Algorithms for Modeling Mass Movements and their Adoption in Social Networks

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Dissertation submitted to the Faculty of the Virginia Polytechnic Institute and State University in partial fulfillment of the requirements for the degree of

Doctor of Philosophy in Computer Science and Applications

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June 2, 2016
Arlington, Virginia

Keywords: Mass Movements, Group Anomalies, Event Detection, Information Propagation, Social Networks

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Online social networks have become a staging ground for many modern movements, with the Arab Spring being the most prominent example. In an effort to understand and predict those movements, social media can be regarded as a valuable social sensor for disclosing underlying behaviors and patterns. To fully understand mass movement information propagation patterns in social networks, several problems need to be considered and addressed. Specifically, modeling mass movements that incorporate multiple spaces, a dynamic network structure, and misinformation propagation, can be exceptionally useful in understanding information propagation in social media.

This dissertation explores four research problems underlying efforts to identify and track the adoption of mass movements in social media. First, how do mass movements become mobilized on Twitter, especially in a specific geographic area? Second, can we detect protest activity in social networks by observing group anomalies in graph? Third, how can we distinguish real movements from rumors or misinformation campaigns? and fourth, how can we infer the indicators of a specific type of protest, say climate related protest?

A fundamental objective of this research has been to conduct a comprehensive study of how mass movement adoption functions in social networks. For example, it may cross multiple spaces, evolve with dynamic network structures, or consist of swift outbreaks or long term slowly evolving transmissions. In many cases, it may also be mixed with misinformation campaigns, either deliberate or in the form of rumors. Each of those issues requires the development of new mathematical models and algorithmic approaches such as those explored here. This work aims to facilitate advances in information propagation, group anomaly detection and misinformation distinction and, ultimately, help improve our understanding of mass movements and their adoption in social networks.
As social media such as Twitter and Facebook gain popularity, they are becoming mainstream venues to stage mass movements, such as protests and uprisings. Modeling such mass movements and studying their adoption patterns gives us insight into understanding events and their precursors. This dissertation targets at general audience and provides a comprehensive study of how mass movement adoption functions in social networks. The goals of the dissertation are to: model mass movements adoption, detect mass movements, distinguish real movements from rumors, and infer precursor to a specific mass movement. Specifically, we make efforts in the following aspects: (1) we address the problem of multiple spaces information dissemination, such as via social networks and outlets; (2) we detect anomalous behavior at different graph resolutions, which in turn allows the identification of event locations and underlying groups; (3) we design strategies that can simulate the ‘doubt’ and ‘believe’ sentiment propagations, and thus could be utilized to facilitate the discrimination of true news from rumors; (4) we analyze climate related protest spikes, and identify linkages between climate change related phenomena and climate protests. The effectiveness of our approach is evaluated using Twitter activity related to civil unrest events in Latin America.
Acknowledgments

Over the past four and half years I have received support and encouragement from a great many individuals.

My deepest debt is to my advisor, Dr. Naren Ramakrishnan. I have been amazingly fortunate to have an advisor who has given me the freedom to explore on my own, while at the same time pulling me back on track when I strayed too far afield. His far-sighted research attitude and the respect he has earned from his peers over the years have made the Discovery Analytics Center he leads a collaborative and productive place. His insight, wisdom and humor have made my graduate study a rich and rewarding journey that I will cherish forever.

I am especially grateful to Dr. Chang-Tien Lu, one of the best teachers that I have ever had. He introduced me to data analytics, opening up a whole new world of research and ideas to me. He has also provided unstinting support and encouragement throughout my search for an academic job.

I would like to thank Dr. Feng Chen, a mentor and a friend, for his support over the past several years as I moved from an idea to a completed study. I am deeply grateful to him for the countless discussions that helped me sort out the technical details of my research.

I appreciate the efforts of Dr. Yang Cao, for his encouragement and practical advice during the work reported in Chapter 5. He has also spared no effort in supporting my job hunt and his belief in me and what I can achieve has lifted my spirits when I became discouraged.

I would like to say thank you to Dr. Chris North for his support, feedback, and many valuable discussions that have helped me understand my research area better. It has always been a pleasure to get to know such a knowledgeable and amiable professor.

I would like to thank Dr. Huzefa Rangwala, who has always been generous with advice and ready to provide help. I hope one day I will become as good an advisor to others as Dr. Rangwala has been to me.

I am especially indebted to all the members of Discovery Analytics Center. Thank you for making our lab group such a warm and joyful family.

I would like to thank my collaborator Edward Dougherty, one of the best collaborators ever. His enthusiasm and efficiency has always inspired me.
Most importantly, I would like to thank my parents for their constant source of strength. I am so grateful to my husband for his care, sacrifice, and love. I hope he knows how much I appreciate the way he has walked alongside me through hardship, challenge and setbacks. His faith that I will succeed has kept me going. Thank you.
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Chapter 1

Introduction

Social microblogs such as Twitter and Weibo are experiencing explosive growth with billions of users around the globe sharing their daily status updates online. For example, Twitter has more than 255 million average monthly active users (78% from mobile) per month as of March 31, 2014, and an estimated growth of 25% per year. In the technology era, online social networks have become a staging ground for modern movements with the Arab Spring being the most prominent example. Interestingly, the role of social networks is not limited to helping organize the activities of disruptive elements. Many key government and news agencies have also begun to embrace Twitter and other social platforms to disseminate information. Without doubt, the analysis of social media networks has become a crucial and irreplaceable task in understanding the social movements.

Social network analysis is the process of gathering data from stakeholder conversations on digital media, and processing into structured insights. These lead to more information-driven decisions, which include but are not limited to understanding social sentiment, discovering topics, identifying ongoing events, and predicting future trends. Social media as a carrier of information, despite its various forms (Facebook, Twitter, Weibo, etc.) shares some common properties in information propagation, that can be approached using the methods of mathematical modeling and data mining.

As social media gains popularity in societies around the world, more and more mass movements are beginning to be organized via social media, with their slogans becoming hashtags in Twitter. In this context, “mass movements” are more akin to social movements supported by large groups of individuals or organizations that focus on specific political or social issues. The research conducted for this dissertation studied mass movement adoption patterns and their related subsequent phenomena from social media.
1.1 Motivation

This dissertation consists of an exploration of four research problems underlying mass movement adoption in social media. In contrast to popular memes, these constitute modeling the process of protest mobilization, detecting graph group anomaly patterns, inferring protest causality, and distinguishing real movements from rumors. (i) How are mass movements mobilized on Twitter, especially those within a specific geographic area? (ii) How can we detect protest activities in social networks by observing group anomalies in graphs? (iii) How can we distinguish real movements from rumors or misinformation campaigns? and (iv) How can we infer the precursors to climate related protests?

Modeling mobilizations: It is well known that network structure plays a key role in information propagation. Several interesting questions arise in this space. Which node is the key player who exerts influence over others? How do we realistically simulate information propagation process within a network? How do specific memes get adopted in the network? When do they translate into mass movements?

Group anomalies in graphs: Group anomalies not only depend on each user’s activity, but are also closely associated with a graph’s structure. In recent year, a significant body of research on group anomaly has focused primarily on two aspects of this problem: (1) modeling users’ behaviors to define group anomalies, paying little or no attention to the underlying network structure; and (2) defining groups at a local scale by imposing distance-based restrictions such as distance, radius, or even node numbers while failing to consider a more global perspective, as nodes located some distance away may still be highly associated. The work reported here looks at global level group anomalies but sets no restrictions on the group definition, considering both the users’ behavior and the underlying graph structure. Investigating this phenomenon of broad group anomalous online behavior holds enormous potential for understanding large-scale, disruptive societal events such as mass movements.

Climate related protests: The occurrence of either a shift in climate, extreme weather, or environmental catastrophe is not sufficient to guarantee that civil unrest will inevitably follow. In general, the causal mechanisms leading to civil unrest are very complex, and there is no easy way to determine a linear pathway to protest. Identifying the pattern involved in the evolution of a climate related protest could provide valuable information regarding the factors involved in a situation escalating from a climate disaster to become an armed protest.

Misinformation campaigns propagation: As millions of users post various messages every second, every one of them is a potential information source, resulting in multiple propagation paths, mixed messages, innuendos, falsehoods, and rumors. How do we track the spread of rumors and misinformation campaigns and can we distinguish them from ‘regular’ or normal propagation patterns? Can we distinguish real movement from rumors or misinformation campaigns?
1.2 Methods

Here we present an overview of the methods used in this dissertation. They will serve as the foundation to the key new information diffusion models proposed in Chapters 3 - 5.

1.2.1 Geometric Brownian Motion

Brownian motion is the random motion of particles suspended in a fluid (a liquid or a gas) resulting from their collision with the quick atoms or molecules in the gas or liquid. This term can also refer to the mathematical model used to describe such random movements, which is often called a particle theory [62].

Geometric Brownian motion is a continuous-time stochastic process in which the logarithm of the randomly varying quantity follows a Brownian motion (also called a Wiener process) with drift. It is an important example of stochastic processes satisfying a stochastic differential equation (SDE); in particular, it is used in mathematical finance to model stock prices (such as the price of a stock over time), subject to random noise.

A stochastic process $S_t$ is said to follow a geometric Brownian motion if it satisfies the following stochastic differential equation:

$$dS_t = \mu S_t dt + \delta S_t dW_t$$

we call $W_t$ as a Wiener process (Brownian motion) and $\mu$ the drift, $\delta$ the volatility.

Consider a Brownian motion trajectory that satisfies the differential equation, $\mu S_t dt$ controls the ‘trend’ of this trajectory and the term $\delta S_t W_t$ controls the ‘random noise’ effect in the trajectory. The analytical solution of this geometric brownian motion is given by

$$S_t = S_0 e^{((\mu - \frac{\delta^2}{2})t + \delta W_t)}$$

According to the GBM properties, $\ln(S_t^{ij})$ is a Gaussian variable given by:

$$\ln(S_t^{ij}) \sim \mathcal{N}((\mu - \frac{\sigma^2}{2})t, \sigma^2 t)$$

1.2.2 Graph Wavelets

Graph wavelets are a form of graphical models bringing three kinds of benefits: (a) they can represent the social network (structure), (b) they perform inference between nodes/edges;
and (c) they can help capture the properties of the social network. We employ graphical models here for spatial information propagation and specifically graph wavelets to study absenteeism. The classic wavelet has been referred to as a mathematical microscope since it is capable of showing signal abnormality with different scales. Wavelets help analyze signals which contain features that vary in time, space, and frequency (scale). Graph wavelets are particularly suited to study complex networks, as they render the graph with good localization properties both in frequency and vertex (i.e. spatial) domains. Their scaling property allows us to zoom in/out of the underlying structure of the graph.

1.2.3 Epidemiological Models

Epidemiological models provide a foundational approach in social network analysis since they elucidate the embedded information diffusion process. These models typically divide the total population into several compartments which reflect the status of an individual. For instance, common compartments denote susceptible (S), exposed (E), infected (I), and recovered (R) individuals. Individuals transit from one compartment to another, with certain probabilities that have to be estimated from data. The simplest model, SI, has two states; susceptible (S) individuals get infected (I) by one of their neighbors and stay infected thereafter. While conceptually easy to understand, it is unrealistic for practical situations. The SIS model is popular in infectious disease modeling wherein individuals can transition back and forth between susceptible (S) and infected (I) states (e.g., think of allergies and the common cold); this model is often used as the baseline model for more sophisticated approaches. The epidemic model SIR was firstly proposed to simulate the disease spreading on population groups in 1927 [51], which enables individuals to recover (R) but is not suited for modeling news cascades on Twitter since there is no intuitive mapping to what ‘recovering’ means. The SEIZ model (susceptible, exposed, infected, skeptic) proposed by Bettencourt et al. [7] takes the interesting approach of introducing an exposed state (E). Individuals in such a state take some time before they begin to believe (I) in a story (i.e., get infected).

1.3 Goals of the Dissertation

The overall aim of this dissertation is to identify modeling approaches and strategies that identify novel information propagate patterns as motivated earlier. We propose four mass movement topics here.

**Topic 1: Mass Protest Adoption in Social Networks** Modeling the movement of information within social media outlets, like Twitter, is key to understanding how ideas spread but quantifying such movement runs into several difficulties. Two specific areas that elude a clear characterization are (i) the intrinsic random nature of individuals to
potentially adopt and subsequently broadcast a Twitter topic, and (ii) the dissemination of information via non-Twitter sources, such as news outlets and word of mouth, and its impact on Twitter propagation. These distinct yet inter-connected areas must be incorporated to generate a comprehensive model of information diffusion. We propose a bispace model to capture propagation in the union of (exclusively) Twitter and non-Twitter environments. To quantify the stochastic nature of Twitter topic propagation, we combine principles of geometric Brownian motion and traditional network graph theory. We apply Poisson process functions to model information diffusion outside of the Twitter mentions network. We discuss techniques to unify the two sub-models to accurately model information dissemination. We demonstrate the novel application of these techniques on real Twitter datasets related to mass protest adoption in social communities.

**Topic 2:Protests Detection from Group Anomalies** Event detection in online social media has primarily focused on identifying abnormal spikes, or bursts, in activity. However, disruptive events such as socio-economic disasters, civil unrest, and even power outages, often result in abnormal troughs involving group absenteeism of activity. We present the first study, to our knowledge, that models absenteeism and uses detected absenteeism as a basis for event detection in location based social networks (LBSN) such as Twitter. Our framework addresses the challenges of (i) early detection of absenteeism, (ii) identifying the point of origin, and (iii) identifying groups or communities underlying the absenteeism. Our approach uses the formalism of graph wavelets to represent the spatiotemporal structure and user activity in a LSBN. This formalism affords multiscale analysis, enabling us to detect anomalous behavior at different graph resolutions, which in turn allows identification of event location and anomalous groups underlying the network. We introduce a systematic two-pass detection method using graph wavelets to detect group absenteeism and then check if there is a subsequent activity spike.

**Topic 3: Distinguishing Real Movements from Rumors** Quantifying information diffusion on social network has been an interesting and unresolved problem for several years now. A better understanding of information diffusion, especially how news and rumors propagate through a network empower us to design strategies that can enhance spreading of news and curbing of rumors. Epidemic models have been used in the past to study information diffusion based on an assumption that rumor/news spreading is no different than the propagation of a contagious disease.

We use an enhanced epidemic model SEIZ that has been specifically designed for information diffusion. The model introduces one more compartment called exposed (E), which refers to the individuals who has been exposed to a story but have still not adopted/rejected it. We use five true news stories and three rumors from varied geographical locations and topics. We also introduce a one-step graph transfer model that can mimic step by step information propagation on Twitter. Our experimental results prove that SEIZ model is far
more accurate in describing information diffusion than the other baseline epidemic models. Further, our one-step graph transfer model imitates information cascades of the stories with a very reasonable error.

**Topic 4: Precursor Inference to Climate Related Protests** To infer climate protest pathways, we need to develop a classifier which is able to separate out climate related protests from others. By analyzing historical climate protest events, we learn that different climate disasters cause related protests with different time spans, depending on the climate disaster influence and frequency. Through constructing knowledge graphs to representing link relationships between entities, we identify protest precursors in Latin American countries, and illustrate the pathways from climate disasters to climate protests.

1.4 **Organization of the Dissertation**

The remainder of the dissertation proposal is organized as follows.

In Chapter 2 we review all of the related work.

In Chapter 3, we address the problem of multiple spaces information dissemination, such as via social networks and outlets such as word of mouth. Specifically, we introduce a trust function to simulate how users are influenced by their friends through direct mention using the ‘@’ symbol. We present how our bispace model can capture propagation in the union of (exclusively) Twitter and non-Twitter environments.

Chapter 4 defines social network movements by an undirected, weighted graph. We detect the group anomaly not only by observing the user activity, but also consider the whole network structure. We propose to use graph wavelet to detect the group anomaly from a global viewpoint. We pay attention to user activity vectors and model their behaviors on graphs and uses detected anomaly as a basis for event detection.

In Chapter 5, we investigate the problem of distinguishing real movements from rumors in social networks. Here we design strategies that can enhance the spreading of news and the curbing of rumors. We present how to simulate the ‘doubt’ and ‘believe’ sentiment propagations. We also introduce a one-step graph transfer model that can mimic step by step information propagation on Twitter. Finally, we test the models using five true news stories and three rumors from varied geographical locations and topics. We also study the problem of misinformation propagation in the era of Ebola. All the experiments are conducted on Ebola-related rumors and all the evaluations are based on real-world data.

Chapter 6 describes how we deal with problem of identifying linkages between climate change related phenomena and climate protests. We build a climate protest classifier which is able to separate out protests directly or indirectly resulting from a major climatic, severe weather, or
environmental event. By analyzing large historical protest reports, we make use of knowledge graphs to represent relationships between entities, and further locate and identify precursors underlying most climate protests.

Chapter 7 presents concluding remarks and illustrates future research directions.
Chapter 2

Related Work

Related work falls in three areas.

2.1 Information Propagation

Social movements: Oliver and Myers [71] develop a foundation for theoretical insights of social movements and describe the limitations of simplified models. The Arab Spring of 2010 served as a context for many researchers [30, 9, 96, 20, 78] to study the role social networking sites play in the spread and recruitment of participants in protests. A detailed anatomy of modern social protests is described by Saad-Filho [78] with the June 2013 anti-government protests in Brazil as a context. In this work, we study the processes and sociological impacts of protests in the modern era, fortified by online social networks and the communities in and around them.

Information diffusion in networks: Previous studies have approached the modeling of information propagation and diffusion in social networks through several means, e.g., contagion models (SIR [15] SISa [38]), diffusion based threshold and cascade models [50], coverage models [88], and survival theory [74]. Other significant work has gone into [17, 54, 75, 104]. Recently, Matsubara etc. [59] conducted research on the rise and fall patterns of information diffusion, and managed to capture the power-law fall pattern and periodicities inherent in such data. Gomez-Rodriguez et al. [29] built a cascade transmission model to track cascading process taking place over a network; they traced overall blogs and news for a one-year period and found that the top 1000 media sites and blogs tend to have a core-periphery structure. A good survey of different models of information diffusion is presented in [31].

External influences: We believe that the effects of influences that originate external to
the observed diffusion network, such as mass media and offline spread of information, can impact the way in which information flows within the online network. Myers et al. [64] study the emergence of URLs on Twitter with a probabilistic generative process using both internal and external exposure curves in a contagion-like model. Similar attention to the role of external factors is paid by Crane and Sornette [21] for tracking the popularity of YouTube videos using a diffusion model. Iwata et al. [43] use a shared cascade Poisson process model to discover latent influences in social activities such as item adoption. Using shared parameters among multiple Poisson processes, they were able to simulate sequences of item adoption events.

**Brownian motion:** Zhou and colleagues (e.g., [110, 32, 111]) develop the notion of Brownian motion on networks which they use to discover communities of hierarchical structure both locally and globally. We extend this approach in this chapter to formulate a propagation algorithm based on geometric Brownian motion (GBM). Borrowed from statistical physics, GBM has been used heavily in finance to model stock price movements. Scale invariance and the ability to model abrupt bumps along propagation paths are the primary motivations for using GBMs to model stochastic processes [93].

Our work builds on the concepts introduced in [32, 43, 110, 111] but differs from the other diffusion models described earlier by considering both the role of communities of users and the abrupt nature of propagation of volatile information such as mass social protests. We include the notion of bispace where both latent (attributed to external influences) and observed user network influences are considered. We infer propagation rates for communities in the observed network and allow implicit recruitment of users into protest actions through a Poisson process.

### 2.2 Event Detection

The relevant methods can be classified into three categories: group anomaly detection, event detection, and graph wavelet.

**Group Anomaly Detection** Anomaly detection in graphs has been well studied using outlier detection methods [3]. When considering group concepts, two directions have been explored [4], namely anomalies in unlabeled/plain graphs [69] and those in attributed graphs. In plain graph anomaly detection, since the only information provided is its structure, features such as distances and communities [91] have been employed to define graph anomalies. In one interesting study [36], additional metrics such as vertices, edges, degree, weight, and connected components are incorporated into the detection framework. In attributed graphs, features regarding node behaviors make it possible to create a richer graphical rep-
presentation, which is usually connected with one or more real-world applications. Other studies, for example [106] define groups based on the term of the role, and model normal groups that follow the same pattern with respect to their role mixture rates. Alternatively, some researchers working on group anomaly detection have built generative models of group anomalies [103] where the goal is to automatically infer the groups and thus detect group anomalies in a social network. Typically these mixed models suffer from high computational complexity, however, due to the size of the data and are as a result heavily parameterized. In this study, we consider both the graph structure and node features in our proposed graph wavelet based approach for group anomaly detection, as this guarantees that the detected group is automatically compact, with polynomial computation complexity and scalability.

**Event Detection** Event detection based on LSBNs is a research area that has attracted significant attention in recent years. Traditional approaches focus on capturing the spatiotemporal burstiness of keywords [55, 56]; Kalman filtering to track the geographical trajectories of hot spots of tweets related to earthquakes [79]; detecting topics of interest that are coherent within specific geographic regions [25, 39, 105]; applying clustering-based approaches to search for emerging clusters of documents or terms using predefined similarity metrics that consider factors such as term co-occurrences and social interactions [1, 81, 98, 99]; and using the notion of compactness of a graph [76] to detect events. Several statistical methods have also been developed, based on Kulldroff’s spatial scan statistic [53], to detect spatial outliers [18] and these have been applied to a wide variety of domains including transportation networks, civil unrest forecasting [108], and heterogeneous social media graphs [19]. The approach we have chosen to address the event detection problem is conceptually different from all the above mentioned studies as it is based on the use of a graph-theoretic framework to detect group anomalies and correlate these to predict future events. Although group absence behavior has been widely studied in the area of organizational behavioral studies [26, 84], it remains largely unexplored in the area of social network analysis. Bearing a close resemblance to group anomaly detection in complex networks, our new detection approach is further distinguished by its focus on groups rather than individuals.

**Graph wavelets** One of the key challenges facing our research is the need to adapt a detection procedure to encompass both missing and bursty activity groups. To address this issue, we incorporate spectral graph wavelets [34] into our algorithm. This strategy has previously been found to be quite effective for multiscale community mining [94]. Wavelet methods based on spectral graph theory have been applied to wide array of data mining tasks such as community detection, anomaly detection [14], and other machine learning tasks [22, 27, 77, 86]. By constructing wavelets over graphs we are able to take advantage of the local information encoded in the graph structure to cluster and identify nodes that are similar to one another in a scale-dependent fashion.
2.3 Rumor Detection

**Epidemiological models** Mathematical modeling of disease spread not only provides vital information about the propagation of the disease in a human network, but also offers insight into the strategies that can be used to control them. The classification of the human population into different groups forms the basic premise of using epidemiological models for modeling information diffusion. The two widely used such models are SIR (Susceptible, Infected, Recovered) and SIS (Susceptible, Infected, Susceptible) models. Newman et al. [66] showed that a large class of standard epidemiological models, viz. the SIR models, can be solved exactly on a wide variety of networks, and confirmed the correctness of solutions with numerical simulations of SIR epidemics on networks. Kimura et al. [52] proposed the application of the SIS model to study information diffusion where the nodes can be activated multiple times. Zhao et al. [109] proposed an SIHR (Spreaders, Ignorants, Hibernators, Removed) rumor spreading model, with forgetting and remembering mechanisms to simulate rumor spreading in inhomogeneous networks. Xiong et al. [102] proposed a diffusion model with four different states: susceptible, contacted, infected, and refractory (SCIR) to identify the threshold value of the spreading rate approaches almost zero. Bettencourt et al. [7] proposed the SEIZ (susceptible, exposed, infected, skeptic) model to capture the adoption of Feynman diagrams by using the publication counts after World War II. They extract the general features for idea spreading and estimate the idea adoption process. Their result showed that the SEIZ model can fit the long term idea adoption process with reasonable error, but does not demonstrate whether this model can be applied on large scale datasets, or whether can be applied on Twitter, where the story unfolds in real-time.

**Rumor modeling** As far as we know, Daley [23] first proposed the similarity between epidemics and rumors using mathematical analysis. Some researchers have studied rumor propagation modeling in different network topologies [65, 107]; however, they do not provide any discussion of propagation differences between news and rumors. Shah et al. [85] detect rumor sources in network using maximum likelihood modeling. In [10], Budak et al. prove that minimizing the spread of the misinformation (i.e., rumors) in social networks is an NP-hard problem and also provide a greedy approximate solution. Castillo et al. [16] delve into twitter content modeling, such as sentiment analysis and hashtags to identify rumors, while Qazvinian et al. [72] try to address this issue using broader linguistic methods, to learn possible features of rumor and determine whether a twitter user believes a rumor or not. More related work appears in [42, 95]. Our goal is to develop an understanding of these processes using diffusion models.
Chapter 3

Spatial Modeling using Geometric Brownian Motion

3.1 Introduction

This chapter was published in the 20th ACM SIGKDD international conference on Knowledge discovery and data mining (KDD 2014) [47].

In recent years social networking sites have provided not just a platform for communication but also a means of mobilization and strategic interaction between key players of social movements, e.g., protests. Traditionally social movements occur within a subset of the population and have spread through on-the-ground communities and unions. With the advent of leaner communication technologies like Twitter, the way such movements form and spread through modern society has changed. With Twitter, in particular, traditional slogans have transformed into hashtags which can offer a consistent way of communicating the reason and motivation of social movements like protests and uprisings.

In this chapter, we focus on Twitter’s user networks during protests and similar civil unrest activities in Latin America. Our goals are to model the propagation and growth of contagion-like protest waves within a social network and to understand the social and structural dynamics underlying such phenomena. The key problem is understanding the nature of information propagation among motivated users of a social network. We have observed that such mass protests emerge very swiftly and sharply. In Twitterspeak, they would be considered trending but most such trends quickly decline on the social network even if not in the physical world. Modeling protest-related topic propagation on networks involves several challenges.

First, social protest propagation through online media can spread over large areas more quickly than traditional methods since users are geographically distributed. For example,
on September 1, 2013, the Mexican government’s education reform bill drew the wrath of teachers country-wide who opposed the reform (which required regular assessments of their performance as educators). Twitter was a virtual loudspeaker, providing a platform for organization and strategization for teachers to put forth their arguments against the bill. A series of mass teacher protests erupted and spread from city to city. As shown in Fig. 3.1, we see the movement spreading over time to different locations with no obvious visual mobilization pattern. The second challenge is that Twitter’s user network embodies many subgraphs based on social ties which might afford different propagation rates due to subgraph-specific structures.

Thus identifying how the cause of a protest is adopted by Twitter users and how mobilization happens in the underlying network is a difficult task. To address this problem we present an integrated framework with new theoretical models as well as empirical validation on real Twitter data for actual protests witnessed in the recent past. Our key contributions are:

- We model the inherent heterogeneity in propagation using a bispace model, comprised of the Twitter mentions network (where both globally and locally influential neighbors contribute to a user’s recruitment) and a latent space (where external exposure to protest-related information is captured).
- We focus on the role of community-driven information propagation over the bispace model. We use geometric Brownian motion (GBM) over the mentions network and...
Poisson processes over the latent space to model information propagation during mass social movements.

- We illustrate the effectiveness of our approach in modeling several key mass protest adoption scenarios in multiple countries of Latin America, viz. Argentina, Brazil, Colombia, Mexico, Uruguay, and Venezuela.

The rest of this chapter is organized as follows. Section 2 covers related work in the areas of social movements, information diffusion in networks, external influences, and Brownian motion. Section 3 proposes the geometric Brownian motion propagation mechanism. Section 4 introduces the bispace propagation model, especially the model of propagation in latent space. In Section 5, we present our dataset and experimental setup, followed by initial experimental findings. Section 6 discusses the evaluation results for our approach followed by a brief discussion in Section 7.

### 3.2 Formalisms

#### 3.2.1 Basics

![Diagram of a network with nodes and edges labeled with numbers.](image)

Figure 3.2: An example mentions network. Nodes denote Twitter users, directed edges denote direction of mentions between users, and edges are labeled with mention frequency.

We model Twitter activity as a network $G(V, E)$ of mentions. Here, each vertex $v \in V$ represents a Twitter user. There is a directed edge from user $v_i$ to user $v_j$ if $v_i$ mentions $v_j$ in a tweet. We define $\omega_{ij}$ to be the number of tweets in which user $v_i$ mentions user $v_j$. Note that $\omega_{ij}$ is not necessarily equal to $\omega_{ji}$. Key players such as celebrities and politicians are more likely to be mentioned by other users, rather than the other way around. As can be seen in Fig. 3.2, the mentions network is a directed graph. Weight $w_{14}$ is the number of
times Twitter user $v_1$ mentions user $v_4$, which is 1, while $w_{41}$ is 6. Note that $w_{21}$ is 5, while $w_{12}$ is 0 (not shown).

We claim, there is an invisible distance between every two nodes within mention network, we call it Brownian distance. We define the neighborhood $N(v_i)$ of a user $v_i$ as the set of all users mentioned by $v_i$, i.e., those for whom there is a directed edge from $v_i$. We define the Brownian distance depends on the mention frequency and number of common direct neighbors. For each user $v_j \in N(v_i)$, the Brownian distance from user $v_i$ to $v_j$ to be

$$d_{ij} = \frac{1}{(\omega_{ij} + 1)(\omega_{ji} + 1)(\eta_{ij} + 1)^\gamma}.$$  \hspace{1cm} (3.1)

Here, $\eta_{ij}$ is the number of common direct neighbors shared by user $v_i$ and user $v_j$ [111]. In Fig. 3.2, node $v_1$ and $v_4$ share two common direct neighbors—$v_3$ and $v_5$—and hence $\eta_{14}$ is 2. Brownian distance is a measurement of the closeness and diffusion possibility of the nodes.

We use the bias coefficient $\gamma \geq 1$ to heuristically weigh mentions that carry more impact. If $v_i$ mentions $v_j$, meaning that $\omega_{ij} > 0$, we believe this expresses $v_i$’s intention to propagate information to $v_j$. Since $v_j$ may not know or care about $v_i$ and consequently may seldom or never mention $v_i$, the return mentions, measured by $\omega_{ji}$, are (up)weighted by $\gamma$. Furthermore, if $v_i$ and $v_j$ share neighbors in the mentions network, the two users may have a closer relationship than other users with no shared mentioned Twitter users, and thus this component is weighted by $\gamma$ as well. A Laplacian-style (+1) correction is used when there are no counter mentions or no mutual mentions. Note that for $\gamma = 1$, $d_{ij}$ is an unbiased Brownian distance since $\omega_{ij}$, $\omega_{ji}$, and $\eta_{ij}$ will have the same weight.

### 3.2.2 Trust Functions and GBM

![Figure 3.3: Trust function. A threshold defines the transition between the pre-trust and trusted period.](image)

Next we introduce the notion of a trust function $S_t$ which we use to model an individual user’s agreement with an idea as expressed in tweets. (The trust function $S_t$ is a function
of the two entities between whom trust is modeled, but in this section we simplify the notation for ease of exposition.) We divide the trust process into a pre-trust period and a trusted period. In the pre-trust period, as a user receives new information, that user’s trust, \( S_t \), increases exponentially until \( S_t \) reaches the trust threshold at time \( T_{th} \) and enters the trusted period. In the trusted period, new information increases \( S_t \) linearly. For simplicity, an individual user cannot revoke trust once this threshold has been crossed. In our Twitter mentions network, a user’s trust in a topic crosses the threshold when they have tweeted about it. During the pre-trust period, we model the trust function as follows (the coefficient \( \mu \) accounts for change in the average value of this stochastic process):

\[
\frac{dS_t}{S_t} = \mu dt
\]  

(3.2)

We then add a Wiener process \( W_t \) to account for stochasticity. According to the properties of a Wiener process [70], \( dW_t \) is essentially Gaussian white noise and contributes to our equation as:

\[
\frac{dS_t}{S_t} = \mu dt + \sigma dW_t
\]  

(3.3)

In this way, we modeled the trust function \( S_t \) as a geometric Brownian motion (GBM) process which is a continuous-time stochastic process [70]. Per convention, we call \( \mu \) the drift and \( \sigma \) the volatility. The drift represents deterministic trends while the volatility refers to the influence of unpredictable events in this model [100]. For simplicity, we consider \( \mu \) and \( \sigma \) to be constant during the pre-trust period in this chapter. (Our concern here primarily is with this period.)

According to Itô’s theorem [70], given the initial value \( S_0 \), the above stochastic differential equation has the following analytic solution:

\[
S_t = S_0 \exp \left( \left( \mu - \frac{\sigma^2}{2} \right) t + \sigma W_t \right)
\]  

(3.4)

The above solution for \( S_t \) is a log-normally distributed random variable with expected value and variance given as [70]:

\[
E(S_t) = S_0 e^{\mu t}
\]  

(3.5)

\[
Var(S_t) = S_0^2 e^{2\mu t} \left( e^{\sigma^2 t} - 1 \right)
\]  

(3.6)

\( S_t \) is a geometric Brownian motion stochastic process, which is typically denoted as \( B(\mu, \sigma) \). In this chapter we use an initial trust of \( S_0 = 1 \) without loss of generality.

### 3.2.3 GBM Propagation

Suppose that user \( v_i \) posts a protest-related tweet at time \( t_0 \) which indicates that \( v_i \) has been recruited or infected. Whether \( v_i \) will infect its neighbor \( v_j \) depends on \( v_j \)’s trust function
with $v_i$. For instance, if $v_j$ is a close friend of $v_i$, then it is more likely that $v_j$ will be infected in a short time because of $v_j$’s trust in $v_i$. But if $v_j$ is not a very close friend of $v_i$, then it might take a long time to build $v_j$’s trust with $v_i$ and to accept $v_i$’s status. Only after $v_j$’s trust with $v_i$ crosses some threshold, $v_j$ gets infected.

For better quantitative analysis, we consider $d_{ij}$ to be the trust threshold. After crossing this threshold, $v_j$ will agree with $v_i$’s opinion. According to the properties of GBMs, the trust function $S_t$ grows continuously over time. This implies that, if some user is infected, all of that user’s neighbors will eventually get infected given enough time for diffusion.

Since we assume a user cannot revoke trust, his or her status will never change once infected. Based on the above assumptions, we now detail our process for GBM propagation through the mentions network; see Algorithm 1. Since GBM is a time-continuous stochastic process, we discretize time using time steps of duration $\delta t$ each. At the start of the simulation, all infected users are considered as newly infected users. Assume that the complete mass protest propagation duration is $T$. Once a user $v_i$ becomes infected, the node is marked as a newly infected user, and the new status begins to affect the statuses of the neighbors, i.e., $N(v_i)$. For each user $v_j \in N(v_i)$, we use $t_{ij} = 0$ to initialize the time instant from which $v_i$ begins to affect $v_j$. After all the time variables $t_{ij}$ of $N(v_i)$ are so initialized, user $v_i$’s status is updated to reflect that $v_i$ is no longer a newly infected user, to avoid duplicate initializations.

Suppose that at current time $t$, $v_j$’s trust with $v_i$ is denoted as $S_{ij}^t$. According to the GBM properties, $\ln(S_{ij}^t)$ is a Gaussian variable given by:

$$\ln(S_{ij}^t) \sim \mathcal{N}((\mu - \frac{\sigma^2}{2})t, \sigma^2 t)$$

(3.7)

If at time $t$, $\ln(S_{ij}^t) \geq d_{ij}$, this means that $v_j$ gets infected since $v_j$’s trust with $v_i$ is bigger than the distance $d_{ij}$. Now $v_j$ begins to affect his or her own neighbors. Instead at time $t$, if $\ln(S_{ij}^t) < d_{ij}$, then at the next time step, $t + \delta t$, the trust is still a Gaussian variable, but with higher expectation and variance:

$$\ln(S_{ij}^{t+\delta t}) \sim \mathcal{N}((\mu - \frac{\sigma^2}{2})(t + \delta t), \sigma^2(t + \delta t))$$

(3.8)

### 3.2.4 GBM Parameter Estimation

We use past protest events in which Twitter played a significant role in propagation to train our GBM model parameters. For each user who gets infected we record their Brownian distance and infection time. Suppose $v_j$ gets infected by $v_i$ after time $t_{ij}$; then as per our propagation model, we claim that $v_j$’s trust function $S_{ij}^t$ with $v_i$ holds:

$$\ln(S_{ij}^t) \geq d_{ij}$$

(3.9)

where $d_{ij}$ is the Brownian distance from $v_i$ to $v_j$. For the convenience of parameter estimation, we can assume that $\ln(S_{ij}^t) = d_{ij}$. It then follows that $d_{ij}$ is a normally distributed random
variable which can be expressed as:

\[ d_{ij} \sim N((\mu - \frac{\sigma^2}{2})t_{ij}, \sigma^2 t_{ij}) \] (3.10)

Because during the parameter estimation process, for each infected user \( v_j \), we are not interested in exactly which user gets \( v_j \) infected, we use \( x_j = d_{ij} \), and \( \tau_j = t_{ij} \) in the following part of this section for simplicity. The set of \( n \) users that are infected during the infection process have independent infection rates, and we get the following likelihood function:

\[
L(\theta, \sigma^2 | v_1, \ldots, v_n) = \prod_{j=1}^{n} \frac{1}{\sigma \sqrt{2\pi \tau_j}} \exp\left(-\frac{(x_j - (\mu - \frac{\sigma^2}{2})\tau_j)^2}{2\sigma^2 \tau_j}\right)
\]

The optimal estimators can be obtained by maximizing the above likelihood function. We differentiate the natural logarithm of the likelihood function above in terms of \( \mu \) and \( \sigma \), and set them to zeros. By solving the two equations simultaneously, we obtain the optimal estimators \( \hat{\mu} \) and \( \hat{\sigma}^2 \).

### 3.3 Bispace Propagation Model

![Figure 3.4: Bispace propagation model. In the latent space, users infections are explained by a Poisson model, and the red nodes denote the infected users from one time step to another. In the mentions network space, users are infected according to the GBM model. Here, the purple nodes (a, b, c, d, e) denote user infections explained by the GBM model.](image)

Many information diffusion models assume that propagation occurs over a single domain. However, it is hard to build a complete, exhaustive network of interactions. For instance, consider building a network based only on which Twitter users follow which other users. This network will miss interactions such as retweets and mentions and the effect of influences originating outside of Twitter. Therefore, considering only a single space will make it difficult to account for all possible factors that influence the spread of information. In this study, we propose a bispace diffusion model that accounts for two domains of diffusion: the observed
Figure 3.5: Major communities of teacher protest events (Sept 1 to Sept 12, 2013, Mexico).

social network and the latent space, as can be seen in Fig. 3.4. In our case, the observed user space is the Twitter mentions network, whereas the latent space refers to any interactions outside of this network. To account for varying diffusion dynamics, each space is intended to have its own propagation model. As described earlier, we model propagation through the Twitter mentions network as Geometric Brownian motion. We use the Poisson distribution to describe information propagation in the latent space.

3.3.1 GBM with Communities

Within networks, a community refers to the appearance of densely connected groups of vertices, with sparse connections between each group [68]. Instead of treating the whole network as a single propagation space, we use network structure to further split the network into communities. For our mentions network we use the Louvain method [8] for community detection to split the network into groups of users. For each community of users we can calculate classical graph features such as average degree, diameter, density, and clustering coefficient with which we can characterize them. In Fig. 3.6 we plot several features for each of the 8 communities found in the case study of Mexican teachers protest of 2013. Diameter $r = \max dist(v_i, v_j)$ is the length (in number of edges) of the longest geodesic path between any nodes $v_i$ and $v_j$ [67]. The clustering coefficient $c_i$ is the proportion of node $v_i$’s neighbors that are connected. Graph density is defined as $\frac{2|E|}{|V||(V|-1)}$ where $E$ is the number of edges.
and \( V \) is the number of nodes [83]. As shown in Fig. 3.6, diameter and graph density vary considerably.

With the observed network further split into several communities, each community is intended to have its own model parameters for GBM. In GBM, \( \ln(S_{ij}^t) \) is a Gaussian distribution \( \mathcal{N}((\mu - \sigma^2/2)t, \sigma^2 t) \). We assume that each user within a community shares the same \( \mu \) and \( \sigma \) so that each community has its characteristic \( \mu \) and \( \sigma \). As information propagates through the mentions network, it may pass through different communities. For an infected user \( v_i \) and one of the non-infected neighbors \( v_j \in N(v_i) \), we assume the following propagation strategy:

1. If \( v_i \) and \( v_j \) are in the same community \( c_i \), the propagation process will follow \( B_{c_i}(\mu_{c_i}, \sigma_{c_i}^2) \).
2. Propagation from one community to another happens as per the source community’s model parameters. For instance, for propagation from community \( c_i \) to community \( c_j \), we will use the source community \( c_i \)’s GBM parameters.
Table 3.1: Mass protests studied in this chapter.

<table>
<thead>
<tr>
<th>No.</th>
<th>Event</th>
<th>Hashtags</th>
<th>Country</th>
<th>Affected cities</th>
<th>Event date(s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.</td>
<td>Anti-government protests against tax reform and other policies pursued by President Juan Manuel Santos</td>
<td>#CacerolazoPaSantos, #5D</td>
<td>Colombia</td>
<td>Nationwide</td>
<td>2012-12-05</td>
</tr>
<tr>
<td>3.</td>
<td>Education reform protests by teachers</td>
<td>#ReformaEducativa</td>
<td>Mexico</td>
<td>Nationwide</td>
<td>2013-09-01</td>
</tr>
<tr>
<td>4.</td>
<td>Social protests against violence and crime</td>
<td>#UruguayosIndignados, #HartosDeLaViolencia</td>
<td>Uruguay</td>
<td>Montevideo</td>
<td>2012-05-14</td>
</tr>
<tr>
<td>5.</td>
<td>Protests against the “media law”</td>
<td>#LorenzettiNoMeFallos, #Medios-Buitres</td>
<td>Argentina</td>
<td>Buenos Aires</td>
<td>2012-11-27</td>
</tr>
<tr>
<td>6.</td>
<td>Protests against Senate President Renan Calheiros’s election</td>
<td>#STFjulgaoRenan, #SocorroJoaquim, #ForaRenan</td>
<td>Brazil</td>
<td>Nationwide</td>
<td>2013-02-22 to 2013-02-26</td>
</tr>
<tr>
<td>7.</td>
<td>Anti-government student protests against abuse of public media for election campaign</td>
<td>#ConatelCareTabla</td>
<td>Venezuela</td>
<td>Caracas</td>
<td>2013-03-20</td>
</tr>
</tbody>
</table>

- After information propagates into a different community, it will spread according to the new community’s parameters. Once the information has entered community $c_j$ from community $c_i$, subsequent infections henceforth will use community $c_j$’s parameters.

At each time step we use the $\mu$ and $\sigma$ of any given node’s current community for propagation from that node.

### 3.3.2 Propagation in Latent Space

As mentioned before, in the latent space, we are modeling unobserved interactions of users. Since there are so many factors that might affect the dissemination of information, such as news outlets, word-of-mouth, it is reasonable to assume that the probability of the number of newly infected users in a given time interval satisfies the Poisson distribution [33] in the latent space.

For each node in the mentions network, it can only be infected by the GBM process. However, for those isolated users outside the mentions network, it is only possible that they get infected via the mechanics of the Poisson process. (Recall that in the GBM process, users get infected primarily via their neighbors.) We use $X$ to represent the number of infected users with time interval $\delta t$ and so the probability of the infected users is given by:

$$\Pr(X = k) = \frac{\lambda^k e^{-\lambda}}{k!}$$  \hspace{1cm} (3.11)

To obtain an estimator of $\lambda$, we can only use information about Twitter users who are outside the mentions network as our training dataset. We count the infected users outside the mentions network with time interval of 15 minutes during the Mexican teachers protest,
and plot them as shown in Fig. 3.7(a). Adequately modelable by a Poisson distribution, we use the average value as the estimate of $\lambda$. Fig. 3.7(b) depicts the Poisson distribution fit with $\lambda = 4.18$. If there are $M_0$ isolated users, the probability of each of these users to get infected in time interval $\delta t$ is $\lambda/M_0$. To summarize, for any user not in the mentions network, infection is only possible via the Poisson process. For a user who is already in the mentions network, infection can only happen via the GBM process over the mentions network, as described earlier.

### 3.4 Experiments

#### 3.4.1 Dataset Description

The study described in this chapter uses two datasets: (i) a gold standard report (GSR) of social unrest events in Latin America provided by MITRE that we use to define major mass protest events, and (ii) tweets collected over 14 months from May 2012 to September 2013 from 20 Latin American countries.

The GSR documents each civil unrest event by location, date, type of protest, and specifies the national news articles that first reported the event. For protests that were prominent on Twitter, the GSR news articles often report hashtags which were used by protestors on social media. We selected only those GSR events for which we were able to find such hashtags. This process resulted in 64 unique hashtags related to 40 different protest that occurred in Latin America since May 2012. In Table 1 we list a few of these events from our study.

Our Twitter dataset was built by querying Datasift’s streaming API. Each tweet payload includes crucial metadata along with the tweet’s content. Though tweets from GPS-enabled devices include geographic coordinates, the percentage of such tweets in the collected sample was too low to be useful.

For this study, we further filtered tweets by removing those that do not contain hashtags relevant to a specific protest. Since most tweets do not have location data, we estimate their location by geocoding the tweet based on each tweet’s content and properties of its user. We developed our own geocoding library that uses the World Gazetteer (http://archive.is/srm8P) database to lookup location names and geographic coordinates. Tweets can be geocoded to the user’s location at the time of tweeting or a location of interest about which the user is tweeting. We focused on event geolocation, which looks for location or landmark names, such as *Plaza de la Independencia* or *Quito, Ecuador*, in a tweet’s text. We generated a list of 2000 landmarks by extracting place names mentioned in GSR events which had high mutual information to civil unrest. In cases where no event location was found in a tweet’s text, we use geo-coordinates or self-reported location string in the tweet’s metadata.

Using the above pipeline we were able to extract and geolocate 20,227,830 unique users to
Brownian distance vs propagation time for teacher protest events.

Figure 3.8: Brownian distance vs propagation time for teacher protest events.

Figure 3.9: GBM and Poisson propagation simulation for Yosoy protests (Mexico) on May 19, 2012.

build our mentions network from the filtered tweets that were spread over daily sub-networks.

3.4.2 GBM Diffusion Model

For each of our mass protest events, we filter by its specific keywords (hashtags) to obtain a set of relevant tweets and construct a mentions network from those tweets. We assume that information propagates from an initial infected user to other users through the network from one node to its neighbors. We build an adjacency matrix based on the mentions network and simulate the propagation using the GBM diffusion process as follows:

1. **Brownian distance:** The Brownian distance is intended to have an inverse relationship with mention frequency. As Fig. 3.8 shows, users with smaller Brownian distance have greater mention frequencies resulting in shorter mean propagation times with less variance. From Fig. 3.8, we can see that infection time and variance generally both increase with an increase in Brownian distance. Heuristically, more frequent mentions
indicate stronger ties which leads to easier adoption of information. We tried $\gamma$ form 1.0 to 5.0 with step of 0.1, and found when $\gamma = 1.2$ GBM model achieved the best prediction performance.

2. Propagation speed: To evaluate our dynamic GBM infection process assumptions, we estimate the GBM parameters for different protest events and depict the GBM propagation curves in Figs. 3.9, 3.10, and 3.11. The blue curve depicts the Poisson propagation in latent space. The red curve depicts GBM propagation through the mentions network. The green curve is the overall simulation result while the magenta curve depicts the ground truth of the protest events process. By comparing the green and magenta curves, we can evaluate the effectiveness of our bispace model in simulating the mass protest events. As shown, we find that, given a mentions network, our bispace model can simulate the propagation speed at a reasonable scale, at the right magnitudes. As seen in Figs. 3.9(a), 3.10(a) and 3.11(a), we find that we can capture the burst of activity at the same time point as the ground truth during protest propagation.
3.4.3 GBM Diffusion with Communities

We were also able to observe the variation in $\mu$ and $\sigma$ as community structure varies. In particular, community features like graph density and diameter as shown earlier in Fig. 3.6 may impact GBM propagation. We experimented with two modeling approaches: (i) one set of parameters for the whole network and (ii) different parameters for each community in the network. We ran simulations for both these situations, and plotted the results of the whole network vs. community-specific approach in Figs. 3.9, 3.10, and 3.11. Comparing these simulation results, we find the community approach performs better, especially at capturing peak values. Taking a closer look at Fig. 3.12, we observe that propagation time and speed of infection are different for each community and we are able to simulate local propagation more accurately, which can be seen, e.g., from Fig. 3.10(b), where the GBM with community method can simulate the burst propagation effectively, while the general GBM method (see Fig. 3.10(a)) fails to capture the exact peak time.

3.4.4 Latent Space Diffusion Model

We use the following steps to calculate the properties of the latent space for each event.

1. **Latent space**: The intent is to consider all possible external influences and latent interactions in this space. We split Twitter data into unique 15 minute intervals and count the total number of infected users in each interval.

2. **Normalize**: Twitter user activity varies based on time of day and day of week (see Fig. 3.13). For each 15 minute window from Step 1, we find the average number of
tweets over a 4 week period and use this value to normalize the count. This baseline count of tweets over time in the latent space is close to the Poisson distribution. Fig. 3.7(a) shows an example of this baseline.

3. **Train:** Using one week’s data split into 15 minute intervals, we train the Poisson distribution parameters. Fig. 3.7(b) shows that the training curve and ground truth curve can be matched quite well.

### 3.5 Evaluation results

We present an exhaustive evaluation of our bispace simulation approach alongside various dimensions next:

- **How effective is the performance of the bispace model?**

Recall that the bispace modeling is comprised of two independent process: the GBM simulation in the mentions network, and the Poisson process within the latent space. Given an initial mentions network, after training the GBM parameters of $\mu$ and $\sigma$, we proceed to conduct the GBM simulation. After estimating the Poisson parameter $\lambda$, we are able to do the Poisson simulation within latent space. We use accuracy, the ratio of correctly predicted observations, to measure how far the bispace model is beyond the ground truth in capturing total infected nodes number. We see that the GBM model is capable of capturing many mass protest scenarios, to the order of magnitude. Even though it cannot simulate the propagation speed accurately at every time point, the method is effective at capturing the total number of infected nodes with an accuracy of $[0.78, 0.95]$, as shown in Fig. 3.14.

- **How adept is the bispace model at capturing surge/burst moments? How reliable are the simulation results?**
Fig. 3.9 depicts the analysis of the YoSoy132 student movement, whose Twitter activity is generally tortuous, and the curve is full of surges and bursts. From Fig. 3.9 we see that the bispace model is capable of simulating the general surge trends. Comparing the bispace simulation results with ground truth, we can see at many time points, the bispace simulation matches the ground truth. Fig. 3.11 shows the second protest of people protesting against the government in Colombia; here the Twitter activity depicts a burst at a single time point which is hard to capture. We can see the bispace model did show there is a burst, but not at the precise time point, one of its current limitations.

- **How is the performance of Bispace model compared with other methods?**

In the massive protest analysis, we are interested in the total number of people participating in the protest. We do not pay much attention on individual people who participates nor not. We use bispace model to predict the protest scale within a certain time period. We evaluate the predicted time series with the ground truth time series using four different criterions: normalized root mean squared error ($NRMSE$), Cosine Similarity, Pearson Correlation, and accuracy [92]. Given the ground truth time series $x_{true}$ and predicted time series $x_{pred}$, the $NRMSE$ is defined as:

$$NRMSE = \frac{1}{\bar{X}} \sqrt{\frac{1}{n} \sum_{i=1}^{n} (x_{true}(i) - x_{pred}(i))^2}$$  \hspace{1cm} (3.12)

, where $\bar{X}$ is the mean of $x_{true}$. Accuracy is defined as:

$$accuracy = \frac{1}{n} \sum_{i=1}^{n} \frac{|x_{true}(i) - x_{pred}(i)|}{\max(x_{true}(i), x_{pred}(i))}$$  \hspace{1cm} (3.13)

We compare bispace model with random assign and naive bayes model for the seven protests. For each model, we run the results for 20 times, and use the average value as the final results. We table the finale results in Table 3.2, which shows that bispace model outperforms other approaches uniformly.

- **Is the performance of the model better taking into account community structure?**

After numerous experiments, we plot the accuracy distribution of both approaches for all our mass protest situations in Fig. 3.14. Although the accuracies are sometimes interspersed, we can see that in overall the community model generally has a higher accuracy.

- **Can the bispace model simulate the propagation path?**
Table 3.2: Bispace model performance evaluation.

<table>
<thead>
<tr>
<th>Protest No.</th>
<th>Model</th>
<th>NRMSE</th>
<th>Cosine Similarity</th>
<th>Correlation</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>random assign</td>
<td>0.39</td>
<td>0.56</td>
<td>0.63</td>
<td>0.67</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.32</td>
<td>0.66</td>
<td>0.62</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.22</td>
<td>0.82</td>
<td>0.74</td>
<td>0.87</td>
</tr>
<tr>
<td>2</td>
<td>random assign</td>
<td>0.37</td>
<td>0.64</td>
<td>0.67</td>
<td>0.69</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.29</td>
<td>0.66</td>
<td>0.69</td>
<td>0.75</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.27</td>
<td>0.83</td>
<td>0.71</td>
<td>0.78</td>
</tr>
<tr>
<td>3</td>
<td>random assign</td>
<td>0.43</td>
<td>0.67</td>
<td>0.61</td>
<td>0.57</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.33</td>
<td>0.66</td>
<td>0.62</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.22</td>
<td>0.77</td>
<td>0.74</td>
<td>0.82</td>
</tr>
<tr>
<td>4</td>
<td>random assign</td>
<td>0.33</td>
<td>0.62</td>
<td>0.73</td>
<td>0.61</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.37</td>
<td>0.65</td>
<td>0.62</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.22</td>
<td>0.88</td>
<td>0.82</td>
<td>0.90</td>
</tr>
<tr>
<td>5</td>
<td>random assign</td>
<td>0.44</td>
<td>0.63</td>
<td>0.67</td>
<td>0.69</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.42</td>
<td>0.66</td>
<td>0.66</td>
<td>0.60</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.27</td>
<td>0.79</td>
<td>0.77</td>
<td>0.81</td>
</tr>
<tr>
<td>6</td>
<td>random assign</td>
<td>0.37</td>
<td>0.63</td>
<td>0.64</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.32</td>
<td>0.66</td>
<td>0.62</td>
<td>0.68</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.20</td>
<td>0.68</td>
<td>0.74</td>
<td>0.81</td>
</tr>
<tr>
<td>7</td>
<td>random assign</td>
<td>0.42</td>
<td>0.56</td>
<td>0.67</td>
<td>0.58</td>
</tr>
<tr>
<td></td>
<td>naive Bayes</td>
<td>0.39</td>
<td>0.66</td>
<td>0.62</td>
<td>0.69</td>
</tr>
<tr>
<td></td>
<td>bispace</td>
<td>0.16</td>
<td>0.88</td>
<td>0.78</td>
<td>0.89</td>
</tr>
</tbody>
</table>

In addition to comparing the simulated counts of tweets over time with ground truth values, we can also compare the propagation path generated by the simulation against the actual propagation path through the mentions network. In Fig. 3.15 we can obtain a sense of the type of infection network bispace modeling creates as compared with the actual network. The simulation produces networks with relatively accurate paths and relevant characteristics as shown in Table 3.3. The component to which a user belongs is that of neighbors who can be reached from connected paths running along edges of the graph [67].

Table 3.3: GBM simulation results for teacher protest events on Sept 2, 2013.

<table>
<thead>
<tr>
<th></th>
<th>Average degree</th>
<th>Diameter</th>
<th>Graph density</th>
<th>Connected components</th>
<th>Average clustering coefficient</th>
<th>Average path length</th>
</tr>
</thead>
<tbody>
<tr>
<td>Simulation</td>
<td>1.791</td>
<td>11</td>
<td>0.002</td>
<td>183</td>
<td>0.083</td>
<td>4.786</td>
</tr>
<tr>
<td>Ground truth</td>
<td>1.726</td>
<td>18</td>
<td>0.002</td>
<td>204</td>
<td>0.068</td>
<td>6.201</td>
</tr>
</tbody>
</table>

- Between the geometric Brownian model and Poisson propagation approaches, which model is more dominant during the simulation process?

From Figs. 3.9, 3.10, 3.11, by observing the blue dashed line (Poisson) and red dashed line (GBM), we can see that the Poisson process shows a mild activity, while the GBM model
Figure 3.14: Performance accuracy of the bispace model for the 7 protest scenarios considered here, with and without community structure.

serves as the dominant component which can capture the moments of key surges.

3.6 Discussion

In this chapter, we have characterized mass protest propagation using a bispace model comprising an observed mentions network space and a latent space. We have introduced a trust function to simulate propagation in observed space using a geometric Brownian motion diffusion process which can be further extended to support communities with different propagation parameters per community. We considered the latent space of all interactions outside the mentions network to be a Poisson distribution process. We have shown how the GBM diffusion model offers a new approach for modeling propagation through social networks like Twitter. Through our experiments, we find that the time required for spread of protest information through such networks is dependent on the network’s substructures. Furthermore, we find that modeling the diffusion process on a community basis provides better results than the assumption that all nodes in the network spread information in the same way.

In future work, we hope to further characterize the hidden network with the goal of uncovering specific latent variables. In our current model, we regard the trust function playing an important role in information propagation modeling. However, it could happen that distrust also play a part, in events related with political views such as police shooting. How to integrate and leverage the two strengths into information propagation model, to get a closer perspective into mass movements adoption, will be our next task. Additionally, we envision applying the GBM model to other networks, such as the Twitter follower network, to identify those paths most susceptible to information dissemination. Finally, we desire to compare propagation of mass protest language against other themes, such as celebratory events, to aid in determining correlations between topic or sentiment and the resulting social
Figure 3.15: Bispace model simulation results compared against ground truth infected nodes for the Mexican teacher protest events.

media diffusion.
Chapter 4

Group Anomalies as Basis for Protest Detection

4.1 Introduction

Various studies have shown that Twitter is a viable ‘social sensor’, and thus holds great promise for detecting and forecasting significant societal events [11, 79]. In recent years, a significant body of research [1, 39, 55, 56, 79, 81, 98, 99, 105] has focused on modeling bursts and increases of user activity in social media.

However, real world events are not only correlated with burst signals, but can also lead to unusually low levels of activity in social networks. An example of this phenomenon is shown in Figure 1, where a protest in the city of Natal, Brazil, began at 5:00 PM (local time) at the Museum of the Republic, with people gradually joining the demonstration. On Twitter, there was an uncharacteristic lull in activity or group absenteeism behavior in the area for the two hours from 6:00 PM - 8:00 PM that day. Another example comes from December 24, 2013, when southern Brazil experienced widespread flash floods. According to news sources, more than 50,000 people were forced to flee their homes in Minas Gerais and Espirito Santo, in the southern states of Brazil. Immediately following the floods, Twitter activity in this region dropped by 51%, reaching its lowest point later that evening.

Developing a better appreciation of this phenomenon of unusually calm behavior online holds enormous potential for understanding localized, disruptive, societal events. In this chapter we focus on absenteeism as a key phenomenon of interest and develop novel group anomaly detection algorithms for this purpose. An absenteeism event in a social network can be defined as an event which is characterized by a significant lull in activity such as a sudden, sharp decrease of Twitter volume within a short period of time (and which may precede a major burst in activity as people react to the event). This chapter presents the first study to systematically investigate group anomaly in location-based social networks (LBSNs). To
appropriately incorporate absenteeism concepts into our detection approach, we must first address the following questions:

- How can we define/adapt anomaly detection algorithms to capture not just bursty situations but also those that involve absenteeism?
- At what scale should we model the absenteeism activity and how can we isolate the locus of interest?
- What is the most efficient way to select abnormal groups that are spatially and temporally localized?
- How do we model an absenteeism signal for event detection? Even though we have clear examples of real world events that explain the observed absenteeism, not all absenteeism occurrences will be associated with underlying events and thus we must be able to differentiate between absenteeism and merely noisy signals for successful event detection.

A graph wavelet approach offers several outstanding advantages to study the above questions, including scalability, localization, low computational complexity, and compactness in defining groups. In this formalism, the data objects are embedded in a general graph as vertices. By employing wavelet transforms on the graph, we can construct a wavelet function with a graph structure. We propose the use of a graph anomaly index that depends on the graph structure in conjunction with an absenteeism score vector in order to define whether a graph is abnormal. When a graph is deemed to be exhibiting abnormal behavior, we can calculate its wavelet coefficient to identify the central node and its coverage area. This approach will enable us to select abnormal groups at different scales. Such group anomaly detection methods are varied and proven to be effective in detecting events such as protest marches and natural disasters.

Our contributions are thus:
• To the best of our knowledge this is the first study to utilize group absenteeism as a basis for event detection. By studying different types of group anomalies, either bursts or absenteeism, we demonstrate that these anomalies are indicative of key events such as civil protests or natural disasters.

• We incorporate graph wavelets as a mechanism to detect the most anomalous subgraphs at different scales. We demonstrate the power of this approach for social media analytics.

• We define a graph anomaly index that can be used to determine whether a graph is abnormal. We then apply the graph wavelet to locate the central node and identify the abnormal groups.

The rest of this chapter is organized as follows. Section ?? reviews related work and existing methodologies and Section 4.2 formalizes the research problem. In Section 4.3, we discuss the graph wavelet formalism for group anomaly detection. Section 4.4 extensive experiments testing our new approach’s effectiveness for real-world event detection, and concludes with a summary of the research in Section 4.5.

4.2 Problem Formulation

In this section, we begin by introducing the mathematical notation used in this chapter and then proceed to formalize our approach to group anomaly detection. After presenting the problem statement, we provide a brief comparison of our approach with conventional solutions, and review the challenging issues that are relevant to this type of event detection problem.

4.2.1 Notation

We are given an undirected, weighted graph $G(V, E; f)$, where $V = \{v_0, v_1, \ldots, v_{N-1}\}$ represents the set of $N$ cities and $E$ refers to the connections between neighboring cities. $W$ is a matrix of non-negative weights associated with each edge, where $w_{ij} \in E$. The function, $f : V \rightarrow \mathbb{R}^N$ maps the vertices of graph $G$, and $f(n)$ stands for the value on the vertex $v_n$. Graph $G$’s adjacency matrix $A$ is of size $N \times N$, where each element $a_{ij}$ is represented as:

$$a_{ij} = \begin{cases} w_{ij} & \text{when } e_{ij} \in E \\ 0 & \text{otherwise} \end{cases} \quad (4.1)$$

Here, $A$ is symmetric since $a_{ij} = a_{ji}$. Let $d_i = \sum_{v_j \in V} a_{ij}$ be the sum of all edge weights that are incident on $v_i$, and $D$ be the diagonal matrix denoted as $D = \text{diag}\{d_1, d_2, \ldots, d_N\}$. 
A Laplacian matrix $L$ is defined as $L = D - A$. It is a symmetric matrix and has real eigenvalues $\lambda_i$ such that $0 = \lambda_0 < \lambda_1 \leq \lambda_2 \leq \ldots \leq \lambda_{N-1} = \lambda_{\text{max}}$. The complete set of $L$'s normalized eigenvectors [6] $\chi_i$ for $i = 0, 1, 2, ..., N - 1$ is described as:

$$L\chi_i = \lambda_i \chi_i$$

(4.2)

The set of eigenvalue and normalized eigenvector pairs is denoted as:

$$\sigma(G) := \{(\lambda_l, \chi_l)\}_{l=0}^{N-1}.$$  

(4.3)

$\sigma(G)$ is also called the graph spectrum of $G$.

4.2.2 Problem Statement

We focus on the problem of group anomaly detection from online social networks, based on the absenteeism behavior observed in user activity in geographically proximal communities or group of cities. Conventionally, this problem can be described as following: \textit{given a graph and absenteeism score vector, $G(V, E; f^t)$ at time interval $t$, select a subset $\Sigma \subseteq V$, such that}

$$\Sigma = \arg \min_{P \subseteq V, P \text{ is compact}} \sum_{v_k \in P} f(k)$$

(4.4)

Defining compactness of the selected subset $\Sigma$ is, of course, the key issue here. A general solution to this problem involves employing a combinatorial optimization method; by defining a constrained objective function over a network one can identify a subset of vertices which minimize the corresponding function [76]. Therefore, Equation 4.4 can be modified as:

$$\Sigma = \arg \min_{P \subseteq V} \sum_{v_k \in P} f(k) + \lambda \mu(P),$$

(4.5)

where $\mu(P)$ is the compactness penalty function of $P$ (e.g., the sum of distances among all pairs of the vertices in $P$ [76]), and $\lambda$ is the regularization parameter. However, such methods suffer from the following issues:

1. Definition of the compactness function $\mu(P)$ is subjective.
2. Determination of an appropriate regularizer $\lambda$ is difficult, as we do not have sufficient training data for this purpose.
3. To solve this objective function is often a NP-hard problem [76], which makes it impractical in many real world applications. Sometimes, even the approximate solutions are of high computation complexity, if there are any.
In contrast, our approach proposes a novel group anomaly algorithm for social networks that is based on spectral graph wavelet theory. The graph wavelets focus on the intrinsic geometric structure of the graph by transforming each vertex \( v_i \in V \), and mining the topological information of both local and global centered vertices to support a multiscale analysis. In addition, the graph wavelet approach identifies anomaly groups that are automatically compact, and provides a fair method at a low computational cost in terms of complexity for identifying abnormal group behavior in broad application scenarios.

![Z-score distribution of city Sao Paulo, Brazil from Aug 1, 2012 to January 30, 2014 with time interval of five minutes.](image)

Figure 4.2: Z-score distribution of city Sao Paulo, Brazil from Aug 1, 2012 to January 30, 2014 with time interval of five minutes.

### 4.3 Algorithm

#### 4.3.1 Graph Fourier Transform

Given a signal \( f \) defined on graph \( G \), its graph Fourier transform is considered as the projection of \( f \) on the complete set of \( \{ \chi_l \}_{l=0}^{N-1} \), and is written as [34]:

\[
\hat{f}(l) = < \chi_l, f > = \sum_{i=1}^{N} \chi_l^*(i) f(i) \quad (4.6)
\]

Since \( \{ \chi_l \}_{l=0}^{N-1} \) is complete, \( f \) can be recovered by its graph Fourier transform coefficients \( \hat{f}(l) \) as [34]:

\[
f(n) = \sum_{l=0}^{N-1} \hat{f}(l) \chi_l(n) \quad (4.7)
\]

Here, \( \hat{f}(l) \) is the coefficient of component \( \chi_l \).
eigenvector $\chi_l$

As an analog with classical signal processing, eigenvector $\chi_l$ is also referred to as the frequency of $G$ by some researchers. In the latter part of this chapter, $\chi_l$ will be referred to as the eigenvector or frequency, alternatively. However, unlike the traditional frequency concept in classical signal processing fields, the frequency of $G$ is a set of discrete vectors with length of $|V|$. Interestingly, like the classical signal Fourier transform, the Parseval relation [87] still holds, i.e.,

$$||f||_2^2 = ||\hat{f}||_2^2$$

Equation 4.8 means that the energy in the vertex domain and frequency domain is equal for any graph signal $f$. Without loss of generality, we assume $||f||_2 = 1$.

Figure 4.3: Graph $G_1$, all edges’ weight are 1.

eigenvalue $\lambda_l$

According to the definition of eigenvalue $\lambda_l$ in Equation 4.2, the following equation holds:

$$\chi_l^T \lambda_l \chi_l = \chi_l^T L \chi_l = \sum_{e_{mn} \in E} w_{mn} [\chi_l(m) - \chi_l(n)]^2$$

Since $\chi_l$ is normalized, and $||\chi_l||_2 = 1$, then,

$$\chi_l^T \lambda_l \chi_l = \lambda_l = \sum_{e_{mn} \in E} w_{mn} [\chi_l(m) - \chi_l(n)]^2$$

From equation 4.10, we can see that $\lambda_l$ summarizes all the eigenvector deviations on any directly connected vertices $v_m$ and $v_n$ in $G$. Since each term in the summation of the right-hand side is non-negative, the eigenvectors associated with smaller eigenvalues are smoother; i.e., the component differences between neighboring vertices are small [87]. As the eigenvalue increases, larger differences in neighboring components of the graph Laplacian eigenvectors are present. Hence, for larger $\lambda_l$, its corresponding eigenvector, $\chi_l(n)$, has larger deviation among connected vertices. According to the definition of Laplacian matrix $L$, it is easy to verify that $\lambda_0 = 0$ since $L \cdot \vec{1} = 0 \cdot \vec{1}$, where $\vec{1} = \{1, 1, 1, ..., 1\}$, and $\chi_0(n) = \frac{\vec{1}}{\sqrt{N}}$. Thus,
Figure 4.4: (a): Eigenvector distribution along each vertex in graph $G_1$. (b): anomaly index $\gamma_f(l)$ of $f_1 = [2, 3, 4, 3, 2, 1]$ on graph $G_1$. (c): anomaly index $\gamma_f(l)$ of $f_1 = [2, 3, 4, 3, 2, 1]$ and $f_2 = [2, 2, -3, 4, 3, 1]$ on graph $G_1$, where $\gamma_{f_1} = 0.905$, and $\gamma_{f_1} = 0.073$, labelled in red ovals.

$\chi_o(n) = \frac{1}{\sqrt{N}}$ means that $\chi_o(n)$ is constant on each vertex, and that there is no deviation among any two vertices in $\chi_0(n)$. For this reason, $\chi_0(n)$ is considered as the least abnormal component of $G$. Similarly, $\chi_{N-1}(n)$ is considered as the most abnormal component of $G$.

Figure 4.3 shows an undirected graph $G_1$ where each edge’s weight is 1. Figure 4.4(a) shows $G_1$’s six eigenvectors distributions along each vertex. We can see that $\chi_0$ is constant on very vertex, and has the smallest deviations along each edge. $\chi_5$ has the largest deviations, and the difference of $\chi_5$ along each edge is larger than any other eigenvector on average.

### 4.3.2 Global Anomaly Index

To quantify the anomaly of a vector $f$ defined on a graph $G$, it’s necessary to incorporate the intrinsic structures of $G$ and $f$. As discussed above, $\hat{f}(l)$ represents the coefficient of frequency $\chi_l$, and $\hat{f}^2(l)$ is considered as the energy of frequency $\chi_l$. In addition, according to equation 4.10, $\lambda_l$ represents the deviation of frequency $\chi_l$ along all the connected vertices. Therefore, in this chapter, we define the anomaly index of $\chi_l$ in $f$ as:

$$
\gamma_f(l; G) = \lambda_l \hat{f}^2(l) = \lambda_l < f, \chi_l >^2
$$

(4.11)
\( \gamma_f(l; G) \) depends on two parts, frequency \( \chi_l \)’s deviation sum \( \lambda_l \), and its energy \( \hat{f}^2(l) \). If the energy \( \hat{f}^2(l) \) is small, even if \( \lambda_l \) is large, the anomaly index of \( \chi_l \) might be small. Obviously, \( \gamma_f(0; G) \) is always 0 since \( \lambda_0 = 0 \). Further, we use the maximal value of \( \gamma_f(l; G) \) to represent the global anomaly of \( f \) on \( G \):

\[
\gamma_f(G) = \max_{0 \leq l \leq N-1} \gamma_f(l; G). \tag{4.12}
\]

Here, \( \gamma_f(l; G) \) refers to the anomaly extension of \( \chi_l \) in \( f \) defined on \( G \), instead of implying the anomaly extension of vertex \( v_l \). For brevity, \( \gamma_f(l; G) \) and \( \gamma_f(G) \) are shortened as \( \gamma_f(l) \) and \( \gamma_f \), respectively, when \( G \) is known.

Figure 4.4(b) plots the anomaly index \( \gamma_f(l) \) of \( f_1 \) on graph \( G_1 \), where \( f_1 = [2, 3, 4, 3, 2, 1] \). The six markers on the dashed blue are the six eigenvalues of \( G \). The yellow line is \( |\hat{f}(l)| \), and the pink line is the anomaly index, \( \gamma_f(l) \) for frequency \( \chi_l \). Because \( \gamma_f(l) \) depends on both \( \lambda_l \) and its power \( \hat{f}^2(l) \), for the yellow line, even though \( \chi_0 \) has the strongest power, its deviation \( \lambda_0 = 0 \), thus \( \gamma_f(0) = 0 \). On the other hand, \( \chi_5 \) has the largest deviation; but its power \( |\hat{f}(5)|^2 \) is small, which makes \( \gamma_f(5) \) is also small. Considering the \( \chi_4 \) has a high deviation (eigenvalue) and a strong power of frequency, it has the largest anomaly index. To compare the influence of different \( f \) on anomaly index, we show an example in Figure 4.4(c).

Setting \( f_1 = [2, 3, 4, 3, 2, 1] \) and \( f_2 = [2, 2, -3, 4, 3, 1] \), we plot their anomaly index \( \gamma_f \) and energy \( |\hat{f}(l)| \) respectively. The light blue curves stand for anomaly indices and the yellow
curves stand for $|\hat{f}(l)|$. The solid line stands for $f_1$, and the dashed line stands for $f_2$. As we can see, for high frequency $\chi_l$, $f_1$ has a larger power than $f_2$, and hence a higher anomaly index than $f_2$, where $\gamma_{f_1} = 0.905$ and $\gamma_{f_2} = 0.073$. This is consistent with that $f_1$ has larger deviations than $f_2$.

As we discussed before, the anomaly index depends on graph structure and $f$. As shown in Figure 4.4(c), different $f$ might have very different anomaly index because the power of $\chi_l$ distribution is different. Similarly, for the same signal $f$ on two different graphs, it might have very different anomaly indices. Figure 4.5 shows two graphs with the same $f = [1, 2, 5, 2]$. Figure 4.6 illustrates the anomaly index of $f$ on $G_2$ and $G_3$, where $\gamma_f(G_2) = 0.073$ and $\gamma_f(G_3) = 0.235$. (This is because in $G_3$ because there is no edge connecting $v_2$ and $v_3$, the difference between $f(2)$ and $f(3)$ is not considered as an anomaly.)

**Remarks:** In this subsection, we have introduced the anomaly index $\gamma_f(l; G)$ to measure the anomaly of $\chi_l$ in $f$ defined on $G$ by combing the spectrum structure of $G$ and $f$. $\gamma_f(l; G)$ depends on two parts: (1) the eigenvalue which reflects the deviations of $\chi_l$; (2) the $|\hat{f}(l)|^2$ which represents the power of $\chi_l$ in $f$. $\gamma_f(l; G)$ reflects the anomaly index of $\chi_l$. We use the maximal value of $\gamma_f(l; G)$ to define the anomaly index of $f$, which denotes the global anomaly index of $f$ on $G$.

### 4.3.3 Graph Wavelets

Classic wavelet formalisms have been referred to as mathematical microscopes because of their capability to depict signal anomalies at different scales. In the case of complex networks, graph wavelets render the graph with good localization properties both in frequency and vertex (i.e. spatial) domains. Their scaling property allows us to zoom in/out of the underlying structure of the graph.

Recall that, from Equation 4.6, the anomaly pattern $\hat{f}(l)$ represents the anomaly components of $f$ from the whole graph perspective. However, information concerning the vertex-location cannot be identified from the Fourier transform. To address this issue, Hammond et al. [34] proposed constructing wavelet transforms functions over the vertices using weighted graphs, described in the following steps:

1. Define a continuous generating kernel functions $g(x)$ on $\mathbb{R}^+$;

2. Then, select a central vertex $a \in V$ and scale $s$, set the frequency coefficients as $g(s\lambda_l)\chi_l^a(a)$ for each frequency component $\chi_l$;

3. Finally, sum up all those frequency components $\chi_l$. 


Figure 4.7: Spectral graph wavelet on South America. (a) vertex at which wavelets are centered in red dot. (b)-(f) wavelets, scales at 0.8, 1.8, 2.6, 8, and 40 respectively.

In this way, the graph wavelet at central vertex \( a \) is constructed as:

\[
\psi_{s,a}(n) = \sum_{l=0}^{N-1} g(s \lambda_l) \chi_l^*(a) \chi_l(n) \tag{4.13}
\]

After setting up the graph wavelet, the wavelet coefficients for \( f \) can be defined as

\[
W_f(s,a) = <\psi_{s,a}, f> = \sum_{l=0}^{N-1} g(s \lambda_l) \hat{f}(a) \chi_l(n) \tag{4.14}
\]

Similar to classical wavelets, graph wavelets obey following three properties, which are presented in detail in [34].

1. **Reconstruction.** When the kernel function \( g(x) \) satisfies the admissibility condition and \( g(0) = 0 \), \( f(n) \) can be reconstructed by the wavelet coefficients.

2. **Discretization and Wavelet Frames.** For practical applications, the scale \( s \) of graph wavelet \( \psi_{s,a} \) should be sampled with a finite number of scales. Given a real
valued function \( h(x) \) satisfying
\[
\hat{h}(\omega) = \sqrt{\int_\omega^\infty \frac{|\hat{g}(\omega')|^2}{\omega'} d\omega'},
\]
(4.15)
where \( \hat{g} \) and \( \hat{h} \) are the classical Fourier transform of \( g(x) \) and \( h(x) \), the scaling function \( \phi_a(n) \) can be generated as:
\[
\phi_a(n) = \sum_{l=0}^{N-1} h(\lambda_l) \chi_l^*(a) \chi_l(n)
\]
(4.16)
Accordingly, the scaling coefficients are defined as
\[
S_f(a) = \langle \phi_a, f \rangle
\]
(4.17)
Using scale set \( \Theta := \{s_j\}_{j=1}^J \), the discretized graph wavelet set \( \{\psi_{s_j,a}\}_{j=1}^J \) and scaling function set \( \{\phi_a\}_{a=0}^{N-1} \) constitute a frame [34]. According to frame theory [24], \( f \in \mathbb{R}^N \) can be reconstructed from those \( NJ + J \) wavelet and scaling coefficients as
\[
f(n) = \sum_{a=v_0}^{v_{N-1}} \sum_{j=1}^J W_f(s_j,a) \psi_{s,a}(n) + S_f(a) \phi_a(n).
\]
(4.18)
For brevity, we assume that
\[
\phi_a(n) = \psi_{s_0,a}(n),
\]
(4.19)
and
\[
S_f(a) = W_f(s_0,a).
\]
(4.20)
Therefore, equation 4.18 can be written as
\[
f(n) = \sum_{a=v_0}^{v_{N-1}} \sum_{j=0}^J W_f(s_j,a) \psi_{s,a}(n).
\]
(4.21)
In the later part of this chapter, we do not differentiate between scaling coefficient and wavelet coefficient. A detailed algorithm and treatment concerning the choice of \( \Theta \) can be found in [34].

3. **Localization in vertex domains.** Given a central vertex \( v_a \) and its graph wavelet \( \psi_{s,a}(n) \), suppose the kernel function \( g \) is \( K + 1 \) times continuously differentiable, let \( v_n \) be an vertex of \( G \) with \( d_G(n,a) > K \), then there exists constants \( D \) and \( \beta \), such that
\[
\frac{|\psi_{s,a}(n)|}{||\psi_{s,a}||} \leq D \beta
\]
(4.22)
for all $s < \beta$. $d_G(n, a)$ is the shortest path distance, which is the minimum number of edges in any path that connect vertices $v_n$ and $v_a$ [34]. Equation 4.22 shows for any vertex $v_n$ that is far away from center vertex $v_a$ ($d_G(n, a) > K$), $|\psi_{s,a}(n)|/||\psi_{s,a}||$ is upper bounded by $D\beta$. In other words, for vertex $v_n$ which is far away from vertex $v_a$, its wavelet value is linearly attenuated by scale $s$. When the scale $s$ is small, their wavelet value of marginal vertices will be vanished quickly. The marginal vertices are those which satisfy equation 4.22. All the other vertices are called kernel vertices, denoted by $K(s,a)$. Obviously, $\forall v_n \in K(s,a)$, $d_G(n,a) \leq K$. Thus $K(s,a)$ is automatically compact. Figure 4.11 shows two graph wavelets centered on the same vertex $a$, but with two different scales, $\psi_{s_1,a}$ and $\psi_{s_2,a}$, where $s_1 < s_2$. The length of the vertical bar on each vertex denotes its graph wavelet value. The highlighted areas denote the kernel vertices ($d_G(n,a) \leq 1$), and the others are marginal vertices. We can see that the wavelet values on marginal vertices in Figure 4.8(a) are smaller than those in Figure 4.8(b). Figure 4.8(c) is $f$'s distribution along each vertex, and Figure 4.8(d) shows the wavelet coefficients with center node $a$ for different scales, which indicates that $W_f(s_2,a)$ has the largest value, and $W_f(s_3,a)$ with the smallest.

**4.3.4 Group Anomaly Detection via Graph Wavelets**

According to Equation 4.22, when $s$ is small, the weights of the marginal vertices are severely attenuated. Essentially, $W_f(s,a)$ is equivalent to the sum of $f$ with large weights on kernel vertices, and small weights on marginal vertices. When $f$ is of uniformly large negative/positive values on kernel vertices, then $W_f(s,a)$ will be a large negative/positive value with scale $s$.

The localization property of graph wavelets makes them appropriate for group anomaly detection since they automatically identify the kernel vertices from marginal vertices. These kernel vertices form a compact subset since each one of them is close to the same center vertex $a$, which avoids the compactness constraint condition in Equation 4.5, thus reducing its computational complexity greatly. We propose our group anomaly detection algorithm based on graph wavelets in Algorithm 1. It iterates $NJ + J$ times, and each iteration selects
Algorithm 1 Group Anomaly Detection using Graph Wavelets

1: Input: graph and absenteeism score vector $G(V, E; f^l)$ at time interval $l$, wavelet threshold $\omega_{th}$.
2: Output: abnormal burst group set $I^{bur}$ and absenteeism group set $I^{abs}$.
3: compute graph spectrum $\sigma(G)$;
4: set graph wavelets $\psi_{s,a}(n)$ and scales set $\{s_j\}_{j=0}^{J}$ for all $a \in V$;
5: for all center node $a \in V$ and $s_j \in \{s_j\}_{j=0}^{J}$ do
6: compute $W_f(s_j, a)$;
7: if $W_f(s_j, a) \geq \omega_{th}$ then
8: add group $K(s_j, a)$ to $I^{bur}$
9: end if
10: if $W_f(s_j, a) \leq -1 * \omega_{th}$ then
11: add group $K(s_j, a)$ to $I^{abs}$
12: end if
13: end for
14: return abnormal burst group $I^{bur}$ and absenteeism group set $I^{abs}$.

Remarks:

1. Graph wavelets form a frame where the function $f$ can be reconstructed by their coefficients. As long as the scale level $J$ is high enough, $f$ can be well decomposed into the frame basis. Thus, using graph wavelets to exploit the structure of functions defined on graphs is much more reasonable.

2. Graph wavelets transform selected kernel vertices, $K(s, a)$, that are close to the central vertex $a$, and attenuate the impact of other marginal vertices that are far away from $a$. The abnormal group selected by graph wavelet approach is automatically compact, and circumvent high computational complexity, which makes it easily adaptable to a wide variety of application scenarios.

3. Graph wavelets are able to identify abnormal burst groups and absenteeism groups simultaneously without extra computation cost.

4.4 Experimental Results

This section discusses the application of our approach for detecting group anomalies. We begin by briefly describing the dataset used for our experiments in Section 4.4.1 and then move on to discussing the implementation details of how the graph $G$ is assembled; we
construct the graph wavelets $\psi_{s,a}$ in Section 4.4.2. The following section presents the group anomaly detection performance for identifying protest events. In Section 4.4.4, we describe three case studies that illustrate how the graph wavelet model is able to capture absenteeism events such as disaster scenarios.

### 4.4.1 Data Collection and Preprocessing

The study described in this chapter uses tweets geolocated to Latin America and collected over a period of two years (Jan 2013 to Dec 2014). We query Datasift’s streaming API to collect tweets that also have meta-information including geotag bounding boxes (structured geographical coordinates), Twitter places (structured data), user profile location (unstructured, unverified strings), and ‘mentions information’ about locations present in the body of the tweet. Typically, we found that the number of tweets with readily available geo-coordinates is too low for conducting meaningful experiments. To circumvent this drawback, we use the geo-enrichment algorithm described in [73]. This algorithm uses a gazetteer-based approach to look-up location names and geo-coordinates. To identify location-specific tweets, we configure the geocoding tool to first consider the tweet’s text for mentions of place names and geographical landmarks (e.g., say, Plaza de la Independencia (Quito, Ecuador)). In cases when no geographical location was found in the tweet text, it then proceeds to process the geographical coordinates and the self-reported location string in user’s profile metadata.
4.4.2 Experimental Setup

**Graph Setup**  Each city $v_i$’s location is represented by its geographical coordinate pair $lat_i$ and $lon_i$. Instead of using the real physical distance, we define the distance of any two cities $v_i$ and $v_j$ as $d_{ij} = \sqrt{(lat_i - lat_j)^2 + (lon_i - lon_j)^2}$. We setup graph $G$ as a $k$ neighbors graph, which means each city is only connected to its $k$-nearest-neighbors. In this chapter, we set $k = 5$, and all the edges’ weights in $G$ are 1. Figure 4.9(a) shows Brazil’s 5 nearest-neighbor graph with 5321 cities.

**Absenteeism Score**  Considering that the tweet volume $X$ varies vastly among cities, instead of using $X$ itself, we use the normalized value of z-score as absenteeism score, which is defined as:

$$z\text{-score} = \frac{X - \mu}{\sigma}$$

(4.23)

where $\mu$ is the mean value of the previous 30 day tweets volume and $\sigma$ is the corresponding standard deviation. As shown in Figure 4.9(b), different node colors denote different z-score values.

**Kernel function $g(x)$ and scaling function $h(x)$**  Our choice for the wavelet generating kernel function, $g(x)$, and scaling function $h(x)$ is motivated by our goal to achieve scale-dependent localization. We follow the kernel function setting in [34], which behaves as a monic power near the origin, and has power law decay for large $x$, as shown in Figure 4.10. $g(x)$ and $h(x)$ are set as:

$$g(x) = \begin{cases} 
  x & \text{for } x < 1 \\
  s(x) & \text{for } 1 \leq x \leq 2 \\
  2x^{-1} & \text{for } x > 2
\end{cases}$$

(4.24)
Figure 4.11: Graph wavelets with center city $v_{83}$. $s_1 = 1.31$, $s_2 = 0.68$.

where $s(x) = -5 + 11x - 6x^2 + x^3$.

$$h_x = 1.385 \exp\left(-\left(\frac{20x}{0.6\lambda_{\text{max}}}\right)^4\right) \quad (4.25)$$

The scale set $\{s_j\}_{j=1}^J$ is selected to be equally logarithmically spaced between the minimum and maximum scales $s_1$ and $s_J$, which are defined in [34]. We set $J = 6$ in the experiment. Figure 4.11 shows two different scaled wavelets on Brazil’s 5-nearest-neighbor graph. Comparing Figure 4.11(a) with Figure 4.11(b), we can see that, when scale increases, more cities (with deeper color) are selected. Figure 4.12 shows the corresponding wavelet coefficients.

We also try another kernel function, i.e. the Mexican hat function, and find that as long as the kernel function monotonicity is the same, the differences in wavelet coefficients are negligible.

**Anomaly index $\gamma_f(G)$ and $\omega_{th}$**  We claim that the event frequency $\eta$ is linear to $\gamma_f(G)$, described as

$$\eta = k_0 \ast \gamma_f(G) + k_1 \quad (4.26)$$

We use historical data to train $k_0$ and $k_1$ by least square error criterion. Once we know $k_0$ and $k_1$, given a new $\gamma_f(G)$, the event number is estimated as $m = \lceil \eta \rceil$. Subsequently the threshold $\omega_{th}$ is set as the $m_{th}$ largest $W_f(s_j, a)$, for all $a \in V$, $0 \leq j \leq J$. 

Figure 4.12: Graph wavelet coefficient $W_f(s_1, a)$ and $W_f(s_2, a)$.

Table 4.1: The performance of graph wavelet vs. baseline and Z-score.

<table>
<thead>
<tr>
<th>Country</th>
<th>Method</th>
<th>Precision</th>
<th>Recall</th>
<th>F-measure</th>
</tr>
</thead>
<tbody>
<tr>
<td>Brazil</td>
<td>Baseline</td>
<td>0.052</td>
<td>0.104</td>
<td>0.060</td>
</tr>
<tr>
<td></td>
<td>Z-score</td>
<td>0.117</td>
<td>0.307</td>
<td>0.159</td>
</tr>
<tr>
<td></td>
<td>Graph wavelet</td>
<td>0.404</td>
<td>0.262</td>
<td>0.292</td>
</tr>
<tr>
<td>Mexico</td>
<td>Baseline</td>
<td>0.074</td>
<td>0.124</td>
<td>0.090</td>
</tr>
<tr>
<td></td>
<td>Z-score</td>
<td>0.221</td>
<td>0.147</td>
<td>0.168</td>
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<tr>
<td></td>
<td>Graph wavelet</td>
<td>0.397</td>
<td>0.384</td>
<td>0.408</td>
</tr>
<tr>
<td>Venezuela</td>
<td>Baseline</td>
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</tr>
<tr>
<td></td>
<td>Z-score</td>
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</tr>
<tr>
<td></td>
<td>Graph wavelet</td>
<td>0.292</td>
<td>0.554</td>
<td>0.355</td>
</tr>
</tbody>
</table>

4.4.3 Performance

The data for this experiment was gathered for three countries experiencing major protest events, namely Brazil, Mexico and Venezuela, from Jan 2013 to Dec 2014. Taking the Gold Standard Report (GSR) [73] as representing ground truth, we applied our new graph wavelet approach as follows. For each day, we determine whether there is any anomaly. If there is, we identify the group of anomalous cities and compare this set with the GSR to determine if the selected cities actually experienced protest events on that day and thus show how many of the model’s predictions matched the ground truth and how many did not. We use recall, precision, and the F-measure to evaluate the model’s performance. To evaluate the effectiveness of our new graph wavelet approach, we also compared the results with those obtained using intuitive approaches such as frequency based random assignment, referred to here as the baseline model, and z-score based selection methods. The baseline model was built according to the historical protest records for each city and thus the model’s predictions of the future occurrence of protests were based on frequency. The z-score approach entails selecting the group of cities whose z-score crosses some threshold, say $|z - score| > 3$. 
We compared the performance of these three models over the two year test period; the overall results are shown in Table 4.1. Generally speaking, the new graph wavelet approach exhibited better precision, recall, and F-measure scores than the baseline model across all three countries. The mean F-measure for the graph wavelet detection across models and countries is greater than that achieved by either of the other prediction models. Interestingly, the graph wavelet approach appears to operate at different efficiency levels for each country. From Figure 4.13 we can see that the graph wavelet model has a much higher recall in Venezuela than in Brazil, and an inferior quality of event detection in Mexico compared to Venezuela.

4.4.4 Case Studies

Case study 1: Iquique Earthquake, Chile. On April 1, 2014 at around 8:46 PM (local time) a large earthquake struck off the coast of Chile, northwest of the port city of Iquique. We show the distribution of absenteeism scores and normalized wavelet coefficient values of the graph wavelets from the beginning of this event and throughout the subsequent 24 hours period. As shown in Figure 4.14(a), we can clearly see absenteeism behavior, where the scores are dominated by very low (blue spectrum) z-score values (indicating high absenteeism). Likewise, Figure 4.14(b) depicts low coefficient values for the northern regions of Chile, where the impact of the earthquake was most significant. As the news of earthquake spread throughout the next day, user activity on social media increased. This bursty behavior is clearly visible on April 2nd, at around 11:00 AM. Figure 4.14(c) shows that the z-scores increase (red spectrum) significantly and the coefficient value distribution (Figure 4.14(d)) of the graph wavelets for northern regions of Chile are also in the red spectrum. The graph wavelet distributions in Figures 4.14(b) 4.14(d) show that the kernel area of the absenteeism/burst wavelets cover most large negative/positive values. In this way, the wavelets identify the abnormal negative/positive groups in absent/burst time intervals, respectively. Furthermore, a high correlation score of 0.726 was calculated for the wavelets from absenteeism and bursty periods of this episode, indicating a strong connection between the burst in activity and the previously observed absenteeism, signaling an event was detected.

The graph wavelets generated during the absenteeism time period Figure 4.14(b) have a central node located in the city of ‘Iquique’. Looking at the time series (Figure 4.14(e)) of Twitter activity for Iquique and the associated word clouds (Figure 4.14(f)), we can see how events unfolded during the course of the earthquake. Strong absenteeism is observed from 8:45 PM to 9:20 PM. Examining user mobility via their geotagged tweets from the city of Iquique, on April 1, 2014, the user mobility fraction had increased by 15.4%.

Case Study 2: Massive power outage in Venezuela. A massive power outage in Venezuela plunged several major cities, including the capital city Caracas, into darkness around 7:40 PM (local time) on December 2, 2013. News media reported\(^1\), that the power

\(^1\)http://www.usatoday.com/story/news/world/2013/12/02/power-failure-caracas-venezuela/3823327/
outage lasted for 10-15 minutes, and the people of Caracas quickly took to the streets to protest. This action at the beginning of the episode coincides with the absenteeism period detected by our algorithm. The scatter plots showing the distribution of absenteeism scores and wavelet coefficients (Figures 4.15(a), 4.15(b)) indicate that most of the low values are less than 0. Shortly after the absenteeism, we detected a huge burst in activity around 8:45 PM, signaled by the increased z-scores (low absenteeism) and coefficient values (Figures 4.15(c), 4.15(d)). A correlation score of 0.617 was calculated when comparing the graph wavelets from the absentee and burst periods.

The absenteeism related graph wavelets indicate that the city of Caracas was the central node. Taking a close look at the Twitter volume and tweets from Caracas and surrounding cities, there is a sharp decline in user activity around 7:40 PM and then a huge spike starting at 8:45 PM. The word clouds for the tweet content show a very similar story, with dominant words being ‘light’ and ‘blackout’; the Spanish phrase ‘sin luz’, which means ‘no light’, became a trending hashtag #sinluz on Twitter.

**Case Study 3: Christmas Day.** As noted earlier, absenteeism behavior may not always lead to a spike in activity. For example, our model detected strong absenteeism in social media activity for major holidays such as Christmas Day that was not followed by a bursty period in Twitter activity. This is likely because people tend to travel to visit family during the holidays. This is supported by low values of z-scores or high absenteeism in Figure 4.16(a) and wavelet coefficients in Figure 4.16(b) with respect to Argentinian tweets on December 25, 2013. Hence, no subsequent burst period was detected for this event. Interestingly as Christmas Day approached, Figure 4.16(c) shows that user mobility gradually increases and the z-score decreases, signaling greater absenteeism. We used Pearson’s correlation coefficient to measure the two time series and found a correlation score of -0.94.

## 4.5 Discussion

Previous research has demonstrated the importance of burst detection in Twitter. In this study, we argue that group absenteeism can also be vital for detecting disruptive societal events. Modeling absenteeism is crucial because it can serve as a surrogate signal for event detection. For example, in the case of the Iquique earthquake, our new algorithm detected absenteeism behavior on Twitter that was closely followed by a spike in user activity. Unlike traditional event detection methods, which identify real time events only after they have occurred because the burst signal must first be identified, an absenteeism signal can be observed much earlier, thus providing greater foresight into future events. This means that our proposed approach offers a significant advantage over current strategies that focus solely on modeling spike or burst related patterns for event detection.

Existing approaches for event detection also suffer from an inherent latency in their detection process. This is because they are based on the use of bursty signals from abnormal activity
on social networks, but miss the absenteeism signal that often precedes these bursts. Our approach addresses this shortcoming by successfully modeling the ‘hull before the storm’. In this study we defined an absenteeism score for groups of cities within the Twitter network and apply it to construct wavelet transforms that not only detect anomalous subgraphs (including both burst and absenteeism groups) at different scales, but can also be used to identify the geographical focal point of the anomaly. This localization property of graph wavelets guarantees that the selected groups are compact automatically. The identified abnormal groups have been verified using real-world datasets and proven to be indicative of events such as civil protests or natural disasters.
Figure 4.13: Brazil, Mexico and Venezuela protest detection performance.
Figure 4.14: Iquique Earthquake, Chile. (a-d) plots show differences in distributions of absenteeism score and wavelet coefficients calculated at 8:45 PM, April 1, 2014 (a-b) involving group absenteeism and later when burst in activity is captured at 11:00 AM, April 2, 2014 (c-d), respectively; (e) Tweet time series for Iquique on April 1, 2014; (f) Word cloud of tweets which mention ‘Iquique’.
Figure 4.15: Power Outage in Venezuela. (a-d) plots show differences in distributions of absenteeism score and wavelet coefficients calculated at 7:40 PM, December 2, 2013 (a-b) involving group absenteeism and later when burst in activity is captured at 8:45 PM in the same day (c-d), respectively; (e) Time series of tweets volume on December 2, 2013; (f) Word cloud of tweets mentioning ‘Caracas’.

Figure 4.16: The Christmas Day in Argentina: (a-b) plots show distributions of (a) absenteeism score and (b) wavelet coefficients calculated on December 25, 2013; (c) Time series comparing absenteeism score and user mobility corresponding to tweets between December 5 - 25, 2013.
Chapter 5

Epidemiological Modeling of Mass Movements

5.1 Introduction

This chapter was published in the ACM SIGKDD Workshop on Social Network Mining and Analysis (SNAKDD 2013) [45] and IEEE Computer, Volume 47, Issue 12, pages 90-94, Dec 2014 [46].

Online social networks have become a staging ground for modern movements, with the Arab Spring being the most prominent example. Nine out of ten Egyptians and Tunisians responded to a poll indicating that they used Facebook to organize protests and spread awareness. As a precautionary measure, governments have taken to blocking social networking websites, showcasing the importance of understanding this phenomenon.

Interestingly, the role of social networks is not limited to helping organize the activities of disruptive elements. Many key government and news agencies have also begun to embrace Twitter and other social platforms to disseminate information. After the tragic 2013 explosions at the Boston Marathon, the FBI resorted to online social networks to broadcast crucial information about the suspects. The viral diffusion of information provided them with vital information about the suspects. At the same time it is well known that online activity on sites such as Reddit led to mistaken identification of some individuals and the spread of several rumors.

We were motivated to apply the latest in epidemiological modeling to understand information diffusion on Twitter, in relation to the spread of both news and rumors. Epidemiological models provide a classical approach to study how information diffuses. These models typically divide the total population into several compartments which reflect the status of an individual. For instance, common compartments denote susceptible (S), exposed (E),
infected (I), and recovered (R) individuals. Individuals transit from one compartment to another, with certain probabilities that have to be estimated from data. The simplest model, SI, has two states; susceptible (S) individuals get infected (I) by one of their neighbors and stay infected thereinafter. While conceptually easy to understand, it is also unrealistic for practical situations. The SIS model is popular in infectious disease modeling wherein individuals can transition back and forth between susceptible (S) and infected (I) states (e.g., think of allergies and the common cold); this model is often used as the baseline model for more sophisticated approaches. The SIR model enables individuals to recover (R) but is not suited for modeling news cascades on Twitter since there is no intuitive mapping to what ‘recovering’ means. The SEIZ model (susceptible, exposed, infected, skeptic) proposed by Bettencourt et al. [7] takes the interesting approach of introducing an exposed state (E). Individuals in such a state take some time before they begin to believe (I) in a story (i.e., get infected). While the authors of [7] used this approach to model the adoption of Feynman diagrams by communities of physicists, our work explores their use in modeling news and rumors on Twitter.

The key contributions of this chapter are:

- Our work is the first to employ the SEIZ model to model real Twitter datasets. We employ non-linear least squares optimization of the underlying systems of ODEs over tweet data, and demonstrate how this model is better at modeling rumor and news diffusion than the traditional SIS model.

- We analyze eight representative stories (four true events and four rumors) across a range of topics (politics, terrorism, entertainment, and crime) and over several geographic regions (USA, Mexico, Venezuela, Cuba, Vatican). While not an exhaustive list, this demonstrates the wide applicability of the proposed model.

- We demonstrate the capability of the SEIZ model to quantify compartment transition dynamics. We showcase how such information could facilitate the development of screening criteria for distinguishing rumors from real news happenings on Twitter.

5.2 Datasets

We focus on twitter datasets that have reliable coverage of the events being studied; the volume of tweets ranges from as low as 791 to nearly three orders of magnitude greater. As described in Table 5.1, the news and rumors studied were drawn from a variety of regions and across a diversity of topics. Data collection was aimed at gathering tweets highly related to the events under study. We employed customized sets of keywords and hashtags pertaining to each incident. Finally, date range restrictions were used to define relevant tweets for each event. It is also pertinent to note that the tweets analyzed spanned a variety of languages: English, Spanish, Italian, and Portuguese.
Table 5.1: Twitter datasets studied in this chapter.

<table>
<thead>
<tr>
<th>No.</th>
<th>Dataset</th>
<th>Date</th>
<th>Area</th>
<th>Type</th>
<th>Country</th>
<th>#Tweets</th>
<th>Response ratio</th>
<th>Keywords &amp; Hashtag</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Boston</td>
<td>04-15-2013</td>
<td>terrorism</td>
<td>news</td>
<td>USA</td>
<td>501259</td>
<td>68.3%</td>
<td>Marathon, (#)bostonmarathon</td>
</tr>
<tr>
<td>2</td>
<td>Pope</td>
<td>02-11-2013</td>
<td>religion</td>
<td>news</td>
<td>Vatican</td>
<td>31365</td>
<td>56.75%</td>
<td>Pope, (#)Benedict</td>
</tr>
<tr>
<td>3</td>
<td>Amuay</td>
<td>08-25-2012</td>
<td>accident</td>
<td>news</td>
<td>Venezuela</td>
<td>49015</td>
<td>62.89%</td>
<td>Amuay, refinery, explosion</td>
</tr>
<tr>
<td>4</td>
<td>Michelle</td>
<td>02-24-2013</td>
<td>entertainment</td>
<td>news</td>
<td>USA</td>
<td>3762</td>
<td>54.45%</td>
<td>Michelle Obama, Oscars</td>
</tr>
<tr>
<td>5</td>
<td>Obama</td>
<td>04-23-2013</td>
<td>politics</td>
<td>rumor</td>
<td>USA</td>
<td>791</td>
<td>46.14%</td>
<td>White House, explosions</td>
</tr>
<tr>
<td>6</td>
<td>Doomsday</td>
<td>12-21-2012</td>
<td>mythology</td>
<td>rumor</td>
<td>Global</td>
<td>11833</td>
<td>52.19%</td>
<td>Doomsday, Mayan, doom</td>
</tr>
<tr>
<td>7</td>
<td>Castro</td>
<td>10-16-2012</td>
<td>politics</td>
<td>rumor</td>
<td>Cuba</td>
<td>3969</td>
<td>54.45%</td>
<td>Fidel Castro, Dr. Marquina</td>
</tr>
<tr>
<td>8</td>
<td>Riot</td>
<td>09-05-2012</td>
<td>crime</td>
<td>rumor</td>
<td>Mexico</td>
<td>4831</td>
<td>47.17%</td>
<td>Antorcha Campesina, Nezahualcoyotl</td>
</tr>
</tbody>
</table>

5.2.1 News Topics

**Boston Marathon Bombings.** Two pressure cooker bombs exploded near the finish line of 2013 Boston Marathon on April 15, 14:49:12 local time, killing three people and injuring more than 264 others. The FBI released photographs and surveillance videos on online social networks which spread like wildfire and provided crucial leads for identifying the suspects.\(^1\)

**Pope Resignation.** Pope Benedict XVI announced his resignation on the morning of February 11, 2013. In nearly 6 centuries, this was the first time a pope has stepped down from his office. This news received reactions from all across the world.\(^2\)

**Amuay Refinery Explosion.** Propane and butane gas leakage caused an explosion at the Amuay refinery in Venezuela on August 25, 2012 1:11 am local time. The blast killed 48 people, injured 151 others and damaged 1600 homes.\(^3\)

**Michelle Obama at the 2013 Oscars.** In the 2013 Oscar awards ceremony, a big surprise was the appearance of US first lady Michelle Obama for presenting the ‘Best Picture’ award.\(^4\)

5.2.2 Rumors

**Obama injured.** A fake associated press (AP) tweet originated on April 23, 2013 that President Obama was hurt in White House explosions which caused a brief period of instability in financial markets. The information was false and it was determined that the Twitter account was hacked.

**Doomsday.** December 21, 2012 was rumored to be the Doomsday as it marked the end date of a 5126 year long cycle in the Mesoamerican long count calendar. This rumor spread like wildfire and social networks were flooded with panic and anxiety posts. Considering

---

\(^1\)http://www.cnn.com/2013/04/15/us/boston-marathon-explosions

\(^2\)http://www.cnn.com/2013/02/11/world/europe/pope-resignation-q-and-a

\(^3\)http://www.cnn.com/2012/08/25/world/americas/venezuela-refinery-blast

that we are still alive, Doomsday turned out to be nothing more than a rumor on a massive scale\(^5\).

**Fidel Castro’s death.** On October 16, 2012 a Naples doctor claimed that former Cuban leader, Fidel Castro suffered a cerebral hemorrhage and is near a neurovegetative state. However, on October 21, 2012, these rumors were denied by Elias Jauva, former Venezuelan vice president, who released pictures of him meeting Castro a few days back\(^6\).

**Riots and shooting in Mexico.** A very interesting example that highlights the perils of rumor spreading on social networks pertains to the false reports of violence and impending attack in Nezahualcóyotl, Mexico. (False) rumors spreading on Twitter and Facebook about shootouts caused (real) panic and chaos in Mexico City on September 5, 2012. Interestingly, authorities themselves turned to Twitter to deny these rumors\(^7\).

\(^5\)http://en.wikipedia.org/wiki/Doomsday
\(^7\)http://www.foxnews.com/world/2012/09/08/tweets-false-shootouts-cause-panic-in-mexico-city/
5.2.3 Preliminary Analysis

We compare the basic properties of news and rumor propagation, by characterizing tweet volume over time, follower/followee distributions, the ‘response ratio’ of a story, and the retweet cascades. In order to maintain brevity, we show results from only two stories in this section: one from our news collection (the Amuay explosion) and one from our rumor collection (Fidel Castro’s purported death).

Tweet Volume. For both examples, we plot the tweet volume over time from the beginning of the story. Figure 5.1(a) shows the activity for the 2012 Amuay refinery explosion example. An activity burst was formed immediately after the news was made public. The number of tweets dropped progressively as the days went by. This activity trend displays attributes similar to breaking news propagation as described by Mendoza et al. [60]. In contrast, Figure 5.1(b) depicts the volume of tweets about a rumor regarding the health of the former Cuban leader Fidel Castro. Here we see occasional spikes of tweet volume; note the increase in tweet volume around October 21st, when the rumors were officially denied.

Followers and Followees Distributions. Figure 5.2(a) is a log-log scatter plot of the followers/followees distribution about the Amuay explosion news, and Figure 5.2(b) is the corresponding plot about Fidel Castro’s death rumor. There is no significant qualitative or quantitative difference in this case; in particular both plots show that the number of followees is less than the number of followers.

Response Ratio. A tweet can either be a post made by the user’s initiative, or a responsive post to some other user’s post (e.g., retweets and replies). As Starbird et al. [89] discuss,
retweets reveal how information propagates through a social network: the ‘deeper’ a retweet, the more relevant the tweet is for the community. Based on this idea, we define the response ratio of a story as the fraction of responsive tweets to the total number of tweets in the story. Table 5.1 lists the response ratio for all the 8 stories. As we can see, response ratios for news are higher than that for the rumors.

Retweet Cascades. A retweet cascade reflects how the social media network propagates information. Figure 5.3 depicts the evolution of the retweet graphs for the Amuay news and Castro rumor dataset. For Amuay news, we plot four graphs with intervals of 6 hours, depicting that a burst has been formed during 6am-12am, only 5 hours after the accident. Fig. 5.3(b) shows the retweet graphs of the rumor for several days. We can see even after one day, there is no burst of tweets related to this rumor. Compared with the network between the news and rumors, we find several features about the rumor. 1) The network for the news instance is more complex and users can obtain news from many sources, while users obtain the rumor information only from limited information centers. 2) There is an immediate burst after a news is made public while there is no obvious burst for the rumors.

5.3 Our Approach

As stated earlier, we used compartmental population models to quantify the propagation of news and rumors on Twitter, focusing primarily on the SIS and SEIZ models.

5.3.1 SIS

As described earlier, this model divides the population into two compartments, or classes: susceptible and infected. Note that in this model, infected individuals return to the susceptible class on recovery because the disease confers no immunity against reinfection.

In order to adapt this model for Twitter, we have given new meaning to these terms. An individual is identified as infected (I) if he posts a tweet about the topic of interest, and susceptible (S) if he has not. A consequence of this interpretation is that an individual posting a tweet is retained to the infected compartment indefinitely; hence, he can not propagate back to the susceptible class as is possible in an epidemiological application. At any given time period t, we use N(t) to denote the total population size, S(t) the susceptible population size, and I(t) the infected population size, such that N(t) = I(t) + S(t). As shown in Figure 5.4, the SIS spreading rule can be summarized as follows:

- An individual that tweets about a topic is regarded as infected.
- A susceptible person has not tweeted about the topic.
• A susceptible person coming into contact with an infected individual (via a tweet) becomes infected himself, thus immediately posting a tweet.

• Susceptible individuals remain so until coming into contact with an infected person.

The SIS model is mathematically represented by the following system of ordinary differential equations (ODEs) [63]:

\[
\frac{d[S]}{dt} = -\beta SI + \alpha I \quad (5.1a)
\]

\[
\frac{d[I]}{dt} = \beta SI - \alpha I \quad (5.1b)
\]
5.3.2 SEIZ

One drawback of the SIS model is that once a susceptible individual gets exposed to disease, he can only directly transition to infected status. In fact, especially on Twitter, this assumption does not work well; people's ideologies are complex and when they are exposed to news or rumors, they may hold different views, take time to adopt an idea, or even be skeptical to some facts. In this situation, they might be persuaded to propagate a story, or commence only after careful consideration themselves. Additionally, it is quite conceivable that an individual can be exposed to a story (i.e. received a tweet), yet never post a tweet themselves.

Based on this reasoning, we considered a more applicable, robust model, the SEIZ model which was first used to study the adoption of Feynman diagrams [7]. In the context of Twitter, the different compartments of the SEIZ model can be viewed as follows: Susceptible (S) represents a user who has not heard about the news yet; infected (I) denotes a user who has tweeted about the news; skeptic (Z) is a user who has heard about the news but chooses not to tweet about it; and exposed (E) represents a user who has received the news via a tweet but has taken some time, an exposure delay, prior to posting. We note that referring to the Z compartment as skeptics is in no way an implication of belief or skepticism of a news story or rumor. We adopt this terminology as this was the nomenclature used by the original authors of the SEIZ model [7].

A major improvement of the SEIZ model over the SIS model is the incorporation of exposure delay. That is, an individual may be exposed to a story, but not instantaneously tweet about it. After a period of time, he may believe it and then be promoted to the infected compartment. Further, it is now possible for an individual in this model to receive a tweet, and not tweet about it themselves. As shown in Figure 5.5, SEIZ rules can be summarized as follows:

- Skeptics recruit from the susceptible compartment with rate $b$, but these actions may result either in turning the individual into another skeptic (with probability $l$), or it may have the unintended consequence of sending that person into the exposed (E) compartment with probability $(1 - l)$.

- A susceptible individual will immediately believe a news story or rumor with probability $p$, or that person will move to the exposed (E) compartment with probability $(1 - p)$.

- Transitioning of individuals from the exposed compartment to the infected class can be caused by one of two separate mechanisms: (i) an individual in the exposed class has further contact with an infected individual (with contact rate $\rho$), and this additional contact promotes him to infected; (ii) an individual in the exposed class may become infected purely by self-adoption (with rate $\epsilon$), and not from additional contact with those already infected.
Table 5.2: Parameter definitions in SEIZ model[7]

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Definition</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta$</td>
<td>S-I contact rate</td>
</tr>
<tr>
<td>$b$</td>
<td>S-Z contact rate</td>
</tr>
<tr>
<td>$\rho$</td>
<td>E-I contact rate</td>
</tr>
<tr>
<td>$\epsilon$</td>
<td>Incubation rate</td>
</tr>
<tr>
<td>$1/\epsilon$</td>
<td>Average Incubation Time</td>
</tr>
<tr>
<td>$bl$</td>
<td>Effective rate of S -&gt; Z</td>
</tr>
<tr>
<td>$\beta \rho$</td>
<td>Effective rate of S -&gt; I</td>
</tr>
<tr>
<td>$b(1-l)$</td>
<td>Effective rate of S -&gt; E via contact with Z</td>
</tr>
<tr>
<td>$\beta(1-p)$</td>
<td>Effective rate of S -&gt; E via contact with I</td>
</tr>
<tr>
<td>$l$</td>
<td>S-&gt;Z Probability given contact with skeptics</td>
</tr>
<tr>
<td>$1-l$</td>
<td>S-&gt;E Probability given contact with skeptics</td>
</tr>
<tr>
<td>$p$</td>
<td>S-&gt;I Probability given contact with adopters</td>
</tr>
<tr>
<td>$1-p$</td>
<td>S-&gt;E Probability given contact with adopters</td>
</tr>
</tbody>
</table>

The SEIZ model is mathematically represented by the following system of ODEs. A slight difference of our implementation of this model is that we do not incorporate vital dynamics, which includes the rate at which individuals enter and leave the population $N$ (represented by $\mu$ [7]). In epidemiological disease applications, this encompasses the rate at which people become susceptible (e.g. born) and deceased. In our application, a Twitter topic has a net duration not exceeding several days. Thus, the net entrance and exodus of Twitter users over these relatively short time periods is not expected to noticeably impact compartment sizes and our ultimate findings$^8$.

\[
\begin{align*}
\frac{d[S]}{dt} &= -\beta S \frac{I}{N} - bSZ \frac{Z}{N} \quad (5.2a) \\
\frac{d[E]}{dt} &= (1-p)\beta S \frac{I}{N} + (1-l)bSZ \frac{Z}{N} - \rho E \frac{I}{N} - \epsilon E \quad (5.2b) \\
\frac{d[I]}{dt} &= p\beta S \frac{I}{N} + \rho E \frac{I}{N} + \epsilon E \quad (5.2c) \\
\frac{d[Z]}{dt} &= lbSZ \frac{Z}{N} \quad (5.2d)
\end{align*}
\]

$^8$http://www.statisticbrain.com/twitter-statistics/
5.3.3 Practical Issues

During our adoption of the SIS and SEIZ models to understand Twitter datasets, we were constrained by several factors. The first constraint was the unknowns in the models. For example, we do not know the transition rates between the compartments nor the initial sizes of the compartments.

![Figure 5.7: Best fit modeling for Boston news.](http://example.com/fig5.7.png)

![Figure 5.8: Best fit modeling for Pope news.](http://example.com/fig5.8.png)

Table 5.3: Fitting error of SIS and SEIZ models

<table>
<thead>
<tr>
<th></th>
<th>Boston</th>
<th>Pope</th>
<th>Amuay</th>
<th>Michelle</th>
<th>Obama</th>
<th>Doomsday</th>
<th>Castro</th>
<th>Riot</th>
<th>Average</th>
</tr>
</thead>
<tbody>
<tr>
<td>SIS</td>
<td>0.058</td>
<td>0.041</td>
<td>0.058</td>
<td>0.056</td>
<td>0.102</td>
<td>0.026</td>
<td>0.098</td>
<td>0.093</td>
<td>0.050</td>
</tr>
<tr>
<td>SEIZ</td>
<td>0.010</td>
<td>0.004</td>
<td>0.027</td>
<td>0.064</td>
<td>0.101</td>
<td>0.029</td>
<td>0.073</td>
<td>0.003</td>
<td>0.050</td>
</tr>
</tbody>
</table>

Another constraint is the inability to quantify the total population size. This value appears to simply be the total number of Twitter accounts; however the value that we truly want is the number of individuals who could be exposed to the news or rumor topic. This value shows to be very different from the total number of Twitter accounts. Consider the ~175 million (M) registered Twitter accounts. Of these, (i) ~90 million have no followers, and (ii) ~56 million follow no one\(^9\). To further complicate the matter, there exists an

\(^9\)http://www.businessinsider.com/chart-of-the-day-how-many-users-does-twitter-really-have-2011-3
abundance of “fake” Twitter accounts, which are never used by any real person. They are simply sold to users wishing to enhance their perceived popularity. Coupling these facts with sporadic Twitter usage due to night-time inactivity and user “unplugging”, it is clear that establishing a reliable estimate of users who could receive a tweet is quite difficult.

Synthesizing all of these factors, we assume the following in our SEIZ model implementation:

1. We do not have reliable population specifics.
   
   (a) We do not know $N$, total population size.
   
   (b) We do not know $S(t_0), E(t_0), I(t_0)$, or $Z(t_0)$, the initial values of each population compartment.

2. **Infected** individuals ($I$) submit a tweet.

3. **Skeptics** ($Z$) have been exposed to story, but do not tweet.

4. Vital dynamics do not contribute to the overall population size. Thus, $N$ is a constant.

The implication of these assumptions is that total population size $N$ and initial population sizes for each compartment $S(t_0), E(t_0), I(t_0)$, and $Z(t_0)$ are viewed as unknowns. They are
therefore treated as parameters in the parameter fit routine, and fit along with the other model parameters [7].

5.3.4 Parameter Identification

For each of the population models (SIS and SEIZ), represented by equation sets 5.1 and 5.2, we performed a nonlinear least squares fit of the model to Twitter data. As shown in Figure 5.6, each step of this fitting process involved selecting a set of parameter values (rate constants and probabilities in equations 5.1 and 5.2, and initial compartment sizes), and numerically solving the system of ODEs with these parameter values. The set of parameter values that minimized $|I(t) - tweets(t)|$ was identified as the optimal parameter set.

The experimental implementation was done in Matlab. The `lsqnonlin` function performed the least squares fit. The ODE systems were solved with a forward Euler function that we developed. This algorithm was selected due to its computational efficiency, and used a time-step of no more than 0.05. This threshold demonstrated to be numerically stable; in several instances we compared the forward Euler solution to those generated by Matlab’s `ode45` ($5^{th}$-order Explicit Runge-Kutta with embedded $4^{th}$-order error control), and observed
nearly identical solutions.

![Figure 5.13: Best fit modeling for Castro rumor.](image)

![Figure 5.14: Best fit modeling for Riot news.](image)

5.4 Experimental Results

5.4.1 Fitting Results

For each of the Twitter datasets, we were interested in quantifying the transitions of users through the different compartments of the SIS and SEIZ models. Figures 5.7 - 5.14 display the results for the best fit of SIS and SEIZ models (Equations 5.1 and 5.2) to the eight Twitter stories. Also displayed for each figure are the relative error in 2-norm

$$\frac{||I(t) - tweets(t)||_2}{||tweets(t)||_2}$$

and the mean error deviation

$$\frac{\sum_{i=1}^{n} |I(t_i) - tweets(t_i)|}{n},$$
where \( n \) is the number of data points.

The error metrics for these eight stories clearly indicate that the SEIZ model fits the Twitter data much more accurately than the SIS model. Furthermore, the low relative error of the SEIZ model fit suggests that this model accurately represents the Twitter data for each of the eight stories; see Table 5.3. A common observation about all the eight stories is that the SEIZ model is far more accurate in modelling the initial spread of the news on Twitter as compared with the SIS model. This behaviour can be explained by the delay caused by individuals in the “Exposed” category taking some time before posting a story themselves [7].

Given that the SEIZ model is superior to the SIS model in this application, and that the SEIZ model demonstrates an accurate representation of information diffusion on Twitter, a natural question arises “How can this model help us?” The answer is really simple. Since
we have a mathematical model for the Twitter data, we can study solutions to some of the constraints as mentioned in the “Practical Issues” section. A well fitted SEIZ model provides values for all contact rates and transition probabilities as defined by Equation 5.2. These parameters empower us to investigate the dynamics of news and rumor spread on Twitter in a fashion that is not possible without a mathematical model. Table 5.2 specifies the SEIZ model parameters that we can now examine to assess news and rumor propagation on Twitter.

5.4.2 Boston Marathon Bombing Analysis

To demonstrate a line of analysis that is now possible with the SEIZ mathematical model, we use quantities from the SEIZ model fit of the Boston Marathon bombing Twitter data (Table 5.2). Results are summarized in Table 5.4.

Here we discuss the dynamics of all 4 compartments, so we specially show all 4 compartments in the SEIZ time-course plot only for Boston Marathon bombing (Figure 5.15(a)). These results suggest that the effective rate of susceptible individuals becoming skeptics is much greater than those that becoming infected. The decrease in $S(t)$ occurs directly with an increase in $Z(t)$, and $S(t)$ becomes stable at the same time that $Z(t)$. $I(t)$ does increase as $S(t)$ decreases, but its rate of change is much slower, and the majority of $I(t)$ increase occurs after $S(t)$ has stabilized to a minimal value, demonstrating that the continued change in the infected compartment has no further influence on the change in the susceptible compartment.

Table 5.4 also demonstrates that the skeptics compartment is more influential on transitioning susceptible users to the exposed class than does infected users. Figure 5.15(a) shows this as the increase in $E(t)$ is strongly correlated with the increase in $Z(t)$. $E(t)$ also peaks as $Z(t)$ peaks, and $E(t)$ begins to decrease at a rate negative to that of the $I(t)$ increase. In fact, the increase in $I(t)$ directly coincides with a comparable decrease in $E(t)$. These data suggest that the increase in infected users is not due in large part by recruitment of susceptible users, but rather from the natural transition to the infected compartment by exposed individuals.

Putting this all together, we can deduce that virtually all individuals are initially in the susceptible compartment. Most susceptible users become skeptics from interaction with skeptics, and those susceptible users that do transition to the exposed class do so by their interaction with skeptics. The infected compartment increases predominately from the exposed class, and not from direct recruitment of susceptible individuals. Thus, these findings suggest that it was in-fact non-Twitter mediums that most greatly aided in the generation of Twitter propagation! Further, the $\epsilon/\rho$ ratio indicates that the exposed users became infected more so due to information incubation and self-adoption, and not so much from direct contact with infected users.

The remaining instances of SEIZ time-course plots are shown in Figure 5.15, we can see how
S, E, and I dynamic change over time. These analyses exemplify the types of analyses that can be used to study Twitter dynamics via the SEIZ population model.

### 5.4.3 Rumor Detection

We next examined if our implementation of the SEIZ model, applied to our Twitter examples, could be utilized to facilitate the discrimination of true news from rumors. We began by assembling an equation to relate the key parameters of the SEIZ model. In our first attempt at performing this, we restricted our attention to the exposed compartment; this class has direct or indirect interconnections between the other three compartments, and is a key path to the infected compartment. To exemplify this, consider the extreme case where susceptible individuals are attempted to be recruited by skeptics, and ultimately end up in the infected compartment (Figure 5.5). This can only be accomplished by passing through the exposed compartment.

We quantify a ratio through $E$ as the ratio of the sum of the effective transition rates entering this compartment (from $S$) to the sum of the transition rates exiting this compartment (to $I$). We define this ratio as $R_{SI}$, using the subscripts to denote the contributions from the susceptible and infected compartments in this quantity:

$$R_{SI} = \frac{(1-p)\beta + (1-l)b}{\rho + \epsilon}$$  \hspace{1cm} (5.3)

$R_{SI}$ possesses all rate constants and probability values of the SEIZ model and relates them to the exposed compartment with a kind of flux ratio, viz. the ratio of effects entering $E$ to those leaving $E$. A $R_{SI}$ value greater than 1 implies that the influx into the exposed compartment is greater than the efflux. Similarly, a value less than 1 indicates that members are added to the exposed group more slowly than they are removed. We hypothesized that this measure could potentially aid in the distinction of rumor topics from news topics; all parameters of the SEIZ fit are utilized in this measure, and they are related via the $R_{SI}$ value to a key compartment of this model. If a distinction between rumors and true news...
stories is to be seen with the SEIZ model, we identify the $R_{SI}$ measure to be a probable candidate in aiding this process.

![Figure 5.16: Ultimate $R_{SI}$ values for eight Twitter datasets.](image)

**Ultimate $R_{SI}$ value** We then computed $R_{SI}$ using the specific parameter values attained from our model fits of the eight cases (Figure 5.16). Here we can see that the true news about the Boston Marathon bombing, Pope resignation, and Amuay refinery explosion do in fact have much higher $R_{SI}$ values than the rumor topics: Doomsday, Fidel Castro death, Mexico City riots, and Barrack Obama injury which each have much lower $R_{SI}$ values. However, the Michelle presence at the Oscars, which is classified as true news, has a very low $R_{SI}$ value. This particular case is interesting since Michelle did not really show up to the 2013 Oscar Awards Ceremony. She simply participated remotely via video telecast. It is thus arguable that this topic could have been discussed in the media in terms similar to rumors.

**Dynamic $R_{SI}$ value** For one story, if we collect related Tweets at the very beginning stage, then the $R_{SI}$ value would be a time series. Figure 5.17 shows the dynamic $R_{SI}$ values for Castro rumor and Boston bombing real news. We can see for the Castro rumor, at the beginning stage, the $R_{SI}$ value was pretty high, which indicate considerable people believe this story. With time pass by, the $R_{SI}$ values decreased sharply. However, for the Boston Marathon bombing real news, the $R_{SI}$ value was very low at beginning, but increased rapidly within several hours and reached around 28.31 very soon. The $R_{SI}$ time series indicate people’s confidence with those stories is dynamically changing.

These findings suggest, for these specific topics, that the parameters in the SEIZ model can potentially aid in the challenge of distinguishing rumor versus true news. We are not
claiming that the $R_{SI}$ value is the unique measure to accomplish this, nor are we claiming that the SEIZ model itself is the sole tool to do this. As is suggested by our findings, we postulate that a fit of a compartmental model, in the spirit of the SEIZ model, to Twitter data provides valuable propagation information that can be coupled with other data analysis strategies (e.g., content modeling) to augment the accuracy and reliability of true news story and rumor topic discrimination.

5.5 Case Study of Ebola Related Rumor

Mark Twain is credited with saying that a lie can travel halfway around the world while the truth is putting on its shoes. As the Ebola disease rages on in West Africa, the only other epidemic being talked about is the rapid spread of misinformation on social media about the disease, its origins and impact, and response strategies. We sought to characterize the spread of both news and rumors on Twitter about the deadly disease with a view to understanding the prevalence of misinformation.

For context, although Ebola is not a new disease, the current outbreak happening in West Africa is believed to be more than three times worse than all the previous Ebola outbreaks in history combined. The three countries that have the most widespread transmission, viz. Guinea, Liberia, and Sierra Leone, are also those where public health experts fear massive under-reporting due to a variety of social considerations. Even syndromic surveillance strategies, e.g., social media mining and participatory surveillance, are not effective in these countries due to poor penetration of Internet use, and lack of roads and communication infrastructure where Ebola is most prevalent.

Social media has become one of the primary sources by which people learn about worldwide
developments so it is instructive to study the spread of Ebola related information on Twitter. Most of the current chatter on Twitter about Ebola reached its peak during late Sept-mid Oct (2014) during which period there have been Ebola-related developments in the US and Europe. (In contrast, Twitter penetration in the three specific West African countries is low.)

A brief timeline of these developments will help in the discussion that follows. On September 30, 2014, the CDC confirmed the first importation of Ebola into the United States when Thomas Eric Duncan traveled from Liberia to visit family in Dallas. On October 6, in Madrid, Spain, Teresa Romero, a nurse, was reported to be the first person to have contracted the disease outside of West Africa.

On October 8, back in the US, Duncan succumbed to Ebola. A few days later, a healthcare worker at Texas Presbyterian Hospital in Dallas who provided care for Duncan, tested positive for Ebola. On the morning of Oct. 14, a second healthcare worker, who also provided care for Duncan, reported to the hospital with a low-grade fever and was isolated. This healthcare worker also tested positive for Ebola subsequently.

Many states and cities began making contingency plans and issuing travel advisories and guidelines. Lawmakers called for screening passengers and proposed travel bans for Ebola-stricken countries. On October 23, Craig Spencer, a doctor returning from work in Guinea, was rushed to Bellevue Hospital Center with a 100.3 fever and became New York City’s first Ebola patient.

### 5.5.1 Rumors on Twitter

![Word clouds constructed from Ebola-related tweets.](image)

The period from end of Sept to mid-late Oct, when Ebola activity happened in the US, is also the period when conspiracy theories, innuendo and rumors began to propagate wildly on Twitter. We gathered tweets during this period and filtered them by either the mention of the keyword ‘ebola’ or relevant hashtags such as #ebola, #EbolaVirus, #EbolaOutbreak, #EbolaWatch, #EbolaEthics, #EbolaChat, #nursesfightebola, #ebolafacts, #StopEbola, #FightingEbola, and #UHCRevolution.
From the gathered tweets, we removed stopwords for further processing. Figure 5.18 depicts word clouds constructed from the tweets for specific days. As can be seen, on 2014-09-29, when there was no Ebola incident in the US, people’s attention were primarily focused on Liberia and other African countries. On 2014-09-30, after CDC confirmed that Mr. Duncan in Dallas tested positive for Ebola, related keywords rose to the fore.

Figure 5.19: Top 10 Ebola-related rumors (by volume; from 09/28/2014 to 10/18/2014).

Two other rumors are noteworthy. The ‘snake’ rumor (which originated at least as early as late summer 2014) asserts that Ebola came across the border from Guinea to Sierra Leone via a snake in a bag. As stated in [4], “a lady had a snake in a bag. When somebody opened the bag, that made the lady die.” The Maldives rumor pertains to an uncorroborated report that Ebola patients have been reported (and quarantined) in the Maldives.

For each of these rumors, we geocoded tweets participating in the spread of such rumors with a view to understanding their geographical scope. As Figure 5.20 shows, the “airborne” and “inject” rumors were most prevalent in the US with specific other rumors (e.g., “patent”) being prevalent in other parts of the world.

Next, we employed a dynamic query expansion model [108] to study the rumors in greater detail. The DQE model begins with a seed set of keywords (e.g., “ebola”, “rumor”), identifies tweets that mentions these keywords, and iteratively expands them into a larger set of keywords. By conducting a modularity-based optimization over the underlying network of expanded tweets connected by shared keywords, DQE can identify specific localized instantiations of rumors.

As shown in Figure 5.21, on 09/29/2014 (when there was no incidence of Ebola in the US),
74

Figure 5.20: Distribution of top-10 rumors obtained from geolocated tweets. Data from 10/08/2014 is used for this plot. Icon size is proportional to the logarithm of the tweet volume.

the dominant rumor is the zombie rumor. By 10/06/2014, other rumors pertaining to how Ebola can be airborne and that it is a potential terrorist weapon gained hold.

Although Figure 5.21 might suggest that rumors are quite rampant, it is important to keep in perspective that they are but a small fraction of all information propagation related to Twitter. Figure 5.22 and 5.23 compare the time-indexed spread of the ‘patent’ rumor versus a true news story (about the first US incidence of Ebola in Dallas). Here different colors denote different communities participating in information propagation, not different rumors/news stories. Each node in these graphs denotes a Twitter user, and an edge between nodes denotes a reply or retweet relationship. As can be seen, news stories permeate better whereas rumors are more localized, distributed, and comparatively smaller in permeation.

5.5.2 Epidemiological Modeling of Rumors

Another way to study the spread of rumors (versus news) is from an epidemiological modeling standpoint. An epidemiological model helps capture the likelihood of an individual getting infected with a virus or, here, of adopting an idea that he or she has been exposed to.

In earlier work [45] we demonstrated how we can accomplish this objective using the SEIZ epidemiological model that was originally proposed to study the adoption of ideas [7]. The SEIZ model is particularly suited to studying rumor propagation as it captures distinctions in how people respond to ideas: whether they adopt it readily or are initially skeptical.
Figure 5.21: How rumors cluster: (a) 09/29/2014. (b) 10/06/2014. Rumors are color coded consistently across the two frames.

The idea in the SEIZ model is to compartmentalize a population into four categories, denoted as S, E, I, and Z. We interpret these categories with specific reference to Twitter propagation. Susceptible (S) represents a user who has not heard the information; infected (I) denotes a user who has (re)tweeted about the information; skeptic (Z) denotes a user who has heard about the information but chooses not to (re)tweet about it; and exposed (E) represents a user who has received the information via a tweet but has taken some time, an exposure delay, prior to reposting or sharing that information.

The transitions between these states are modeled as shown in Fig 5.24. We caution that referring to the Z compartment as a “skeptic” is in no way an implication of the underlying truth or falsehood of the information; it simply helps capture whether users readily adopt an idea or take some time to adopt it.

Model fits of SEIZ to the different rumors and time course information for each of the state variables is given in Figure 5.25. As can be seen the SEIZ model is capable of capturing a variety of information spread patterns: quasi-linear (e.g., ‘patent’), sigmoidal (‘white’), and other non-linear patterns (‘zombies’ and ‘airborne’).

Time course results from the SEIZ compartmental model as shown in Figure 5.25 depict broadly similar patterns. Here ‘N’ denotes the total size of the population (distinct Twitter users). High values of S rapidly decrease with a relatively comparable increase in Z, and a gradual increase in I that continues as E decreases. However, the patent rumor time-course data has a noticeably different response profile than the other rumor examples.

Here, the initial value of the S group begins with less than half of the total population size,
Figure 5.22: Ebola-related patent rumor propagation over time.

Figure 5.23: Ebola-related Dallas news propagation over time.

and only slightly higher than the initial values of the Z and E groups. Second, the Z group is essentially constant, meaning that the number of skeptics does not change throughout the propagation time course. Third, the decrease in S does not correspond to a change in Z, as is observed in the other rumor examples. Rather, the drop in S is met with a near identical increase in E.

These findings hint that a large influx into E without a corresponding efflux to I combined with a stagnant Z group will produce an elevated response ratio. In other words, there is a large exposure to the rumor topic without significant change in skepticism.

In our earlier work on characterizing rumors [45], we defined the notion of a ‘response ratio’ which quantifies transitions through the exposed compartment. The response ratio provides a relative measure of the population influx into the E compartment versus the efflux from this compartment. We hypothesize that this ratio could be one of the factors useful in
discriminating rumors from true news, with larger response ratios associated with factual news topics.

To compare response ratios across rumor and news, we select three breaking (true) news stories pertaining to Ebola: ‘Dallas’ refers to the story of the first Ebola patient (Duncan) identified in the US; ‘NYC’ refers to the first confirmation of an Ebola patient (Spencer) in New York City; and ‘Spencer’ refers to the specific symptoms and travel activities of Spencer in the days before he was diagnosed.

**Ultimate $R_{SI}$ value** The ultimate response ratios for these three news stories and other rumors are shown in Figure 5.26. It can be seen that all three news stories (blue bars) have response ratios higher than 25, with a mean value of approximately 38, while eight of the 10 rumors stories (red bars) have a response ratio less than or equal to 6.4, with a mean of only 3.33. Two of the 10 rumors (green bars; ‘paten’ and ‘airborne’) have elevated response values, suggesting that there was greater belief associated with these topics than the other eight rumors.

**Dynamic $R_{SI}$ value** Figure 5.27 illustrates the dynamic response ratio of Zombie rumor and Dallas real news. We can see the response ratio for Ebola Zombie rumor swings between 0 to 4, which means people’s believe extent to Zombie rumor has been very low. However, the dynamic response ratio for Dallas real news kept increasing and reached as high as nearly 100, which reveals more and more people accept this real news.

The study here has shown that propagation of misinformation can sometimes have the same characteristics as genuine newsworthy developments. In an age where many consumers receive their news from real-time social media platforms, it is imperative that rumors and half-truths be characterized as such and able to be distinguished from news. The tools presented here can support the quantitative evaluation of information spread as it happens.
Figure 5.25: Model fits of SEIZ to different rumors: (from left to right) 'white', 'zombies', 'airborne', and 'patent'. (top row) Fitting results. (bottom row) time-course profiles of different compartments.

5.6 Conclusion

In this chapter, we have demonstrated how true news and rumor stories being propagated over Twitter can be modelled by epidemiologically-based population models. We have shown that the SEIZ model, in particular, is accurate in capturing the information spread of a variety of news and rumor topics, thereby generating a wealth of valuable parameters to facilitate the analysis of these events. We then demonstrated how these parameters can also be incorporated into a strategy for supporting the identification of Twitter topics as rumor or news. As of now, we are modeling propagation over static data. In future, we plan to adapt this model for capturing news and rumors in real-time.
Figure 5.26: Ultimate response ratios for 3 news stories (left) and 10 rumors related to Ebola.

Figure 5.27: Dynamic $R_{SI}$ values for Zombie rumor and Dallas real news.
Chapter 6

Modeling Precursors to Climate Related Protests

6.1 Introduction

Climate change, extreme weather, and the state of the environment directly impact the availability of food [5] [2], energy [61], and shelter [97]. As finite resources become scarce, the residual impacts on local economies can have disastrous and sometimes long-lasting effects on the fundamental livelihoods of inhabitants for decades [57]. In some cases, the resulting instability can severely detriment the ability of an established political system to maintain peace. The examples of this occurring are numerous. The extended drought in Syria in 2011 is cited as one of the principle causes of civil war [28, 49]. In a smaller scale example, the environmental impact of lead contamination in the drinking water in the United States led to protests in 2016.\(^1\) As we later show as an example of extreme weather, tropical storm Manuel devastated the western coasts of Mexico leading to subsequent protests over resources at times as long as 17 months after the initial event.

The path from climate, extreme weather and environmental effects to civil unrest is causally complex [40, 82] and involves various combinations of climate change [12], natural resources, human security, and social stability. In general, sensitivities to climate change, exposure to climate change, and the ability of a society to adapt are indicators of whether or not violence will erupt [41]. A commonly studied pathway is the effect of climate on food prices that then induces civil unrest. An example of this occurrence is the Arab Spring uprisings in 2011, and how weather effects food prices [48]. The pathway to civil unrest is also not limited to a local region, where one study shows the Chinese drought effecting the supply wheat causing prices to rise in the Egyptian break market leading to protest [90]. The pathways of food prices to protest have also been studied in the global south [13], Africa, and Asia [101, 37].

\(^{1}\)http://www.cnn.com/2016/01/11/health/toxic-tap-water-flint-michigan/
However, even this path of climate effects on income level leading to conflict is not eminently clear [80].

Of course, the occurrence of either a shift in climate, extreme weather, or environmental catastrophe is not sufficient to guarantee that civil unrest is likely to follow. In general, the causal mechanisms leading to civil unrest are very complex, and there is no easy way to determine a linear pathway to protest. However, to date, little quantitative analysis has been performed on the residual effects of changes resulting from climate, extreme weather, and the environment using a large volume of data. In this analysis, we focus on the breadth of the climate events by looking at events generated from a large Gold Standard Report (GSR) [73] containing all of the protests that have occurred in Latin America from 2011-2015.

GSR is a gold standard report of protests organized by MITRE, using human analysts, to survey newspapers for reporting of civil unrest. The GSR includes many features, as shown in Figure 6.1, such as protest location, event date, protest type, status, crowd size, headline, date, population, protest description, first reported links, etc.. The description feature is brief description of the protest, generally, it tells us who, where, why and when protest. As Figure 6.1 shows, a sample protest description is ‘small farmers want the bank to forgive their debts due to the drought, which has hampered production’.

![Figure 6.1: Gold standard report (GSR) format.](image)

We address three foundational problems. First, we use machine learning to classify climate related protests. By developing a logistic regression classifier, 25,352 GSR civil unrest events were classified as either being climate or non-climate related using terms in the description of the event. Second, we use the textual description of protests to extract the climate protest category for protests in each country. For each major climate category, we adopt a knowledge
graph approach to define linkage relationship between entities, and study potentially related protest attributes. Third, we find that the massive climate protests show that certain protest types are shown to correlate with other protest types. Specifically, we find clues such as a lack of water is highly linked with power shortage. This is the first large-scale study of climate related protests to our knowledge. Generally, the main contribution of this chapter can be summarized as:

1. We develop a logistic regression classifier, which can classify climate protests from non-climate protests automatically based on protest event descriptions.

2. We analyze climate protest spikes and disclose its relationship with climate disasters. For instance, the time span caused by storm and hurricane events in Mexico last much longer. However, for drought events in Brazil, the protests being initiated more swiftly, also last much shorter.

3. We identify precursors to climate protests. By studying major climate disasters, we also discover each protest category’s evolution pattern, thus how the climate disasters lead to climate protests.

4. We investigate co-occurrence relationships, e.g., that water related protests are often accompanied by electricity shortage, while land ownership protests are often associated with farmers.

6.2 Climate Protest Classifier

The classifier is designed to label text documents into two or more predefined categories. In this work, we only have two categories: climate or non-climate related protest. By sample analysis, more than 90% records belongs to non-climate related protest, thus the dataset can be ascribed as un-balanced dataset. So we consider majority assign classification as baseline, adopt other four classical classification methods: K-Nearest Neighbor, Naive Bayes, weighted SVM and Logistic regression.

6.2.1 Majority Assign

A majority assign method is taken as a baseline for the unbalanced classification dataset. It first calculates the climate related protest rate with the training dataset as \( p \), and non-climate related protest as \( 1 - p \), and then uses this distribution to randomly assign each testing event. Suppose there are \( N \) testing events, by this algorithms, the true-positive would be \( Np^2 \), false-positive and false-negative would both be \( Np(1-p) \), on average. Hence the precision, recall and \( F - measure \) would all be \( p \), and the accuracy would be \( p^2 + (1-p)^2 \).
For unbalanced dataset, since \( p << (1 - p) \), the accuracy approximately equals to \((1 - p)^2\), while the \( F \) measure is \( p \).

### 6.2.2 K Nearest Neighbor

K Nearest Neighbor (KNN) classifier is to label data based on a majority vote of its neighbors, where the vote is measured by a distance function. Distance function is used to measure similarity, which is not necessarily be Euclidean distance or the cosine value although they are most commonly used. Clearly, text similarity plays a fundamentally important role in labeling dataset. In our study, we calculate two GSR records’ similarity using cosine similarity [58]. KNN is a supervised learning method which require to prepare training dataset. In the training dataset, each GSR record is transformed into vectors and are labelled as climate or non-climate protest. How to choose the optimal value for \( K \) is another factor influencing classification result. After a set of comparison, we found setting \( K \) to be 100 tends to get the best performance.

### 6.2.3 Naive Bayes

Essentially, Naive Bayes is to maximize a posteriori classifier, which can be represented as \( c = \arg \max_c p(c|e) \). \( e \) is the protest description, and consists of multiple words \( w_i \), and can be denoted as \( e = < w_0, w_1, ... > \). \( c = \{ \text{climate protest}, \text{non-climate protest} \} \). However, there is no trivial solution to measure the joint probability distribution for \( e, c \) considering the extremely complex underlying structures among \( w_i \). Naive Bayes circumvents this problem by assuming the independency among \( w_i \). Hence, the probability of each protest \( e \) being class \( c \) can be simplified as:

\[
p(c|e) \propto p(c) \prod_i p(w_i|c)
\]

where \( p(w_i|c) = \frac{f^c_{w_i}}{f^c_w} \) is the conditional probability of term \( w_i \) that appears in the description of \( e \). \( f^c_{w_i} \) is the occur frequencies of \( w_i \) in class \( c \), and \( f^c_w \) is the total word number in class \( c \). If a new term \( w_i \) does not occur in the training dataset, then \( p(w_i|c) = 0 \). \( p(w_i|c) \) measures how much likeness of being \( c \) for the existence of term \( w_i \). To mitigate the zeroing affects, Laplace smoothing modifies \( p(w_i|c) \) as

\[
p(w_i|c) = \frac{f^c_{w_i} + 1}{f^c_w + W}
\]

where \( W \) is the total word number for climate and non-climate protests together. Usually, the conditional probability is small which might results in float point underflow. In reality, it is converted as:

\[
c = \arg \max_c p(c|e) = \arg \max_c \{ \log(p(c)) + \sum_i \log(p(w_i|c)) \}.
\]
6.2.4 Weighted Support Vector Machine

Traditionally, the Support Vector Machine works as follows. The training data consists of \( N \) pairs \((x_1, y_1), (x_2, y_2), \ldots, (x_N, y_N)\), with \( x_i \in \mathbb{R}^p \), and \( y_i \in \{-1, +1\} \). By introducing a hyperplane of \( P := \{x | x^T \beta + \beta_0 = 0\} \), the classification rule is defined as \( G(x) = \text{sign}[x^T \beta + \beta_0] \). To find the hyperplane \( P \) for inseparable sets, it is often converted into the following quadratic convex optimization problem by defining the slack variables \( \zeta = (\zeta_1, \zeta_2, \ldots, \zeta_N) \) [35].

\[
\begin{align*}
\min_{\beta, \beta_0} & \quad \frac{1}{2} ||\beta||^2 + C \sum_{i=1}^{N} \zeta_i \\
\text{subject to} & \quad y_i(x_i^T \beta + \beta_0) \geq 1 - \zeta_i, \quad \forall i \\
& \quad \zeta_i \geq 0, \quad \forall i
\end{align*}
\]

(6.1)

where \( C \) is the penalty parameter. For separable sets, \( C \) corresponds to \( \infty \).

The problem with above classifier is that the penalty for misclassification are the same. However, in cases with unbalanced dataset, the miss alarm should have a much higher cost than the false alarms. As in our study, the climate related protest is more important. To consider these scenarios, we introduce two different penalties for misalarm and false alarm. For simplicity, \( I \) and \( J \) denotes the subscript of positive and negative set. Thus, the problem of 6.1 can be re-formulated as:

\[
\begin{align*}
\minimize_{\beta, \beta_0} & \quad \frac{1}{2} ||\beta||^2 + C_1 \sum_{i \in I} \zeta_i + C_2 \sum_{j \in J} \eta_j \\
\text{subject to} & \quad y_i(x_i^T \beta + \beta_0) \geq 1 - \zeta_i, \quad \forall i \\
& \quad x_j^T \beta + \beta_0 \leq -1 + \eta_j, \forall j \in J \\
& \quad \zeta_i \geq 0, \forall i \in I \\
& \quad \eta_j \geq 0, \forall j \in J
\end{align*}
\]

(6.2)

The Lagrange function of 6.2 is

\[
L_p = \frac{1}{2} ||\beta||^2 + C_1 \sum_{i \in I} \zeta_i + C_2 \sum_{j \in J} \eta_j \\
- \sum_{i \in I} \alpha_i [x_i^T \beta + \beta_0 - (1 - \zeta_i)] - \sum_{i \in I} \mu_i \zeta_i \\
+ \sum_{j \in J} \theta_j [x_j^T \beta + \beta_0 - (1 - \eta_j)] - \sum_{j \in J} \tau_j \eta_j
\]

(6.3)
6.2.5 Logistic Regression

The classifier is built based on the logistic regression method. To reduce the computation complexity, we only apply the GSR description text as input to the logistic regression classifier. First of all, we construct a bag of words from the training dataset descriptions by deleting meaningless stop-words, like “the”, “a/an”, “at”, and etc.. The bag of words is composed of \( M \) words denoted as \( \{w_1, w_2, ..., w_M\} \). Each GSR description \( X \) is considered as a vector of length \( M \). If word \( w_i \) occurs in its description, then \( X(i) \) will be assign with 1; otherwise 0. Further each protest in the training dataset is assigned \( Y = 1 \) as climate protest, or \( Y = 0 \) as non-climate protest by manually checking its description meaning. In this way, each GSR record is converted to a corresponding vector based on the bag of words. Second of all, we estimate \( k_i \) and \( b \) based on maximum likelihood criterion. This process is usually converted to convex optimization problem with efficient solutions [44]. Once the coefficients of \( k_i \) and \( b \) are estimated, the probability for each class is calculated by:

\[
P(Y = 0|X = x) = \frac{1}{1 + exp(\sum_{i=1}^{N} k_i x_i + b)}
\]

\[
P(Y = 1|X = x) = \frac{exp(\sum_{i=1}^{N} k_i x_i + b)}{1 + exp(\sum_{i=1}^{N} k_i x_i + b)}
\]

If the probability of \( P(Y = 1|X = x) \) is larger than 0.5, then the protest event will be classified as climate protest, otherwise, non-climate protest.

6.2.6 Evaluation

We manually labelled 1700 GSR protest records as climate or non-climate protests, using 70% dataset as training, and the rest 30% as test. To ensure we have trustworthy classification results, we evaluate the performance carefully by cross evaluation. The evaluation criteria are precision (positive predictive value), recall (true positive rate), F-measure (a measure that combines precision and recall) and accuracy (the proportion of true results both true positives and true negatives among the total number of cases examined). We compare with four well-known classification methods: majority assign, K-nearest neighbor, Naive Bayes, and weighted support vector machine (SVM). Since the climate events only account for a small portion of all the events, which make it an unbalanced classification problem, so we change the traditional support vector machine into weighted SVM, by adding more importance to the climate protest events (we set the class weight to be 100). The experiment results are shown in Table 6.1, where we demonstrate logistic regression method outperforms other methods uniformly.
Table 6.1: Classification methods comparison.

<table>
<thead>
<tr>
<th>Method</th>
<th>Precision</th>
<th>Recall</th>
<th>F_measure</th>
<th>Accuracy</th>
</tr>
</thead>
<tbody>
<tr>
<td>Majority assign</td>
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<td><strong>0.6018</strong></td>
<td><strong>0.9322</strong></td>
</tr>
</tbody>
</table>

6.3 Experimental Results

There were a total of 25352 recorded civil unrest events in Latin American countries from July 2011 to March 2015 that were included in our dataset. Using our climate protest classifier, we were able to separate out protests directly or indirectly resulting from a major climatic, severe weather, or environmental event. In the subsequent analysis, these three categories of event types are labeled with a common definition of “climate event”. Of the candidate civil unrest events, 991 (3.9%) events are classified as climate-motivated across all Latin American countries for that time period. In the subsequent sections, we conduct a multi-dimensional analysis of these protests to understand potential implications of the breadth of impact resulting from climate motivated protests.
Figure 6.3: Blue bar shows all the climate related protests for each country, yellow bar shows the climate protest percentage over its total protest, from January 2011 to March 2015.

6.3.1 Frequency Analysis by Country

The first analysis we conduct is a comparison of the representative number of protests within and across each country. The results of our classifier selection show the number of climate motivated protests and the percentage over all the protests in that country, as can be seen in Figure 6.3. The country with the most climate protests overall is Mexico, and Costa Rica has the least. As evidenced by the climate to non-climate protest ratio, the portion of protests related to climate remains fairly constant across countries with the exception of Peru. In this particular case, there were numerous protests centered on mining and its effect on the environment that dominate the overall protest landscape. As the number of total protests decrease, we see more variability in the ratio as expected. For these countries, which typically have smaller populations, the significance of a single type of protest has more of an impact on the measure than larger countries.

To show the effect of the population on the number of climate protests, we plot the result of a linear regression in Figure 6.5. The result of this shows an $R^2 = 0.64$, showing a slight linear relationship. However, the interesting part of this analysis lies in the residual errors. The set of countries including Mexico, Venezuela, Paraguay, and Colombia, all demonstrate the occurrence of more climate protests than would be expected given the entire dataset. On the contrary, Brazil has fewer climate protests given the size of their population. There could be a number of reasons for these findings such as socio-political stability, environmental sensitivity, and the type of climate events. All of these are potential avenues for further causal
Figure 6.4: (a) Climate related protests events numbers; (b) Climate related protests percentage in Latin American countries, from January 2011 to March 2015.

or anecdotal studies. In the following, however, we choose Brazil, Mexico, and Venezuela for further analysis into overall trends of climate protests, and how these are shaped in the data recovered by the classifier.

6.3.2 Spatial Distribution of Climate Protests

In this manuscript we are defining the climate protest as being different from a regular civil-unrest event by a relation to an climate event. Next, we investigate if there is any fundamental difference in terms of where these protests occur in relation to protests in general. For this analysis we use Mexico, Brazil, and Venezuela which all have many protest events, and the percentage of those that are related to the climate are all at about 4%. The spatial distribution of events is shown in Figure 6.6. Both the total number of protests and those that are climate motivated are shown and represented by the size of the blue and red shaded circles, respectively.

In both Brazil and Venezuela, many of the protests appear at or near their coastal boundaries, and Mexico has more inland activity. However, we have already established a connection between population and protests. This is no different for the spatial distribution, where much of the population of Brazil and Venezuela is located in coastal regions. The protests in Brazil mainly center at two major cities Sao Paulo and Rio de Janeiro. In Mexico and Venezuela climate protests have a more uniform distribution across the cities. Therefore, there is no particularly strong evidence to suggest that certain regions of these countries are more prone to protest with respect to the climate than they would normally be willing to protest in general. In terms of the climate events defined in this study, effects of climate,
the environment, and extreme weather are not regionally exclusive to certain populations. Through complex channels such as food supply, the effects of climate impact can ripple across spatial networks.

### 6.3.3 Temporal Dependency on Climate Events

The temporal dependency of climate protest occurrences is analyzed for each country. As with the spatial domain, the effects of climate events are non-local in time in some cases. The ground truth for the events was established for extreme weather only, as the event itself is more local in time than climate and environmental changes. This data is available by combining the following sources: International Disaster Database EMDAT\(^2\), World Disasters Timeline\(^3\) and European Commission’s Humanitarian Aid and Civil Protection department (ECHO)\(^4\). The official climate disaster report for each country is shown with climate related protests in Figure 6.7.

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\(^2\)http://www.emdat.be/database
\(^3\)http://www.mapreport.com/
\(^4\)http://ec.europa.eu/echo/
Figure 6.6: Climate and non-climate protests from January 2011 to March 2015. Red circle represents climate related protest events, and blue circle represents non-climate related protests.

**Mexico climate disasters**  Figure 6.7(a) shows the Mexican extreme weather events and protests where the blue time series represents the climate protests events, and the two red bars shows the occurrence of two storms. The first storm is the combined tropical storm Manuel (category 1) and hurricane Ingrid in September 17, 2013. The track maps can be seen in Figure 6.8(a). Tropical storm Manuel crossed the west coast of Mexico and resulted in more than 23,000 people fleeing their homes due to heavy rains spawned by what had been Hurricane Ingrid. Of those displaced 9,000 went to emergency shelters. In terms of infrastructure, at least 20 highways and 12 bridges had been damaged. After the storm, related protests and other civil unrest events broke out and lasted for more than 17 months because the government’s response had been inadequate. The storm related protests reached a climax in January 2014, and second climax in April 2014. On November 19, 2013, there was a report saying “it’s been 63 days since the onslaught of ‘Ingrid’ and ‘Manuel’ and families were left homeless are still without help”. Four months after the storm Manuel and the effects of Hurricane Ingrid, they say “we have not received anything”. On April 7, protest descriptions said “Affected by Tropical Storm ‘Manuel’ in the municipal head of Tixtla marched to demand the construction of a controlled channel, it will prevent a flood like that caused the overflow from the Black Lagoon in September 2013”. The last protest event we have on record from the climate protest classifier occurred 17 months after the original event. This demonstrates that the residual capacity of these events to impact the livelihoods of people is not guaranteed to be local in time. As we show, the range of impact can extend even beyond the occurrence of other storms.

In Figure 6.7(a), the second red bar shows hurricane Odile. It is a category 3 storm that occurred in 2014, and the track of the storm’s path is shown in Figure 6.8(b).

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6Quotes are translated from the native language of the country.
hurricane Odile being a more intense storm, there were not many protests related to the event. Comparing the storm’s paths in Figure 6.8, Tropical Storm Manuel hit Mexico’s mainland, which caused more destruction. Hurricane Odile 2014 had less of an impact on the Mexican mainland, even though it crossed the state of Baja California. However, this is the second smallest Mexican state by population. This can explain why storm 2013 lead to tremendous protests, while hurricane 2014 does not.

Brazil climate disasters Figure 6.7(b) shows the relationship between protests classified by our algorithm and actual extreme weather events in Brazil. The three yellow bars show three separate drought events in Brazil, which resulted in drought related protests almost immediately. The drought in February 2012 hampered production, which caused farmers to protest. The heat wave in February in 2014, and drought in October 2014 resulted in water shortages, causing civil unrest. The biggest spike in June 2013 described protests against government’s projects for the construction of hydroelectric plants in the Amazon region\(^7\) and is more of an environmental impact type of event. In general, for these events we see predominantly local relationships in time between the protest and the preceding event. For Brazil in particular, the extreme weather event matches fairly well with the onset of drought.

Figure 6.8: The map shows population density of all Mexico’s 32 states. The track shows Tropical Storm Manuel of 2013 and Hurricane Odile of 2014, points in different color represent the wind speeds.

Figure 6.9: Word cloud of Mexico storm Manuel, September 13, 2013.

**Venezuela climate disasters** In Figure 6.7(c), the climate motivated events are shown in relation to relevant extreme weather events for Venezuela. The pink bar represents sudden onslaught of rain in June 2013 that caused a heightened risk of flooding and landslides in the densely populated communities on the outskirts of Caracas. It triggered a small portion of protests to prevent flooding. The yellow bars denote drought disasters. The drought in May 2014 triggered rationing of tap water in the capital, Caracas, where residents formed lines lasting hours to fill jugs of water\(^8\). This drought disaster lasted so long that related protests reached a climax in September 2014. Unlike Brazil, the data in Venezuela on droughts proved tough to ascribe to a particular drought event. They occur rather frequently and there is a substantial amount of overlap in the residual protest events that it was difficult to distinguish to which it was referring.

\(^8\)http://www.breitbart.com/national-security/2014/05/31/severe-scarcity-prompts-venezuelan-government-to-ration-water/
6.4 Discussion of Results

Of the climate related protests, we are interested in what the protesters are demanding. To have a birds eye view of climate protests, we extract all the climate protest descriptions and plot the word cloud, as shown in Figure 6.10. We can see words like ‘water’, ‘storm’, ‘mining’, ‘rain’, ‘construction’, ‘power’, ‘heat’, ‘gas’, ‘environment’, ‘electricity’, and other weather, environment related keywords are dominant, which gives us a general idea of what protesters are demanding.

As stated previously, we are not blind to the realization that the causes of climate motivated protests are in general complex. In the following, we analyze the descriptions of the protest events in order to gain insight into the general pathways by which protests within our corpus have occurred. Shown in Figure 6.11 is a weighted Sankey diagram showing the bipartite graph of the most common keywords in the descriptions of protests from each country. Apparently, many of the protests identified by the classifier in one way or another have something to do with lack of water followed by climateal effects in general. Other prominent keywords include mentions of power and energy issues. Each country also exhibits its own protest keyword categories. In Mexico, the most notable protest keywords involve are lack of water, environmental concern, storm and hurricane. In Venezuela, apart from lack of water and environment problems, the dominant keywords are blackout and energy issues. In Peru, more than half of climate protests are about a mining project, which is an environment concern. While in Argentina, 35% events protest against blackout issues. We expand on these observations in the following where we analyze several dimensions of the keywords to extract details about pathways to protest.
Figure 6.11: Climate motivated protest keywords diagram, from January 2011 to March 2015. Countries on the left are matched with keywords appearing in the description of the protest event on the right.

### 6.4.1 Climate Protest Precursors

For some severe and dominant climate events, such as storm, hurricane, flood, and drought events, we employ the knowledge graph to represent the link relationships between entities. By matching the object or subject with climate related keywords, and predicate to be causality relationship like result of, cause by, lead to, blamed, accused of, demanding, against, request, we can locate and further identify the pathways of most protest descriptors.

Figure 6.12(a) shows the storm caused protests demands in Mexico, which generally falls into four categories: supply, home, government and reconstruction. In the supply related protest, the causality includes but not limited to: lack of drinking water, lack of good support, and power outage. The second category is about home, they protest either because of lost homes, or request to relocate to avoid storm, or request to reconstruct homes. Another protest type targets the government, where they either protest because government did not take action, or blame government’s indifference to damages, or request finance compensation to the damages. In the reconstruction category, residents demand reconstruct channels to avoid more storms, request to reconstruct bridges, roads, schools, or unsatisfied with the slow pace of rebuilding homes. Figure 6.12(b) describes the precursors underlying the Brazil climate related protests. One stream of thought concludes that the heat wave hampered production, which caused farmers’ protests, while another pathway concludes that drought caused a lack of drinking water thus leading to protest, and the third pathway involves lack of water causing farmers facing the risk of losing land, which resulted in protests. In
Venezuela, the protests are more water-electricity centralized, as shown in Figure 6.13(c). Scarce rainfall, drought plus failing infrastructure, which makes water shortage and blackout is an everyday fact of life in Venezuela. The electricity shortage deteriorates water shortage, leads to food shortage, and worsens food quality, and so forth. All those situation touches off climate related protests.

6.4.2 Climate Protest Pattern

The above analysis shows events that commonly co-occur with protests; however, we intend to further illuminate the correlations surrounding protest activity. In the following we take a graph theoretic approach, where we treat each protest event as a node and connect two nodes with a weight based on their protest descriptions and text similarity. Specially, we pay attention to the protest themes or protest demands. If two descriptions have the same protest demand, their weight will be very high. Otherwise, their connection weight tends to be 0. In this way, we build a weighted undirected network $G(V, E, W)$, with each protest as node $V$, and their connection as edge $E$, their weight as $W$. If the weight between two
nodes is 0, there will be no edge. We employ Louvain method [8] to split the network into several clusters.

We show in Figure 6.13 the climate protest clustering results that provides the protest proportion and coherent correlations among different protest types. Figure 6.13(a) illustrates Brazil’s climate protest pattern. We see that the largest protest cluster is about land ownership which accounts for 26.7% of the protests. The second cluster is lack of water and takes up 20.7%. The farmers cluster occupies 13.8%. We note that land and farmer clusters are closely correlated, and lack of water is also closely binded to farmers as well. Amazon rainforest is another striking protest which is responsible for 11.3%. Figure 6.13(b) shows the protest patterns of Mexico, which has the most climate protest events and most complex patterns. We can see the red cluster which denotes lack of water is the most dominant protest, accounting for 20.5%. The green cluster represents the tropical storm, and is the second largest protest type, taking up 19.0%. The dark blue cluster construction accounts for 17%, and the yellow cluster land is responsible for 11.8%. We find that water related protests are intertwined with environment protests and power protests. Land protests are closely related with farmers, while construction clusters are coherent with homes (2.6%). Figure 6.13(c) gives the overview clustering results of Venezuela climate protests. We see the yellow cluster representing lack of water protests takes up the largest portion, as high as 55.8%, and the green cluster denoting power outages accounts for the second part at 22.1%. The blue cluster, which stands for gas shortage accounts for 5%. The purple cluster shows the rest climate protest portion, which includes food shortage, medicine shortage, water tank robbery behavior, etc. The lack of water protest is intertwined with power outage protest, which corresponds to the fact that lack of water and power shortage is everyday life in Venezuela.

6.4.3 Climate Protest Influence

We are also interested in climate events influence on social media, such as Twitter. Using keywords list we are able to filter tweets, then cluster tweets into different partitions based
on similarity among tweets using distance function, taking tweets content, geolocation and other features into consideration.

Event clustering is used to separate events happened at same place or at same time, or the separate different events happened simultaneously on local and entire country. By measure the distance among tweets based on similarity, tweets collection can be clustered into subsets in which tweets are exactly related and similar. Each partition includes similar tweets stand for a specific event. Without events clustering, different events will be mixed. As shown in Figure 6.14(a), Mexico Hurricane were mixed with severe drought happen in Culiacan, with the aid of event clustering, we are able to distinguish those distinct extreme weather events, even though they may happen at the same time. For each event, we plot the related Tweets word cloud besides the flag. Figure 6.14(b) illustrates four drought events in Brazil, on May 2012.

![Figure 6.14: Climate protest events in Mexico, September 2013 and Brazil, May 2012. Different flag represents different climate disasters. The adjacent world cloud shows Twitter discussion as per that event.](image)

6.5 Conclusion

Climate changes, extreme weather and environmental catastrophes can all exert a devastating amount of harm to people around the world. To better understand how these events lead to protest behaviors, we show different pathways to protest following severe events in Latin America from 2011 to 2015. Our analysis differs from those previously published in that we consider the breadth of climate protests over a wide spatial and temporal domain. This is accomplished by identifying climate related protests using a logistic regression classifier acting over keyword vectors of protests descriptions in our protest GSR dataset. We found this approach achieved an F-score of 0.60 and accuracy of 0.93, which was the best preforming
of other common binary classifiers. The results of the classifier indicate a number of broad properties about climate related protests.

From our analysis, we found different climate disasters may cause related protests with different time span. For example, the tropical storm Manuel in Mexico was followed by a wave of climate related protests lasting as long as 17 months. In Venezuela, the protests caused by one drought always overlap with the other drought. This chapter discloses protest causalities in Latin American countries, and illustrates the pathways from climate disasters to climate protests. This chapter also identifies the climate related protest patterns, and discovers the coherent relationships among different protests.
Chapter 7

Conclusions and Future Directions

7.1 Contributions

As social media such as Twitter continue to increase in popularity, they are effectively becoming social sensors that can be utilized for real-world mass movement event detection. Modeling and studying the related adoption patterns provide new insights for investigating both the social and physical aspects of these events and their precursors. This dissertation has presented several approaches and strategies aimed at detecting and predicting mass movements and further inferring their causality, given information composed of a volatile mixture of real news and rumors. Techniques have been presented that are designed to capture information propagation across multiple spaces, as well as a new graph wavelet approach that broadens predictive capabilities to capture group anomalies within networks. A number of different types of mass movements have been investigated and diverse aspects of modeling addressed.

Using social media as indicators for real-word event detection can indeed be a helpful tool, but several limitations apply, perhaps most notably when applied to a specific event type such as the mass movements studied here. First, modeling protest-related topic propagation across networks is never trivial. One challenge is that social protest propagation through online media can spread over large areas far more quickly than traditional methods since users are geographically distributed, while other challenges include the way mass protest information can be spread by multiple social media types and paths, such as word of mouth, and radio and TV news broadcasts. Second, even detecting group anomalies on social media is challenging. For example, Twitter’s user network embodies many subgraphs based on social ties with dynamic graph structures that are constantly changing since users are actively contributing content. The other challenge includes real-world events that are not only correlated with burst signals, but can also exhibit unusually low levels of activity in social networks. Despite these restrictions, graph wavelets have in fact proven to offer a powerful
capacity for capturing graph anomalies (in terms of both burst behavior and absenteeism behavior), even on dynamic changing networks.

A fundamental objective of this research has been to model mass movement adoption behavior, and in doing so, several significant additional advantages have been gained. One contribution is the ability to model information propagation across multiple networks/spaces, and capture the propagation speed and possible propagation paths, as demonstrated in Chapter 3. Another benefit gained through enhancing the mass movement detection capability is the opportunity this provided to introduce a new group anomaly detection approach, as described in Chapter 4. The use of graph wavelets made it possible to develop a more appropriate definition of group anomaly that covers both bursts and absenteeism utilizing different scales, thereby increasing the probability of capturing protest behaviors. Another benefit is the ability to quantify compartment transition dynamics using the epidemic model SEIZ, thus facilitating the development of screening criteria that can distinguish real movements from rumors on Twitter, as demonstrated in Chapter 5.

Understanding information propagation over dynamic social networks is becoming a highly popular way to address real-world problems in social network analysis. The research reported in this dissertation analyzed several fundamental questions that underlie a broad range of propagation-like processes, focusing particularly on mass movement adoption and rumor transmission. These methodologies can easily be extended to applications such as infectious diseases, public health and marketing, among others.

### 7.2 Future Directions

Given the wide scope of this relatively new field, there are many opportunities for conducting potential fruitful research. For example, one very attractive area would be to continue to focus on social network analysis, specifically research into information propagation over dynamic rapidly changing social networks. Here, future research directions fall into two general categories, with one being to deepen the existing theories and algorithms by exploring them in more detail while the other is to broaden the current research by adopting a wider perspective. Examples of these and other research possibilities are presented below.

**Extend GBM model**  What happens to the geometric Brownian motion model if the underlying mention network changes over time? How can this model be adopted or modified to apply to multiple networks? In addition to these theoretical questions, a number of practical applications are worth further investigation, for example would it be possible to introduce the GBM model into the infectious disease domain to model the spread of the zika virus? Assuming that bispace is composed of both a connection network and physical space, can we train the GBM model to estimate individuals’ infection probability based on their environment?
Further studies involving graph wavelets  It should be possible to extend the graph wavelet applications presented in Chapter 4 into other areas based on the two of the major distinguishing properties of graph wavelets. The ability to detect graph anomalies could be utilized to detect the wealth gap between rich and poor in a given region, identify brain neural network anomalies, or detect traffic congestion through road network analysis. Similarly, the ability to identify the central point of a subgraph could be employed to rank key players within networks, detect those spreading rumors in some cascade, or find the sources of infection for certain diseases.

Broaden rumor detection scenarios  Instead of determining whether a particular story is true or false, it may instead be more practical to predict how likely people are to believe it. Newspapers in particular would find it very useful, especially when it comes to a breaking news story that has not yet been officially confirmed. Before reporting to the public, they need to know how believable the story is. Also this offers a valuable way to decide whether vendors are cheating during online shopping.

Deepen our understanding of personalized information propagation  It would be useful to know how users’ behavior either delays or boosts information propagation, especially when accompanied by strong sentiments. This may help formulate better advertisement strategies if a better way to manipulate the information flow can be identified. Further, it would be interesting to explore opportunities to extract personalized information spread patterns. What kind of news arouse the interest of individual consumers? What kind of role is he or she likely to play? and What kind of push strategy might stimulate their activity? This type of study would be invaluable for precision marketing or personalized recommendations, providing refined content filtering.

Build an intelligent disaster detection system  Another interesting option would be to build an intelligent system that is efficient at event detection, especially for disasters, protests, and other extraordinary events. Such a system would not only be capable of immediate reporting, but also able to track events and perform causality analyses and even provide future predictions. This type of system would require several critical building blocks: natural disaster detection could be based on the use of graph wavelets for detecting group anomalies, rumors or news detection could employ an epidemic SEIZ model, story causality analysis and event coding. Consider the Flint water crisis for example. First, it would need to identify the water crisis events from a social media analysis and confirm it to be a true story, after which it would trace all the relevant historical news to identify the causality, leading finally to the generation of a complete report using event coding.

Combine social network analysis with physical data.  The advent of social media provides unprecedented opportunities to access vast quantities of information that could
potentially benefit our research. This opens up new possibilities for reinvigorating traditional research in many areas, hopefully gaining new insights and leading to extraordinary discoveries. Take vaccines and the study of their potentially adverse effects, for example. Traditionally, vaccine research depends heavily on the raw data collected by the CDC, hospitals, patient reports, and vaccine adverse event reports. However, this data frequently suffers from problems such as lengthy time delays and incomplete information. Worse, most of the data is considered in isolation. If we can find a way to combine conventional statistical data with social media data such as tweets and Facebook posts, it may be possible to extract more information and create a complete picture showing what kind of people likely to be more vulnerable to a specific vaccine. In this way, it may be possible to better predict adverse events or even contribute to the design of new vaccine approaches that minimize or eliminate serious vaccine-related reactions. Given current advances in data mining, this is a revolutionary time for research in real-world applications using social network analysis.
Bibliography


