (HSIP) requires state highway agencies to improve their roadway network safety through a ‘strategic’ and ‘data-driven’ approach. As part of HSIP, the Federal Highway Administration (FHWA) mandates that states develop a Pavement Friction Management (PFM) System to reduce the rate of fatal and injury-causing crashes and prioritize their safety improvement projects based on the crash risk. This paper aims to predict the rate of wet and dry vehicle crashes based on surface friction, traffic level, and speed limit using an artificial neural network (ANN). Three learning algorithms, Levenberg-Marquardt, conjugate gradient, and resilient back-propagation, were examined to train the network. Levenberg-Marquardt produced the best precision and was used to develop the model. The results of the study suggest that the ANN model can reliably predict the rate of crashes. The prediction model can be used as a scale to prioritize safety improvement projects based on the rate of fatal and injury-causing crashes.

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<sup>4</sup> This manuscript will be submitted to the International Journal of Pavement Engineering (IJPE) for publication. Co-authors include: Gerardo Flintsch, and Seyedmeysam Khaleghian.

## **INTRODUCTION**

The ‘Moving Ahead for Progress in the 21st Century Act (MAP-21)’ was signed into law on July 6, 2012, and went into effect on October 1, 2012, (United States Department of Transportation 2013). MAP-21 ‘continued the Highway Safety Improvement Program (HSIP) as a core Federal-aid program’ (FHWA 2014). The goal of HSIP is to reduce traffic fatalities and serious injuries. As part of HSIP, the Federal Highway Administration (FHWA) has established measures for state highway agencies to assess the rate of fatal and injury-causing crashes (Federal Highway Administration 2014). HSIP project selection is based on ‘crash experience, crash potential, or other data supported means as identified by the State, and establishes the relative severity of those locations’ (Federal Highway Administration 2010). To establish criteria to prioritize projects for HSIP funds, states should implement a pavement friction management (PFM) program (Federal Highway Administration 2010). PFM allows states to incorporate safety into their asset management decision making process. Locations with high risk of fatal and injury-causing crashes are identified and corrective measures taken to address friction deficiencies in those locations. Projects can be prioritized based on the crash risk.

In 2009, the American Association of State Highway and Transportation Officials (AASHTO) published the Guide for Pavement Friction to provide guidelines for state highway agencies to develop and implement a PFM program (Hall et al. 2009). The AASHTO guide suggests three methods to define investigatory and intervention levels for friction. The methods provided in the AASHTO guide are based on traditional regression analysis. This paper investigates the suitability of one of the methods provided by the AASHTO guide to be implemented in PFM and it proposes an alternative approach based on an artificial neural network (ANN) to model the relationship between friction and crashes. The proposed method can be used as a scale to prioritize projects for safety improvements.

## **BACKGROUND**

The effect of tire-pavement friction on the rate of vehicle crashes is well known among researchers (Flintsch et al. 2012). Several researchers have attempted to define an acceptable level of friction at which the rate of crashes will be minimized. Rizenbergs et al. (1972) did a friction study on rural interstate routes in Kentucky using a ribbed-tire locked-wheel friction

tester. They found that wet crash rates as well as wet-to-dry crash ratios increased once the friction numbers dropped below 40 (Rizenbergs et al. 1972). McCullough and Hankins (1996) studied the relationship between friction and crashes for 571 sites in Texas. The result of the study revealed that the majority of crashes happened on the sites with low friction, while a few crashes happened on the sites with high friction values. They proposed a minimum desirable friction threshold of 0.4 measured at 30 mph (McCullough and Hankins 1966).

The AASHTO Guide for Pavement Friction has defined three methods to establish two distinctive friction threshold levels, investigatory level and intervention level. Sites with friction values below the investigatory level will be selected for detailed investigation to determine if there is a need for posting warning signs. Sites with friction values below the intervention level will be selected for corrective action, such as resurfacing or other programmatic maintenance treatment. The first AASHTO method uses the friction deterioration curve by plotting friction loss versus pavement age. The friction value at which significant loss rapidly begins is selected as the investigatory level. The intervention level is defined at a fixed percentage below investigatory level (Figure 17) (Hall et al. 2009).

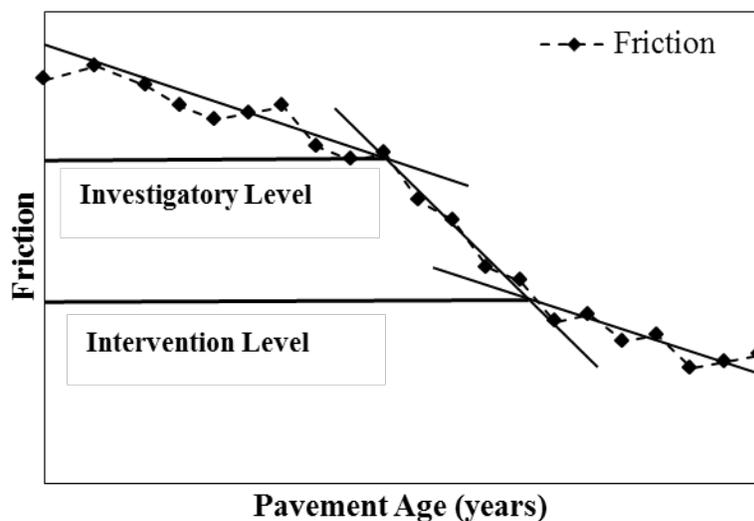


Figure 17 Friction deterioration curve (after Hall et al. (2009)).

The second AASHTO method uses both the friction deterioration curve and historical crash data. The investigatory level is set where there is a significant drop in friction level and the

intervention method is set where there is a significant increase in crashes (Figure 18) (Hall et al. 2009).

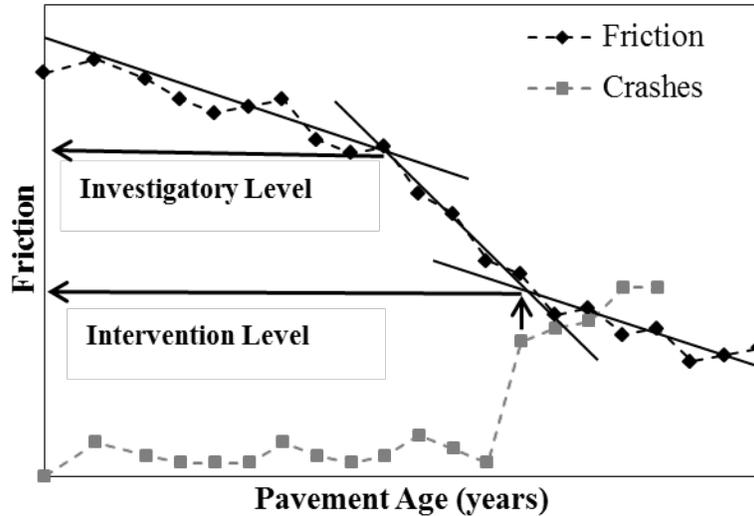


Figure 18 Investigatory and intervention friction level based on friction deterioration and crash rate (after Hall et al. (2009)).

The third AASHTO method uses the friction distribution and crash rate for each roadway category to determine the investigatory and intervention levels of friction. The histogram of pavement friction and wet-to-dry crash ratio is plotted first (Figure 19). The mean and standard deviation of the friction distribution are then calculated. The investigatory level is set as the mean friction minus X (e.g., 1.5 or 2.0) standard deviations and it is adjusted to where wet-to-dry crashes begin to increase considerably. The intervention level is set as the mean friction minus Y (e.g., 2.5 or 3.0) standard deviations and it is adjusted to a minimum satisfactory wet-to-dry crash rate or by the point where enough funding is available to address the friction deficiencies (Hall et al. 2009). This method is more robust than other two approaches since an agency can adjust the intervention friction level based on available funding.

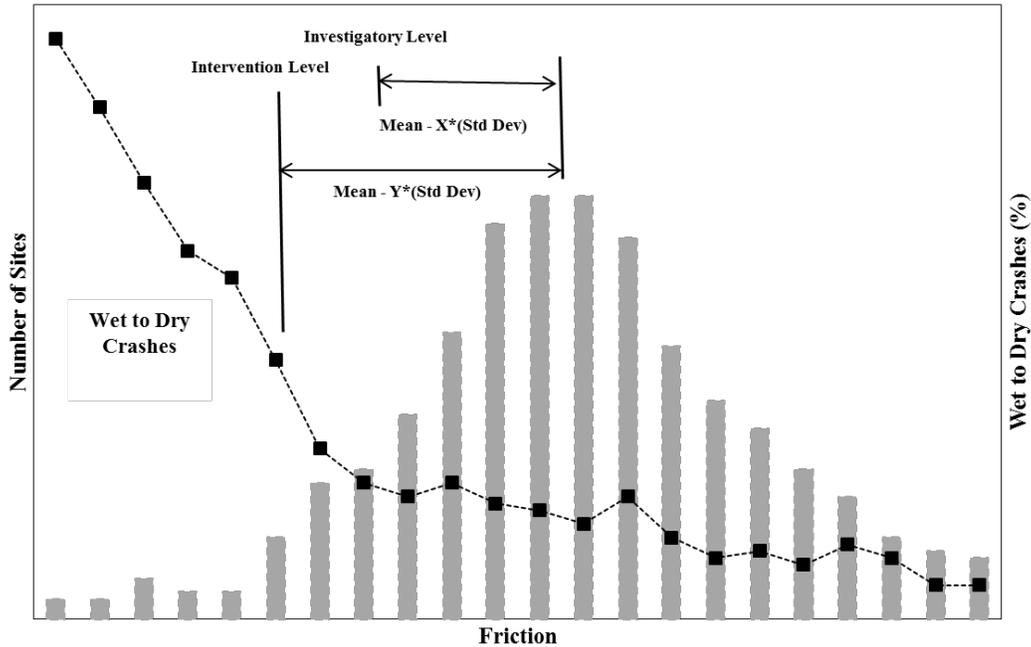


Figure 19 Investigatory and intervention level of friction based on friction distribution and wet-to-dry crash ratio (after Hall et al. (2009)).

## OBJECTIVE

The objective of this paper is to investigate the suitability of one of the methods provided by the AASHTO guide to be implemented in PFM and to propose alternative methods to model the relationship between the rate of vehicle crashes and friction.

## DATA COLLECTION

The data for this study were provided by the New Jersey Department of Transportation (NJDOT). The database includes the network-level friction measured by an ASTM E-501 ribbed-tire locked-wheel skid trailer. The locked-wheel skid trailer is the predominant friction tester in the United States (Flintsch et al. 2010, Najafi 2010), while continuous friction measuring equipment (CFME) is more common in Europe (Najafi et al. 2011, 2013). The database also includes Annual Average Daily Traffic (AADT), speed limit, roadway functional classification (urban principle arterial, urban interstate, etc.), type of accident (fatal, injury-causing, etc.), and the road surface condition at the time of accident (wet, dry, etc.).

Fatal and injury-causing crashes for various urban roads were used for this study. The total number of wet and dry, fatal and injury-causing vehicle crashes, as well as average speed limit for each roadway type, is provided in Table 5.

Table 5 Fatal and injury-causing accident counts (after Najafi *et al.* 2014).

Functional Class	Number of sites with accidents			
	Surface Condition		Speed Limit (kph)	
	Dry	Wet	Min	Max
Urban Principal Arterial	20308	5010	40	88
Urban Interstate	3963	1251	56	104
Urban Minor Arterial	2979	714	40	88
Urban Freeway Expressway	2409	665	40	104

## DATA ANALYSIS

The first two methods suggested by the AASHTO guide require historical friction data, which was not available for this study. Thus, the authors tested only the third method. Friction numbers were grouped into bins with two-unit increments (i.e.,  $20 < FN \leq 22$ , etc.). The friction and crash data were then matched using route and milepost information. If the distance between the location of the crash and the measured friction was less than 0.1 miles, the data were matched. The total numbers of friction sites for each bin, as well as the ratio of wet-to-dry fatal and injury-causing crashes for each friction bin, were then calculated. The summary of data is provided in Table 6.

Table 6 Fatal and injury-causing crash count.

Urban Principal Arterial 1						Urban Interstate 2				
FN	# of sites	Avg. AADT	Avg. Speed Limit (mph)	# of Dry Crashes	# of Wet Crashes	# of sites	Avg. AADT	Avg. Speed Limit (mph)	# of Dry Crashes	# of Wet Crashes
<20	69	15,570	43	97	28	2	37,902	35	4	1
22	69	14,590	43	98	24	2	47,062	65	0	0
24	105	15,114	42	131	32	0	-	-	0	0
26	210	13,023	40	255	54	3	15,131	65	1	0
28	294	13,508	43	345	93	6	29,602	65	0	0
30	587	13,864	42	817	216	24	46,438	63	10	12
32	756	14,613	44	840	202	28	43,246	62	21	8
34	1099	15,632	44	1269	324	90	41,233	62	78	23
36	1418	16,230	45	1445	353	113	48,393	60	131	48
38	1734	16,713	45	1690	451	125	46,171	60	163	43
40	1995	18,223	46	1934	505	164	47,710	61	216	74
42	2247	17,692	46	1990	536	286	41,209	62	246	80
44	2154	17,314	47	1991	495	471	38,000	63	383	152
46	2179	16,667	47	1928	445	618	38,432	62	439	155
48	1915	16,681	47	1609	393	655	40,396	63	522	133
50	1601	17,036	47	1290	287	512	40,793	63	344	109
52	1329	16,192	48	983	206	565	43,261	63	407	114
54	811	17,660	48	667	137	522	45,121	64	339	124
56	580	17,826	49	445	93	468	48,739	63	303	71
58	355	16,735	49	239	65	309	51,520	62	239	71
60	182	15,936	48	103	35	82	55,464	61	81	22
62	154	14,388	45	94	20	32	49,447	62	29	10
>64	77	11,421	44	48	16	6	65,294	62	7	1
Urban Minor Arterial 3						Urban Free way Expressway 4				
FN	# of sites	Avg. AADT	Avg. Speed Limit (mph)	# of Dry Crashes	# of Wet Crashes	# of sites	Avg. AADT	Avg. Speed Limit (mph)	# of Dry Crashes	# of Wet Crashes
<20	19	5971	40	19	1	6	67,521	44	2	0
22	9	5653	41	7	3	6	46,975	53	4	3
24	43	5466	40	18	3	14	53,975	53	19	2
26	50	6024	42	25	10	8	40,852	58	10	2
28	85	5917	42	91	28	13	40,270	56	7	7
30	137	6553	42	109	24	8	45,817	55	10	4
32	228	7114	42	212	51	44	50,614	55	58	20
34	322	7509	43	257	65	75	49,143	54	104	36
36	429	7404	46	248	68	120	50,328	55	169	38
38	493	7143	45	289	75	117	40,244	55	125	44
40	502	7148	44	278	72	205	31,822	56	160	47
42	479	6660	45	212	62	214	27,168	57	126	33
44	470	7224	45	240	51	326	26,964	58	268	71
46	420	7267	45	187	38	369	27,411	58	205	54
48	413	6521	45	147	28	375	28,778	57	314	79
50	384	6731	44	155	45	344	28,490	57	222	66
52	321	6764	44	130	26	349	25,777	59	169	48
54	230	7168	44	129	24	265	25,270	60	140	44
56	221	9070	46	120	25	162	25,350	58	93	26
58	178	9573	46	66	12	74	19,898	55	37	7
60	54	10793	48	13	3	58	16,484	54	19	6
62	26	7240	43	13	0	37	16,058	44	34	4
>64	43	13237	47	14	0	96	22,210	47	114	24

The friction distribution and wet-to-dry crash ratio for each type of roadway is provided in Figure 20 through Figure 23. The mean and standard deviation of the friction distribution for each roadway type were calculated. The investigatory level and intervention level of friction were defined as the mean minus 'X or Y' standard deviation as described before. The intervention level was adjusted to match the point that a sudden drop in the wet-to-dry ratio was observed.

The summary of friction thresholds and the percentage of the sites that fall below the thresholds are provided in Table 7.

Table 7 Investigatory and intervention friction thresholds.

Functional Classification	Mean Friction	St. Dev. Friction	Investigatory Level	% sites below Inv. Level	Intervention Level	% sites below Int. Level
Urban Principal Arterial	43	7.77	35.2	15%	31.3	6%
Urban Interstate	48	6.38	35.2	3%	32.1	1%
Urban Minor Arterial	43	8.39	34.6	16%	30.4	6%
Urban Freeway Expressway	47	7.67	35.5	5%	31.7	1%

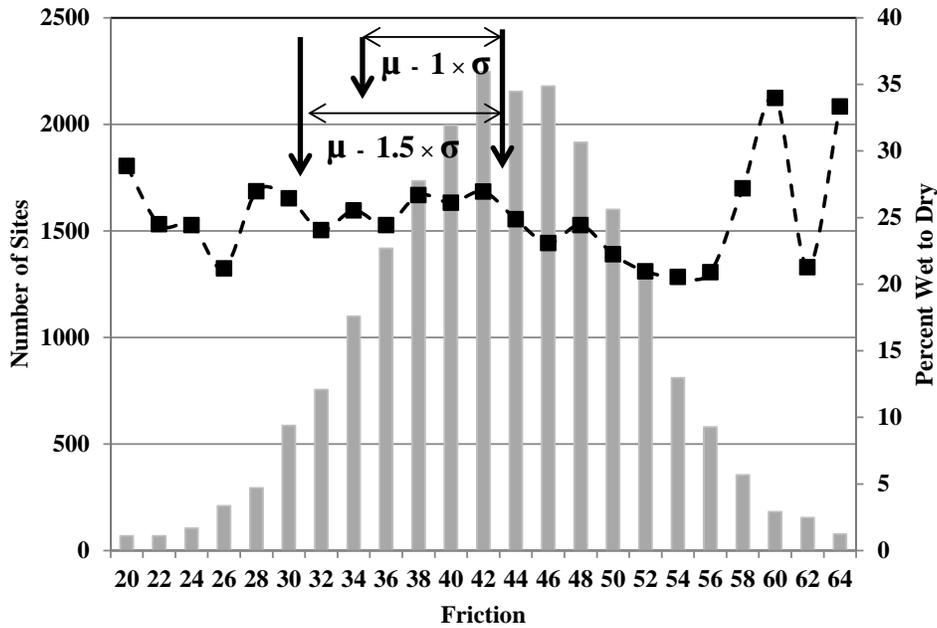


Figure 20 Friction distribution and wet-to-dry crash ratio (urban principal arterial).

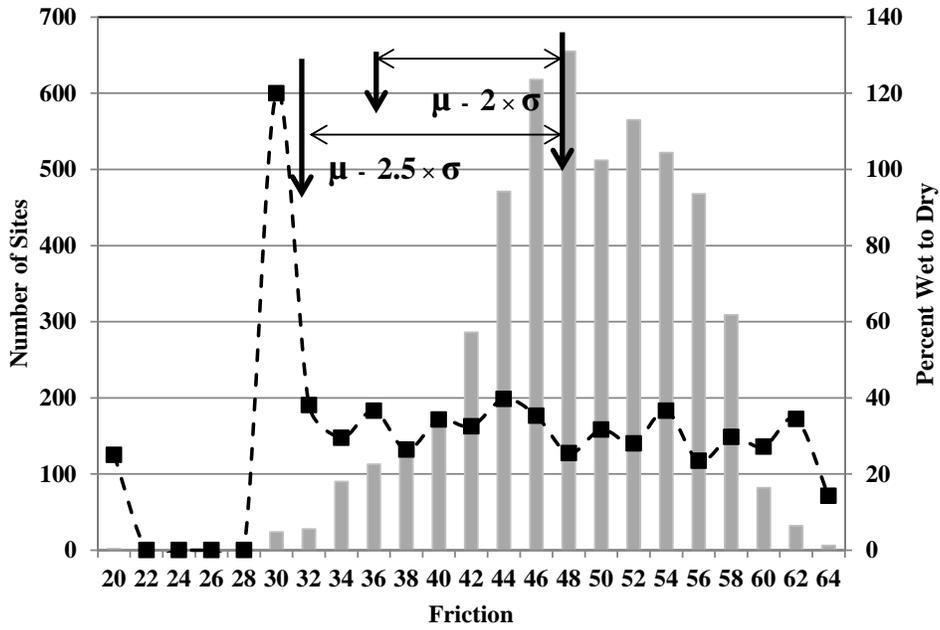


Figure 21 Friction distribution and wet-to-dry crash ratio (urban interstate).

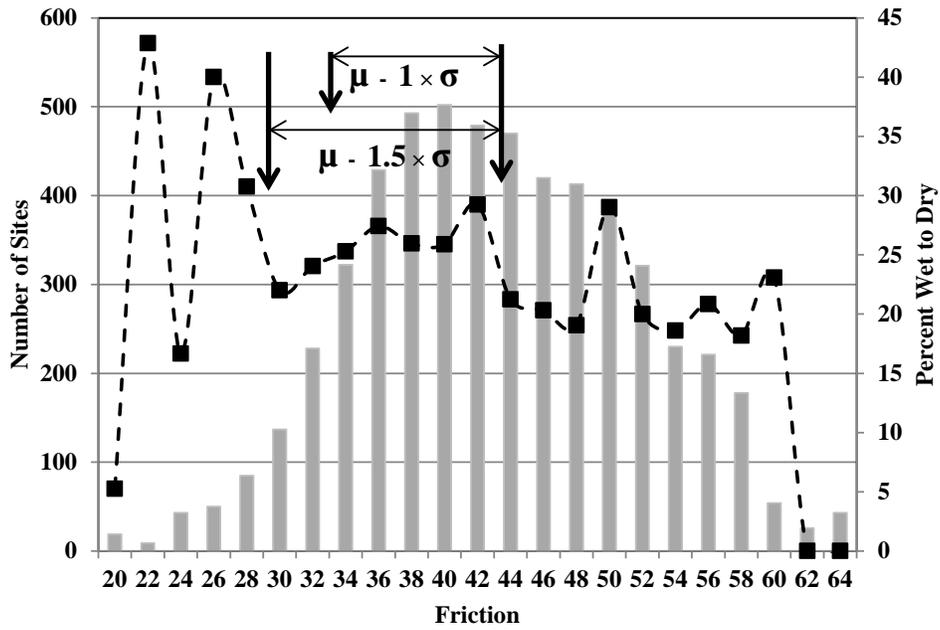


Figure 22 Friction distribution and wet-to-dry crash ratio (urban minor arterial).

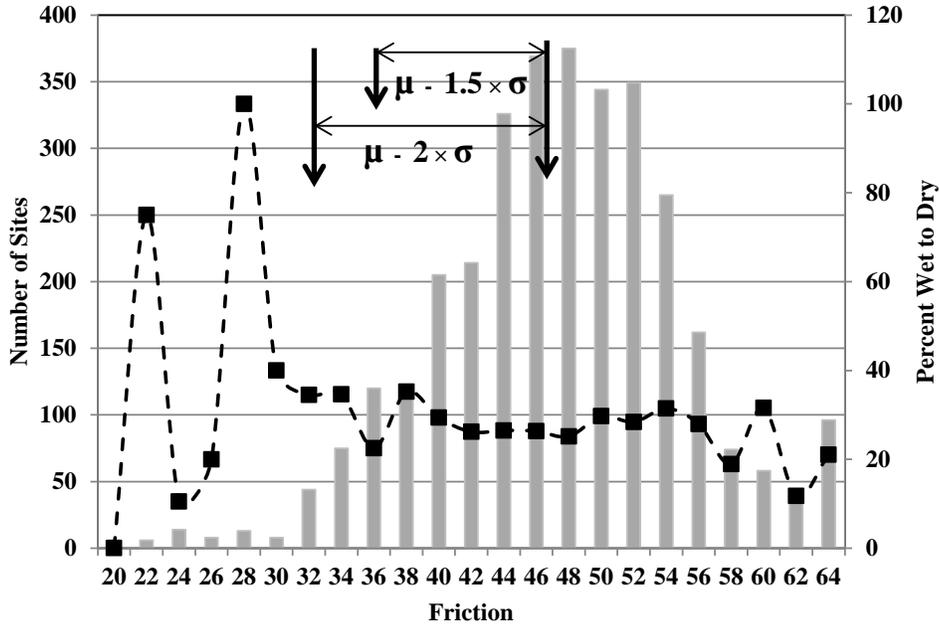


Figure 23 Friction distribution and wet-to-dry crash ratio (urban freeway expressway).

High variability with some peak crash rates can be observed for low friction numbers. For all cases except urban principal arterial roads, a significant drop in the wet-to-dry crash ratios was observed around friction number 32. However, no clear trend can be observed for wet-to-dry crash ratios for urban principal arterial roads, which account for the majority of the network. A previous study by the authors showed a significant relationship between both wet and dry crash ratio and friction that can explain the lack of relationship between the wet-to-dry crash ratio and friction (Najafi et al. 2014). It should also be noted that there are only a few sites with extremely low (and high) friction values. Defining friction threshold based on a small sample size may not be appropriate.

To consider the effect of wet and dry crashes separately, the wet and dry crash rate for each interval was computed by dividing the crash count by exposure (Gan et al. 2012):

$$Crash \cdot Rate = \frac{Number \cdot of \cdot crashes \times 1,000,000}{Exposure} = \frac{Number \cdot of \cdot crashes \times 1,000,000}{AADT \times n \times Y \times L} \quad (6)$$

where

AADT: total AADT (averaged for each bin)

*n*: wet or dry time exposure  
*Y*: study duration in years  
*L*: length of the roadway segments.

Weather information was extracted from the National Oceanic and Atmospheric Administration (NOAA) database (2015). The crash rates were then normalized between zero and one for each roadway type and crash type (wet or dry):

$$\text{Normalized} \cdot \text{Crash} \cdot \text{Rate}_i = \frac{\text{Crash} \cdot \text{Rate}_i - \text{MIN}(\text{Crash} \cdot \text{Rate})}{\text{MAX}(\text{Crash} \cdot \text{Rate}) - \text{MIN}(\text{Crash} \cdot \text{Rate})} \quad (7)$$

where Normalized Crash Rate<sub>(i)</sub> corresponds to the normalized crash rate for the *i*<sup>th</sup> friction bin.

In a previous study, the authors used linear regression to model the relationship between the crash rate and friction (Najafi et al. 2015). In this study, ANN was implemented as an alternative to model the relationship.

### **Artificial neural network (ANN)**

ANN is a soft computing approach that is inspired by the way the human brain and nervous system work (Khdair 2006). ANN's processing system consists of several 'interconnected' cells—known as neurons—that work harmoniously to solve a problem. The pattern and strength of connectivity between neurons encrypt the knowledge of a network. Similar to a human's brain, ANN can learn by example, and it can be trained to predict an unknown system or behavior. ANN can make generalizations, and it is very suitable in cases for which many examples are available (Flintsch and Chen 2004). ANN is known to be capable of extracting complex nonlinear relationships between multiple variables (Somers and Casal, 2009).

ANN has been successfully implemented in the past to support infrastructure asset management decisions (Flintsch and Chen 2004). Flintsch et al. (1998) used ANN to select pavement candidates for preservation. Suman and Sinha (2012) and Thube (1997) developed a pavement condition forecasting model using ANN. The effectiveness of ANN in accident prediction modeling has also been confirmed by several researchers (Moghaddam et al. 2011, Duddu and Pulugurtha 2012, Kunt et al. 2012, Jafari et al. 2013). Moghaddam et al. (2011) used

ANN to model the relationship between human factors, road, vehicle, weather conditions, traffic volume, and speed flow on the severity level of crashes on urban. Kunt et al. (2012) predicted the severity level of crashes on a freeway using ANN.

One of the main benefits of the ANN approach is that it can work with uncertain and incomplete data. Furthermore, it can learn from examples. This is particularly appealing at the early stages of friction management program development. The system can be established with limited data and improved over time as more data become available. The main disadvantage of ANN is that it behaves like a ‘black box’, which makes it hard to understand.

ANN’s structure consists of input, hidden layers, and output layers (Shekharan 1998). The number of layers in an ANN depends on the number of hidden layers. Each layer contains several interconnected neurons. Each neuron has an output, which relates to its activation level, and it can spread out to other neurons. A simple schematic of neuron function is illustrated in Figure 24 (Khdaire 2006).

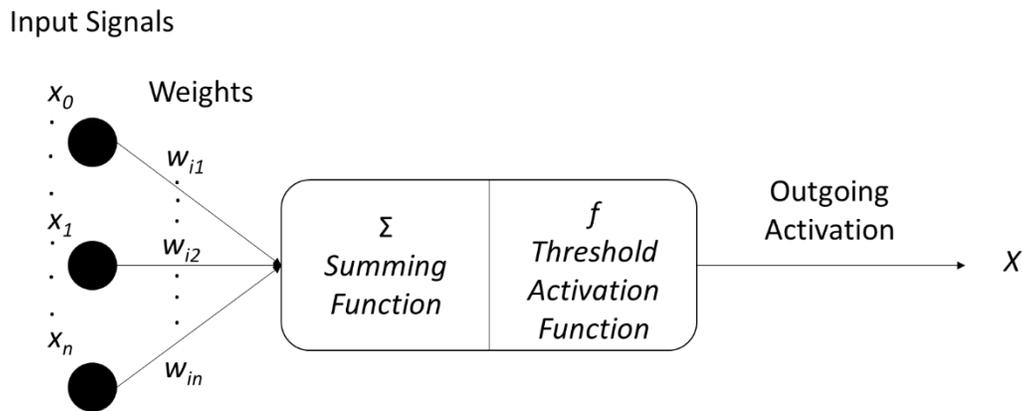


Figure 24 Neuron model (after Khdaire 2006).

Input signals are received by neurons and are given a weight and summed. This can be mathematically expressed as follows (Moghaddam et al. 2011):

$$\begin{aligned} net_i &= \sum w_{ij}x_i \\ X_i &= f(net_i) \end{aligned} \tag{8}$$

Where,

$f$  is the threshold activation function

$X_i$  is the output signal

$x_i$  is the input signal, and

$w_{ij}$  is the weight's coefficient from the  $i$ -th neuron of the first layer to the  $j$ -th neuron of the second layer.

Threshold function is typically nonlinear. On a simple form for discrete neural networks it can be expressed by the step function (Khdair 2006):

$$f(x) = \begin{cases} 1 & x > 0 \\ f'(x) & x = 0 \\ -1 & x < 0 \end{cases} \quad (9)$$

where  $f'(x)$  is the previous value of  $f(x)$  and  $X$  is the summation of the input neuron's activation as defined in Equation 8. For non-discrete networks, threshold function can be expressed in sigmoidal form (Khdair 2006):

$$f(x) = \frac{1}{1 + e^{-x}} \quad (10)$$

where  $f(x)$  is the threshold activation function.

The input data are propagated through the network to generate outputs. The outputs are then compared with the target values to calculate the error. Using a back-propagation learning algorithm, the connection weights are modified to minimize the target error. Basically, the back-propagation algorithm uses the rule repeatedly to calculate the effect of each connection weight with respect to the error. This can be mathematically expressed as follows (Riedmiller and Braun 1993):

$$\frac{\partial E}{\partial w_{ij}} = \frac{\partial E}{\partial X_i} \frac{\partial X_i}{\partial net_i} \frac{\partial net_i}{\partial w_{ij}} \quad (11)$$

where  $E$  is the error function.

Once the partial derivate for the entire network's connection weight is calculated, the error function is minimized using a simple gradient descent (Riedmiller and Braun 1993):

$$w_{ij}(t+1) = w_{ij}(t) - \varepsilon \frac{\partial E}{\partial w_{ij}}(t) \quad (12)$$

where

$w_{ij}(t)$  is the weight coefficient in step  $t$ , from neuron  $i$  to neuron  $j$ , and  $\varepsilon$  is the learning coefficient.

The training process continues until the error reaches its desired values after many steps (epochs). The time needed to reach the desired values is directly affected by how learning rate ( $\varepsilon$ ) is selected. If the learning rate is set too small, many epochs are needed to reach coverage. On the other hand, if learning rate is set too high, then the network may learn too quickly and may not learn very well or at all if there is a lot of variation in the data. One way to cope with this issue is to introduce a momentum term (Riedmiller and Braun 1993):

$$\Delta w_{ij}(t) = -\varepsilon \frac{\partial E}{\partial w_{ij}}(t) + \alpha \Delta w_{ij}(t-1) \quad (13)$$

where  $\alpha$  is the momentum parameter.

The momentum parameter scales the effect of previous step ( $t$ ) on the current step ( $t+1$ ). It is believed that the momentum term makes the learning procedure more stable; however, in practice this is not always the case. In fact, finding an optimum value for the momentum parameter is as problematic as finding an optimum value for learning rate (Riedmiller and Braun 1993). To overcome the disadvantages of a gradient-descent-based back-propagation algorithm, several alternative learning algorithms have been proposed over the years. Levenberg-Marquardt, conjugate gradient, and resilient back-propagation algorithms were examined in this study to train the network. The algorithm with the best performance was selected to develop the final model. All training networks work in a similar fashion as they attempt to reduce the global error by adjusting the weights.

### ***Levenberg-Marquardt algorithm***

The Levenberg-Marquardt algorithm can approach second-order timing speed without the need to calculate a Hessian matrix. The gradient descent in Equation 11 can be expressed as follows:

$$g = J^T e \quad (14)$$

where

$e$  is the error vector, and

$J$  is the Jacobian matrix of the first derivatives of the network errors ( $\frac{\partial E}{\partial w_{ij}}$ ).

To minimize the gradient descent, the second order partial derivative must be taken, which requires calculating the Hessian matrix. Calculating the Hessian matrix is typically very time-consuming. In the Levenberg-Marquardt algorithm, the Hessian matrix for performance function, in the form of a sum of squares, can be approximated as follows (Kisi and Uncuoglu 2005):

$$H = J^T J \quad (15)$$

Calculating the Jacobian matrix is much simpler than calculating the Hessian matrix as it can be calculated through a standard back-propagation technique. The Levenberg-Marquardt algorithm uses a Newton-like update to approximate the Hessian matrix (Kisi and Uncuoglu 2005):

$$w_{t+1} = w_t - (J^T J + \mu I)^{-1} J^T e \quad (16)$$

where

$\mu$  is always positive and called the combination coefficient, and

$I$  is the identity matrix.

This turns into Newton's method when  $\mu$  is zero, and it turns into the gradient descent with a small step size when  $\mu$  is large.  $\mu$  is initialized to be large and it is decreased after each successful

step, which results in reduction in the performance function.  $\mu$  is only increased if a tentative step increased the performance function. This allows the solution to converge quickly to the local minimum. The goal is to shift to Newton's method as quickly as possible since it is faster and more accurate near a minimum error (Kisi and Uncuoglu 2005).

### ***Conjugate gradient algorithm***

The back-propagation algorithm adjust the weights in the steepest descent direction (the most negative gradient), which is the direction that the performance function is decreasing most rapidly. This approach does not produce the fastest convergence. The conjugate gradient algorithms search along the conjugate direction, which generally results in a faster convergence than the steepest descent directions (Kisi and Uncuoglu 2005).

Generally, the step size is adjusted at each iteration, and a search is made along the conjugate gradient direction in order to find the step size that minimizes the performance function. The first iteration starts by searching the steepest descent direction (Kisi and Uncuoglu 2005):

$$p_0 = -g_0 \quad (17)$$

A line search is performed in order to find the optimal distance to move along the current search direction (Kisi and Uncuoglu. 2005):

$$x_{k+1} = x_k + \alpha_k g_k \quad (18)$$

The next search direction is considered to be conjugate to the previous search direction, which is generally done by combining the new steepest descent direction with the previous search direction (Kisi and Uncuoglu 2005):

$$p_k = -g_k + \beta_k p_{k-1} \quad (19)$$

where  $\beta_k$  is the ratio of the norm squared on the current gradient to the norm squared on the previous gradient (Kisi and Uncuoglu 2005):

$$\beta_k = \frac{\mathbf{g}_k^T \mathbf{g}_k}{\mathbf{g}_{k-1}^T \mathbf{g}_{k-1}} \quad (20)$$

### ***Resilient back-propagation algorithm***

A resilient back-propagation algorithm modifies the weight step based on gradient information to make the convergence faster. The magnitude of the weight update ( $\Delta_{ij}$ ) is determined by an adaptive update value, which evolves during the learning process, based on the following rules:

$$\Delta_{ij}^{(t)} = \begin{cases} \eta^+ \Delta_{ij}^{(t-1)}, & \text{if } \frac{\partial E^{(t-1)}}{\partial w_{ij}} \frac{\partial E^{(t)}}{\partial w_{ij}} > 0 \\ \eta^- \Delta_{ij}^{(t-1)}, & \text{if } \frac{\partial E^{(t-1)}}{\partial w_{ij}} \frac{\partial E^{(t)}}{\partial w_{ij}} < 0 \\ \Delta_{ij}^{(t-1)}, & \text{else} \end{cases} \quad (21)$$

where  $0 < \eta^- < 1 < \eta^+$ .

If the partial derivative of the weight changes its sign, it means the last update was too big and the algorithm has passed the local minimum. In that case, the update value ( $\Delta_{ij}$ ) is decreased by the factor  $\eta^-$ . On the other hand, if the derivative retains its sign, the update value will be slightly increased by the factor  $\eta^+$  to accelerate convergence. The weight update can be determined based on update values (Riedmiller and Braun 1993):

$$\Delta w_{ij}^{(t)} = \begin{cases} -\Delta_{ij}^{(t)}, & \text{if } \frac{\partial E^{(t)}}{\partial w_{ij}} > 0 \\ +\Delta_{ij}^{(t)}, & \text{if } \frac{\partial E^{(t)}}{\partial w_{ij}} < 0 \\ 0, & \text{else} \end{cases} \quad (22)$$

and

$$w_{ij}^{(t+1)} = w_{ij}^{(t)} + \Delta w_{ij}^{(t)} \quad (23)$$

If the derivative is positive, it means the error is increasing, so in that case the weight is decreased by the update value. If the derivative is negative, the weight will be increased by the update value. As explained before, if the partial derivative changes sign, it means the last update was too big and the local minimum was missed. In that case the previous weight update is revised (Riedmiller and Braun 1993):

$$\Delta w_{ij}^{(t)} = -\Delta w_{ij}^{(t-1)}, \quad \text{if } \frac{\partial E^{(t-1)}}{\partial w_{ij}} \frac{\partial E^{(t)}}{\partial w_{ij}} < 0 \quad (24)$$

The slopes of sigmoidal functions, which are often used as transfer functions, approach zero as the input gets very large. This causes issues when using the steepest gradient descent to train the network as a gradient's magnitude can be very small and result in very small changes in weights even though they are far from optimum. The resilient back-propagation algorithm is only dependent on the sign of the partial derivative, and the magnitude of the derivative has no effect on the weight update, which makes it more efficient than a pure gradient descent-based back-propagation method (Kisi and Uncuoglu 2005).

### **Selection of Learning Algorithm**

The MATLAB software package was used to develop and train the ANN. The data were randomly divided into three sets: 70% of data were used to train the network, 15% were used to validate the network, and 15% were used to test the network. The validation data set is used to determine a stopping point for the learning algorithm and the test data set is used to assess the performance of the trained network outside the training set. The inputs to the model are Roadway Functional Classification, friction number, AADT, and speed limit. The output was dry or wet normalized crash rate. The mean squared error (MSE) between the network's outputs and the targets was used as a measure of prediction accuracy of the trained network. The number of neurons in the hidden layer was increased to minimize the MSE. All three learning algorithms were used to train the network. The network with one hidden layer with eight neurons produced a satisfactory MSE for predicting both wet and dry normalized crash rate. The MSE and training

time for each network is provided in Table 8. The Levenberg-Marquardt algorithm had the highest prediction accuracy (lowest MSE) and the fastest convergence time, and it was selected for further analysis.

Table 8 Comparison of learning algorithms.

Learning Algorithm	Dry Crash Prediction		Wet Crash Prediction	
	MSE	Training Time (s)	MSE	Training Time (s)
Levenberg-Marquardt	0.006	0.988	0.016	0.447
Conjugate gradient	0.023	1.04	0.031	0.546
Resilient back-propagation	0.011	1.677	0.025	0.574

First, the validation performance of the network was evaluated. Figure 25 depicts the ANN’s validation performance for dry crashes. As explained before, an epoch is the process of providing the network with inputs and updating the weights for all the neurons within the network. The error in training data decreases as the network learns. Generally, several epochs are needed to train the ANN. Training stops once the validation error stops decreasing. The epoch corresponding to this error is called the optimum epoch number (5 in this case). The error on the test data indicates how well the network will respond to the new data set.

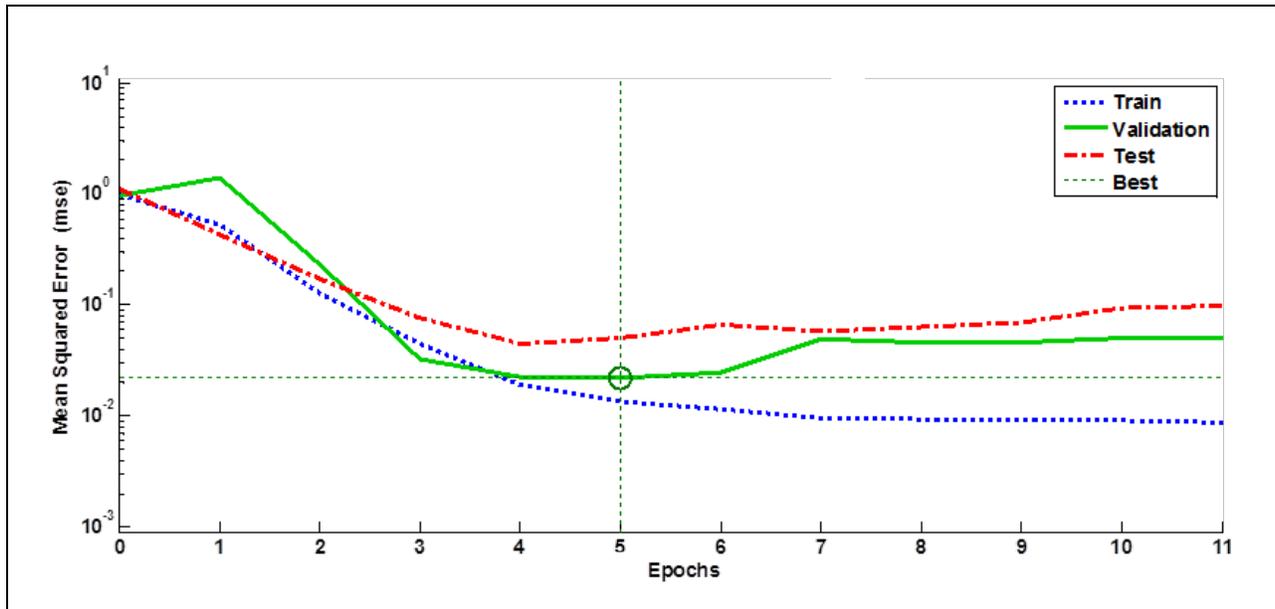


Figure 25 Validation performance for dry crashes.

The distribution of the errors is shown in Figure 26. Most errors are close to zero. Ideally, the errors should be tightly grouped around zero. The error distribution can be improved by adding more neurons to the hidden layer. In this case, the number of neurons and error seem to be satisfactory.

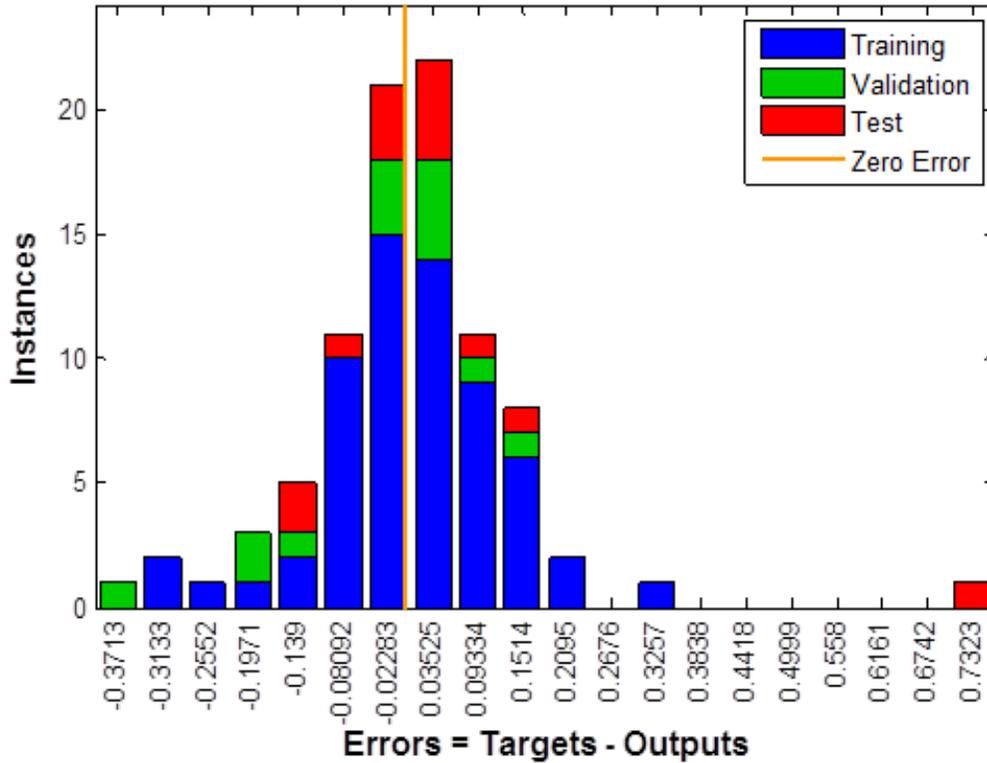


Figure 26 Error distribution for dry crashes.

To have a visual comparison, the regression plots of the outputs are provided in Figure 27 and Figure 28. Ideally, each point should fit close to the unity (dotted) line. Any points far from the group indicate potential outliers and may require further investigation. Regression lines show how well the outputs correlate with the targets. The regression line should follow close to the dotted line. The overall distance between the dotted line and regression line is summarized by the *R* value, which should ideally be close to 1.

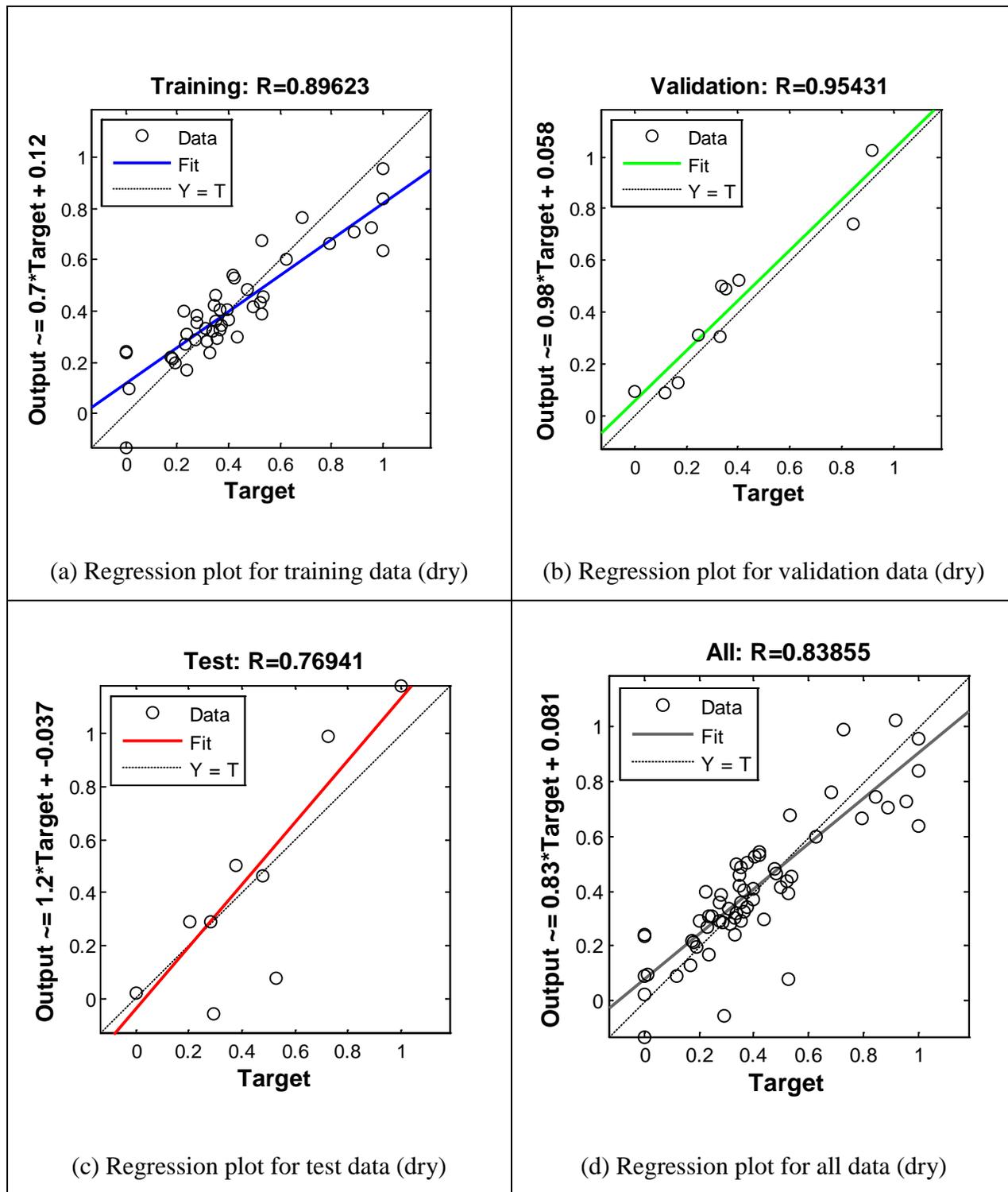


Figure 27 Regression plots for ANN outputs vs. targets: (a) training data (dry); (b) validation data (dry); (c) test data (dry); (d) all date (dry).

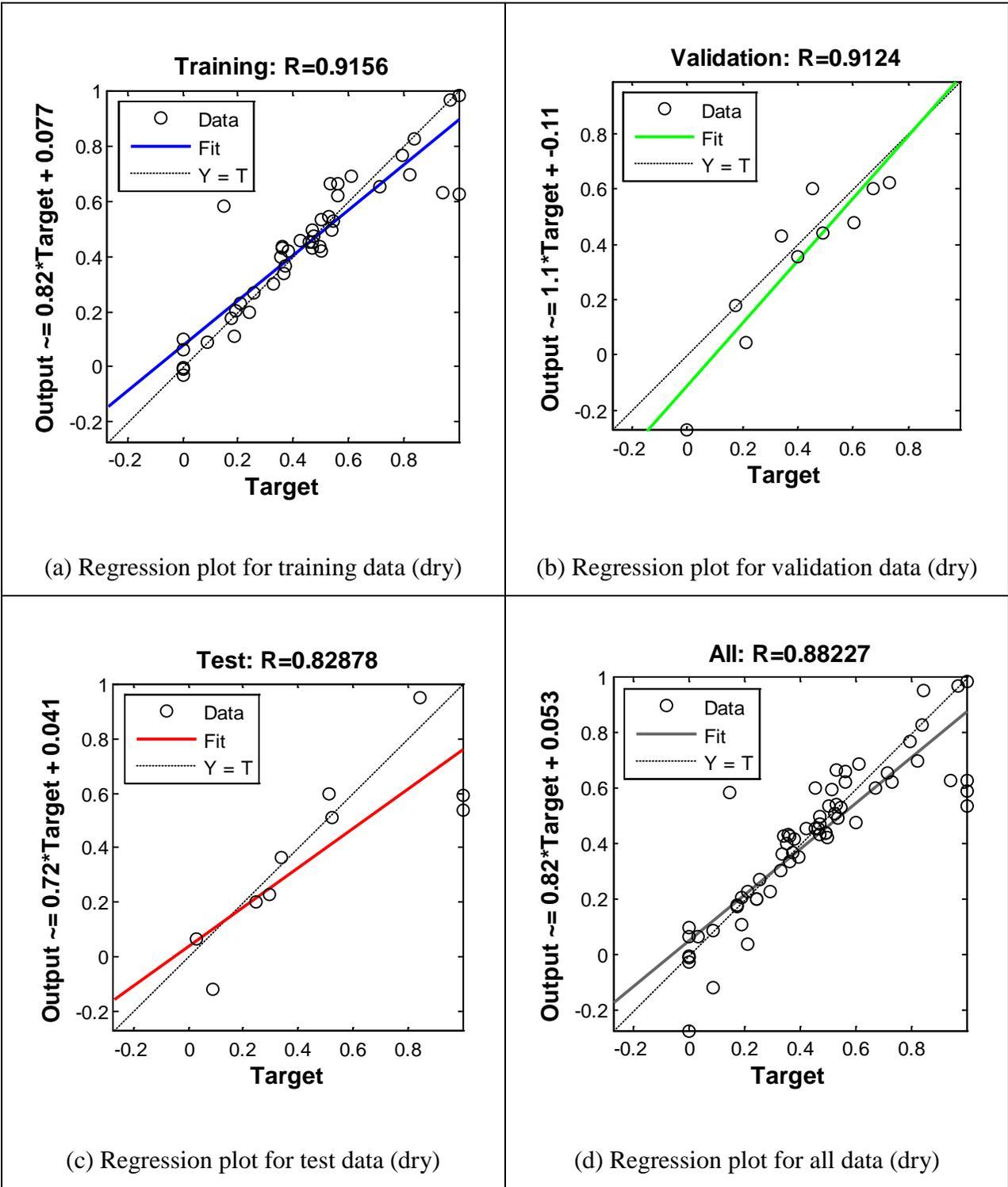


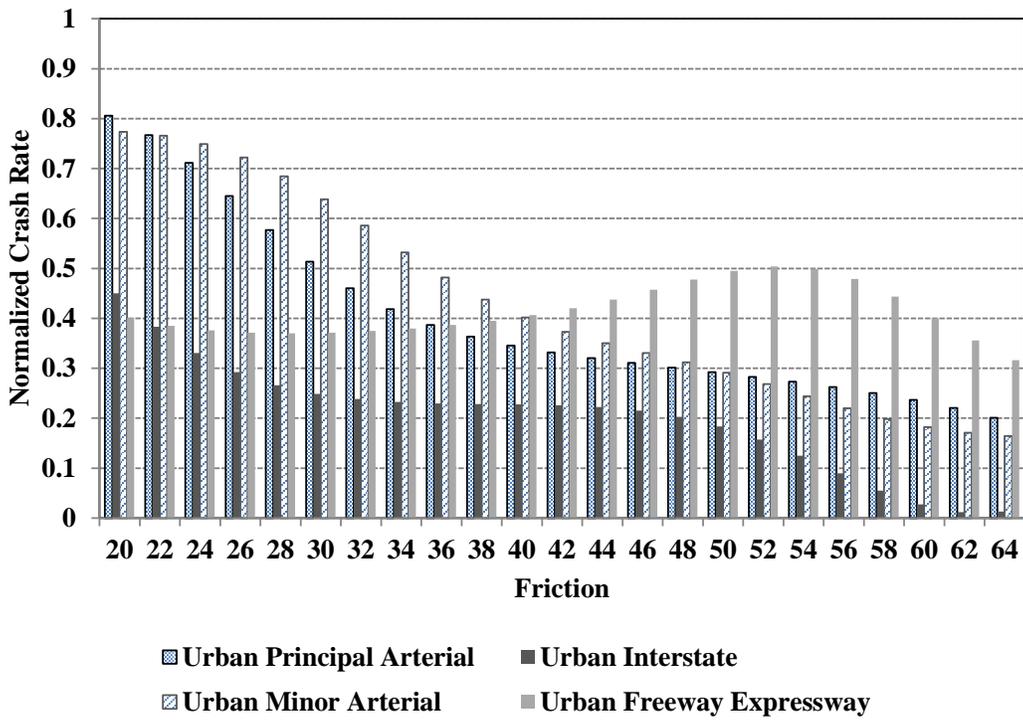
Figure 28 Regression plots for ANN outputs vs. targets: (a) training data (wet); (b) validation data (wet); (c) test data (wet); (d) all date (wet).

Sensitivity analysis was performed to illustrate the effect of friction on the rate of crashes for urban principle arterial roads. AADT and speed limit were set to average. The friction number was varied from 20 to 64 and the normalized crash rate was calculated for each friction level (Figure 29). In all cases except for urban freeway expressway, the crash rate decreased as the friction increased to average level. This is in agreement with author's previous findings (Najafi *et al.* 2015). For urban principle arterials, an approximately 40% reduction was observed in the rate of wet crashes as friction increased from 32 to 45. Similarly a 15% reduction was observed in the rate of dry crashes by increasing the friction number from 32 to 45. Overall, the effect of friction on reducing the rate of wet crashes appears to be more pronounced. An agency can define the investigatory or intervention level for friction based on the funding and crash rate. For instance, sites with a wet crash rate of 0.6 can be flagged as high risk and the friction level corresponding to this level can be selected as the investigatory level. This will require sites on principle arterial, interstate, and minor arterial roads with friction levels below 32 to be further investigated. No clear relationship between wet or dry crashes can be observed for freeway/expressways.

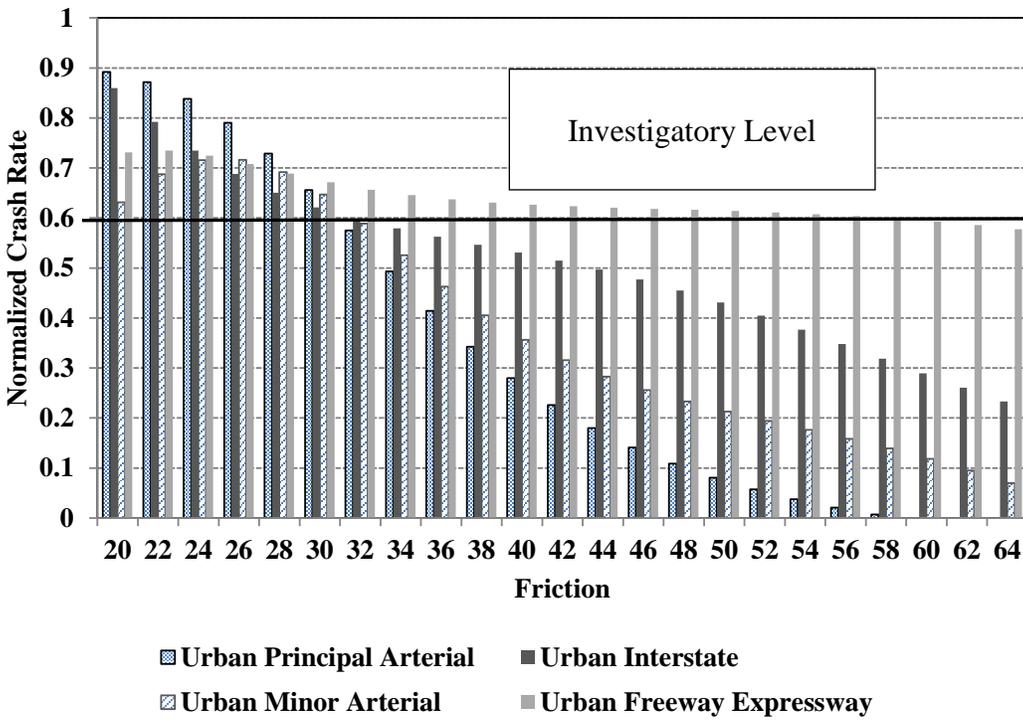
## **DISCUSSION**

The goal of a PFM program or policy is to establish criteria to prioritize safety improvement projects based on the crash risk. The ANN model discussed is capable of predicting the crash rate of wet or dry crashes based on friction, AADT, and speed limit. The crash rate can be used as a ranking to prioritize projects within each roadway category. High priority is given to the segments of roadway with a high crash rate (closer to 1).

An ANN-based PFM decision-making framework with eight neurons in the hidden layer is illustrated in Figure 30. The network can be developed and trained based on an agency's current friction and crash database. Each year the model can be improved by incorporating new friction and crash data. The network can predict the rate of wet and dry crashes using the network trained with the Levenberg-Marquardt learning algorithm. An agency can define an acceptable level of crash risk for various roadway networks based on their policies. The sites that exceed the acceptable level of crash rate will be selected for improvement. The acceptable level of crash risk can be balanced based on the available funding, and the intervention and investigatory friction thresholds can be adjusted accordingly.



(a) Dry crashes



(b) Wet crashes

Figure 29 ANN-predicted normalized crash rate vs. friction: (a) dry crashes; (b) wet crashes.

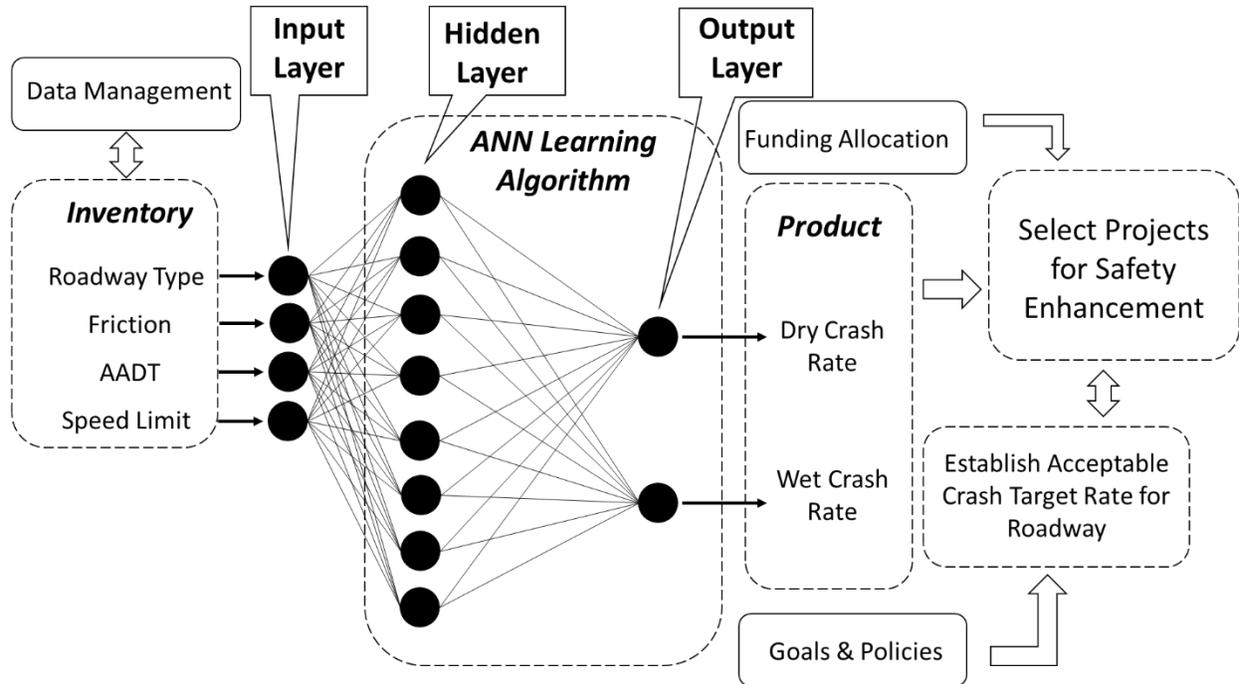


Figure 30 ANN-based PFM framework.

Compared to the regression models discussed in the previous chapter, ANN has higher prediction accuracy (lower MSE). The main drawback of ANN is it act as “black-box” as it is hard to understand. It also requires a higher computation power which makes it rather limiting for real-time applications as well as connected vehicles. Next an alternative soft-computing approach to ANN that requires less computation power and can be implemented in real-time applications.

## SUMMARY OF FINDINGS

This paper proposed two new approaches for PFM based on ANN. Following is the summary of the findings of this study:

- The Levenberg-Marquardt algorithm had the highest prediction accuracy (lowest MSE) and the fastest convergence time compared with conjugate gradient and resilient back-propagation learning algorithms.
- ANN was used to predict the rate of vehicle crashes based on friction, AADT, and speed limit. The crash rate can be used as a ranking scale to prioritize safety improvement projects.

- The rate of wet crashes observed for site with friction number below 32 was 40 percent higher than sites with friction higher than networks average (45). In case of dry crashes, 15 percent higher crash rate was observed for sites with friction number below 32 compared to sites with friction level above average.
- The effect of friction on reducing the rate of wet crashes is more pronounced than dry crashes.

## **CONCLUSIONS**

The learning ability of the proposed approach makes it appealing for developing a PFM compared with traditional statistical approaches because it can be developed from a limited database. The prediction accuracy of the network can be improved by incorporating more data into the system. The model can be updated every year at the end of the friction data collection cycle.

## **ACKNOWLEDGMENTS**

The authors would like to acknowledge the New Jersey Department of Transportation and, in particular Susan Gresavage, for their contribution and support in providing the data for this study.

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## **CHAPTER 4 – DEVELOPING A PAVEMENT FRICTION MANAGEMENT (PFM) FRAMEWORK USING FUZZY LOGIC<sup>5</sup>**

### **ABSTRACT**

Minimizing roadway crashes and fatalities is one of the primary objectives of highway engineers, and can be achieved in part through appropriate maintenance practices. Maintaining an appropriate level of friction is a crucial maintenance practice, due to the effect it has on roadway safety. This paper presents a fuzzy logic inference system that predicts the rate of vehicle crashes based on traffic level, speed limit, and surface friction. Mamdani and Sugeno fuzzy controllers were used to develop the model. The application of the proposed fuzzy control system in friction management is demonstrated. The results of this study provide a decision support model for highway agencies to monitor their network's friction and make appropriate judgments to correct deficiencies based on crash risk.

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<sup>5</sup> This manuscript will be submitted to the Journal of Accident Analysis & Prevention for publication. Co-authors include: Gerardo Flintsch and Seyedmeysam Khaleghian.

## **INTRODUCTION**

Friction is known to be an important factor affecting the risk of vehicle crashes (Flintsch et al. 2013; Henry 2000). Minimizing roadway crashes and fatalities is one of the Federal Highway Administration's (FHWA) and U.S. Department of Transportation's (USDOT) top priorities (FHWA 2014). The FHWA's Highway Safety Improvement Program (HSIP) policy states that 'each State shall develop, implement, and evaluate on an annual basis a HSIP that has the overall objective of significantly reducing the occurrence of and the potential for fatalities and serious injuries resulting from crashes on all public roads' (FHWA T5040.38). Furthermore, HSIP project locations shall be selected based on 'crash experience, crash potential, or other data supported means as identified by the State, and establishes the relative severity of those locations' (FHWA T5040.38). To achieve this to the greatest extent possible, State highway agencies will require the development of a Pavement Friction Management (PFM) program.

The FHWA has implemented various policies throughout the years to minimize friction-related vehicle crashes (Najafi et al. 2011). In 1980, the FHWA introduced the Skid Accident Reduction Program (SARP) (FHWA T 5040.17). The goal of the SARP was to minimize wet-weather skidding accidents. A subsequent publication supplied new guidelines for selecting appropriate treatments to achieve optimum surface textures for providing a high level of wet friction and a low level of tire-pavement noise (FHWA T5040.36). In 2010, the agency canceled the SARP and introduced the PFM program (FHWA T5040.38). The new program introduces a more proactive and systemic approach to identifying and correcting friction deficiencies and prioritizing resources based on needs.

FHWA technical advisory T5040.36 and the American Association of State Highway and Transportation Officials (AASHTO) Guide for Pavement Friction Management have presented several approaches to defining minimum and desirable friction levels (Hall et al. 2009). Most approaches require historical friction and accident data, which may not be readily available. In a previous study, authors suggested using an Artificial Neural Network (ANN) to model the relationship between friction and vehicle crashes and used the model to define a desirable network level friction threshold. And while an ANN provides high prediction accuracy, it is also hard to understand and typically requires high computational power. Fuzzy logic models, on the

other hand, are easy to understand and can be modified based on engineering judgment and experts' opinions. This makes them very appealing, since they can be modified based on an agency's needs.

## **BACKGROUND**

Fuzzy logic systems are based on traditional rules-based expert systems and can use approximate data and 'linguistic rules' to drive human-like decisions (Zadeh 1965). Experts' opinions can be incorporated into the fuzzy logic system through these linguistic rules (Flintsch et al. 2004). The fuzzy logic inference system consists of a fuzzifier, fuzzy inference engine, fuzzy rules and defuzzifier (Suman 2012).

The fuzzifier converts the numerical input values into linguistic variables. Several linguistic sets can be defined for each variable. Input variables can partially belong to more than one linguistic set. The belonging of any input variable to a certain linguistic set is defined as the degree of membership to that set and can take any value in the [0, 1] interval (i.e., the degree of membership will be zero if the value does not belong to the set) (Suman 2012). The inference engine transforms the inputs into the linguistic set of output based on linguistic rules. Fuzzy rules can be defined based on expert opinion or based on the observed relationship between the input variables and the outputs. Finally, the defuzzifier converts the fuzzy output set to a single 'crisp' value (Suman 2012).

Over the last few years, several researchers have proposed a fuzzy decision-making approach to determining pavement maintenance and safety needs based on various pavement characteristics (Sandra et al. 2000; Chassiakos 2006; Chen 2007; Suman et al. 2012; Xiao et al. 2000). Sandra et al. developed a fuzzy logic-based decision making tool to prioritize pavement needs based on the severity of various pavement distresses (Sandra et al. 2000). Chen used a fuzzy approach to predict the life-cycle cost of various pavement maintenance strategies based on pavement condition (Chen 2007). Both studies used expert opinion to develop fuzzy rules. Xiao et al. used fuzzy-logic to predict the risk of wet pavement crashes (Xiao et al. 2000). The researchers used accident and traffic data from 123 sections of highways in Pennsylvania, collected from 1984 to 1986. Researchers' results showed that fuzzy-logic can, indeed, be used

to predict the rate of crashes. Furthermore, they found that fuzzy-logic can also be used to determine the corrective action(s) that should be taken to improve safety (Xiao et al. 2000).

## **OBJECTIVE**

This paper uses a fuzzy logic inference system to model friction's relationship to speed limit, traffic volume, and crash rate. Mamdani and Sugeno fuzzy controllers are used to develop the proposed model, which provides a reliable and customizable tool that agencies can use to establish a relationship between crash rate and friction level and also employ as a scale to prioritize safety projects based on crash risk. Furthermore, the model can be used in real-time crash warning systems to alert drivers to potential slippery spots. The application of the proposed fuzzy system in a real-time crash warning system is demonstrated as a proof of concept.

## **DATA COLLECTION**

The data for this study were provided by the New Jersey Department of Transportation (NJDOT). The friction data were collected every 0.16 kilometer (km) on more than 3,218 km of urban principle arterial roads using an ASTM E-501 ribbed-tire locked-wheel skid trailer<sup>6</sup> (Figure 31) (Najafi et al. 2014). The data also included crash location (route and milepost), accident type (fatal, injury-causing, etc.), roadway surface condition at the time of accident (wet, dry, etc.), annual average daily traffic (AADT), and speed limit. Weather information was extracted from the National Oceanic and Atmospheric Administration (NOAA) database. (NOAA, 2015).

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<sup>6</sup> The results of previous chapters showed promising relationship between friction and crash rate for Urban Principle Arterial roads. For this reason the database for this type of roadway were investigated in this chapter.



Figure 31 Locked-wheel skid trailer.

Only fatal and injury causing crashes were considered in the study. Overall, 20,308 dry-condition and 5,010 wet-condition fatal and injury causing crashes were observed. To aggregate the data, fictional numbers were divided into bins with two unit increments ( $20 < SN \leq 22$ ,  $22 < SN \leq 24$ , etc.). The wet/dry crash distribution in relation to friction is illustrated in Figure 32.

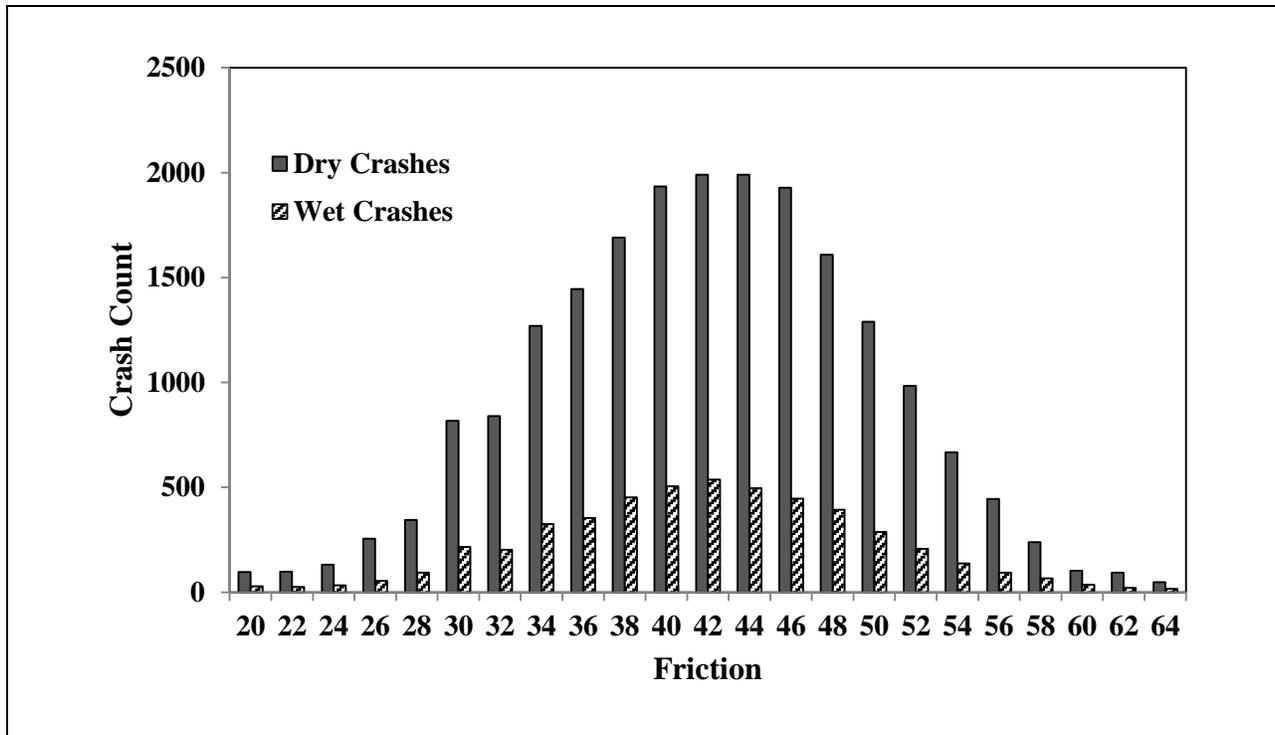


Figure 32 Crash distribution for fatal and injury causing crashes.

More dry-condition crashes were observed than wet-condition crashes. This is due to wet time exposure. Also, more crashes were observed around the average friction range (40-46). This necessitates normalizing the crashes based on friction distribution and wet time exposure. To normalize the crashes, the crash rate was derived for each friction interval by dividing the crash count by exposure (Gan et al. 2012):

$$\text{Crash} \cdot \text{Rate} = \frac{\text{Number} \cdot \text{of} \cdot \text{crashes} \times 1,000,000}{\text{Exposure}} = \frac{\text{Number} \cdot \text{of} \cdot \text{crashes} \times 1,000,000}{\text{AADT} \times n \times Y \times L} \quad (25)$$

Where,

AADT: total annual average daily traffic (vehicles per day [vpd])

n: wet or dry time exposure (days)

Y: study duration in years (year)

L: length of the roadway segments (km).

The crash rates were then normalized between 0 and 1 for each crash type (wet or dry):

$$\text{Normalized} \cdot \text{Crash} \cdot \text{Rate}_i = \frac{\text{Crash} \cdot \text{Rate}_i - \text{MIN}(\text{Crash} \cdot \text{Rate})}{\text{MAX}(\text{Crash} \cdot \text{Rate}) - \text{MIN}(\text{Crash} \cdot \text{Rate})} \quad (26)$$

Where Normalized Crash Rate<sub>(i)</sub> corresponds to the normalized crash rate for the  $i^{\text{th}}$  friction bin.

## DATA ANALYSIS

MATLAB software was used to develop Mamdani and Sugeno fuzzy systems. The inputs to the models are speed limit, traffic and friction and the output is wet or dry crash rate. The discussion for each system is provided in the following sections.

### Mamdani Fuzzy Inference System

The Mamdani fuzzy inference is one of the most widely used fuzzy inference systems. It was proposed by Mamdani in 1975 to serve as a control system for a steam engine by utilizing sets of linguistic rules that were determined from experts' knowledge (Mamdani 1975). In the Mamdani

inference, inputs are first fuzzified using membership functions. Let's assume X is a space of points and the generic element of X is denoted by x ( $X = \{x\}$ ). A membership function  $f_A(x)$  characterizes a fuzzy set of A in X in which each point in X is a real number in the [0,1] interval and the values of  $f_A(x)$  at x represent the degree of membership of x in A. If the value of  $f_A(x)$  is closer to 1, it means x has a higher degree of membership in A (Zadeh 1965). The most commonly used membership function shapes include triangle, trapezoid, Gaussian, and sigmoidal. This study used triangular membership functions. The distribution can be mathematically expressed as follows:

$$triangle(x, a, b, c) = \begin{cases} 0 & x \leq a \\ \frac{x-a}{b-a} & a \leq x \leq b \\ \frac{c-x}{c-b} & b \leq x \leq c \\ 0 & c \leq x \end{cases} \quad (27)$$

Where a, b, and c are the x coordinates of the three corners of the triangle.

### ***Membership Functions***

Friction, speed limit, and AADT are the inputs of the system and the output is the wet or dry crash rate. Friction was broken down into five levels: very low (less than 25), low (25 to 35), medium (35 to 45), high (45 to 55), and very high (above 55). As previously discussed, the degree of membership to each set is varied between 0 and 1. For example, in Figure 33, the friction number 22's degree of belonging (membership) to the very low group and low group are 75%, and 25% respectively. As a friction number increases, its degree of belonging to the low friction group increases and so on. So at any friction level, we can incorporate some level of uncertainty by overlapping the sets. Similar membership functions were defined for traffic and speed limit. Traffic and speed limit were categorized into three levels: low, medium, and high, as shown in Figure 34 and Figure 35.

Five levels of cash risk were also defined based on the crash rate: very low, low, medium, high and very high (Figure 36 and Figure 37). The levels can be modified based on the agency's

needs. Crash risk levels can be used to define investigatory and intervention levels for network friction. For instance, sites with very high crash risk are selected for intervention, and sites with high crash risk are selected for investigation. The agency can also add more levels of crash risk to increase flexibility in determining the list of routes that need to get attention and prioritizing projects based on various budget scenarios.

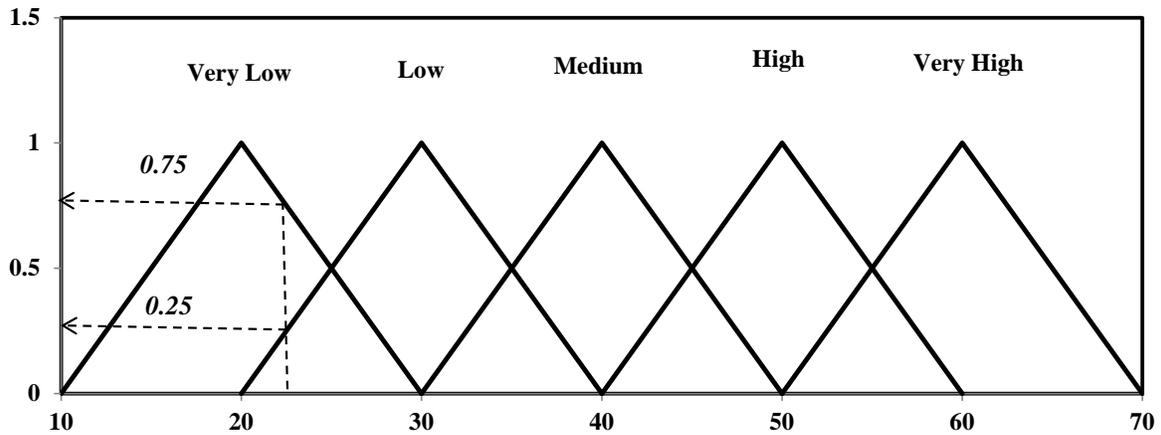


Figure 33 Friction membership function.

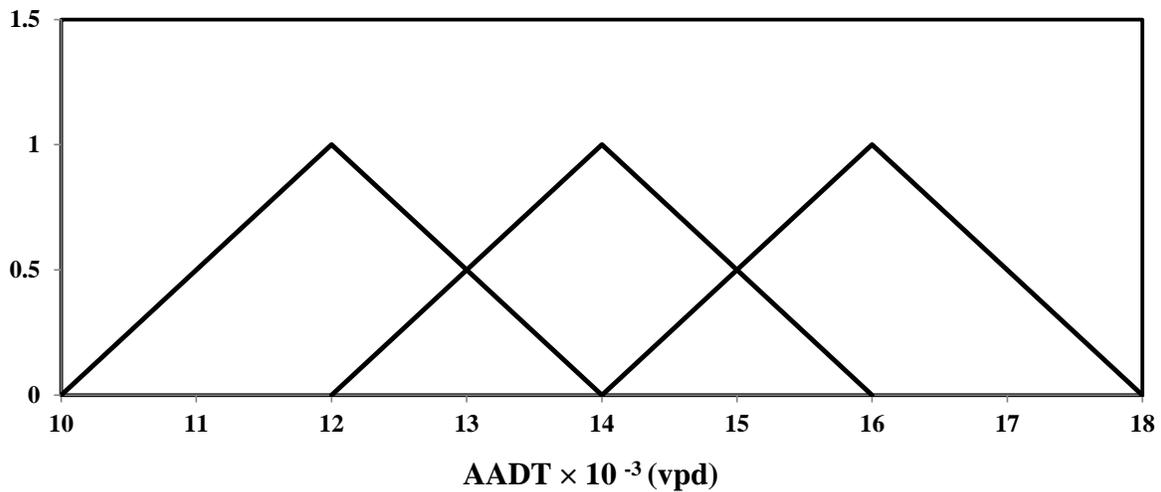


Figure 34 AADT membership function.

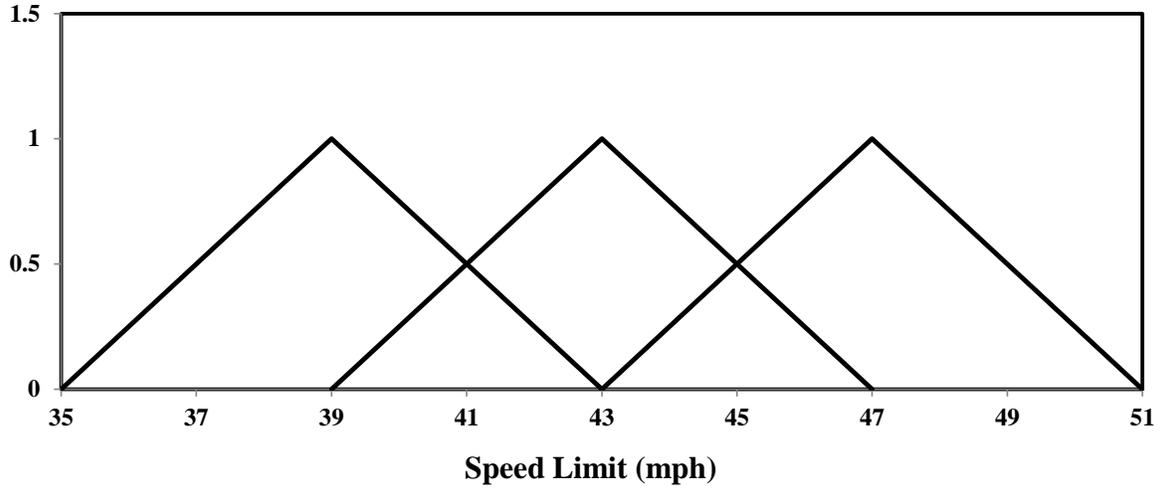


Figure 35 Average speed limit membership function.

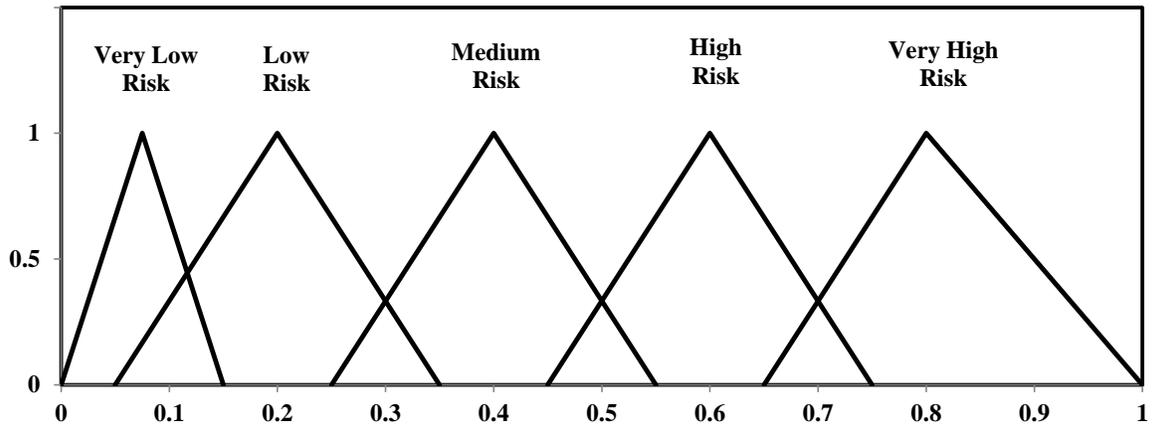


Figure 36 Dry crash rate membership function.

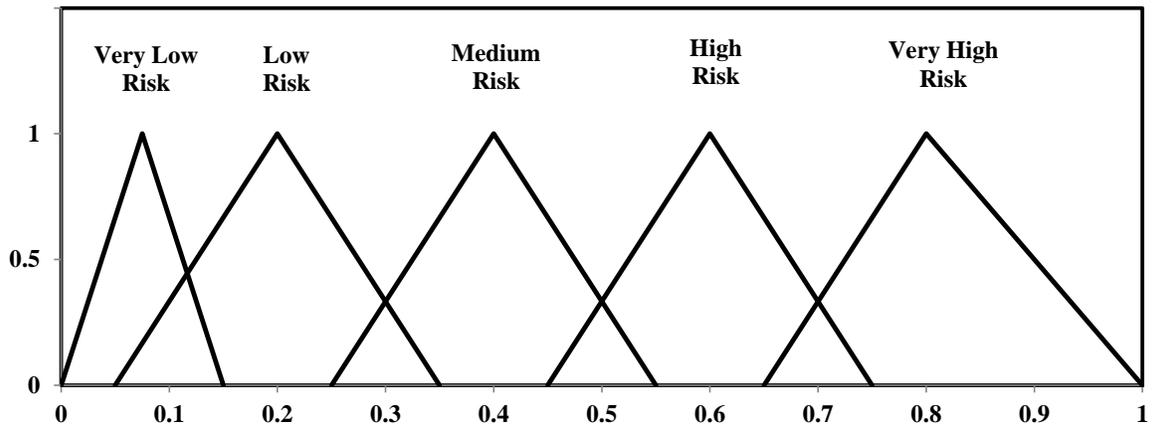


Figure 37 Wet crash rate membership function.

## **Fuzzy Rules**

Once the membership functions are defined, the fuzzified inputs are combined according to fuzzy rules. Mamdani fuzzy rules are if-then in nature (*i.e.*, **IF** functional classification is urban principal arterial **AND** friction is very low **AND** speed limit is high **AND** AADT is high **THEN** dry crash rate is high and wet crash rate is high). The rules are then combined to generate the output distribution. In the Mamdani interface, ‘max’ and ‘min’ operators are used to aggregate the fuzzy rules. The Mamdani fuzzy logic operator can be mathematically expressed as follows (Youssefi et al. 2011):

$$f(\mu_A(x), \mu_B(y)) = \mu_A(x) \wedge \mu_B(x) \quad (28)$$

Where  $\mu_A(x)$  indicates the membership function of  $x$ .

The outputs can then be defuzzified to a ‘crisp’ value using the centroid method (Lee 1990):

$$x^* = \frac{\int \mu_i(x)xdx}{\int \mu_i(x)dx} \quad (29)$$

Where,

$x^*$  is the defuzzified output

$\mu_i(x)$  is the aggregated membership function, and

$x$  is the output variable.

The Graphical User Interface (GUI) of MATLAB software package was used to develop the Mamdani fuzzy inference system. The inputs to the model included friction, AADT, and speed limit. The outputs are dry and wet condition crash rates. The centroid method was used to defuzzify the outputs.

Mamdani fuzzy rules are provided in Table 9. The rules were developed by observing trends in the database. The mean squared error (MSE) between predicted and actual crash rates was calculated to estimate the accuracy of the model. A value closer to zero is desirable as it indicates smaller random error in the model. The MSE between observed and predicted for both dry and wet crash rates was approximately 0.01.

Table 9 Mamdani Fuzzy Rules

<b>Friction</b>	<b>AADT</b>	<b>Speed Limit</b>	<b>Dry Crash Rate</b>	<b>Wet Crash Rate</b>
very low	medium	medium	very high	very high
low	medium	high	very high	very high
low	medium	low	very high	high
low	high	high	high	high
medium	high	high	medium	medium
high	high	high	low	very low
very high	low	high	low	medium
very high	medium	high	low	very low
very high	high	high	very low	very low

### Sugeno Fuzzy Inference System

The Sugeno fuzzy inference system is similar to Mamdani's system in several ways. Both systems fuzzify the inputs in the same way and apply the same fuzzy operator. The main difference is that Sugeno output functions are either linear or constant. Sugeno fuzzy rules have the following form (Sugeno 1985):

$$\begin{aligned}
 & \text{If} \\
 & \quad \text{Input 1} = x \\
 & \quad \text{and} \\
 & \quad \text{Input 2} = y \\
 & \\
 & \text{then} \\
 & \quad z = ax + by + c
 \end{aligned} \tag{30}$$

Where the output  $z$  will be constant if  $a = b = 0$ . The outputs will be assigned a weight ( $w_i$ ) based on their strength. Unlike the Madani system, the Sugeno system doesn't use defuzzification to generate outputs. Instead, the weighted average of rule outputs is used to calculate the crisp output (Sugeno 1985):

$$\eta = \frac{\sum_{i=1}^n w_i z_i}{\sum_{i=1}^n w_i} \tag{31}$$

Where,  
 $\eta$  is the final crisp output, and

$n$  is the number of rules.

The final outputs are compared with the targets to calculate the error. The membership function parameters are then fine-tuned using learning methods similar to ANNs to minimize the error.

MATLAB's artificial neuro-fuzzy inference system (ANFIS) function was used to train the system. The function uses least square and back propagation gradient decent methods to train fuzzy logic membership function to match given data. The MSE between observed and predicted crash rates was approximately 0.02 for both wet and dry crashes after training membership functions.

The Sugeno system's rules are illustrated in a 3D model in Figure 38 and Figure 39. The rules are developed based on the observations. This provides good insight into how a low level of friction and a high level of speed contribute to a high cash rate. Overall, the relationship between wet and dry crash rate and friction seems to be very similar. The highest wet/dry crash rate is observed for friction numbers below 30. In the case of speed limit, high crash rates can be observed for speed limits above 68 kilometers per hour (kph). The effect of high speed limit is more pronounced on wet crashes than on dry crashes.

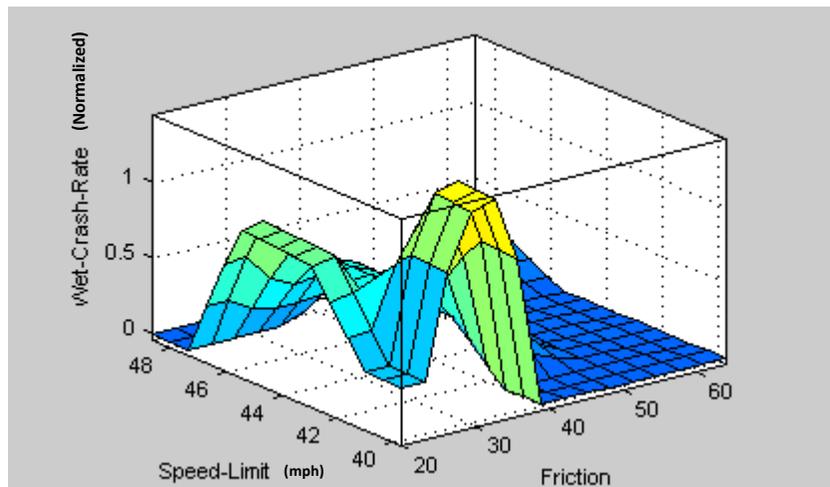


Figure 38 Sugeno rules 3D surface – friction and speed (mph) vs. dry crash rate.

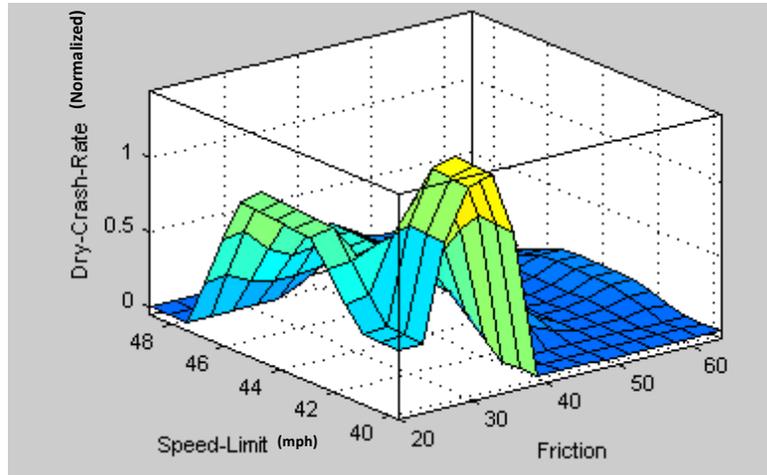


Figure 39 Sugeno rules 3D surface – friction and speed (mph) vs. wet crash rate.

## DISCUSSION

Overall, the Mamdani controller produced a higher precision (lower MSE) output than the Sugeno system. The Mamdani system uses linguistic rules, which are more appropriate for decision-making purposes. The advantage of the Sugeno system is that it can be used with other adaptive learning methods such as backpropagation. It should be noted that friction numbers used in this study were measured using a ribbed tire, locked-wheel skid trailer. In general, ribbed tire measurements are higher than those of smooth tires (Flintsch et al. 2010). Friction threshold is expected to be lower if a smooth tire locked-wheel skid trailer is utilized to collect the data.

Compared to the results of previous chapter, Fuzzy logic has a lower prediction precision (higher MSE) compared to Neural network. The benefit of Fuzzy logic over neural network is that it requires less computation power and it can be stored in micro-chips and vehicles' computers. This allows the model to be implemented for real-time crash prediction application. Application of such a system is discussed in the next chapter.

## EXAMPLE APPLICATION

The goal of a Pavement Friction Management (PFM) program is to minimize the risk of vehicle crashes by addressing friction deficiencies. With shrinking funding, agencies often need to prioritize projects based on their importance. The crash rate defined herein provides a scale for

highway agencies to use for prioritizing safety projects based on crash risk so they can advance a resurfacing project if the site is already in the queue for resurfacing and the crash risk is high.

To better understand the relationship between friction and crash rate, a sensitivity analysis for both systems was performed by setting the speed limit and ADDT to average (72 kph and 15,000 vph respectively) and changing the friction level (Figure 40). Both wet and dry crash rates decreased as friction increased. This is in agreement with previous findings that friction affects crash rate in both wet and dry conditions (Najafi et al. 2015).

The relationship between friction and crash rate can also be used to define the desirable friction threshold. For instance, a friction level that induces high crash risk—at any given traffic level and speed limit—can be selected as the investigatory threshold. An agency can define multiple levels of friction and crash risk based on their internal policies. This will allow them to narrow sections of roadway designated for improvement into smaller sets, and gives them the flexibility to prioritize the sections based on available funds. More sections can be added to the list as funding becomes available.

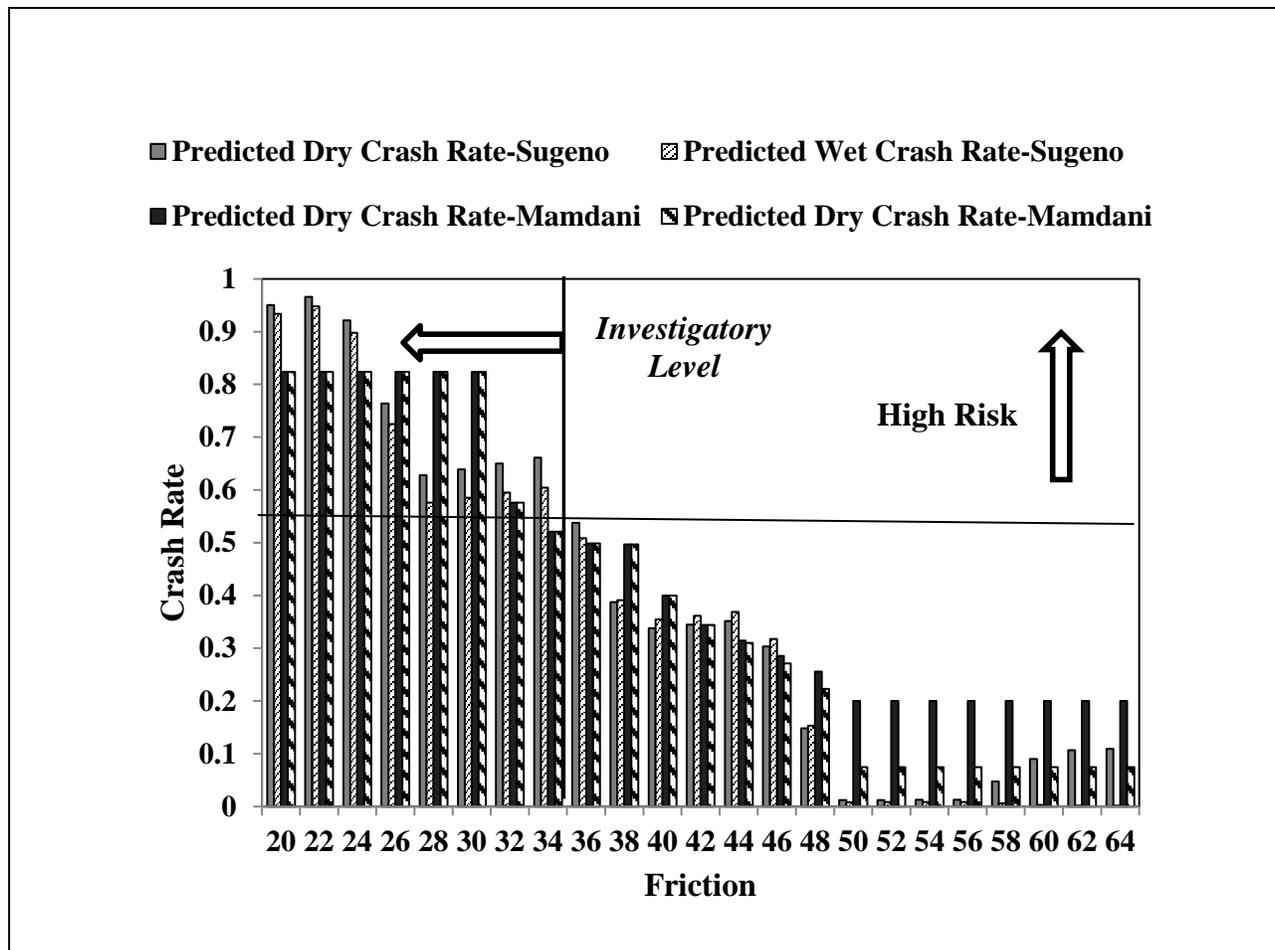


Figure 40 Sensitivity analysis.

## FINDINGS AND CONCLUSIONS

This paper proposed a fuzzy logic approach for PFM. Following are the main findings and conclusions of the study:

- The fuzzy logic interface system is a reliable tool for the PFM decision-making process. The system can be easily modified based on agency needs. The model uses linguistic and human like rules and is easy for practitioners and highway engineers to understand.
- Crash risk can be predicted based on friction, traffic, and speed limit using both Mamdani and Sugeno controllers. The Mamdani controller produced a higher precision (lower MSE) prediction than the Sugeno system. The advantage of the Sugeno system is that it can be used with other adaptive learning methods such as backpropagation. The

Mamdani system uses linguistic rules, which are more appropriate for decision-making purposes.

- The rate of both wet and dry condition crashes increases as the roadway friction decreases. The highest wet/dry crash rate was observed for friction numbers below 30 and speed limits above 68 kph. Using both wet and dry condition crashes in PFM studies is suggested.
- The investigatory threshold level of friction can be defined based on the crash risk. Agencies can modify the level based on available funding. This allows highway agencies to prioritize resources based on safety needs so they can advance a resurfacing project if the site is already in the queue for resurfacing and the crash risk is high.

## **ACKNOWLEDGEMENT**

The authors would like to acknowledge the New Jersey Department of Transportation and, in particular, Susan Gresavage for their contribution and support in providing the data for this study.

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## **CHAPTER 5 – APPLICATION OF FUZZY LOGIC INFERENCE SYSTEM IN A REAL-TIME SLIPPERY ROAD WARNING SYSTEM -A PROOF OF CONCEPT STUDY**

### **INTRODUCTION**

Recently, the USDOT has begun promoting the concept of connected vehicles to improve the safety of, and ease of mobility throughout, the transportation infrastructure system. Connected vehicles can increase drivers' awareness and reduce the risk of crashes through vehicle-to-vehicle (V2V) and vehicle-to-infrastructure (V2I) data transmission. This application will inform drivers of roadway hazards in real-time. According to the USDOT, 'combined V2V and V2I systems potentially address about 81 percent of all-vehicle target crashes; 83 percent of all light-vehicle target crashes; and 72 percent of all heavy-truck target crashes annually' (USDOT 2015).

The USDOT has also performed a safety pilot study to collect V2V and V2I data under real-world conditions. The safety applications evaluated in the safety pilot include the following: Blind Spot Warning/Lane Change Warning (warns drivers if there is a car in the blind spot during an attempted lane change), Forward Collision Warning (warns drivers when a vehicle in their path is stopped or is traveling slower and they fail to brake), Electronic Emergency Brake Lights (notifies the driver when a vehicle ahead of them is braking hard), Intersection Movement Assist (warns the driver if it is unsafe to enter an intersection), Do Not Pass Warning (warns drivers if they attempt a lane change when there is another vehicle coming from the opposite direction in the passing zone), Control Loss Warning (warns the driver if another adjacent vehicle has lost control) (USDOT 2015).

'Slippery when wet' and 'Watch for ICE' signs have been implemented for years across US highways and other parts of the world. A real-time slippery road warning system can provide immediate alerts to drivers for potentially hazardous locations. The information can also be transmitted to a central traffic control center to be used in snow and ice removal operations or to plan maintenance activities to correct friction deficiencies. The fuzzy system discussed in the previous chapter is capable of predicting the crash risk based on available friction and speed limit. Most modern Global Positioning Systems (GPS) report the speed limit and traffic volume

information in real-time. This means the model can be used in real-time if friction can be measured simultaneously.

## **REAL-TIME FRICTION ESTIMATION**

Due to the importance of tire-pavement friction in vehicle dynamics and stability control, several researchers have investigated various methods of estimating the tire-pavement friction in real time. (Erdogan et al. 2009). Real-time friction estimation can be separated into two categories: 1) sensor-based estimation, and 2) vehicle dynamic-based estimation (Rajamani et al. 2010). The main drawback of sensor-based tire-pavement friction estimation is the cost associated with acquiring the sensors. Installing the sensors in the vehicle or tire carcass can also raise liability issues. Some sensor lasers also have limited application during wet weather conditions. For these reasons, the sensor-based method will not be further investigated for this study. In the vehicle dynamic control-based approach, tire-pavement friction is estimated based on the vehicle's motion. This method uses the measurements from the sensors already installed in the vehicle, which gives it an advantage over the sensor-based approach, which requires the installation of additional sensors.

As the tire rolls freely on the pavement surface, longitudinal frictional forces are generated at the tire and pavement interface. The relative speed between the tire circumference and the pavement surface is very low during the free rolling (no braking) condition. Applying a constant brake to the tire will increase the slip speed to the potential maximum equivalent of the vehicle speed. The slip ratio ( $S_r$ ) can be calculated from the vehicle's directional speed ( $V$ ), the wheel's angular velocity ( $\omega$ ) and the wheel-rolling radius ( $R$ ):

$$S_r = \frac{V - \omega R}{V} \quad (32)$$

Where slip ratio is zero under normal driving condition ( $V = \omega R$ ) and it is 1 when the wheel is fully locked ( $\omega = 0$ ).

The relationship between tire friction force and slip ratio for various road surfaces with different friction levels is presented in Figure 41. For small slip ratios, the tire friction force is 'proportional' to slip ratio (Rajamani et al. 2010). The coefficient of friction can be determined

based on the slope at the low slip region; this is commonly known as slip-slope (Rajamani et al. 2010). As illustrated by the figure, the slip-slope for roads with higher friction is larger. Some references argue that tire properties influence the ‘shape’ of the low slip region more than the road surface properties (Henry 2000; Uchanski et al. 2003). However, studies show that for slip ratios greater than 0.005, the slip-slope method can reliably estimate the coefficient of friction (Rajamani et al. 2010). Several studies (Dieckmann 1992; Germann et al. 1994; Gustafsson 1997; Yi et al. 1999; Hwang and Song 2000) have previously used this method to estimate the tire-pavement friction.

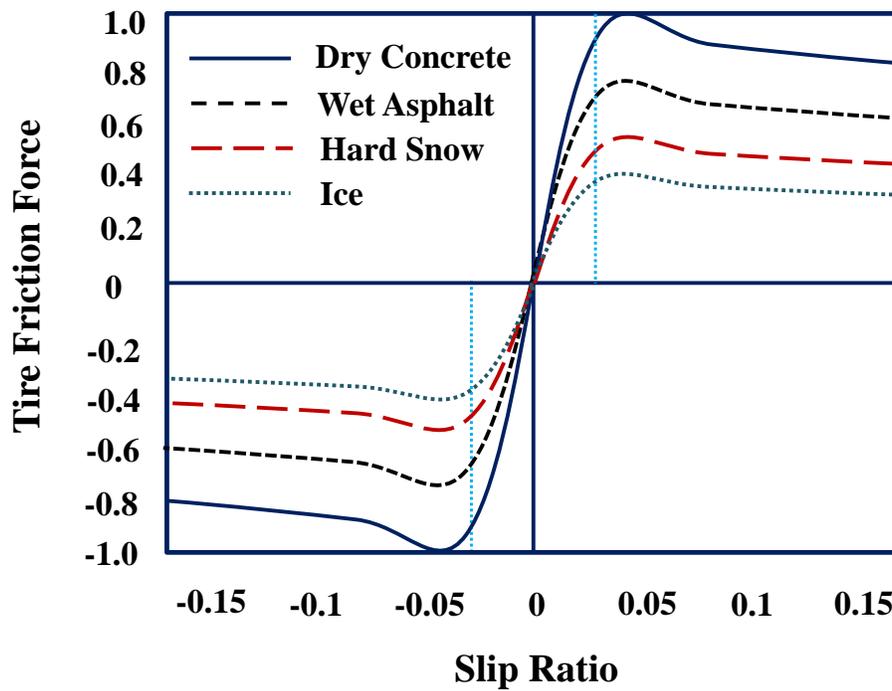


Figure 41 Tire Friction Force versus slip ratio (after Rajamani et al. (2010)).

### Slip-slope based Friction Estimation

The inputs to the slip-slope based friction estimation method include normalized longitudinal tire force and slip ratio. The normalized longitudinal tire force (also known as normalized traction force) can be determined by dividing the traction force ( $F_f$ ) by the normal force on the drive wheel ( $N$ ). For a vehicle in longitudinal motion, this relationship can be expressed as follows:

$$\frac{F_f}{N} = K S_r \quad (33)$$

Where,

$F_f$  = Longitudinal traction force  
 $N$  = Normal tire force, and  
 $K$  = Slip-slope.

The total longitudinal traction forces can be estimated using Newton's second law of motion ( $\sum F_x = ma_x$ ). Where  $m$  is the mass of the vehicle and  $a_x$  is the longitudinal acceleration or deceleration. This relationship can be formulated as follows (Rajamani et al. 2010):

$$F_f = m|a_x| + |F_r| + |D_a V^2|, \quad \text{for acceleration} \quad (34)$$

$$F_f = m|a_x| - |F_r| - |D_a V^2|, \quad \text{for deceleration} \quad (35)$$

And,

$$F_r = C_{roll} mg \quad (36)$$

$$D_a = \frac{1}{2} \xi V^2 C_d A \quad (37)$$

Where,

$F_r$  = Rolling resistance force  
 $D_a$  = Aerodynamic drag force  
 $C_{roll}$  = Rolling resistance coefficient  
 $\xi$  = Air density  
 $V$  = Speed  
 $C_d$  = Aerodynamic drag coefficient  
 $A$  = Frontal area of the vehicle

The longitudinal acceleration/deceleration ( $a_x$ ) can be measured using accelerometers. The vehicle's directional speed can be measured with a GPS. The angular speed of the wheels can be obtained from the antilock brake system (ABS). The normal tire force ( $N$ ) can be calculated using a simple static force equilibrium model of the vehicle, assuming that the vehicle's weight is known. More details about the procedure can be found in Rajamani et al. (2010). Assuming that the vehicle is all-wheel-drive, we will have:

$$F_{f_{total}} = F_{f_{front}} + F_{f_{rear}} = K_{front} N_{front} S_{r_{front}} + K_{rear} N_{rear} S_{r_{rear}} \quad (38)$$

For two-wheel drive vehicles,  $K_{front}$  or  $K_{rear}$  is zero. The ratio between  $K_{front}$  and  $K_{rear}$  is known to be constant and depends on tire properties and number of tires for front and rear axles (Rajamani et al. 2010):

$$F_{f_{total}} = K_{rear} (\alpha N_{front} S_{r_{front}} + N_{rear} S_{r_{rear}}) \quad (39)$$

$F_{f_{total}}$ ,  $N_{front}$ ,  $S_{r_{front}}$ ,  $N_{rear}$ , and  $S_{r_{rear}}$  are measured in real time, so the equation can be written as a function on time (t):

$$F_{f_{total}}(t) = K_{rear}(t)(\alpha N_{front} S_{r_{front}}(t) + N_{rear} S_{r_{rear}}(t)) \quad (40)$$

Equation can be expressed as a state space model as follows (Gustafsson 1998; Rajamani, et al. 2010):

$$y(t) = \varphi^T(t)\theta(t) + e(t) \quad (41)$$

Where,

$y(t) = F_{f_{total}}$ , is the system output

$\phi(t) = \alpha N_{front} S_{r_{front}}(t) + N_{rear} S_{r_{rear}}(t)$ , is the measured regressor vector

$\theta(t) = K_{rear}(t)$ , is the unknown parameter to be estimated

$e(t)$  = error term

The solution to equation can be found using the recursive least square (RLS) algorithm (Germann et al. 1994; Gustafsson 2000; Rajamani et al. 2010; Sastry and Bodson 2011), or using a Kalman filter (Ray 1997; Gustafsson 1998; Rajamani et al. 2010).

## CarSim Simulation Results

To test the model, a CarSim software package was used to simulate a vehicle's response to braking (Mechanical Simulation Corporation, 2015). The CarSim library has several simulations for various types of vehicles and tires that have been validated with experimental data. The simulations were performed on a B-class sport car. The assumptions for the vehicle and tire properties are provided in Figure 42.



Figure 42 B-Class Sport Car (CarSim, (2015)).

The vehicle and tire properties were kept constant and the surface friction was changed to simulate the braking response. Two surfaces were considered: one with very low friction (friction coefficient = 0.2) and one with high friction (friction coefficient = 0.8). Longitudinal and angular velocity, tire longitudinal force, and slip ratio were simulated in real-time for both surfaces. The simulated data were then used to predict the real-time friction using the Kalman filter in the MATLAB software package. For brevity, the procedure for the Kalman filtering process is not provided here. Figure 43 and Figure 44 illustrate the MATLAB's estimated friction force versus CarSim's simulation (real) data. As the figure illustrates, the estimated friction is almost identical to real friction in the low slip region. As expected, the slip-slop for the slippery road is lower than for the high friction surface (7% versus 17% respectively).

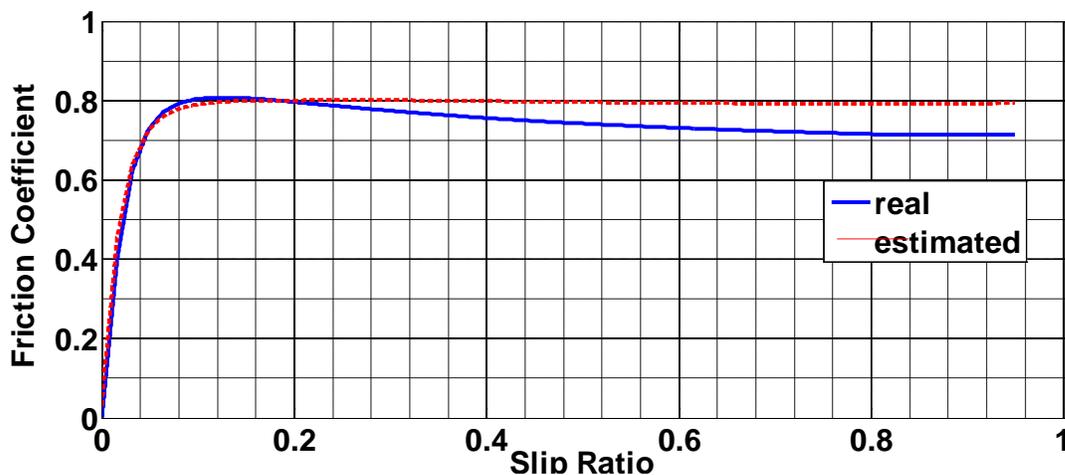


Figure 43 Friction vs. slip ratio estimation – high friction surface (friction coefficient = 0.8).

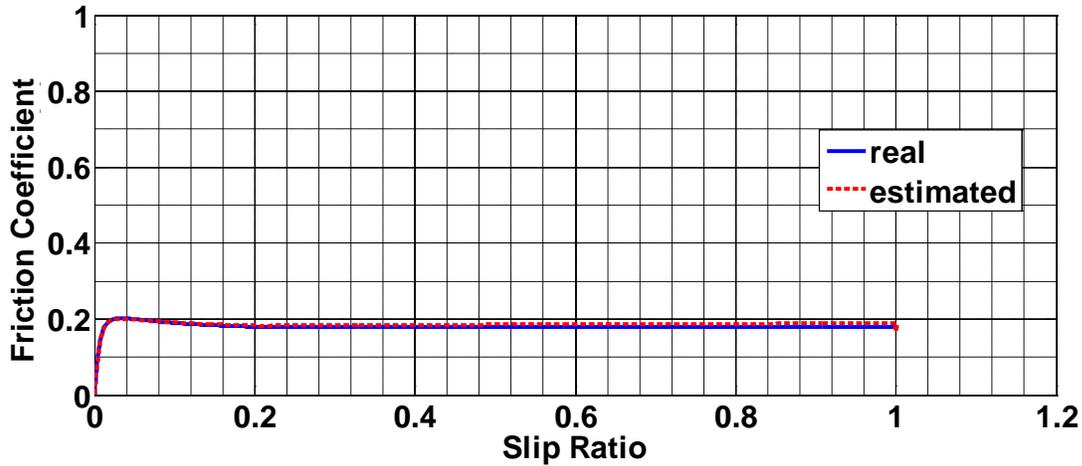


Figure 44 Friction vs. slip ratio estimation – slippery surface (friction coefficient = 0.2).

## FINDINGS AND CONCLUSIONS

Application of the fuzzy system in a real-time slippery spot warning system was demonstrated as a proof of concept. Fuzzy systems require very little storage space and can be easily stored on microchips or vehicles' ECUs. This system can be implemented in the connected vehicle environment to warn drivers of potentially slippery locations.

All the simulated parameters in the preceding section can be measured in real time from ABS sensors, GPS, and accelerometers, which are readily available. Once the friction is estimated, the fuzzy system can be used to predict the crash risk and warn the driver of potential hazards. The benefit of the fuzzy system is that it can summarize these complex relationships into simple rules, which can be easily stored in vehicles' Engine Control Unit (ECU). The schematic of such a system is illustrated in Figure 45. The warning system can be incorporated as a light on the vehicle's dashboard or via steering wheel vibration.

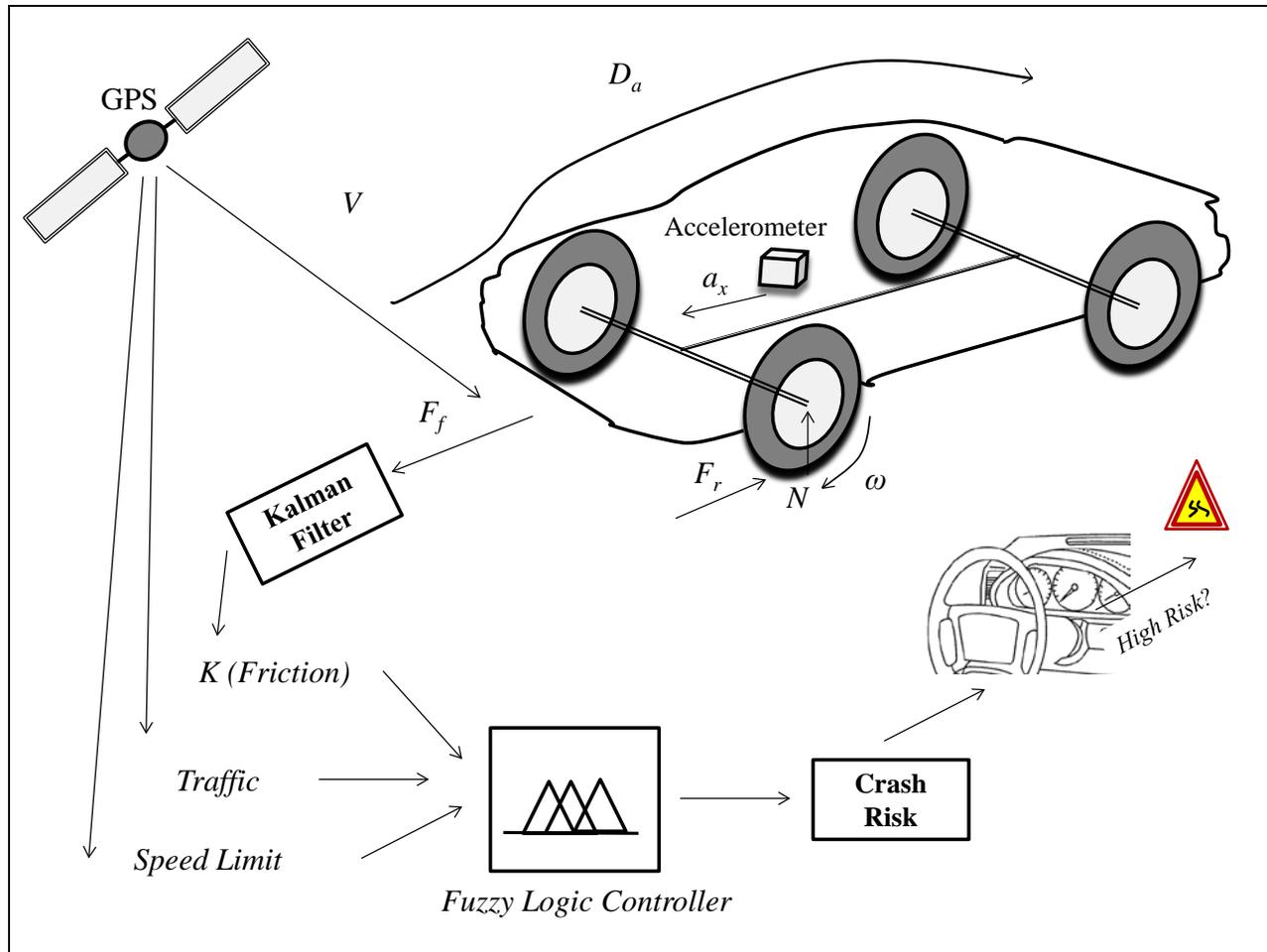


Figure 45 Fuzzy controller real-time slippery road warning system framework.

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## **CHAPTER 6 - OPTIMIZING PAVEMENT SURFACE CHARACTERISTICS THROUGH DIAMOND GRINDING AND GROOVING TECHNIQUE – A CASE STUDY AT THE VIRGINIA SMART ROAD<sup>7</sup>**

### **ABSTRACT**

Providing a smooth, safe, and quiet riding surface is an ultimate goal for pavement engineers. To achieve this goal a balance between high friction level and low roughness and noise level needs to be made. Diamond grinding and grooving is one of the techniques that can be used to improve pavement smoothness while increasing the drivers' safety by improving the frictional properties of the riding surface. This paper evaluates the effect of diamond grinding and grooving on various surface characteristics of concrete pavements. Measurements for texture, friction, and smoothness have been collected on two continuously reinforced concrete pavements at the Virginia Smart Road. One of the sections was diamond grinded and longitudinally grooved while the other section was transversely tinned.

The results of the study show that diamond grinding and grooving increases the surface macrotexture which helps in improving the surface friction. Friction was measured using both smooth tire and ribbed tire locked wheel trailers. Smooth tire measurements confirmed that diamond grinding and grooving increases the friction, however, ribbed tire skid trailer did not show this effect. Several single spot laser profilers and a SURPRO reference profiler were used to measure the surface smoothness before and after grinding and grooving. Longitudinal grooving made the single spot laser profilers incapable of measuring the correct road profile. Power Spectral Density (PSD) analysis revealed that longitudinal grooving introduces artificial wavelengths in the profiles collected by single spot laser profilers. According to the reference profiler results, diamond grinding and grooving improved the concrete surface smoothness.

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<sup>7</sup> This manuscript IJP-P13-02 has been accepted for publication in the International Journal of Pavements and it is in pre-print. Co-authors include: Sameer Shetty, Gerardo Flintsch, and Larry Scofield.

## **INTRODUCTION**

Diamond grooving is a technique that is used in order to improve the frictional properties of the pavement surfaces (Martinez 1997). Most of the developments in diamond grinding and grooving occurred in the state of California in the early 1960s (Scofield 2012). The main purpose of this practice was to restore the skid resistance of old concrete pavements (Scofield 2012). Friction of the pavement surface is an important factor contributing to road safety. Each year many people around the United States (U.S.) lose their lives as a result of car crashes. Due to the importance of friction in reducing the rate of car crashes, the Federal Highway administration (FHWA) has started to implement new policies that require the state Departments of Transportation (DOTs) to implement highway safety programs. Diamond grinding and grooving can be a good option for state DOTs to restore the frictional properties of old concrete pavement in their road network.

Along with friction, roadway smoothness is an important surface characteristic that affects the ride quality, operation cost, and vehicle dynamics. Currently, most state DOTs use laser inertial profilers to measure the road roughness. Measurements are summarized using the International Roughness Index (IRI) which was developed by National Cooperative Highway Research Program (NCHRP) and World Bank. Smoothness measurements can be used to evaluate the ride quality of existing road networks or as a quality check for newly constructed pavements. Due to the importance of ride quality to the road users, highway agencies have implemented smoothness based specification for newly constructed as well as rehabilitated pavements. The smoothness specification identifies an acceptable range of smoothness that the contractor must achieve to obtain full payment. All highway agencies assess penalties if the achieved smoothness is less than specified, while many highway agencies give bonuses to contractors who achieve a smoothness level that is higher than the specified level. Diamond grinding and grooving is one of the methods which can be used to improve the smoothness of both old and new pavement surfaces.

## **OBJECTIVE**

The objective of this paper is to evaluate the effect of diamond grinding and grooving on surface characteristics of concrete pavement. In particular, the paper investigates the changes in macrotexture, friction, and smoothness of a concrete pavement subjected to diamond grinding and longitudinal grooving. Measurements for this study were collected at the Virginia Smart Road during the 2010 and 2011 annual equipment round up (Rodeo 2010 & 2011).

## **BACKGROUND**

One of the main goals of pavement engineers is to provide a smooth, safe and quiet riding surface for road users. In order to achieve this goal, a balance should be made between high level of friction and low level of smoothness and noise. Both, friction and noise are affected by pavement macrotexture. High macrotexture improves road safety by increasing the draining properties of the road surface. It also helps reducing the tire-pavement noise level (Karamihas et al. 2004). Several devices are available for measuring friction. Most state DOTs in the U.S. currently use the locked wheel friction trailer. The trailer can measure the longitudinal friction in fully locked condition (100% slip). Because Most of skidding accidents happen during wet weather condition due to friction deficiencies (Wambold et al. 1986), the device is equipped with a water distribution system that sprays water in front of the tire during the test so it can measure the wet friction.

From the functional point of view, smoothness is an important roadway performance indicator since road users primarily judge the quality of a road based on its roughness and/or ride quality. According to the national highway user survey (1995 and 2000) (Perera et al. 2002), pavement roughness/ride quality was rated as one of the top three principal measures of public satisfaction within a road system. Earlier studies (Karamihas et al. 1999) have shown that rough roads lead to user discomfort, increased travel time due to lower speeds and higher vehicle operating cost. As such, road roughness is now widely recognized as one of the principal measures of pavement performance. Different techniques are available for measuring road smoothness, most of which measure the vertical deviations of the road surface along a longitudinal line of travel in a wheel path, known as a profile (Sayers et al. 1998). Traditionally, the profilograph has been used to measure the smoothness of road pavements. The profile

recorded by the profilograph is analyzed to determine the profile index (PI), which is the smoothness index that is used to judge the ride quality of the pavement. However, several inherent weaknesses were observed in the profilograph and PI for judging the ride quality of a pavement, and hence many state highway agencies have instead adopted the International Roughness Index (IRI) as the ride quality parameter for assessing the smoothness of new/rehabilitated pavements. Inertial profilers are used to obtain profile data to compute the IRI (Shahin et al. 2005).

Diamond grinding and grooving is one of the rehabilitation practices that can be used on old concrete pavements in order to make the surface smoother. The method uses diamond infused steel cutting blades for grinding and grooving concrete pavement. For grinding, the blades are spaced close together so that they can cut the pavement's unevenness (megatexture) and leave a rough pavement surface (high microtexture). For grinding, the blades are further spaced out so they create channels on the pavement surface (high macrotexture). Diamond grooving is mainly used for new concrete pavement to texture the pavement which increases the friction by improving water drainage (Wulf et al. 2008).

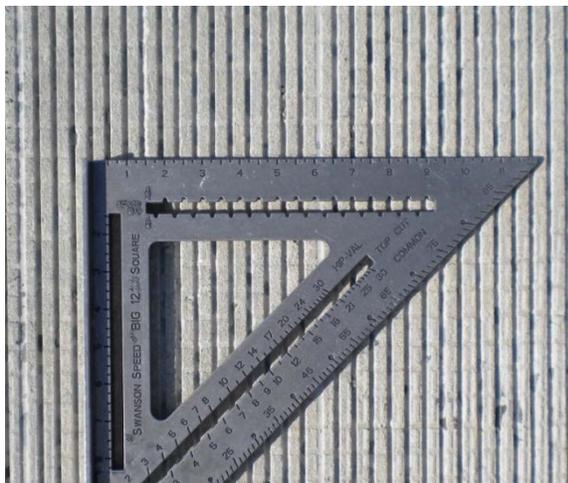
Several studies have recently been performed to investigate the effect of diamond grinding and grooving on the noise level of pavements. Research has shown that longitudinal diamond grinding is one of the quietest types of surface finishing for concrete pavement (Dare et al. 2011). In the U.S. most of the grooving on highways are longitudinal while transverse grooving is more common for runways (Martinez 1977).

## **TEST PROCEDURE**

The data for this study was collected at the Virginia Smart Road during the annual equipment roundup (Rodeo) in two consecutive years; 2010 and 2011. The Virginia Smart Road provides a 3.2 km (2 mi) controlled test track available for transportation research. The road consists of two lanes and it has various types of pavement surfaces. Each year several state DOTs meet at the Virginia Smart Road with the purpose of equipment comparison on the available surfaces. This event is called the annual equipment Rodeo.

The road has three continuously reinforced concrete sections on both east-bound and west-bound directions that are transversely tinned. These sections were originally built and

tinned in 1999, at the time when the Smart Road was constructed. In order to evaluate the effect of diamond grinding and grooving on Portland Cement Concrete (PCC) pavements, one of the sections located along the west-bound direction was ground and longitudinally grooved by International Grooving and Grinding Association (IGGA) in January 2011. The procedure included a Conventional Diamond Ground (CDG) followed by longitudinal grooving. Two different groove spacing were used for each half of the lane; 13 mm ( $\frac{1}{2}$  inch) along the left wheel path and 19 mm ( $\frac{3}{4}$  inch) along the right wheel path (Roberts 2011). Figure 46 illustrates the close up of grooving on the PCC section.



(a) PCC left wheel path, 13 mm ( $\frac{1}{2}$  - inch) groove spacing.



(b) PCC right wheel path, 19 mm ( $\frac{3}{4}$  - inch) groove spacing.

Figure 46 Grooving on PCC section.

To evaluate the effect of diamond grinding and grooving on surface properties, several measurements for texture, friction and smoothness were collected. The various tests used to measure the surface properties are explained below.

### Texture

Texture measurements were obtained using the ASTM E-2157 CTMeter. This static device has a displacement sensor mounted on an arm at a radius of 142 mm (5.6 in) which rotates at a fixed

elevation from the surface. The device reports the Mean Profile Depth (MPD) and Root Mean Square (RMS) according to ASTM E-2157 standard.

In order to determine the effect of diamond grinding and grooving on surface macrotexture, measurements were collected on both tinned and grooved PCC. The tinned PCC section is located along the east-bound lane while the grooved section is located along west-bound lane. All the measurements for both sections were collected in the left wheel path and overall three sets of measurements were obtained for each section. Table 10 shows the macrotexture data for each test section.

Table 10 Macrotexture Measurements Using CT-Meter.

Section type	# of Measurements	Average MPD (mm)
Original tinned PCC	3	0.38
Diamond ground and grooved PCC	3	2.14

From the results of Table 10, it can be seen that diamond grinding and grooving has significantly increased the macrotexture of the PCC pavement (higher MPD). This high macrotexture can improve the skid resistance of the surface by reducing the effect of hydroplaning.

### Friction

Friction measurements were obtained using two locked-wheel skid trailers. One of the locked wheels used the ASTM E-524 smooth test tire while the other used the ASTM E-501 ribbed tire. Five sets of measurements were obtained on both original tinned and grooved PCC at three speeds; 40, 64, and 88 kph (25, 40, and 55 mph). All measurements were collect during Rodeo 2011. Figure 47 shows the layout of the test sections. The summary of the locked wheel measurements is presented in Table 11.

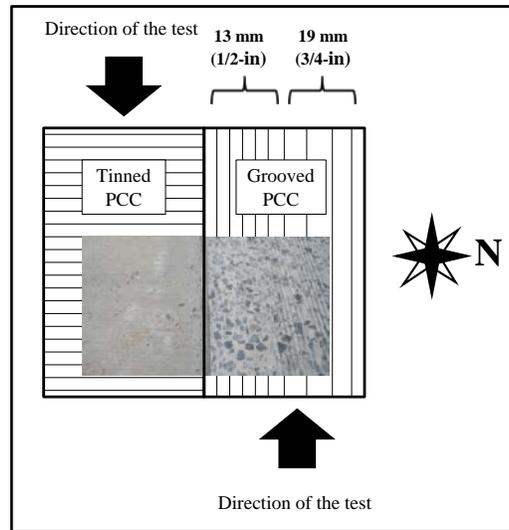


Figure 47 Test sections layout.

Table 11 Summary of locked wheel skid trailer measurements

Unit #	Test tire	Test section	Test speed (kph)	# measurements	Average skid number
1	Smooth	Original Tinned PCC	40	5	51.23
			64	5	36.60
			88	5	28.65
		Ground and Grooved PCC	40	5	58.90
			64	5	56.07
			88	5	44.97
2	Ribbed	Original Tinned PCC	40	5	67.77
			64	5	64.07
			88	5	53.10
		Ground and Grooved PCC	40	5	62.23
			64	5	59.65
			88	5	48.82

To evaluate the frictional properties of the tested surfaces, the correlation between skid number and the test speed was calculated. In a previous study, the authors found a statistically significant linear relationship between skid number and speed of the test vehicle for the range of speeds from 32 to 96 kph (20 to 60 mph) (Flintsch et al. 2010).

Linear correlations were made for all measurements in Figure 48. Several observations can be made. Smooth tires results show a significant increase in the skid numbers of the concrete section subjected to diamond grinding and grooving. This agrees with the higher measured macrotexture achieved on concrete after grinding and grooving. Another interesting observation for smooth tires is the slope of the correlation line between skid number and speed for the sections. This slope is less for ground and grooved PCC than it is for tinned PCC which suggests that friction is less sensitive to the changes of speed for this section. At lower speeds (40 kph) smooth tires measurements for both sections seem to be relatively close. However, at high speeds the difference is much more evident (64 and 88 kph). In general, the effect of hydroplaning is more pronounced at higher speeds; since the grooved section has a greater macrotexture, it is less sensitive to hydroplaning and consequently provides increased friction at high speeds.

Ribbed tires results, on the other hand, do not show a significant difference in the skid values collected on the two test surfaces. The sensitivity of friction to speed is similar for both tinned and ground and grooved test sections (parallel slopes). It is surprising that the ribbed tires skid numbers are slightly higher for tinned PCC than the ground and grooved PCC. This seeming paradox between smooth tire and ribbed tire results may be explained by sensitivity of the test tire to the pavement surface texture and surface condition. Smooth tires are more sensitive to macrotexture while ribbed tires are more sensitive to microtexture. It can therefore be postulated that tinned PCC has a greater microtexture while ground and grooved concrete has a greater macrotexture. Since the difference between ribbed tire measurements for the two types of PCC surfaces is not significant, grooved concrete is a preferred choice for pavement surface as it prevents hydroplaning at high speeds (i.e., it increases macrotexture). The lack of sensitivity of ribbed tires to the effect of macrotexture has been cited by other researches (Wambold et al. 1986). There is evidence that pavement grooving significantly decrease the rate of wet-weather accidents; however, ribbed tires fail to show this effect. For this reason some researchers believe that smooth tires are a better choice for predicting skidding potentials (Wambold et al. 1986).

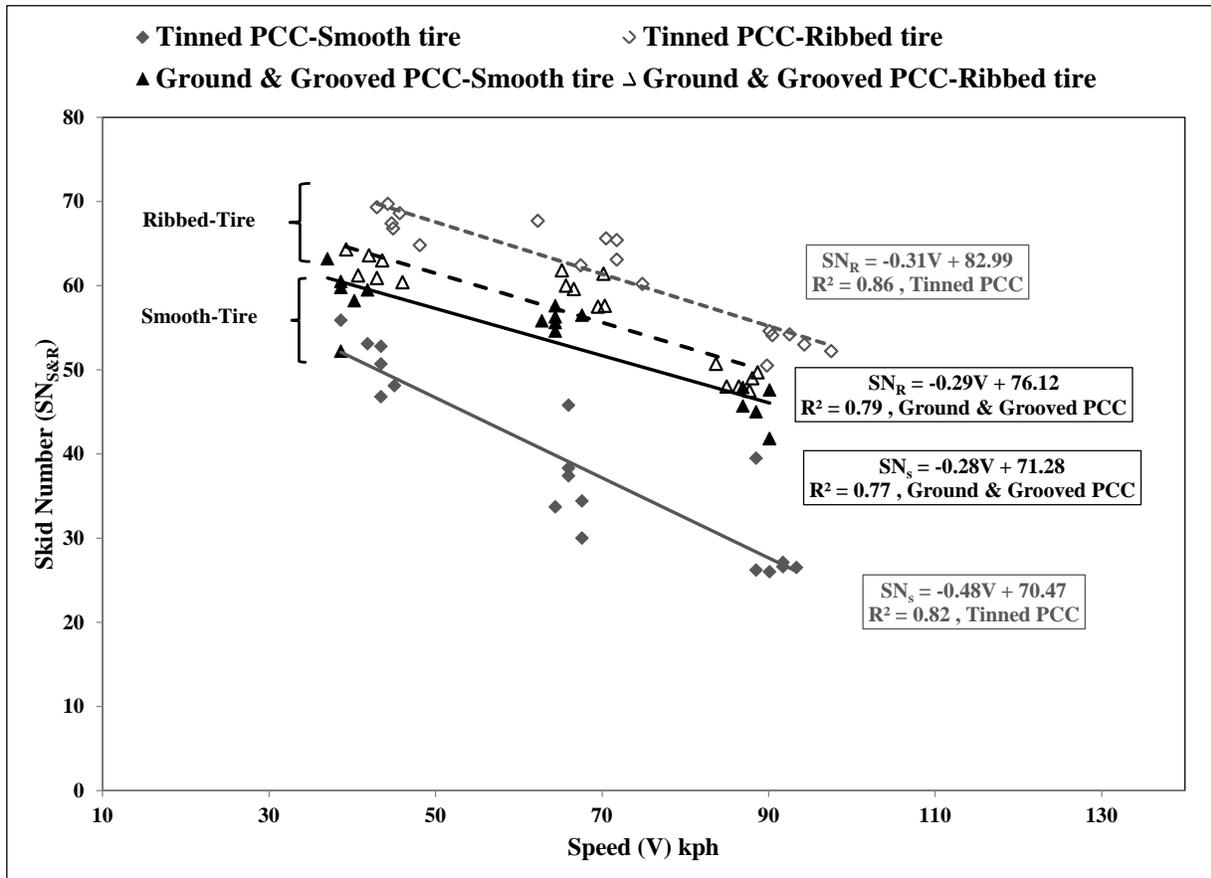


Figure 48 Correlation between skid number and speed.

### Smoothness

For smoothness assessment, longitudinal profile measurements were made before- & after-diamond grinding and longitudinal grooving was performed. The tested section was 161 meters (528 feet) long, and the wheel-path was marked every 3 meters (10 feet) with paint so that the operators could align the profilers when traveling at the required speed off 80 kph (50 mph). The paintings would also help reduce possible wandering away from the wheel-path followed by the profilers (Perera et al. 2006). The left and right wheel paths were marked 87 cm (34.5 inches) from the center line. The test section also had paint-marked lead-in 46 meters (150 feet) apart starting going over a 25 mm (1 inch) high electrical rubber cable cord protector that was placed as an artificial bump to indicate the start of the lead-in section. The bump produces a spike in the profiles measurements which would make it possible to determine the exact location of the test section (Perera et al. 1996).

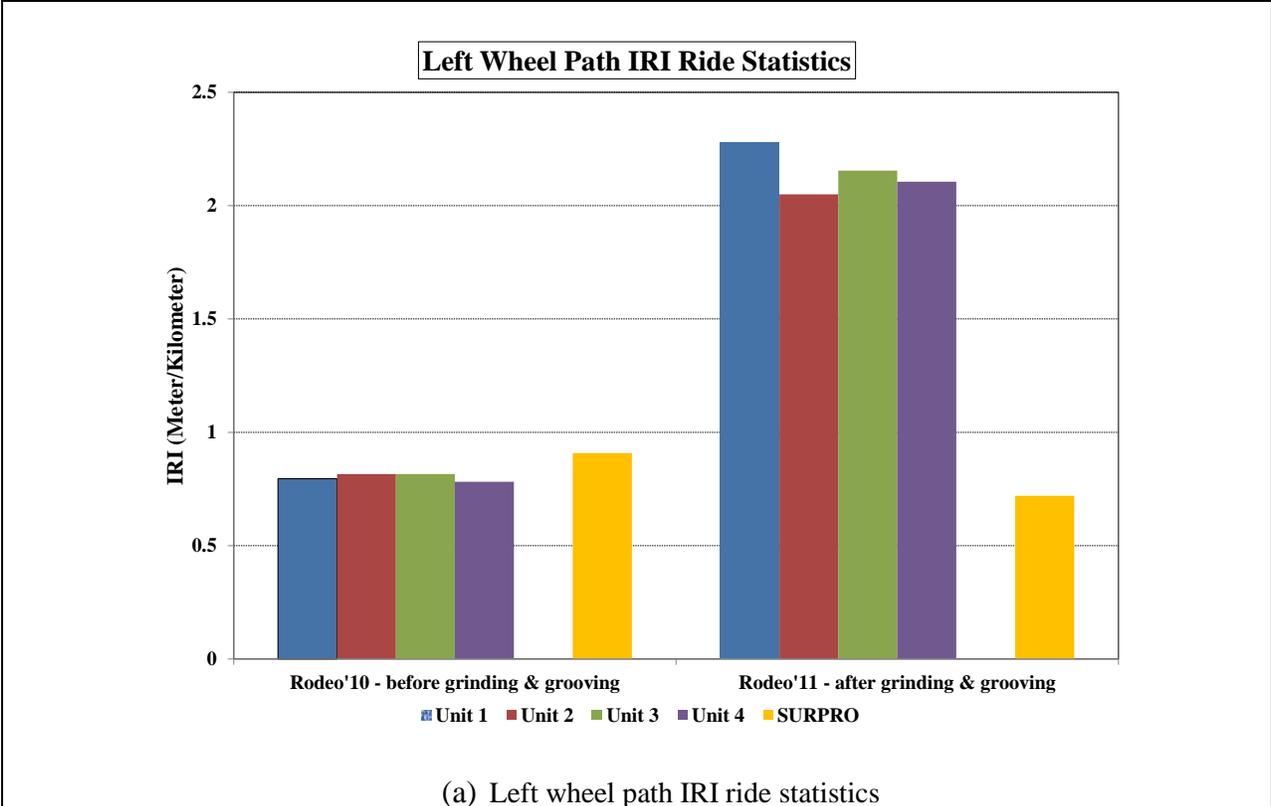
Several high-speed inertial profilers participated in this study and prior to testing, all devices were subjected to block and bounce tests in order to calibrate their height sensors and accelerometers. For reference comparisons, an inclinometer-based ICC SURPRO walking-profiler was used. All the profiles were collected using the procedures mentioned in AASHTO PP-49: "Standards for Certification Inertial Profiling Systems" (Flintsch et al. 2010). Table 12 is a list of the profilers' manufacturers, sensor types and the sampling intervals of all the profilers that participated in study conducted as part of Rodeo in 2010 and 2011 respectively.

Table 12 Summary of the profiler tests.

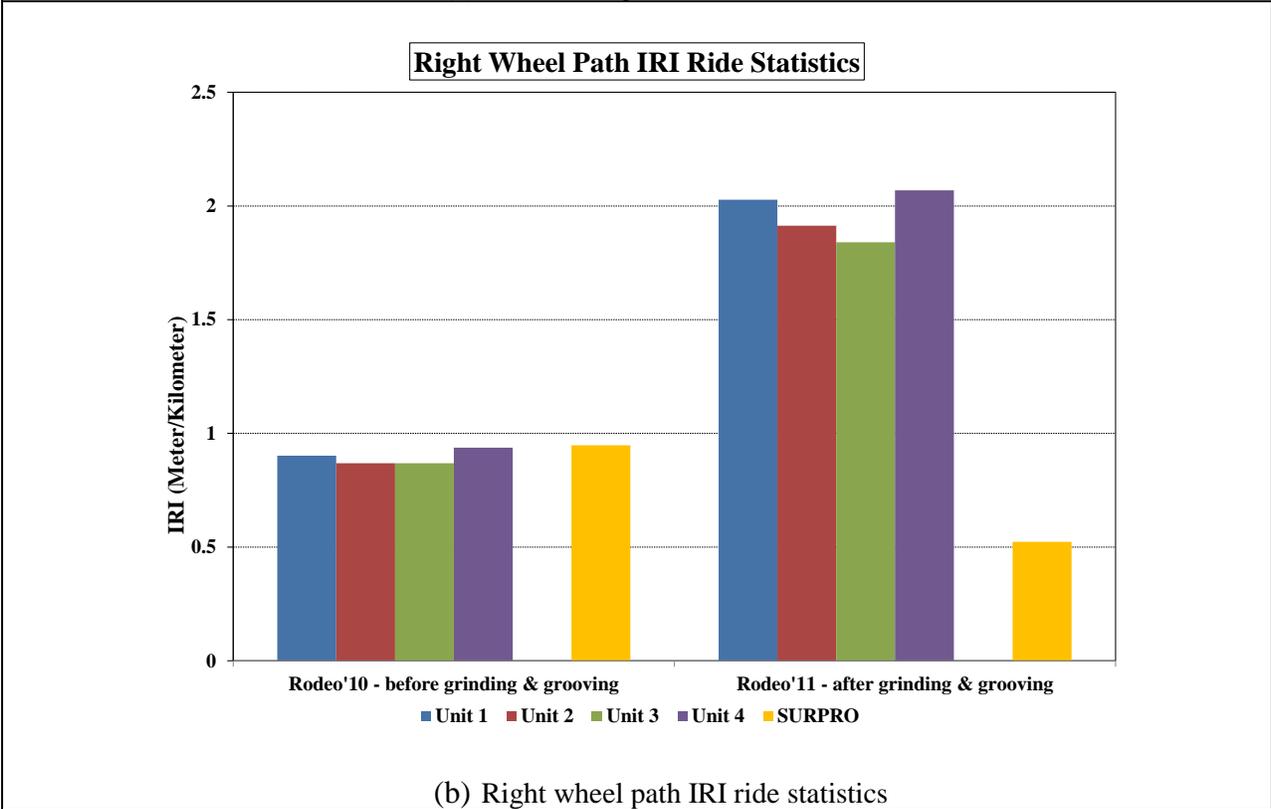
Profiler unit	Manufacturer	Sensor type	Data Recording Interval (mm)	
			Rodeo - 2010	Rodeo - 2011
Unit 1	Dynatest	Single spot laser	25.4	25.4
Unit 2	Dynatest		25.3	25.4
Unit 3	ICC		31.7	30.7
Unit 4	ICC		78.7	77.7
SURPRO	ICC	Inclinometer	25.4	25.4

To evaluate the effect of the diamond grinding and longitudinal grooving on the smoothness of the PCC section, the IRI values of the profiles were computed using ProVAL. All IRI computations used a 250 mm moving average filter. Figure 49 shows the IRI results from four profilers before- and after- diamond grinding and grooving were performed on the PCC section.

As expected, the SURPRO IRI measurements made on a ground and grooved PCC section were found to be less than the transversely tinned PCC section. On the other hand, a significant increase in the average IRI values was observed for profiles collected by single-spot laser profilers on the ground and grooved PCC section. This illustrates the problems often reported with using inertial profilers on longitudinally textured pavement. This is mainly caused by the wander of the inertial profiler as it travels along the road.



(a) Left wheel path IRI ride statistics



(b) Right wheel path IRI ride statistics

Figure 49 IRI ride statistics for PCC before- & after- diamond grinding and grooving.

Figure 50 shows the continuous roughness plots for profile collected by Unit 2 on the left wheel path of ground and grooved PCC section against the corresponding SURPRO profile. The plot shows that there are significant differences in the roughness distribution among the profiles collected by the single spot laser profilers compared to the reference instrument. This difference is caused by the presence of longitudinal grooves on the pavement surface, which causes the height-sensor of the single spot laser profiler unit to obtain measurements at the bottom of the groove as well as on the pavement surface because of lateral wander.

**Error! Reference source not found.** shows that there is very poor agreement between the participant profile and the reference profile at short, medium and long wavebands respectively. Since IRI is most sensitive in the wavelength range of 1 to 30 meter (4 to 100 feet) (Karamihas et al. 1999), the participant profiles produced IRI that were significantly higher than that measured by reference instrument.

The difference in PSD is attributed to the presence of the diamond ground texture and the longitudinal grooves on PCC section which resulted in incorrect recording of the profile data by the single-spot sensors of the participant units which introduced artificial wavelengths in the profile and over-estimating the IRI values higher than the 'true' IRI of the pavement section measured by the reference profiler (Figure 51, Figure 52, and Figure 53).

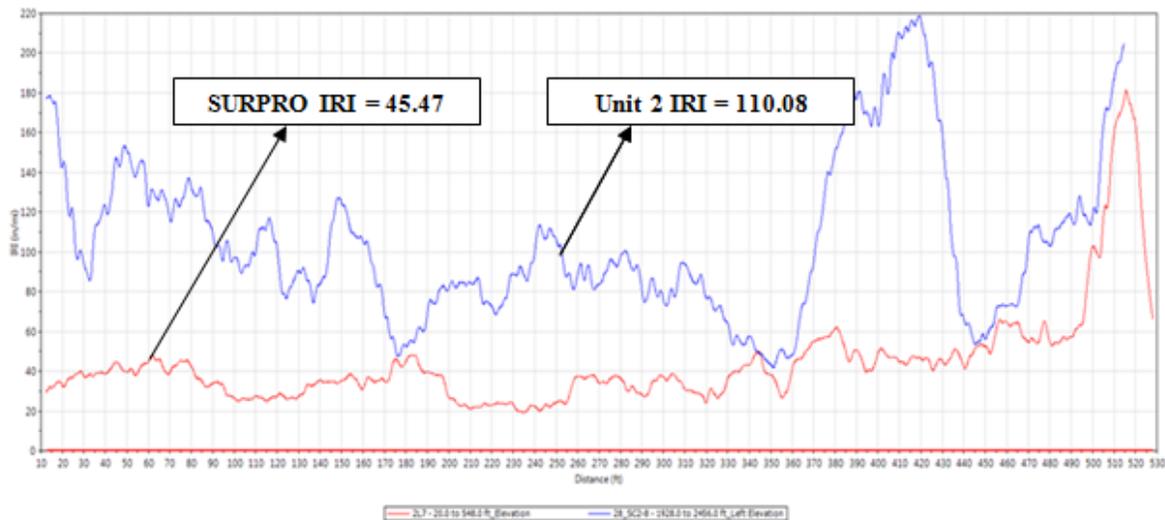


Figure 50 Continuous roughness distribution profile of Unit-2 and SURPRO on ground and grooved PCC section [Base-length = 7.6 meter (25 feet)].

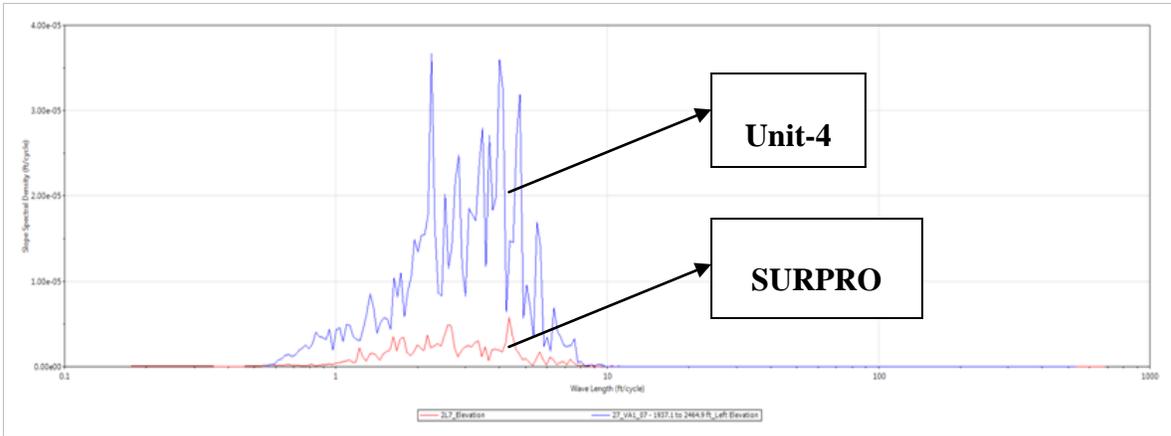


Figure 51 PSD plot for profiles passed through high-pass cut-off wavelength of 1.6 meter (5.25 feet).

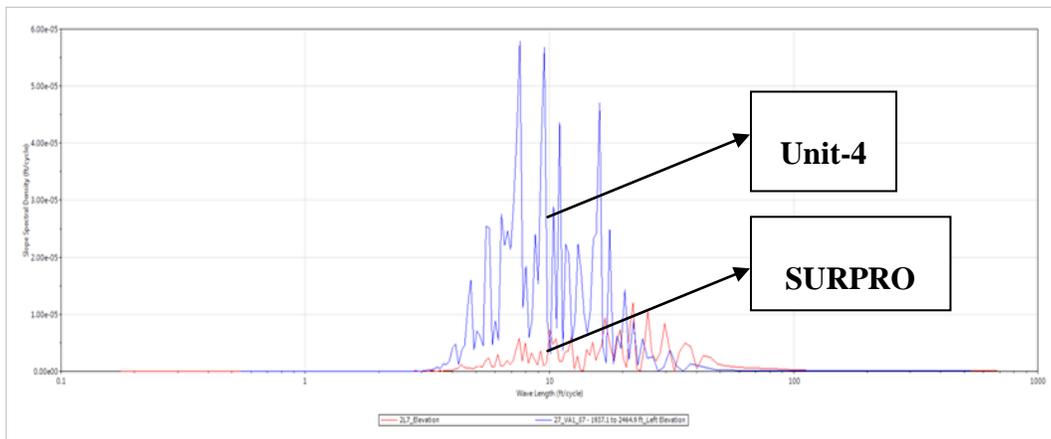


Figure 52 PSD plot for profiles passed through high-pass cut-off wavelength of 8 meter (26.2 feet) and low-pass cut-off wavelength 1.6 meter (5.25 feet).

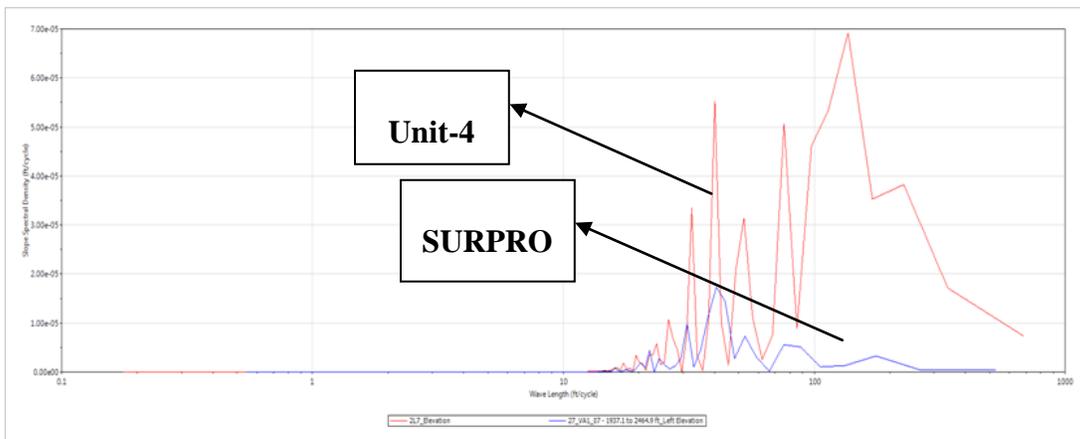


Figure 53 PSD plot for profiles passed through high-pass cut-off wavelength of 40 meter (131.2 feet) and low-pass cut-off wavelength 8 meter (26.2 feet).

## FINDINGS AND CONCLUSIONS

The paper investigated the effect of diamond grinding and grooving on the surface characteristics of PCC. Improvements in macrotexture, friction, and smoothness for a PCC pavement subjected to diamond grinding and grooving was evaluated. Following is the summary of the findings and conclusions of the study:

- Diamond grinding and grooving significantly increased the macrotexture of the PCC surface. High macrotexture can aid in removing water from the pavement surface which can cause hydroplaning and skidding problems during wet-weather condition.
- Friction measurements revealed that friction measured with the smooth tire increased after applying diamond grinding and grooving to the PCC surface. This effect was found to be more significant at higher speeds.
- Ribbed tire skid trailers results did not show a significant difference in friction measurements made on the ground and grooved PCC compared to the tinned PCC. This was expected as ribbed tire measurements are not very sensitive to pavement macrotexture.
- SURPRO reference profiler results showed a decrease in IRI values on the PCC surface after grooving. The improvement in smoothness was substantial on the right wheel path with 19 mm ( $\frac{3}{4}$  inch) grooving compared to the left wheel path with 13 mm ( $\frac{1}{2}$  inch) grooves.
- Compared to the reference profiler, single spot laser profilers over-predicted the IRI values on the ground and grooved PCC. This disagreement is thought to be due to grooves on the section, which render the single-spot profilers incapable of measuring the correct profile. PSD analysis confirmed the presence of artificial wavelengths in the profiles collected by single spot laser profiler which is due to the longitudinal grooving.

The authors recommend using wide-footprint profiling systems in future research on pavement with longitudinal grooves.

## **ACKNOWLEDGEMENTS**

The data for this study was collected during the annual equipment rodeo as part of the Pavement Surface Properties Consortium. The experiment has been made possible thanks to contribution of the Virginia Tech Transportation Institute (VTTI), the Virginia Center for Transportation Innovation and Research, the Federal Highway Administration (FHWA), the Connecticut, Georgia, Mississippi, Pennsylvania, South Carolina, and Virginia DOTs. The authors would like to thank William Hobbs, Stephen Valeri, Chris Tomlinson, and James Bryce for their contribution in data collection and Grinding & Grooving L.D. for their support by grinding and grooving the test sections at no charge to the study.

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## **CHAPTER 7 - SUMMARY, FINDINGS, CONCLUSIONS, AND RECOMMENDATIONS**

It is important for highway agencies to monitor the pavement friction periodically and systematically to support their safety management programs. The collected data can help implement preservation policies that improve the safety of the roadway network and decrease the number of skidding-related crashes. This dissertation evaluates different approaches to model the relationship between vehicle crashes and friction and provides some guidelines on how to use this relationship for managing pavement friction.

The study started with an extensive literature review on tire pavement friction and its relationship to vehicle crashes. It then evaluated the effect of friction on wet and dry crashes using both, traditional regression analysis and soft-computing approaches. The effectiveness of diamond grinding and grooving technique for correcting friction deficiencies is also evaluated. The main finding and conclusions of the study are summarized in this section.

### **FINDINGS**

The results of chapter two show that friction is a significant factor affecting the ratios of both wet- and dry-condition vehicle crashes. Contrary to other studies that only emphasize the effect of friction on wet-condition crashes; this study revealed that friction impacts the rate of dry-condition crashes as well. The normal probability plot of residuals and residual plots for predicted values and regressors suggested, as expected, that the relation between friction and vehicle crashes is not linear and that a logarithmic transformation was necessary for the data. Transformation improved the coefficient of determination (R-square) of the models.

Two alternative soft-computing approaches to traditional regression were used in chapter three and four: Artificial Neural Network and Fuzzy Logic. Both methods are capable of predicting the crash rate based on friction, traffic volume and speed limit. Neural network approach produces the highest precision (lowest MSE) compared to fuzzy logic and regression method. The down side of neural networks is that it acts as a “black-box”. Fuzzy logic on the

other had is easy to understand as it used linguistic rules. Fuzzy logic rules also take less computation spaces compared to neural network and regression and they can be easily stored on microchips and vehicles' ECU. This makes fuzzy logic approach more appropriate for real-time application.

The learning ability of neural network is very sensitive to the learning rate which is defined in the back-propagation algorithm. If the learning rate is set to high, the algorithm may miss the global minimum. On the other hand, if the learning rate is set too high, the algorithm may not converge. To handle the effect of learning rate in the traditional back-propagation algorithm, three alternative learning algorithms were implanted: Levenberg-Marquardt, conjugate gradient, and resilient back-propagation. Levenberg-Marquardt algorithm had highest prediction accuracy (lowest MSE) and the fastest convergence time compared to conjugate gradient and resilient back-propagation learning algorithm and was used to train the neural network model in this study.

The results of ANN analysis show that the rate of wet crashes for sites with friction number below 32 is 40 percent higher than sites with friction higher than networks average (45) while for dry crashes the difference was approximately 15 percent. The effect of friction on reducing the rate of wet crashes is more pronounced than dry crashes.

Fuzzy Logic Interface System provides another reliable tool for PFM decision making process. The system can be easily modified based on agency needs. The model uses linguistic and human like rules and it is easy to understand for practitioners and highway engineers. Crash risk can be predicted based on friction, traffic and speed limit using both Mamdani and Sugeno controllers. Mamdani controller produced a higher precision (lower MSE) than Sugeno. The advantage of Sugeno system is that it can be used with other adaptive learning methods such as backpropagation. Mamdani is using linguistic rules which is easier to use for decision making purposes.

Fuzzy logic model also confirms that the rate of both wet and dry condition crashes increase as the friction increases. Highest wet/dry crash rate was observed for friction number below 30 and speed limit above 42 mph. Authors suggest using both wet and dry condition crashes in PFM studies. Similar to neural network approach, investigatory threshold level of

friction can be defined based on the crash risk. Agency can modify the level based on the available funding. This allows highway agencies to prioritize resources based on safety needs so they can advance the resurfacing project if the site is already in the queue for resurfacing and the crash risk is high. Application of the fuzzy system in real-time slipper spot warning system was demonstrated as a proof of concept. Fuzzy systems take a very small storage space and they can be easily stores on microchips or vehicles' ECU.

Diamond grinding and grooving technique discussed in chapter six, significantly increased the macrotexture of the PCC surface. High macrotexture can aid in removing water from the pavement surface which can cause hydroplaning and skidding problems during wet-weather condition. Friction measurements revealed that friction increased after applying diamond grinding and grooving to the PCC surface, especially when using the smooth tire. This effect was found to be more significant at higher speeds. Ribbed tire skid trailers results did not show a significant difference in friction measurements made on the ground and grooved PCC compared to the tinned PCC. This was expected as ribbed tire measurements are not very sensitive to pavement macrotexture.

## **CONCLUSIONS**

Friction is a significant factor affecting the rate of both wet and dry vehicle crashes. Dry crashes should be considered along with wet crashes in future friction and safety studies. The relationship between friction and crash rates can be used by DOTs and highway agencies to define acceptable levels of friction for various types of roadways in their networks. It also provides them a systemic way to prioritize projects for HSIP funds based on the crash rate.

Both ANN and Fuzzy Logic are valid approaches for developing a PFM. The benefit of Fuzzy Logic over ANN and regression techniques is that it can be used for real-time application. This allows the model to be used in connected vehicle applications. Real-time slippery spot warning system can be developed using the sensors that are already installed in the vehicle. Such a system can warn the drivers of potential hazardous condition so they can adjust their speed based on the available friction; especially in inclement weather condition. The system can also be used in snow and ice removal operation to detect the areas that need plowing or chemical treatment as well as monitoring the contractors plowing operation. Such data can be provided to

the citizens in form of a state-wide map. The routes can be color coded based on the real-time available level of friction. This will allow citizens to select safe routes to commute.

## **RECOMMENDATIONS FOR FUTURE RESEARCH**

Friction data is the heart of PFM. Collecting data with locked-wheel skid trailers can be a very time consuming task. Further research needs to be done on implementing non-contact friction measurement into PFM. Based on the literature review that was done in chapter 1, it seems that vehicle dynamic-based friction estimation can be a good alternative to locked-wheel skid trailers. It can be incorporated into regular fleet vehicles with minimal cost to the agency. The data collection rate is also very high as it does not require water for testing.

More research needs to be done on the real-time slippery spot detection system. The potential of the system in ice and snow removal operation need to be further investigate. Such a system would allow the chemical and brine rate application to be adjusted based on the level of available friction.

Factors such as seasonal variation and temperature changes can affect the friction measurement. This effect needs to be further investigated and incorporated into the PFM program. This will allow the agency to collect friction data throughout the year and make correction based on the temperature/season to make comparison possible.

## APPENDIX A – SAS CODE FOR CRASH ANALYSIS

```
data Project;
```

```
input Dry FN Speed Traffic;
```

```
lines;
```

```
.
```

```
.
```

```
.
```

```
;
```

```
run;
```

```
proc reg data=Project;
```

```
model Dry = FN Speed Traffic /clb clm cli ;
```

```
plot RESIDUAL.*PREDICTED.;
```

```
run;
```

```
proc reg data=Project;
```

```
model Dry = FN Speed Traffic /clb clm cli ;
```

```
plot Dry*FN Dry*Speed Dry*Traffic RESIDUAL.*FN RESIDUAL.*Speed  
RESIDUAL.*Traffic RESIDUAL.*PREDICTED.;
```

```
run;
```

## APPENDIX B – MATLAB NEURAL NETWORK CODE FOR LEVENBERG-MARQUARDT LEARNING ALGORITHM

```
% Solve an Input-Output Fitting problem with a Neural Network

% Script generated by NFTOOL

% Created Sun Jun 14 09:39:52 EDT 2015

%

% This script assumes these variables are defined:

%

%   NDRYINPUT - input data.

%   NDRYOUTPUT - target data.

inputs = NDRYINPUT';

targets = NDRYOUTPUT';

% Create a Fitting Network

hiddenLayerSize = 8;

net = fitnet(hiddenLayerSize);

% Choose Input and Output Pre/Post-Processing Functions

% For a list of all processing functions type: help nprocess

net.inputs{1}.processFcns = {'removeconstantrows', 'mapminmax'};

net.outputs{2}.processFcns = {'removeconstantrows', 'mapminmax'};

% Setup Division of Data for Training, Validation, Testing

% For a list of all data division functions type: help ndivide

net.divideFcn = 'dividerand'; % Divide data randomly
```

```

net.divideMode = 'sample'; % Divide up every sample
net.divideParam.trainRatio = 70/100;
net.divideParam.valRatio = 15/100;
net.divideParam.testRatio = 15/100;

% For help on training function 'trainlm' type: help trainlm
% For a list of all training functions type: help ntrain
net.trainFcn = 'trainlm'; % Levenberg-Marquardt

% Choose a Performance Function
% For a list of all performance functions type: help nnperformance
net.performFcn = 'mse'; % Mean squared error

% Choose Plot Functions
% For a list of all plot functions type: help nnplot
net.plotFcns = {'plotperform', 'plottrainstate', 'ploterrhist', ...
    'plotregression', 'plotfit'};

% Train the Network
[net,tr] = train(net,inputs,targets);

% Test the Network
outputs = net(inputs);
errors = gsubtract(targets,outputs);
performance = perform(net,targets,outputs)

```

```
% Recalculate Training, Validation and Test Performance

trainTargets = targets .* tr.trainMask{1};
valTargets = targets .* tr.valMask{1};
testTargets = targets .* tr.testMask{1};

trainPerformance = perform(net,trainTargets,outputs)
valPerformance = perform(net,valTargets,outputs)
testPerformance = perform(net,testTargets,outputs)

% View the Network

view(net)

% Plots

% Uncomment these lines to enable various plots.

%figure, plotperform(tr)
%figure, plottrainstate(tr)
%figure, plotfit(net,inputs,targets)
%figure, plotregression(targets,outputs)
%figure, ploterrhist(errors)
```

## APPENDIX C – MATLAB NEURAL NETWORK CODE FOR CONJUGATE GRADIENT LEARNING ALGORITHM

```
% Solve an Input-Output Fitting problem with a Neural Network

% Script generated by NFTOOL

% Created Sun Jun 14 09:39:52 EDT 2015

%

% This script assumes these variables are defined:

%

%   NDRYINPUT - input data.

%   NDRYOUTPUT - target data.

inputs = NDRYINPUT';

targets = NDRYOUTPUT';

% Create a Fitting Network

hiddenLayerSize = 8;

net = fitnet(hiddenLayerSize);

% Choose Input and Output Pre/Post-Processing Functions

% For a list of all processing functions type: help nprocess

net.inputs{1}.processFcns = {'removeconstantrows', 'mapminmax'};

net.outputs{2}.processFcns = {'removeconstantrows', 'mapminmax'};

% Setup Division of Data for Training, Validation, Testing

% For a list of all data division functions type: help ndivide

net.divideFcn = 'dividerand'; % Divide data randomly
```

```

net.divideMode = 'sample'; % Divide up every sample
net.divideParam.trainRatio = 70/100;
net.divideParam.valRatio = 15/100;
net.divideParam.testRatio = 15/100;

% For help on training function 'trainscg' type: help trainscg
% For a list of all training functions type: help ntrain
net.trainFcn = 'trainscg'; % Conjugate-Gradient

% Choose a Performance Function
% For a list of all performance functions type: help nnperformance
net.performFcn = 'mse'; % Mean squared error

% Choose Plot Functions
% For a list of all plot functions type: help nnplot
net.plotFcns = {'plotperform', 'plottrainstate', 'ploterrhist', ...
    'plotregression', 'plotfit'};

% Train the Network
[net,tr] = train(net,inputs,targets);

% Test the Network
outputs = net(inputs);
errors = gsubtract(targets,outputs);
performance = perform(net,targets,outputs)

```

```
% Recalculate Training, Validation and Test Performance

trainTargets = targets .* tr.trainMask{1};
valTargets = targets .* tr.valMask{1};
testTargets = targets .* tr.testMask{1};

trainPerformance = perform(net,trainTargets,outputs)
valPerformance = perform(net,valTargets,outputs)
testPerformance = perform(net,testTargets,outputs)

% View the Network

view(net)

% Plots

% Uncomment these lines to enable various plots.

%figure, plotperform(tr)
%figure, plottrainstate(tr)
%figure, plotfit(net,inputs,targets)
%figure, plotregression(targets,outputs)
%figure, ploterrhist(errors)
```

## APPENDIX D – MATLAB NEURAL NETWORK CODE FOR RESILIENT BACK PROPAGATION LEARNING ALGORITHM

```
% Solve an Input-Output Fitting problem with a Neural Network

% Script generated by NFTOOL

% Created Sun Jun 14 09:39:52 EDT 2015

%

% This script assumes these variables are defined:

%

%   NDRYINPUT - input data.

%   NDRYOUTPUT - target data.

inputs = NDRYINPUT';

targets = NDRYOUTPUT';

% Create a Fitting Network

hiddenLayerSize = 8;

net = fitnet(hiddenLayerSize);

% Choose Input and Output Pre/Post-Processing Functions

% For a list of all processing functions type: help nprocess

net.inputs{1}.processFcns = {'removeconstantrows', 'mapminmax'};

net.outputs{2}.processFcns = {'removeconstantrows', 'mapminmax'};

% Setup Division of Data for Training, Validation, Testing

% For a list of all data division functions type: help ndivide

net.divideFcn = 'dividerand'; % Divide data randomly
```

```

net.divideMode = 'sample'; % Divide up every sample
net.divideParam.trainRatio = 70/100;
net.divideParam.valRatio = 15/100;
net.divideParam.testRatio = 15/100;

% For help on training function 'trainrp' type: help trainrp
% For a list of all training functions type: help ntrain
net.trainFcn = 'trainrp'; % Resilient-Back-Propagation

% Choose a Performance Function
% For a list of all performance functions type: help nnperformance
net.performFcn = 'mse'; % Mean squared error

% Choose Plot Functions
% For a list of all plot functions type: help nnplot
net.plotFcns = {'plotperform', 'plottrainstate', 'ploterrhist', ...
    'plotregression', 'plotfit'};

% Train the Network
[net,tr] = train(net,inputs,targets);

% Test the Network
outputs = net(inputs);
errors = gsubtract(targets,outputs);
performance = perform(net,targets,outputs)

```

```
% Recalculate Training, Validation and Test Performance

trainTargets = targets .* tr.trainMask{1};
valTargets = targets .* tr.valMask{1};
testTargets = targets .* tr.testMask{1};

trainPerformance = perform(net,trainTargets,outputs)
valPerformance = perform(net,valTargets,outputs)
testPerformance = perform(net,testTargets,outputs)

% View the Network

view(net)

% Plots

% Uncomment these lines to enable various plots.
%figure, plotperform(tr)
%figure, plottrainstate(tr)
%figure, plotfit(net,inputs,targets)
%figure, plotregression(targets,outputs)
%figure, ploterrhist(errors)
```

## APPENDIX E – MATLAB NEURAL NETWORK CODE FOR DRY CRASH PREDICTION

```
% Solve an Input-Output Fitting problem with a Neural Network
% Script generated by NFTOOL
% Created Sun Jun 14 09:39:52 EDT 2015
%
% This script assumes these variables are defined:
%
%   NDRYINPUT - input data.
%   NDRYOUTPUT - target data.

inputs = NDRYINPUT';
targets = NDRYOUTPUT';

% Create a Fitting Network
hiddenLayerSize = 8;
net = fitnet(hiddenLayerSize);

% Choose Input and Output Pre/Post-Processing Functions
% For a list of all processing functions type: help nprocess
net.inputs{1}.processFcns = {'removeconstantrows', 'mapminmax'};
net.outputs{2}.processFcns = {'removeconstantrows', 'mapminmax'};

% Setup Division of Data for Training, Validation, Testing
% For a list of all data division functions type: help nndivide
```

```

net.divideFcn = 'dividerand'; % Divide data randomly
net.divideMode = 'sample'; % Divide up every sample
net.divideParam.trainRatio = 70/100;
net.divideParam.valRatio = 15/100;
net.divideParam.testRatio = 15/100;

% For help on training function 'trainlm' type: help trainlm
% For a list of all training functions type: help nntrain
net.trainFcn = 'trainlm'; % Levenberg-Marquardt

% Choose a Performance Function
% For a list of all performance functions type: help nnperformance
net.performFcn = 'mse'; % Mean squared error

% Choose Plot Functions
% For a list of all plot functions type: help nnplot
net.plotFcns = {'plotperform', 'plottrainstate', 'ploterrhist', ...
    'plotregression', 'plotfit'};

% Train the Network
[net,tr] = train(net,inputs,targets);

% Test the Network
outputs = net(inputs);
errors = gsubtract(targets,outputs);
performance = perform(net,targets,outputs)

```

```
% Recalculate Training, Validation and Test Performance
trainTargets = targets .* tr.trainMask{1};
valTargets = targets .* tr.valMask{1};
testTargets = targets .* tr.testMask{1};

trainPerformance = perform(net,trainTargets,outputs)
valPerformance = perform(net,valTargets,outputs)
testPerformance = perform(net,testTargets,outputs)

% View the Network
view(net)

% Plots
% Uncomment these lines to enable various plots.
%figure, plotperform(tr)
%figure, plottrainstate(tr)
%figure, plotfit(net,inputs,targets)
%figure, plotregression(targets,outputs)
%figure, ploterrhist(errors)
```

## APPENDIX F – MATLAB NEURAL NETWORK CODE FOR WET CRASH PREDICTION

```
% Solve an Input-Output Fitting problem with a Neural Network

% Script generated by NFTOOL

% Created Sun Jun 14 10:30:52 EDT 2015

%

% This script assumes these variables are defined:

%

%   NWETINPUT - input data.

%   NWETOUTPUT - target data.

inputs = NWETINPUT';

targets = NWETOUTPUT';

% Create a Fitting Network

hiddenLayerSize = 8;

net = fitnet(hiddenLayerSize);

% Choose Input and Output Pre/Post-Processing Functions

% For a list of all processing functions type: help nprocess

net.inputs{1}.processFcns = {'removeconstantrows', 'mapminmax'};

net.outputs{2}.processFcns = {'removeconstantrows', 'mapminmax'};

% Setup Division of Data for Training, Validation, Testing

% For a list of all data division functions type: help nndivide

net.divideFcn = 'dividerand'; % Divide data randomly
```

```

net.divideMode = 'sample'; % Divide up every sample
net.divideParam.trainRatio = 70/100;
net.divideParam.valRatio = 15/100;
net.divideParam.testRatio = 15/100;

% For help on training function 'trainlm' type: help trainlm
% For a list of all training functions type: help ntrain
net.trainFcn = 'trainlm'; % Levenberg-Marquardt

% Choose a Performance Function
% For a list of all performance functions type: help nperformance
net.performFcn = 'mse'; % Mean squared error

% Choose Plot Functions
% For a list of all plot functions type: help nplot
net.plotFcns = {'plotperform', 'plottrainstate', 'ploterrhist', ...
    'plotregression', 'plotfit'};

% Train the Network
[net,tr] = train(net,inputs,targets);

% Test the Network
outputs = net(inputs);
errors = gsubtract(targets,outputs);
performance = perform(net,targets,outputs)

```

```
% Recalculate Training, Validation and Test Performance

trainTargets = targets .* tr.trainMask{1};
valTargets = targets .* tr.valMask{1};
testTargets = targets .* tr.testMask{1};

trainPerformance = perform(net,trainTargets,outputs)
valPerformance = perform(net,valTargets,outputs)
testPerformance = perform(net,testTargets,outputs)

% View the Network

view(net)

% Plots

% Uncomment these lines to enable various plots.

%figure, plotperform(tr)
%figure, plottrainstate(tr)
%figure, plotfit(net,inputs,targets)
%figure, plotregression(targets,outputs)
%figure, ploterrhist(errors)
```

## APPENDIX G – MATLAB CODE FOR MAMDANI FUZZY INFERENCE SYSTEM

```
[System]

Name='Crash_Predictor_September'

Type='mamdani'

Version=2.0

NumInputs=3

NumOutputs=2

NumRules=7

AndMethod='min'

OrMethod='max'

ImpMethod='min'

AggMethod='max'

DefuzzMethod='centroid'

[Input1]

Name='Friction'

Range=[0 100]

NumMFs=5

MF1='Very-Low':'trimf',[10 20 30]

MF2='Low':'trimf',[20 30 40]

MF3='Medium':'trimf',[30 40 50]

MF4='High':'trimf',[40 50 60]

MF5='Very-High':'trimf',[50 60 70]

[Input2]

Name='AADT'
```

Range=[0 20]

NumMFs=3

MF1='Low': 'trimf',[10 12 14]

MF2='Medium': 'trimf',[12 14 16]

MF3='High': 'trimf',[14 16 18.3]

[Input3]

Name='Speed-Limit'

Range=[0 70]

NumMFs=3

MF1='Low': 'trimf',[33.5 38 42.5]

MF2='Medium': 'trimf',[38 42.5 47]

MF3='High': 'trimf',[42.5 47 51.5]

[Output1]

Name='Dry-Condition-Crashes'

Range=[0 1]

NumMFs=5

MF1='Very-Low-Risk': 'trimf',[0 0.075 0.15]

MF2='Low-Risk': 'trimf',[0.05 0.2 0.35]

MF3='Medium-Risk': 'trimf',[0.25 0.4 0.55]

MF4='High-Risk': 'trimf',[0.45 0.6 0.75]

MF5='Very-High-Risk': 'trimf',[0.65 0.8 1]

[Output2]

Name='Wet-Condition-Crashes'

Range=[0 1]

NumMFs=5

MF1='Very-Low': 'trimf',[0 0.075 0.15]

MF2='Low': 'trimf',[0.05 0.2 0.35]

MF3='Medium': 'trimf',[0.25 0.4 0.55]

MF4='High': 'trimf',[0.45 0.6 0.75]

MF5='Very-High': 'trimf',[0.65 0.8 1]

[Rules]

1 2 2, 5 5 (1) : 1

2 2 3, 5 5 (1) : 1

2 2 1, 5 4 (1) : 1

3 3 3, 3 3 (1) : 1

4 3 3, 2 1 (1) : 1

5 1 3, 2 3 (1) : 1

5 2 3, 2 1 (1) : 1

## APPENDIX H – SUGENO FUZZY INFERENCE SYSTEM FOR DRY CRASH PREDICTION

[System]

Name='Nafise\_Dry'

Type='sugeno'

Version=2.0

NumInputs=3

NumOutputs=1

NumRules=45

AndMethod='prod'

OrMethod='probor'

ImpMethod='prod'

AggMethod='sum'

DefuzzMethod='wtaver'

[Input1]

Name='Friction'

Range=[20 64]

NumMFs=5

MF1='inlmf1':'trapmf',[12.3 16.7 23.299988423472 27.69998201196]

MF2='inlmf2':'trapmf',[23.2999913854456 27.6999884234771 34.3000001393631 38.7000017765564]

MF3='inlmf3':'trapmf',[34.299999713892 38.7000001393631 45.3000031421955 49.7000042369533]

MF4='inlmf4':'trapmf',[45.3000044863956 49.7000031421965 56.2999960844553 60.6999971286629]

MF5='inlmf5':'trapmf',[56.2999939031986 60.6999960844557 67.3 71.7]

[Input2]

Name='Speed-Limit'

Range=[11.42079221 18.22254035]

NumMFs=3

MF1='in2mf1':'trapmf',[9.040180361 10.400529989 12.440997521194  
13.8012891780393]

MF2='in2mf2':'trapmf',[12.4410049098752 13.8013471501842 15.8419567211799  
17.2023701298859]

MF3='in2mf3':'trapmf',[15.8419574700658 17.2023063498596 19.242802571  
20.603152199]

[Input3]

Name='input3'

Range=[39.73809524 48.73275862]

NumMFs=3

MF1='in3mf1':'trapmf',[36.589963057 38.388895733 41.0872977751319  
42.8862403427283]

MF2='in3mf2':'trapmf',[41.0872938627281 42.8862304510758 45.5846268839716  
47.3835609463655]

MF3='in3mf3':'trapmf',[45.584623650545 47.3835595599716 50.081958127  
51.880890803]

[Output1]

Name='output'

Range=[0 1]

NumMFs=45

MF1='out1mf1':'linear',[0.00482983408312524 0.00241910201291762  
0.00738186179956265 0.000185762849350971]

MF2='out1mf2':'linear',[0 0 0 0]

MF3='out1mf3':'linear',[0 0 0 0]

MF4='out1mf4':'linear',[0.00429153397174817 0.00231932434127984  
0.00692165551907249 0.000171821505095094]

MF5='outlmf5': 'linear', [0.00774921472988964 0.00547356549175409  
0.0156310511296665 0.000364552331974243]

MF6='outlmf6': 'linear', [0 0 0 0]

MF7='outlmf7': 'linear', [0 0 0 0]

MF8='outlmf8': 'linear', [0 0 0 0]

MF9='outlmf9': 'linear', [0 0 0 0]

MF10='outlmf10': 'linear', [0.0082376476839911 0.00411550487042829  
0.0125847002956306 0.000315275713612044]

MF11='outlmf11': 'linear', [0.00219454867212264 0.00105868258945856  
0.00333234431484177 7.83767382900944e-005]

MF12='outlmf12': 'linear', [0 0 0 0]

MF13='outlmf13': 'linear', [0.0145211014250384 0.00697872443637483  
0.0213204217838228 0.000518523099829214]

MF14='outlmf14': 'linear', [0.00556025858556883 0.00276111206396054  
0.00945121565793634 0.000234670268558178]

MF15='outlmf15': 'linear', [0 0 0 0]

MF16='outlmf16': 'linear', [0 0 0 0]

MF17='outlmf17': 'linear', [0.00100412355738779 0.000443472611202026  
0.00121200632622665 2.66692733163315e-005]

MF18='outlmf18': 'linear', [0 0 0 0]

MF19='outlmf19': 'linear', [0 0 0 0]

MF20='outlmf20': 'linear', [0 0 0 0]

MF21='outlmf21': 'linear', [0 0 0 0]

MF22='outlmf22': 'linear', [0 0 0 0]

MF23='outlmf23': 'linear', [0.00338953082843443 0.00144404394840397  
0.00395874264436442 8.66534953146861e-005]

MF24='outlmf24': 'linear', [0.00222481054798854 0.000794432831736099  
0.00224246153631363 4.76514409483934e-005]

MF25='outlmf25': 'linear', [0 0 0 0]

MF26='outlmf26': 'linear', [0.00251293316833102 0.00107006454056108  
0.00311835875032929 6.87018128780091e-005]

MF27='outlmf27': 'linear', [0.00277898002135836 0.000933419637214528  
0.00271934694409705 5.72906193084864e-005]

MF28='outlmf28': 'linear',[0 0 0 0]

MF29='outlmf29': 'linear',[0 0 0 0]

MF30='outlmf30': 'linear',[0 0 0 0]

MF31='outlmf31': 'linear',[0 0 0 0]

MF32='outlmf32': 'linear',[0.000121176044053968 4.3905333757998e-005  
0.000123359374416825 2.63426182726018e-006]

MF33='outlmf33': 'linear',[0.000921517937405561 0.000370152921882098  
0.0010206527185091 2.18984276634642e-005]

MF34='outlmf34': 'linear',[0 0 0 0]

MF35='outlmf35': 'linear',[0.000186797058895674 6.76815890455568e-005  
0.000190162738090462 4.06080562816683e-006]

MF36='outlmf36': 'linear',[-0.00274233714339715 -0.000705296340087817 -  
0.00185940623250555 -3.55253492177377e-005]

MF37='outlmf37': 'linear',[0 0 0 0]

MF38='outlmf38': 'linear',[0.00304837112329041 0.00054398145590725  
0.00210008521983716 4.76307988014126e-005]

MF39='outlmf39': 'linear',[0 0 0 0]

MF40='outlmf40': 'linear',[0 0 0 0]

MF41='outlmf41': 'linear',[0.00108181007556809 0.000251042480461975  
0.000790849845694004 1.74485496059369e-005]

MF42='outlmf42': 'linear',[-0.000514634485619607 -0.000145195713512136 -  
0.000427242336129284 -8.79050386544379e-006]

MF43='outlmf43': 'linear',[0 0 0 0]

MF44='outlmf44': 'linear',[0 0 0 0]

MF45='outlmf45': 'linear',[-0.000719090641267726 -0.000207233383704046 -  
0.000603144353934947 -1.23919724751366e-005]

[Rules]

1 1 1, 1 (1) : 1

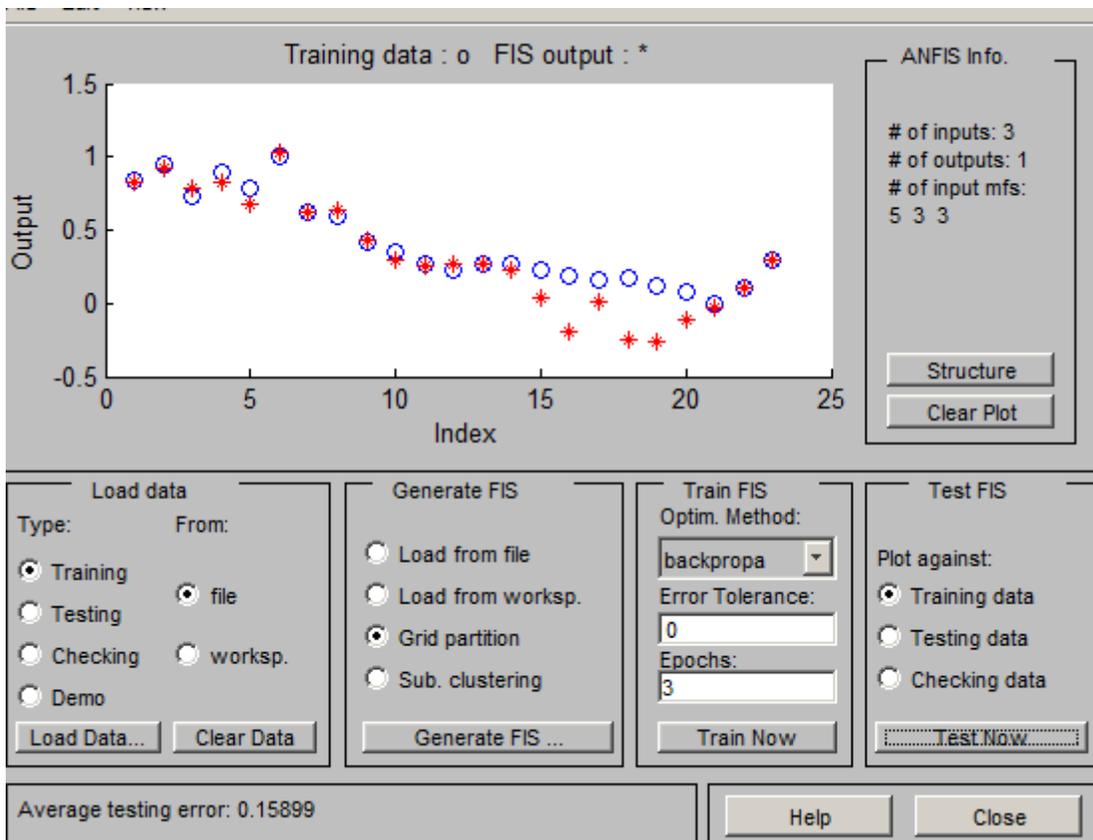
1 1 2, 2 (1) : 1

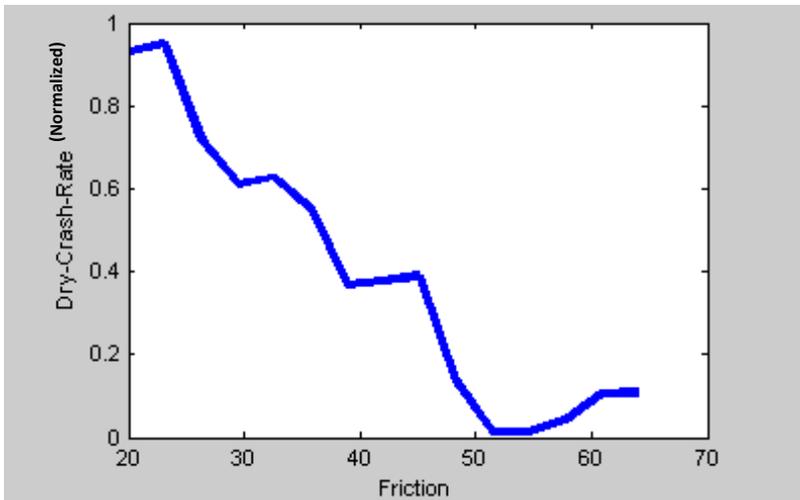
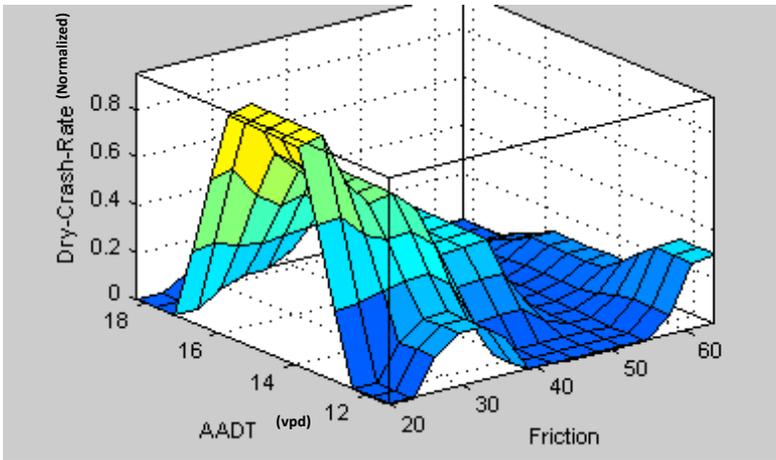
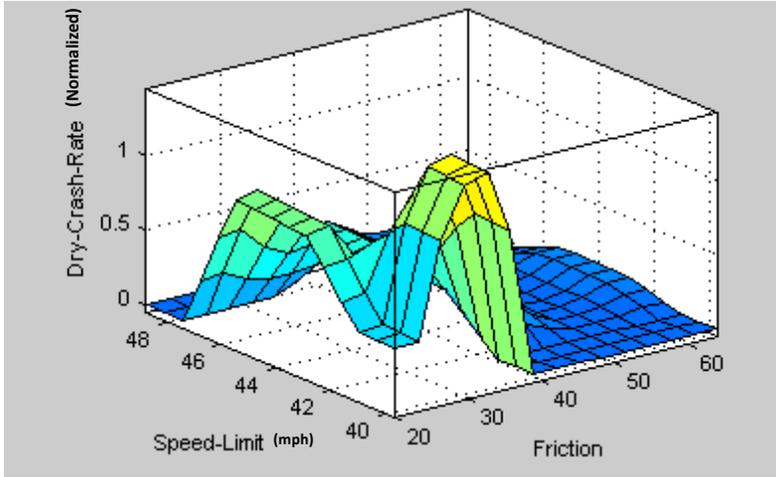
1 1 3, 3 (1) : 1

1 2 1, 4 (1) : 1

1 2 2, 5 (1) : 1  
1 2 3, 6 (1) : 1  
1 3 1, 7 (1) : 1  
1 3 2, 8 (1) : 1  
1 3 3, 9 (1) : 1  
2 1 1, 10 (1) : 1  
2 1 2, 11 (1) : 1  
2 1 3, 12 (1) : 1  
2 2 1, 13 (1) : 1  
2 2 2, 14 (1) : 1  
2 2 3, 15 (1) : 1  
2 3 1, 16 (1) : 1  
2 3 2, 17 (1) : 1  
2 3 3, 18 (1) : 1  
3 1 1, 19 (1) : 1  
3 1 2, 20 (1) : 1  
3 1 3, 21 (1) : 1  
3 2 1, 22 (1) : 1  
3 2 2, 23 (1) : 1  
3 2 3, 24 (1) : 1  
3 3 1, 25 (1) : 1  
3 3 2, 26 (1) : 1  
3 3 3, 27 (1) : 1  
4 1 1, 28 (1) : 1  
4 1 2, 29 (1) : 1  
4 1 3, 30 (1) : 1  
4 2 1, 31 (1) : 1  
4 2 2, 32 (1) : 1

4 2 3, 33 (1) : 1  
 4 3 1, 34 (1) : 1  
 4 3 2, 35 (1) : 1  
 4 3 3, 36 (1) : 1  
 5 1 1, 37 (1) : 1  
 5 1 2, 38 (1) : 1  
 5 1 3, 39 (1) : 1  
 5 2 1, 40 (1) : 1  
 5 2 2, 41 (1) : 1  
 5 2 3, 42 (1) : 1  
 5 3 1, 43 (1) : 1  
 5 3 2, 44 (1) : 1  
 5 3 3, 45 (1) : 1





## APPENDIX I – SUGENO FUZZY INFERENCE SYSTEM FOR WET CRASH PREDICTION

[System]

Name='Nafise\_Wet'

Type='sugeno'

Version=2.0

NumInputs=3

NumOutputs=1

NumRules=45

AndMethod='prod'

OrMethod='probor'

ImpMethod='prod'

AggMethod='sum'

DefuzzMethod='wtaver'

[Input1]

Name='Friction'

Range=[20 64]

NumMFs=5

MF1='inlmf1':'trapmf',[12.3 16.7 23.2999926542859 27.6999887502761]

MF2='inlmf2':'trapmf',[23.299993987022 27.6999926542881 34.2999996917995 38.7000014539204]

MF3='inlmf3':'trapmf',[34.2999990153264 38.6999996917994 45.3000050679573 49.7000074719509]

MF4='inlmf4':'trapmf',[45.3000051116814 49.7000050679593 56.2999941172106 60.6999962171955]

MF5='inlmf5':'trapmf',[56.299990680464 60.6999941172114 67.3 71.7]

[Input2]

Name='Speed-Limit'

Range=[11.42079221 18.22254035]

NumMFs=3

MF1='in2mf1':'trapmf',[9.040180361 10.400529989 12.4409981989535  
13.8012669812085]

MF2='in2mf2':'trapmf',[12.4410141884075 13.8013478279169 15.8419750775997  
17.2024298851188]

MF3='in2mf3':'trapmf',[15.8419735885896 17.2023247073738 19.242802571  
20.603152199]

[Input3]

Name='input3'

Range=[39.73809524 48.67605634]

NumMFs=3

MF1='in3mf1':'trapmf',[36.589963057 38.388895733 41.0873110699916  
42.8862693961987]

MF2='in3mf2':'trapmf',[41.0873000914189 42.8862437460096 45.584626483101  
47.3835603507286]

MF3='in3mf3':'trapmf',[45.5846230049706 47.3835591591014 50.081958127  
51.880890803]

[Output1]

Name='Wet-Crash-Rate'

Range=[0.001799903 1]

NumMFs=45

MF1='out1mf1':'linear',[0.00403585142156673 0.00202142270929338  
0.00616834800633493 0.000155225054675644]

MF2='out1mf2':'linear',[0 0 0 0]

MF3='out1mf3':'linear',[0 0 0 0]

MF4='out1mf4':'linear',[0.00345798277984982 0.00194386775518549  
0.00576956653201852 0.000143083452024022]

MF5='out1mf5': 'linear', [0.00724810793531277 0.00551435616068157  
0.0154717100940833 0.000361109545183596]

MF6='out1mf6': 'linear', [0 0 0 0]

MF7='out1mf7': 'linear', [0 0 0 0]

MF8='out1mf8': 'linear', [0 0 0 0]

MF9='out1mf9': 'linear', [0 0 0 0]

MF10='out1mf10': 'linear', [0.00719069271349823 0.00358716987421002  
0.0109824220126841 0.000274420054754571]

MF11='out1mf11': 'linear', [0.00302350440531358 0.0014585830397467  
0.00459108419144812 0.000107982300189771]

MF12='out1mf12': 'linear', [0 0 0 0]

MF13='out1mf13': 'linear', [0.014526102711803 0.00693713135542547  
0.021248087766914 0.000514558433407573]

MF14='out1mf14': 'linear', [0.0047955312617654 0.00242737540490173  
0.00889256196078528 0.000225664587078229]

MF15='out1mf15': 'linear', [0 0 0 0]

MF16='out1mf16': 'linear', [0 0 0 0]

MF17='out1mf17': 'linear', [0.000981038722402203 0.000429860312852655  
0.0011658452677155 2.56026359544277e-005]

MF18='out1mf18': 'linear', [0 0 0 0]

MF19='out1mf19': 'linear', [0 0 0 0]

MF20='out1mf20': 'linear', [0 0 0 0]

MF21='out1mf21': 'linear', [0 0 0 0]

MF22='out1mf22': 'linear', [0 0 0 0]

MF23='out1mf23': 'linear', [0.00354957461140924 0.00152512508099454  
0.0041584498053195 9.10943688226852e-005]

MF24='out1mf24': 'linear', [0.00207266541538367 0.000734634786084428  
0.00207859812273166 4.40582454067726e-005]

MF25='out1mf25': 'linear', [0 0 0 0]

MF26='out1mf26': 'linear', [0.00253364239779784 0.00112701312133315  
0.00329875546644942 7.32022177485687e-005]

MF27='out1mf27': 'linear', [0.00192058462353626 0.00058939268034942  
0.00179746735894887 3.73230510099656e-005]

MF28='outlmf28': 'linear', [0 0 0 0]

MF29='outlmf29': 'linear', [0 0 0 0]

MF30='outlmf30': 'linear', [0 0 0 0]

MF31='outlmf31': 'linear', [0 0 0 0]

MF32='outlmf32': 'linear', [8.17374198106952e-005 2.96156614562187e-005  
8.32101514207051e-005 1.77690043066729e-006]

MF33='outlmf33': 'linear', [-0.000473899476754339 -7.61244243379448e-005 -  
0.000323836694471694 -6.2133892448134e-006]

MF34='outlmf34': 'linear', [0 0 0 0]

MF35='outlmf35': 'linear', [0.000126012836731792 4.56578335899244e-005  
0.000128283315642819 2.73940949416939e-006]

MF36='outlmf36': 'linear', [-0.00314994497541608 -0.000839999484946351 -  
0.00221130774295487 -4.25222871314913e-005]

MF37='outlmf37': 'linear', [0 0 0 0]

MF38='outlmf38': 'linear', [0.00543718910761521 0.000970265734446074  
0.00374579079139064 8.49560798064877e-005]

MF39='outlmf39': 'linear', [0 0 0 0]

MF40='outlmf40': 'linear', [0 0 0 0]

MF41='outlmf41': 'linear', [1.82751362894918e-005 4.24088816374305e-006  
1.33599132056446e-005 2.94760262733742e-007]

MF42='outlmf42': 'linear', [0.00176443506867425 0.000467236458182481  
0.00142151827202665 2.9372084557417e-005]

MF43='outlmf43': 'linear', [0 0 0 0]

MF44='outlmf44': 'linear', [0 0 0 0]

MF45='outlmf45': 'linear', [1.89857980309647e-005 2.36328141221602e-006  
1.15229308967072e-005 2.49261733181951e-007]

[Rules]

1 1 1, 1 (1) : 1

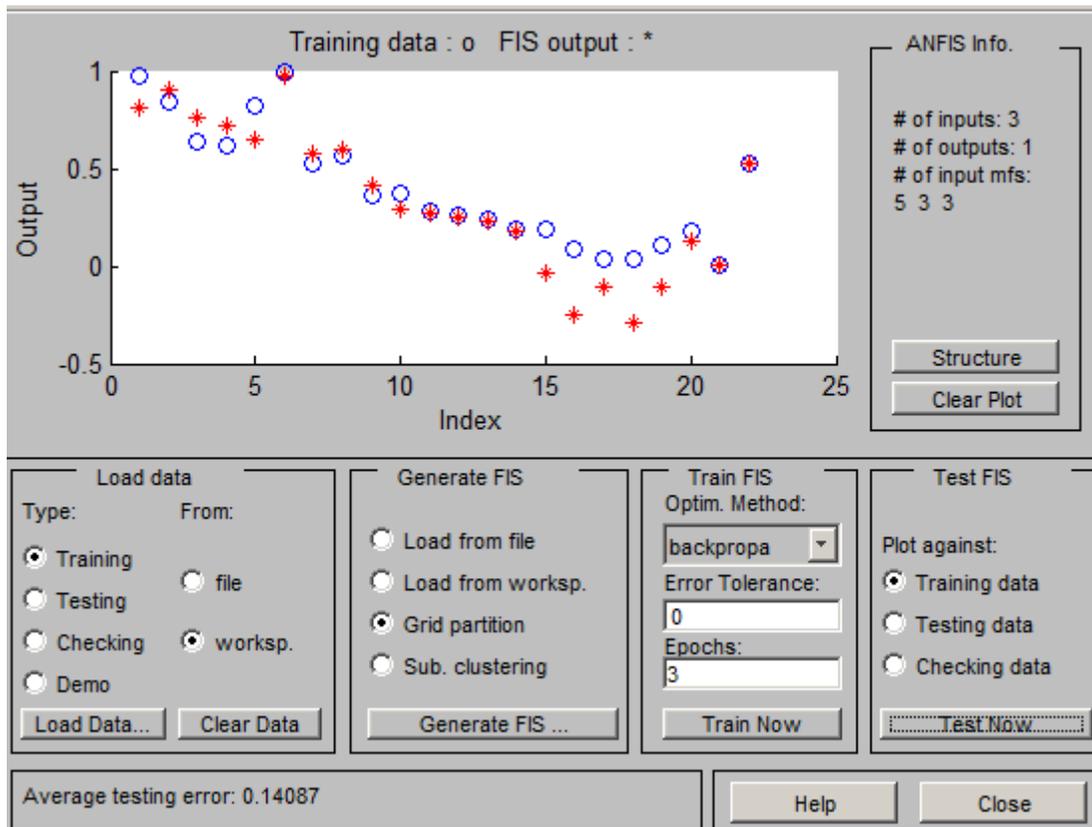
1 1 2, 2 (1) : 1

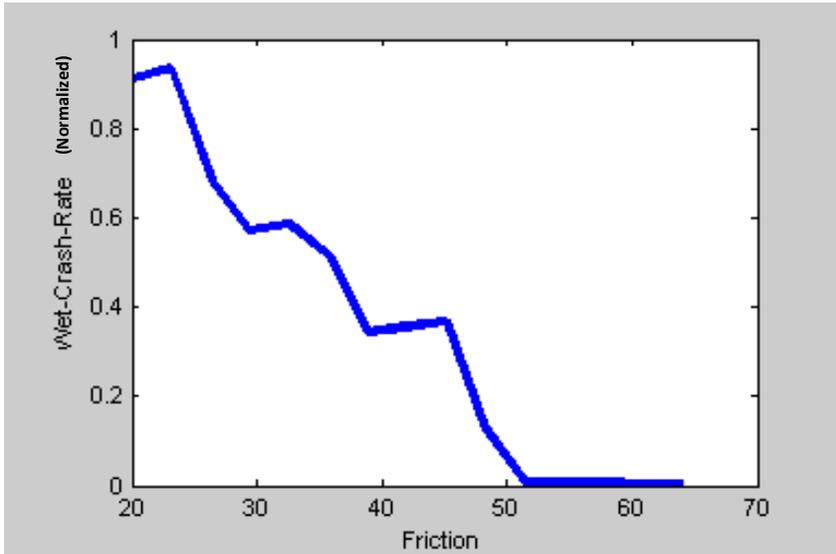
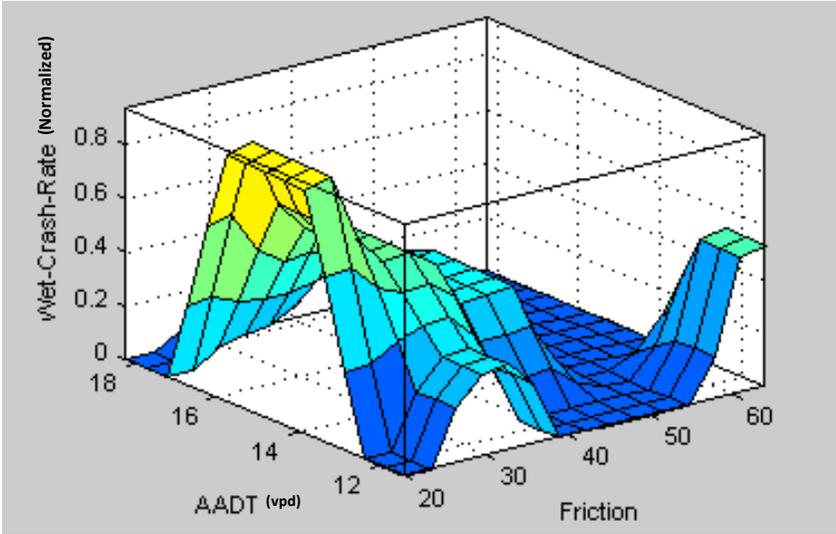
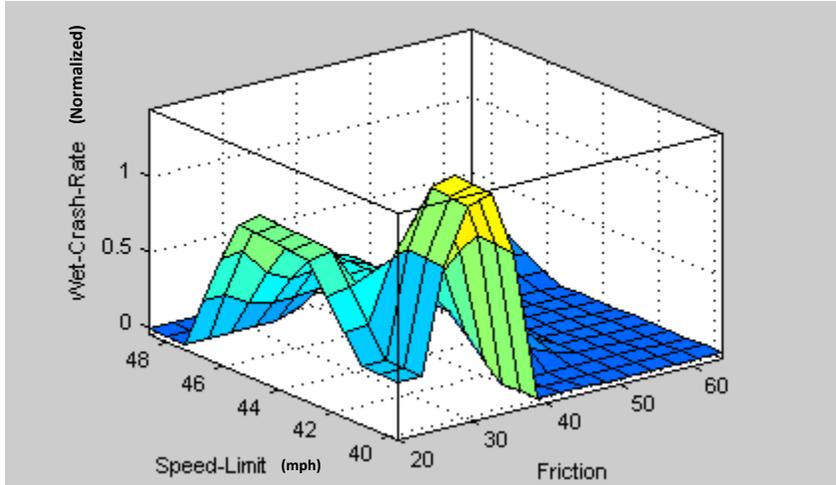
1 1 3, 3 (1) : 1

1 2 1, 4 (1) : 1

1 2 2, 5 (1) : 1  
1 2 3, 6 (1) : 1  
1 3 1, 7 (1) : 1  
1 3 2, 8 (1) : 1  
1 3 3, 9 (1) : 1  
2 1 1, 10 (1) : 1  
2 1 2, 11 (1) : 1  
2 1 3, 12 (1) : 1  
2 2 1, 13 (1) : 1  
2 2 2, 14 (1) : 1  
2 2 3, 15 (1) : 1  
2 3 1, 16 (1) : 1  
2 3 2, 17 (1) : 1  
2 3 3, 18 (1) : 1  
3 1 1, 19 (1) : 1  
3 1 2, 20 (1) : 1  
3 1 3, 21 (1) : 1  
3 2 1, 22 (1) : 1  
3 2 2, 23 (1) : 1  
3 2 3, 24 (1) : 1  
3 3 1, 25 (1) : 1  
3 3 2, 26 (1) : 1  
3 3 3, 27 (1) : 1  
4 1 1, 28 (1) : 1  
4 1 2, 29 (1) : 1  
4 1 3, 30 (1) : 1  
4 2 1, 31 (1) : 1  
4 2 2, 32 (1) : 1

4 2 3, 33 (1) : 1  
 4 3 1, 34 (1) : 1  
 4 3 2, 35 (1) : 1  
 4 3 3, 36 (1) : 1  
 5 1 1, 37 (1) : 1  
 5 1 2, 38 (1) : 1  
 5 1 3, 39 (1) : 1  
 5 2 1, 40 (1) : 1  
 5 2 2, 41 (1) : 1  
 5 2 3, 42 (1) : 1  
 5 3 1, 43 (1) : 1  
 5 3 2, 44 (1) : 1  
 5 3 3, 45 (1) : 1





# APPENDIX J – CARSIM SIMULATION INPUTS

**Vehicle Body**

Sprung mass: Rigid Sprung Mass

Aerodynamics

**Animator Data**

Vehicle animator data: Vehicle Shape

**Systems**

Powertrain: Rear-wheel drive

Brake system: 4-wheel system

Steering system: 4-wheel steer

Misc. keywords and values

3x1 image scale
 

**Front**

Suspension type: Independent

Front kinematics: Independent

Front compliance: Independent

Right-front tire: Tire

Left-front tire: Tire

**Rear**

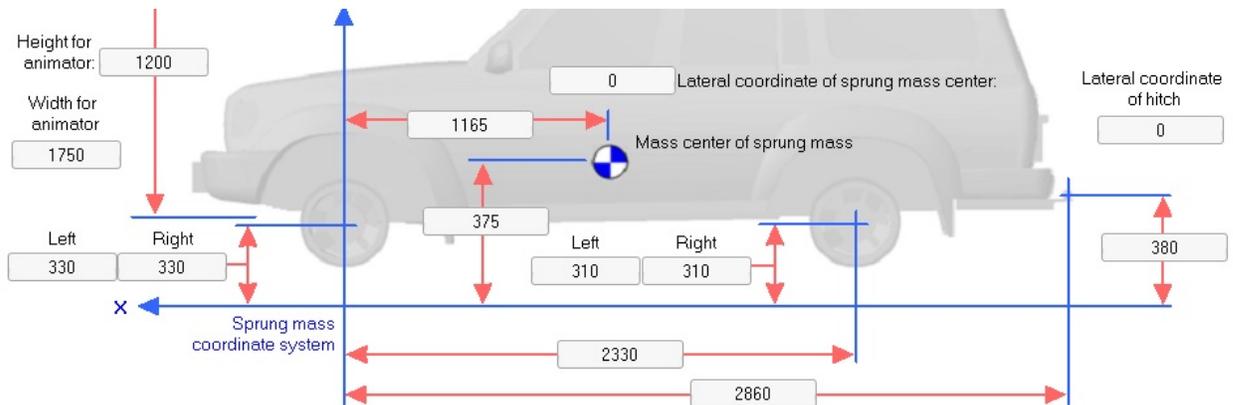
Suspension type: Independent

Rear kinematics: Independent

Rear compliance: Independent

Right-rear tire: Tire

Left-rear tire: Tire



The inertial properties are for the sprung mass in the design configuration, with no additional loading.

Advanced settings (optional license required)

Sprung mass: <input type="text" value="1020"/> kg	<input type="checkbox"/> Edit radii of gyration
Roll inertia (I <sub>xx</sub> ): <input type="text" value="308.6"/> kg-m <sup>2</sup>	R <sub>x</sub> : <input type="text" value="0.550"/> m
Pitch inertia (I <sub>yy</sub> ): <input type="text" value="1020.0"/> kg-m <sup>2</sup>	R <sub>y</sub> : <input type="text" value="1.000"/> m
Yaw inertia (I <sub>zz</sub> ): <input type="text" value="1020.0"/> kg-m <sup>2</sup>	R <sub>z</sub> : <input type="text" value="1.000"/> m
Product (I <sub>xy</sub> ): <input type="text" value="0"/> kg-m <sup>2</sup>	
Product (I <sub>xz</sub> ): <input type="text" value="0"/> kg-m <sup>2</sup>	
Product (I <sub>yz</sub> ): <input type="text" value="0"/> kg-m <sup>2</sup>	

Inertia and radius of gyration are related by the equation:  $I = M \cdot R^2$

### Vertical Force

Use tire force table

Effective rolling radius:  mm

Unloaded (free) radius:  mm

Spring rate:  N/mm

Maximum allowed force:  N

Tire Model Option

### Rolling Resistance Moment

Rr\_c:  -

Rr\_v:  h/km

Include rolling resistance due to Fx

### Shear Forces and Moments

Longitudinal force: Tire: Fx

Lateral force: Tire: Fy

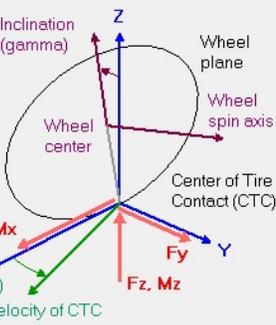
Aligning moment: Tire: Mz

Camber thrust

### Animator Settings

Tire width:  mm

The unloaded radius is also used to scale the animated wheel.

The X, Y, Z axes define the tire/ground coordinate system

Use custom animator shape

Animator: Shape Group

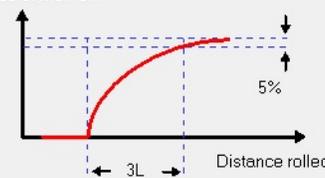
Animator: Sound Set

### Dynamic Properties

Tire and wheel spin moment of inertia (added to the spin inertia of the unsprung mass):  
 kg-m<sup>2</sup>

### Tire Lag

Tire force or moment



L for Fx:  mm

L for Fy and Mz:  mm