Filter Design for Interference Cancellation for Wide and Narrow Band RF Systems

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Filter Design for Interference Cancellation for Wide and Narrow Band RF Systems

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Scholarly Abstract

In radio frequency (RF), filtering is an essential part of RF transceivers. They are employed for different purposes of band selection, channel selection, interference cancellation, image rejection, etc. These are all translated in selecting the wanted signal while mitigating the rest. This can be performed by either selecting the desired frequency range by a band pass filter or rejecting the unwanted part by a band stop filter.

Although there has been tremendous effort to design RF tunable filters, there is still lack of designs with frequency and bandwidth software-tuning capability at frequencies above 4 GHz. This prevents the implementation of Software Defined Radios (SDR) where software tuning is a critical part in supporting multiple standards and frequency bands. Designing a tunable integrated filter will not only assist in realization of SDR, but it also causes an enormous shrinkage in the size of the circuit by replacing the current bulky off-chip filters. The main purpose of this research is to design integrated band pass and band stop filters aimed to perform interference cancellation.

In order to do so, two systems are proposed for this thesis. The first system is a band pass filter capable of frequency and band with tuning for C band frequency range (4-8 GHz) and is implemented in 0.13 µm BiCMOS technology. Frequency tunability is accomplished by using a variable capacitor (varactor) and bandwidth tuning is carried out by employing a negative transconductance cell to compensate for the loss of the elements. Additional circuitry is added to the band pass filter to enhance the selectivity of the filter. The second system is a band stop filter (notch) with the same capability as the band pass filter in terms of tuning. This system is implemented in C band, similar to its band stop counterpart and is capable of tuning its depth by using a negative transconductance in an LC tank. A negative feedback is added to the circuit to improve the bandwidth. While implemented in the same process as the band pass filter, it only employs CMOS transistors since it is generally more attractive due to its lower cost and scalability. Both of the systems mentioned use a varactor for changing the center frequency which is a nonlinear element. Therefore, the nonlinearity of it is modelled using two different methods of nonlinear feedback and Volterra series in order to gain further understanding of the nonlinear process taking place in the LC tank. After the validation of the models proposed using Cadence Virtuoso simulator, two methods of design and tuning are suggested to improve the linearity of the system.

After post layout-extraction, the band pass filter is capable of Q tuning in the range of 3 to 270 and higher. With the noise figure of 10 to 14 dB and input 1-dB compression point as high as 2 dBm, the system shows a reasonably good performance along its operating frequency of 4 to 8 GHz. The band stop filter which is designed in the same frequency band can achieve better than 55 dB of rejection with the noise figure of 6.7 to 8.8 dB and 1-dB compression point of -4 dBm. With the power consumption of 39 to 70 mW, the band stop filter can be used in a low power receiver to suppress unwanted signals. The technique used in the band stop filter can be applied to higher frequency ranges if the circuit is implemented in a more advanced silicon technology.
Implementing the mentioned filters in a receiver along with other elements of low noise amplifiers, mixers, etc. would be a major step toward full implementation of SDR systems. Studying the linearity theory of varactors would help future designers identify the sources of nonlinearity and suggest more efficient tuning techniques to improve the linearity of RF electronic systems.
Filter Design for Interference Cancellation for Wide and Narrow Band RF Systems

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General Audience Abstract

Wireless systems are becoming more widespread every day. These systems consist of mobile phones, laptops with wireless capabilities, wearable devices, etc. The ultimate goal of such systems is to replace current bulky and expensive wires and provide mobility and more flexibility. That requires a robust wireless system capable of supporting different standards and applications. The mentioned requirements can be achieved by implementing Software Defined Radios (SDR). An SDR is a wireless system which can be tuned to support different wireless standards using a software. One key element of an SDR is a Radio Frequency (RF) filter which is responsible for selecting the desired frequency band to receive useful information depending on the application while rejecting the unwanted signals.

Although there has been designs to realize SDR, most of them are using separate circuits as RF filters. Using separate off-chip filters will significantly increase the overall size of the circuit. Moreover, such filters have less tunable parameters compared to their integrated filters counterpart. An integrated filter is a circuit on the same chip as the rest of the radio. Using an integrated filter can significantly reduce the overall size of the system. However, integrated filters often show lower performance compared to off-chip filters. In order to achieve a performance comparable to non-integrated filters, new electronic circuit methods need to be developed to enhance the performance of the filter. The main goal of this research is to introduce novel integrated filters with outstanding performance.

After designing the filters and running post layout simulations, the circuit shows promising performance. Based on the simulation results, it can be proven that it is feasible to design an integrated filter with a wide range of tunable parameters with the potential to be integrated with the rest of the SDR. Successful implementation of the system in integrated circuit level can pave the way for the next generation of wireless systems with the capability of supporting multiple applications by programming the device without changing the hardware.
To my wife, Zahra and my parents
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Chapter 1

Introduction

1.1 Motivation

software defined radio (SDR) is one of the trending topics in wireless communication. SDR necessitates that a wireless transceiver supports multiple wireless standards in order to adapt itself to the new environments required by the software. This can be translated into a single transceiver capable of transmitting and receiving in different frequency bands. While the existing wireless systems employ separate integrated circuits (IC) for each wireless standards, integrating the whole system into a single chip with one transceiver module will significantly shrink the size of the system. While achieving the mentioned goal has its own challenges which will be later discussed, the issue of coexistence with other wireless standards imposes stricter design requirements. [1]

There is an increasing demand for high-data rate transfer turning into higher bandwidth requirement. Consequently, the frequency spectrum is subjected to more traffic and interferers. With the advent of Internet of Things (IoT) and 5th generation mobile networks (5G) expected to be introduced commercially by 2020 [2], the issue of busy spectrum and strong interferers will become even more detrimental. Strong blockers cause significant degradation in the sensitivity and desensitization of the receiver, ultimately reducing the dynamic range of the system. Therefore, proper filtering is required to suppress unwanted signals in order to sustain the normal operation of the system. Existing off-chip filters can offer sufficient out of band rejection. However, they lack the ability to tune to different frequencies and their out of band rejection cannot be altered. Moreover, using off-chip components will increase the area of the system. Consequently, an on-chip filter with tuning capability would revolutionize traditional RF systems by moving them towards modern software tunable systems.

The goal of this research project is to address the issues of tunability and integrability by developing a new filter structure. Additionally, the theoretical study of the linearity of the proposed system is conducted to gain a better understanding of the system’s behavior.

1.2 Scope of the Proposed Research

The main role of a filter in an electronic system is to suppress unwanted signals while maintaining a linear relationship for the desired ones in order to avoid distortion. Previous active filter designs suffer from low dynamic range due to the fact that using amplifiers as the cornerstone of the filter limits the linearity of the system since the amplifier itself is a nonlinear element [3]. There have recently been efforts to improve the linearity of the filter with the assistance of passive techniques such as N-path filter [4]. Although the mentioned technique would address the issue of linearity, implementing it in the frequency of higher than 2 GHz has not been reported yet.
The design proposed by Laya Mohammadi in [5] aims to improve the dynamic range while implementing a tunable filter along a wide frequency range for frequencies higher than 2 GHz up to 4 GHz. The structure of the filter is based on a simple second order LC filter. However, due to the low Quality factor (Q) of the elements especially the inductors, a Q-enhancement technique is employed to improve the selectivity of the filter. With the assistance of the technique, Q can be adjusted from 10 to 100 and higher. A wide continuous tuning range of 2x is achieved by using a varactor to control the center frequency of the filter.

While Mohammadi’s design brings about a wide range of selectivity (Q) along with a broad tuning range, it has performance limitations which need to be addressed. First, the filter employs a negative transconductance (gm) cell in order to compensate the loss of the LC tank and enhance the selectivity (Q). It turns out the technique will significantly downgrade the noise figure for high Q where the noise penalty introduced by the gm cell notably contributes to the overall noise of the system. In the system, the noise figure can be as low as 10 dB for Q of 20 and it is increased to 20 dB for Q of 100. Second, the capacitance of the varactor used in the filter for frequency tuning is sensitive to the voltage across its terminals. In the ideal small signal situation, the capacitance is assumed to be constant with the value determined by its bias point. However, as the voltage increases, the assumption will no longer be valid and the system becomes more nonlinear. This thesis aims to introduce systems which can handle bottlenecks of noise and linearity while retaining a wide tuning range and Q. Moreover, the theory behind the nonlinearity imposed by the varactor will be studied and investigated.

1.3 Contributions of the Proposed Research

Two separate interference cancelling systems have been designed for this research, a band pass filter to select the desired frequency band and a band stop (notch) filter aimed at rejecting strong interferers. Both circuits benefit from feedback principles to achieve the desired performance. The major design target of both systems is to break the trade-off between linearity and noise by improving one without altering the other. The research contributions of the thesis are as follows.

First, Mohammadi’s circuit is studied and the nonlinearity of the varactor used in her circuit is analyzed using volterra series and it is verified with cadence simulation. A nonlinear feedback model is also developed for modeling the nonlinearity of the varactor in order to gain more intuition in the nonlinear process. Recommendations are made on how to design and bias the tank to maximize the linearity.

Second, a feedback-based band pass filter is designed by adding additional circuitry to Mohammadi’s original LC tank. A feedback notch is also developed using the same concept of feedback and Q-enhancement using a negative transconductance cell. Specifically, the band pass filter has a main LC tank in the feedforward path and an auxiliary tank in the feedback which can control the Q of the system by adjusting the feedback gain and minimally adding noise to the main path. For the notch, the current of a transistor is controlled by an LC tank and a feedback is added to boost the Q of the system when higher rejection is needed. Both systems have the capability of terminating the feedback path for low Q where the stand alone open loop system can provide the required specification.

Third, the band pass filter is implemented and laid out in IBM 8HP 0.13 µm BiCMOS process. The notch is also laid out in the same process. However, it only employs CMOS transistors
of the process. For both of the designs, post layout simulations have been run. In the post layout simulation, the S parameters are simulated to verify the main functionality of the systems. Moreover, linearity and noise of the system is evaluated to ensure the effectiveness of the proposed techniques. Lastly, the stability test has also been performed on the designs since both of the filters are feedback based which has the potential to be unstable.

The major contribution of this research is to realize software tunable systems over a wide frequency range. Moreover, based on the research conducted in this study regarding the linearity of varactors, designers will better understand the nonlinear process taking place in an LC tank and they will be able to improve it based on the developed model.

1.4 Organization of the Thesis

The organization of this research thesis is as follows. Chapter 2 provides background information and the introduction of important performance characteristics of a filter. Moreover, a literature review of the previous techniques and their shortcomings is presented. Chapter 3 introduces the two proposed designs with their block diagrams and the detailed circuit diagram of each block. The detailed design of each stage and component is discussed in detail. Moreover, the noise and nonlinearity of the system is studied and the nonlinearity is modelled using both volterra series and nonlinear feedback method. Both the theory and the designs are simulated and verified using Cadence Virtuoso. Chapter 4 examines the actual implementation and the lay out of the designs. For each design, the detailed layout of the system and their challenges is discussed. The designs are post layout simulated and the results are compared against schematic simulations. Finally, chapter 5 concludes on the research and ideas to possibly improve the system and suggests future work based on the simulations.
Chapter 2

Preliminaries

This chapter provides preliminary information about the concepts related to filtering, different type of filters and previous work performance comparison. The knowledge is critical to understand the approach taken with the two proposed filters. In this chapter, section 2.1 is dedicated to the introduction of basic concepts in filtering and the important performance metrics of a filter. Section 2.2 reviews the different filter topologies. Section 2.3 studies the state of the art in RF filter design and their performances are compared. Lastly, section 2.4 summarizes the chapter.

2.1 Basic Concepts

2.1.1. Filtering in RF Transceivers

Filters are one of the corner stones of each RF transceiver. In a dual conversion receiver, which is demonstrated in Figure 2.1, four filters are used in the receiving chain between antenna and baseband. First, a band select filter is employed to select the desired band. This filter has to be extremely low noise and low loss since it is the first block in Rx chain. Additionally, it has to be immune to the blockers. Therefore, high out of band linearity becomes a critical aspect of band select filters. Surface Acoustic Wave (SAW) filters are often used as band select filters. However, their lack of tunability makes the use of integrated filters more attractive in the future. The next three filters are for image rejection and band selection. Since these filters are preceded by a low noise amplifier, their noise requirement is more relaxed. However, the linearity requirement becomes more stringent as the filter gets closer to the base-band since the signal level increases. It is worthy to mention that in a zero-IF receiver, image is no longer a problem. However, a low pass filter is used after the mixer to select the desired channel.

Figure 2.1 Dual IF receiver architecture

Filters are also needed in transmitters. Figure 2.2 shows a Heterodyne transmitter where a band pass filter (BPF) is used after the second stage mixer. As can be observed from the figure, the filter is proceeded by a power amplifier (PA) which is responsible for delivering the required power to the antenna. The required power is usually set by the standard. If the output power of the PA is large (for example 30 dBm), the input power of it may also be considerable since PA is only
capable of providing a limited gain. In this case, linearity of the filter plays a crucial role in the transmitter chain. While the noise figure on the transmitter side is not a major concern, it has to be kept below the maximum out of band level allowed by the standard.

In a two-way communication, devices are designed to accomplish both receiving and transmitting. In this case, if the transmitter (TX) and receiver (RX) send and receive at the same time using the same frequency band, interference occurs and information loss takes place. Consequently, methods called multiple access techniques are compulsory to make the simultaneous transmit and receive feasible. There are three well-known multiple access techniques. Time Division Multiple Access (TDMA) is a method where the same frequency band is utilized by TX and RX concurrently. In order to avoid interference in this method, time slots are assigned to each path where TX and RX are only active in their own allowed time. In TDD transceivers, a switch is often used between TX and RX to avoid leakage. Code Division Multiple Access (CDMA) is another method of multiple access which utilizes orthogonal codes for each path in order to facilitate information transfer from different paths at the same time. Finally, Frequency Division Multiple Access (FDMA) allocates different frequency spectrum to TX and RX to avoid interference. FDMA makes it possible for the transceiver to transmit and receive at the same time. However, due to the non-idealities of RF blocks, a portion of transmitted signal may leak into the receiving path. This is demonstrated in Figure 2.3. This type of leakage is called self-interference or in-band interference, and it can be avoided by placing a filter called duplexer between TX, RX and antenna. The role of the duplexer is to allow passing of the signal from antenna to RX and from TX to antenna while blocking any signal passage from TX to RX. [3]
2.1.2. Performance Metrics

Filters are categorized in five types of low pass (LPF), high pass (HPF), band pass (BPF), band stop or notch (BSF) and all pass (APF). In this research, the focus is on BPF and BSF. The first important metric for a BPF or BSF is the center frequency. When the center frequency of a filter is determined, it is important to gain information on how wide the pass-band is and how sharp the transition from band pass to band stop would be. The former is determined by 3-dB bandwidth in a BPF, and the latter is characterized by the order of the filter. For BSF, the two mentioned parameters are determined by its BPF counterpart which will be explained later in this section. A BPF (or BSF) can be as low as second order and the general transfer function for a second order BPF, which is what this research is mostly concentrated on, is as follows:

\[
H(S) = A_v \frac{\omega_0 S}{S^2 + \omega_0^2}
\]  

(2.1.1)

Where \(A_v\) is the pass band gain, \(\omega_0\) is the center frequency and \(Q\) is the quality factor which is proportional to the ratio of the center frequency divided by the bandwidth of the filter. The transfer function of a BSF is derived by subtracting a constant equal to the gain of the BPF from its transfer function. The transfer function of a second order BSF will then be:

\[
H(S) = A_v \frac{S^2 + \omega_0^2}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}
\]  

(2.1.2)

The general form of BPF and BSF frequency response is shown in Figure 2.4. As can be observed from the figure, all three mentioned parameters of BPF can be determined from its frequency response. However, bandwidth (or \(Q\)) cannot be measured directly from the frequency response of BSF. In order to measure \(Q\) for a BSF, an all pass response has to be subtracted from it.
At the presence of a blocker, it is important to adjust the center frequency of the band pass filter and its bandwidth to select the desired band while rejecting the interferer. If the blocker level is large, a band stop filter is used and its center frequency is placed in the frequency of the blocker and its bandwidth is adjusted according to the blocker’s bandwidth. Therefore, the range of Q and center frequency tunability are important performance metrics.

The metrics introduced in the previous paragraph are all linear metrics neglecting the nonlinear effects. The assumption is valid if the filter used is a passive filter with no active component. However, in order to make the filter frequency and Q tunable, nonlinear components may be added to the system. Therefore, nonlinearity has to be quantified. There are two types of nonlinearity in filters, out of band nonlinearity, which determines how blocker resilient the system is and in band linearity defined to measure the linearity of the system when processing the desired signal. Both in band and out of band linearity can be defined in terms of 1-dB compression point or 3rd order intercept point (IP3). For 1-dB compression point, the input power is increased until the gain is dropped by 1-dB. Depending on the frequency of the tone, it defines in or out of band linearity. For IP3, two tones (in or out of band) are applied to the system and by applying the following formula, IP3 can be obtained:

$$IP3 = P(\text{main tone}) + \frac{\Delta P}{2}$$  \hspace{1cm} (2.1.3)

Where $\Delta P$ is the power difference between the main tones and their third order products. This method is called two tone test. 1-dB compression point and 3rd order intercept points are demonstrated in Figure 2.5.
When multiple stages are cascaded, the overall third order intercept point (or 1-dB compression point) in term of IP3 of each stage can be approximated as:

$$\frac{1}{A_{IP3,total}^2} = \frac{1}{A_{IP3,1}^2} + \frac{\alpha_1^2}{A_{IP3,2}^2} + \frac{\alpha_1^2\alpha_2^2}{A_{IP3,3}^2} + \cdots$$

(2.1.4)

Where $\alpha_i$ is the linear gain of each stage. It can be concluded from 2.1.4 that the linearity of the last stages is more important than the linearity of the first stages and as the gain of a stage increases, it imposes stricter requirements for the linearity of its proceeding stage. This can also be implied by intuition. In a receiver, the first stage experiences a low intensity signal and hence remains in its linear region. However, if it amplifies the signal with a large gain, the second stage may not necessarily work only in its linear region around its bias point. In conclusion, if the target filter is a duplexer or a band select filter appearing before the LNA the linearity is not of main concern. However, for the channel select/image reject filters the effect of nonlinearity becomes more severe. It is important to mention the relaxed linearity requirement for the first stage filters may not always be true. While the signal level at the first stage is low in most cases, the interference level may not be. Therefore, high out of band linearity may be required while low in band linearity could be sufficient. Another important fact is that although the issue of out of band interference is not of concern on the transmitter side, self-interference due to the nonlinear elements in a transmitter could be detrimental to the receiver.

Noise is another issue which needs to be addressed in RF filter design since it determines the sensitivity and the dynamic range of the receiver. Sensitivity is defined as the minimum detectable signal with an acceptable quality and is calculated by the following formula:

$$P_{sensitivity} = -174 \frac{\text{dBm}}{\text{Hz}} + NF + 10\log(\text{Bandwidth}) + \text{SNR}_{\text{min}}$$

(2.1.5)

Where NF is the overall noise figure of the system and $\text{SNR}_{\text{min}}$ is the acceptable signal to noise ratio. The overall noise figure of the system is obtained using Friis equation:

$$NF_{\text{tot}} = NF_1 + \frac{NF_2-1}{A_{P_1}} + \cdots + \frac{NF_{m-1}}{A_{P_1\cdots P_{m-1}}}$$

(2.1.6)
Where $A_p$ is the power gain of each stage and $m$ is the number of stages. If the gain of the first stage is large, the overall noise figure is determined by the noise figure of the first stage and the noise figure of the following stages will be negligible. Therefore, if a filter is not on the first stage of a receiver, its noise figure requirement will be more relaxed.

As it will be explained in next chapter, a trade-off exists between NF and linearity. Consequently, one can improve NF by degrading linearity and vice versa. However, this type of improvement is not considered as an improvement in the system. In order to have a fair comparison between different filter structures, dynamic range is defined as the maximum input level a receiver can handle divided by the minimum level it can process. Therefore, even if NF is improved at the cost of linearity the dynamic range remains constant. There are different standards for the maximum power a system can handle. For this research, the focus is on linear dynamic range which is defined by:

$$ DR_1 = P_{1-dB} - P_{sensitivity} $$  \hspace{1cm} (2.1.7)

Where $P_{1-dB}$ is the 1-dB compression point and $P_{sensitivity}$ can be obtained from equation 2.1.5.

### 2.2 Filter Topologies

Filtering is a general mathematical concept independent of its actual implementation. While mathematically, there is a singular way to define a second order band pass filter, the filter implementation could be in multiple methods. In this work, the focus will only be on analog and mixed-signal filters where the implementation is accomplished in electronic circuit level design. The concept of analog filtering is an old concept dating back to 1915. However, the monolithic filters became widespread after 1980. Using Integrated Filters for RF communication was introduced after 1996 when active RLC prototypes were implemented [6]. Integrated filtering for interference cancellation is an ongoing hot topic thanks to the invention of software defined radios (SDR) where filter tuning using software becomes attractive.

Over the past decades, with the development of Integrated Circuit technology, high quality active and passive components were realized which caused different filter topologies to emerge. In this section, different filter topologies will be studied and their pros and cons will be qualitatively discussed and the detailed quantitative comparison of the best achieved performances will be left to section 2.3.

#### 2.2.1. Passive Filters

Passive filters in traditional way are the most basic type of filters. However, the term passive can be applied to all filters where active elements are not an integral part of filtering function. In this section, two types of passive filters will be discussed. The first type, traditional passive filters are the design targets of this work and additional circuitry will be added to them to boost the performance. Since the added circuits will have active elements, these type of filters are regarded as active Q-enhanced LC filters. However, they are different than other types of active filters which will later be discussed in this chapter.

The second type, N-path filter is another emerging filter in the state of the art RF tunable filter design.
Traditional passive filters consist of pure passive elements to synthesize the desired transfer function. The first design step of most type of filters starts by designing a passive prototype and converting it to the desired active topology in later steps. Therefore, understanding passive filters is not only essential for the designing of passive filters themselves but also it is imperative to design a non-passive filter. The most basic types of passive filters are RC and RL filters. An RC filter is demonstrated in Figure 2.6. The input-output transfer function for a first order RC filter can be obtained as:

\[
\frac{V_{\text{out}}(S)}{V_{\text{in}}(S)} = H(S) = \frac{1}{1+SRC}
\]  

(2.2.1)

2.2.1 is a low pass filter with a cut-off frequency of \(1/2\pi RC\). The high pass counterpart of the mentioned filter can be synthesized by substituting R and C which leads to the high pass function with the same cut-off frequency.

![First order low pass and high pass filters](image)

Figure 2.6 First order low pass (left) and high pass (right) filters

Low pass and high pass functions can also be implemented using R and L. The in common characteristic between all the mentioned filters is that they are one pole systems. In a one pole system the energy delivered from the source can be stored in one element and if the source is turned off the stored energy starts dissipating in the resistor until it vanishes. In order to realize a band pass function, at least one RLC tank has to be used. When L and C are placed together in a circuit, they can exchange energy between each other. In this case, the system becomes a two pole system. It is important to mention a two pole system can also be synthesized by cascading two one pole systems. However, that doesn’t produce a band pass function. In an RLC circuit, the stored energy in L or C starts a decaying oscillation when the source of the energy is nulled. As R increases, the oscillation continues to run for a longer period. The frequency of the oscillation is \(1/2\pi\sqrt{LC}\). The mentioned phenomena can be translated into the Quality factor (Q) of the band pass transfer function. When R is larger, the filter is more selective around the frequency of oscillation and consequently leads to a higher Q. The basic diagram of RLC circuits are shown in Figure 2.7. The left diagram is when the tank input is a voltage source and the right diagram is when the input of the tank is current. Both circuits show same behavior and they are Thevenin/Norton equivalent of each other.
Figure 2.7 Thevenin (left) and Norton (right) second order band pass filters

The transfer function of the Thevenin circuit is:

\[
\frac{V_{out}(S)}{V_{in}(S)} = H(S) = \frac{1}{\frac{1}{RC}S + \frac{1}{LC}} \quad (2.2.2)
\]

And for the Norton circuit:

\[
\frac{V_{out}(S)}{I_{in}(S)} = H(S) = R \frac{1}{\frac{1}{RC}S + \frac{1}{LC}} \quad (2.2.3)
\]

The difference between 2.2.2 and 2.2.3 is that the pass band gain for the voltage driven circuit is 1 while it is proportional to the tank resistance for the current driven case. The practical pros and cons of each circuit will be discussed in detail in chapter 3. By comparing 2.2.2 with 2.1.1, \(Q\) can be derived as \(R \left( \frac{\sqrt{L/C}}{Q} \right)\) and by dividing the center frequency by \(Q\), the bandwidth of the filter will be \(1/RC\). In circuits of Figure 2.7, the center frequency of the tank can be controlled by changing the capacitance (or the inductance) and the bandwidth (\(Q\)) of the circuit can be fully controlled by changing the resistance. However, this is only valid when the \(Q\) of the capacitor and inductor are infinite. When the storing elements (L and C) have finite \(Q\), the \(Q\) of the tank is limited by the \(Q\) of the elements. Figure 2.8 shows how finite \(Q\) of the elements impact the equivalent resistance of the tank and consequently degrade the bandwidth of the circuit.

Figure 2.8 The effect of finite \(Q\) of the elements on the overall \(Q\) of the system

Where \(R_L\) and \(R_C\) are \((L\omega_0)/Q_L\) and \(1/(Q_C C\omega_0)\) respectively and \(Q_L\) and \(Q_C\) are the \(Q\) of each component which depends on the technology used to fabricated them. By applying series to parallel conversion at the center frequency of the tank, \(R_L'\) and \(R_C'\) are derived as \((1 + Q_L^2).R_L\) and \((1 + Q_C^2).R_C\). By assuming the \(Q\) of the components are large enough, L and C remain unchanged after series to parallel conversion. After the conversion, the new \(Q\) of the system will be \(R_{eq}/\left( \sqrt{L/C} \right)\) where \(R_{eq} = R||R_L'||||R_C'\). In practice, capacitors have higher \(Q\) and the equivalent resistance of the tank will be the parallel of
tank resistance and inductor resistance. While R can be implemented as a variable resistor by using CMOS transistors, the designer doesn’t have much control over the value of R<sub>L</sub>. Therefore, the Q tuning using R will only be limited to the cases where the tank resistance is significantly smaller than parallel inductor resistance. That limits the maximum achievable Q to less than 15 in 4 to 8 GHz frequency range using IBM 0.13 µm BiCMOS technology. It can be concluded that if only passive components are used in a filter, a very selective filter cannot be implemented. In order to address the issue of low Q, Q-enhancement techniques are used to boost the Q to higher values. While the implementation of the Q-enhancement circuits varies, the basic of all of them is to design a negative resistance circuit which can cancel out the finite resistance of the elements. Since negative resistance is achieved by using active components, Q-enhanced filters are regarded as active filters.

A band-stop filter has also been designed in this thesis. The circuit diagram of a band stop filter is demonstrated in Figure 2.9. Similar to its band pass counterpart, a band stop filter can be inputted with both voltage and current.

![Thevenin and Norton equivalent circuits](image)

**Figure 2.9 Thevenin (left) and Norton (right) second order band stop filters**

The transfer function for the Thevenin circuit is:

\[
\frac{V_{\text{out}}(S)}{V_{\text{in}}(S)} = H(S) = \frac{S^2 + \frac{1}{LC}}{S^2 + \frac{R}{L}S + \frac{1}{LC}}
\]  

(2.2.4)

And for the Norton’s equivalent:

\[
\frac{V_{\text{out}}(S)}{I_{\text{in}}(S)} = H(S) = R \frac{S^2 + \frac{1}{LC}}{S^2 + \frac{R}{L}S + \frac{1}{LC}}
\]  

(2.2.5)

Comparing both of the equation with 2.1.2, the center frequency of the filter will be \(1/\sqrt{LC}\) with the Q of \((\sqrt{L/C})/R\). For the voltage-driven circuit, the gain is unity while it is proportional to the resistance for the current-driven one. In a band stop filter, in contrast to band pass filter, the Q is inversely proportional to the resistance of the circuit. While this may not be important in theory, it introduces serious practical issues for the implementation of a band stop filter. For the proposed design, as it will be explained in next chapters, the
characteristic impedance of the tank which can be calculated from $\sqrt{L/C}$ is in the order of 10. As an example, if the value of the resistance is in the order of 1 $\Omega$, the Q of the circuit limits to the values less than 10. When laying out a circuit, the parasitic resistance of 100 m$\Omega$ and larger is typical. Even if the resistance is reduced by using thicker lines, the circuit still needs a driver. For the voltage driven case, the typical value of the driver’s resistance is tens of ohms. For current driven circuit, although driving with a very small resistance might be possible, the gain is also proportional to the resistance meaning the gain has to be compromised to achieve a large Q. If the circuit is designed to provide a 100 m$\Omega$ resistance, a transconductance of at least 10 A/V is required to keep the gain at 0 dB. This value is impractical in BJT and CMOS circuits. Reducing the transconductance to any value less than 10 A/V makes the filter a lossy element and consequently the NF gets degraded. Therefore, using only passive elements, it is not possible to achieve a high Q band stop response. It will be explained in next chapters how the mentioned issue is going to be addressed.

- The invention of N-path filter which is another type of passive filters dates back to 1960. N-path filter is an alternative approach to the traditional passive filters in order to realize filter transfer functions [7]. The basic idea of N-path filter is conceptually demonstrated in Figure 2.10 [4]:

![Figure 2.10 Block diagram of an N-path filter architecture](image)

In the figure, p(t) and q(t) are mixing functions aiming to up and down convert the signal, $T$ is the period of the mixing function and $h(t)$ can be any arbitrary function depending on the desired functionality of the system. The detailed analysis of N-path filters is beyond the scope of this work. However, in order to compare the performance, a band pass filter architecture is explained. A band pass N-path filter operation is shown in Figure 2.11. In order for the system to act as a band pass filter, $h(t)$ needs to be a low pass function. The
circuit down converts the signal to base band using p mixers. In baseband, a sharp low pass function is implemented. After up conversion with q functions, the output is a band pass filter with the center frequency equal to the frequency of mixing functions and the bandwidth equal to the cut-off frequency of low pass $h(t)$.

![Figure 2.11 Conceptual N-path frequency plots for a band pass filter](image)

While each block in the filter can be implemented in different ways, the design presented in [4] is the basic of all current N-path filter designs. The circuit schematic of a band pass filter using N-path technique along with its simplified version is shown in Figure 2.12. The low pass function is implemented using an RC circuit. Passive switches are used to realize mixing functions. Since both p and q mixers are in phase for each path, the circuit sees an RC when both are on and an open circuit when both are off. Therefore, they can be replaced by one switch in order to simplify the circuit. Non-overlapping clocks have to be generated for each path. As can be observed from the figure, all the elements used in an N-path filter are passive elements. Therefore, N-path filters can be regarded as passive filters. However, there are different from traditional passive filter in the sense that mixing function is used in them which is a nonlinear function in order to realize a band pass filter while traditional passive filters only use linear elements. N-path filters are capable of providing an outstanding linearity due to the using of only linear elements and passive mixers. The power consumed by the circuit is only coming from the clock generation part and it increases as the frequency of operation increases. This fact makes N-path filters less desirable at higher frequency ranges. Moreover, generating non overlapping clocks can be extremely challenging at high frequencies. Another factor limiting the performance of N-path filters is the resistance and parasitic capacitance of the switches. It can be shown the mentioned non idealities of switch degrades selectivity of the filter.
Other types of filter while not as popular as band pass can be implemented by N-path techniques. As an example, if \( h(t) \) is a high pass function, the overall transfer function would be a band stop filter.

N-path filters are capable of providing outstanding linearity and noise since they only use passive components. While their low NF is ideal for those filters to be used as the first building block of transceivers, they can also be used at the stages where linearity is a main concern. However, due to the difficulty of generating non overlapping clock and high parasitic capacitance of switches at higher frequencies, their performance is limited to a few gigahertzes.

### 2.2.2. Switched Capacitor Filters

Switched Capacitor filters (SC) are discrete-time filters. In a CMOS integrated circuit technology, MOSFET transistors can be fabricated along with capacitors. Therefore, SC filters become attractive when the only elements used are transistors and capacitors. The idea of the switched capacitor is to transfer electronic charge from one capacitor to another to simulate a resistor. SC filters provide the highest accuracy of all analog and mixed-signal filters and they are programmable with digital circuits.

The main building block of a SC filter is a switched capacitor which aims to provide same behavior as a resistor. A resistor by definition is an element which the ratio of its terminal voltage over its current is constant and the constant is called the resistance. The main block of a switched-capacitor is shown in Figure 2.13.
There are two phases on each cycle. At phase 1, $S_1$ is closed while $S_2$ is open which makes the voltage of capacitor $C$, $V_A$ and its charge will be $CV_A$. At phase 2, $S_1$ becomes open while $S_2$ is closed making the voltage $V_B$ and charge will be $-CV_B$. Now, the charge going from node A to node B on each cycle is going to be:

$$Q = C(V_A - V_B)$$  \hspace{1cm} (2.2.6) \\

In order to calculate the current flowing through the switched capacitor elements on each cycle, the amount of charge transferred has to be divided by the transfer time which is one period. Doing so will result it:

$$I = \frac{Q}{T} = \frac{(V_A - V_B)C}{T}$$  \hspace{1cm} (2.2.7) \\

It can be seen from 2.2.7 the ratio of voltage and current is equal to $T/C$ which defines the equivalent resistance of a switched capacitor. In a first order low pass filter, the cut-off frequency of the circuit is proportional to $R_{eq}C_{eq}$. If the switched-capacitor element is placed in a first order circuit with a capacitor $C_{eq}$, the resulting cut-off frequency will be:

$$f_{\text{cut-off}} = \frac{C}{C_{eq}T}$$  \hspace{1cm} (2.2.8) \\

Two important points can be extracted from 2.2.8. First, the cut-off frequency can easily be tuned by changing the period of switching. Second, the frequency is proportional to the ratio of two capacitors. Therefore, SC filters can be implemented with the accuracy of better than 0.1 percent [6]. While an attractive choice for low frequency and base-band filtering, switched capacitor cannot be implemented in high frequency due to the difficulty in generating a high frequency clock and the parasitic capacitances of the circuit which degrade the performance of the filter.

### 2.2.3. Active Filters

As it was explained in 2.2.1, for generating a band pass response with passive components, using of an inductor is unavoidable. The main motivation of active filters is to replace the bulky and low Quality factor (Q) inductors with active elements. In order to realize that, a combination of amplifiers, resistors and capacitors are used.

Depending on how inductors are replaced with active elements, there will be different active filter categories [6]:

- In active-RC filters, an operational amplifier is used along with Rs and Cs in feedback loops to replace inductors. This is the most traditional method of active filtering.
In some cases, the technology available to the designer is not capable of providing high quality resistors. In those cases, the resistor can be replaced by a MOSFET transistor where the new category is called MOSFET-C filters. Although MOSFET-C structure makes the integration of the filter using traditional technologies possible, it comes with drawbacks. MOSFET transistor is an active element in contrast to a simple resistor where voltage and current relation is always linear. This introduces nonlinearities compared to the original active-RC filter. In addition to the previous disadvantage, every MOSFET transistor requires a certain gate to source voltage to realize a certain value of resistance. If that voltage changes, the resistor will change. Therefore, the voltage swing will be limited in MOSFET-C filter compared to active-RC.

Gm-C or OTA-C is another category of active filters. In contrast to the active filters introduced so far where feedback loops are employed, Gm-C filters are open loop filters. This makes Gm-C filters a more attractive solution compared to other types of active filters for high frequency applications. Another advantage of this filter is unlike MOSFET-C, the tuning and swing can be independent of each other. It will be explained in 2.3 that while Gm-C filters are attractive for frequencies up to 1 GHz, Q-enhanced filter is still superior for higher frequencies due to its higher dynamic range for the same Q.

In the design of each active filter, first, the type and order of the filter is determined based on the design requirements. Second step is the passive realization of selected filter using Rs, Ls and Cs. After this step, inductors are transformed to active elements depending on the type of active filter to be used in the design.

Active filters are attractive solutions where high performance is needed in a moderate frequency and the silicon area is limited. However, they suffer from lower accuracy compared to switched capacitor filters. Therefore, a tuning circuitry is often used to reach an accuracy of better than 1 percent. Another shortcoming which makes it impractical to design an active filter for this research is lack of a practical method for Q tuning which is one of the design requirements of this work.

2.3 Literature Review

While one of the limitations of active-RC filters is the fact they are based on feedback techniques, with the advent of new advanced technologies, their implementation in higher frequencies becomes more feasible. [8] presents an active-RC filter for 0.8 to 2.2 GHz frequency range. Due to the high NF of around 20 dB, the filter has to be used after an amplifier which can be done since circuit shows outstanding in and out of band IIP3. While the active filter presented in this paper achieves a promising performance, there is still lack of Q tuning technique for the filter. Although there has been numerous effort to improve the performance of active-RC filters for RF applications, the maximum operating frequency hasn’t been exceeded to more than 3 GHz to the knowledge of the author.

The major focus of recent RF filter designs has been on N-path filters. As mentioned in the previous section, the concept of N-path filtering is an old concept. However, [4] has revolutionized the use and modeling of N-path filters for RF frequencies with tuning capabilities. There have been efforts since then to implement different types of filters using the N-path technique. [9] presents 6th order filter using the N-path technique for 600 MHz to 850 MHz. The design provides an in-band 1-dB compression point of 0 dBm with the NF of 8.6 dB. Q ranges from 40-90 along the
frequency range and it is not tunable. [10] develops a new filtering structure by combining the N-path filter with gm-C resulting a 4th order band pass filter with the frequency ranging from 0.4 to 1.2 GHz. The filter has the in-band 1-dB compression point of -4.4 dBm and NF of 10 dB. The bandwidth of the filter is 21 MHz and it is not tunable. [11] presents a 6th order band pass filter for 0.1 to 1.2 GHz frequency range with the NF of 2.8 dB and bandwidth of 8 MHz. There is no data on the in-band linearity of the filter. However, the filter is capable of tolerating up to +7 dBm of blockers.

Q-enhanced LC filters have also been developed for RF applications. In [12], a Q-enhanced LC filter has been designed for 1.98 to 2.02 GHz frequency range with the NF of 15 dB and in-band 1-dB compression point of -6.6 dBm. The filter provides 130 MHz of bandwidth for 2 GHz center frequency and it is not bandwidth tunable. Although employing Q-enhanced LC structures in the TRX chain is common, designing RF filters using the technique has not been a major focus for RF designers. Recently, [5] has proposed a Q-enhanced 2nd order LC band pass filter capable of both frequency and bandwidth tuning. The frequency operation of the circuit ranges from 2.25 to 4.5 GHz. Q is tunable from 5 to 150. NF ranges from 10 dB for the minimum Q and rises up to 18.5 dB for the highest achieved Q. 1-dB compression point is ranging from -8 dBm to 9 dBm. A 4th order version of [5] has been implemented in [13].

The second design in this work is a band stop filter (notch). Therefore, recent works on notch has to be studied as well. The mentioned techniques for band stop filter can also be used to create a notch. In [14], efforts have been done to design and model notch filters using N-path concept. A tunable notch with the center frequency ranging from 0.1 to 1.2 GHz has been designed. The notch is capable of providing up to 24 dB of rejection while imposing 1.6 dB to 2.5 dB of NF with the 1-dB compression point of better than 2 dBm. No Q tenability has been reported for this design.

[15] develops LC notch along with a low noise amplifier capable of achieving up to 35 dB of rejection along its frequency range of 5 to 6 GHz. With the noise figure of better than 6.2 dB the in band 1-dB compression point of the filter is better than -30 dBm.

Notch filter has also been developed using RF MEMS. [16] demonstrates a high performance notch with 40 dB of rejection along 1.1 to 2.7 GHz frequency range with the bandwidth of 125 MHz. Although the notch presented in the mentioned paper shows high performance characteristics, it cannot be compared with CMOS and BiCMOS Integrated Circuits since it is not capable of software based tuning.

[17] implements a band stop filter by subtracting a Q-enhanced filter response from an all pass response. Two filters are designed for 2 to 4 GHz and 4 to 8 GHz ranges. The 2-4 GHz prototype can provide as high as 50 dB rejection with the NF of 12.8 to 13.5 dB and 1-dB compression point of -3 dBm to -1 dBm. For 4 to 8 GHz design, the numbers are 8 to 10.8 dB of NF and -9 to -6 dBm of 1-dB compression point.

The designs mentioned so far are listed as band stop and band pass filters. There are other systems called “interference cancelling” systems which are aimed to provide same functionality of the mentioned filters by employing additional circuit techniques compared to traditional filters. [18] categorizes the interference cancelling techniques into three categories of frequency translational filtering, feedback filtering and feedforward filtering. The three mentioned techniques are demonstrated in Figure 2.14.
Figure 2.14 Interference Cancellation Techniques – Frequency translational filtering (left), Feedforward filtering (middle) and Feedback technique (right)

Frequency translational technique is a technique where the signal is down-converted to the low frequency and low pass-filtered to mitigate the blocker. It is more trivial to perform filtering function in base band than RF. If the mixer used before the filter is a passive mixer, the system will be highly linear at the cost of high NF. The technique can also be used to reject the leakage from the transmitter to receiver. However, the noise imposed by transmitter to receiver has to be carefully studied. In addition to all the mentioned characteristics, this structure has the pros and cons of direct conversion receivers such as flicker noise and LO feedthrough to antenna.

Feedforward is a method where the signal is rejected in an alternative path and is then subtracted from the main path in order to cancel the interferer. The notch in the alternative path can be implemented using different methods. [19] proposes a new design based on the feedforward technique. The notch is implemented in the paper using down-conversion and high pass filtering followed by an up-conversion. While the architecture can show a promising performance, the noise imposed by the alternative path has to be reduced. Moreover, since the interferer is not mitigated at the input, the low noise amplifier (LNA) has to be able to handle large blockers without going to saturation.

The third technique is called feed-back. Both of the designs in this work are based on this method. In the feedback method, the notch is placed in the feedback path and by applying gain to feedback, the out of band signal level is reduced while the level of in band signal remains unchanged and consequently the system can provide large Q and high out of band rejection. The advantage of the feedback system proposed in 2.14 is the blocker is cancelled before the LNA and hence the linearity requirement of the amplifier will be more relaxed. In this method, the stability of the circuit has to carefully considered since all feedback systems have the potential to become unstable. Moreover, the noise penalty by the feedback path increases if a high rejection is desired. This will be explained in the implementation of the system in next chapter. Same as feedforward system, the implementation of the notch can vary. The notch can be synthesized by placing a band pass filter in the main path and subtracting it from an all pass response as the filter implemented in [17]. The output of the notch can then be fed back using a variable gain amplifier to control the Q of the system.

2.4 Chapter Summary

This chapter starts by introducing the basic concepts of RF filtering and its importance in both transmit and receive chain. Then, the important parameters and performance characteristics are introduced. After introducing the basics of filtering, three different types of passive, switched capacitor (mixed-signal) and active filters are discussed. For each type of filter, the basics are discussed and the advantages and disadvantages of each type of filter are reviewed. Lastly, the
most recent work on each type of filter is presented. Moreover, the concept of interference cancelling and its different types of frequency translational, feed forward and feedback is discussed. For each mentioned method, the pros and cons are mentioned. The proposed design in this work will consist of Q-enhanced LC filter design as well as employing feedback based interference cancelling technique to achieve a better performance.
Chapter 3

Proposed Designs

There are two proposed designs for this work. Both of the systems are required to have a wide center frequency and bandwidth tuning range. The most important requirement for an interference canceller is to be able to tolerate strong interferers without going into nonlinear region. Noise is another important factor that needs to be considered especially if the systems are meant to be used in the receiving chain. High linearity and acceptable noise figure along with wide bandwidth and center frequency tuning range is achieved by adding a feedback path to Q-enhanced LC filters.

This chapter starts by defining the design requirements for the band pass and band stop filters. Then, the block diagram of the proposed solutions will be introduced to gain a better understanding of the techniques employed for this work. The circuit details of each design will then be explained by mentioning component values. In order to model the nonlinearity of the LC tank for the designs of this work, the Volterra nonlinearity analysis of the varactors along with simulations verifying the analysis will be presented. A nonlinear feedback-based model of the LC tank will also be introduced and compared with Volterra analysis.

3.1 Design Requirements

The proposed BPF is an enhancement based on the system designed by Laya Mohammadi [5]. While mentioned system is a second order Q-enhance LC filter designed for 2-4 GHz frequency range, the target of this thesis is to design a BPF for 4-8 GHz with the Q ranging from lower than 10 up to 150 and more. Q tuning is attractive since the position of the blocker in frequency spectrum varies and higher Q may be required if the blocker is closer to the desired signal.

In a Q-enhanced filter, the noise increases as Q increases [5]. Moreover, since a nonlinear element is used to increase the Q of the filter, 1-dB compression point (in band) is increased for the higher Q cases. As it has been shown in [5], 1-dB compression point can be as high 10dBm for low Q and -10dBm for high Q. Minimum NF varies from 10 dB for low Q and 20 dB for the Q of higher than 100.

The notch is designed for 4 - 8 GHz frequency range as well. The design is based on 0.13 μm BiCMOS where f_T of CMOS transistors are limited to less than 100 GHz while HBT transistors are capable of providing up to 200 GHz. However, if a more advanced CMOS technology is used, the same idea can be implemented for higher frequency ranges. The minimum depth of the notch is targeted to be at 40 dB. However, it should be adjustable for the cases where 40 dB is not required. NF has to be lower than 8 to 10.8 dB, which is reported at [17], and 1-dB compression point should be better than -6 dBm to -9 dBm, which is reported at [17]. Moreover, depending on the bandwidth of the blocker, Q has to be tuned from values below 10 to 60 and higher.
As it will be explained later in this chapter, both of the systems proposed in this research are feedback based where stability is a major issue. Therefore, K stability factor has to be simulated and kept above 1 in order to ensure proper function of the systems.

3.2 Block Diagram

3.2.1 Band-Pass Filter

The basic idea of this design originates from the notch proposed in [17]. In a negative feedback system with the forward gain of $A_{OL}$ and loop gain of $T$, the input-output relationship is:

$$\text{OUT} = \text{IN} \cdot \frac{A_{OL}}{1+T}$$

Comparing it with an open-loop system where the input is only multiplied by $A_{OL}$, it can be concluded that the signal gets smaller by the factor of $1/(1 + T)$ in a feedback system compared to an open-loop system if a circuit can be designed in a way that only out of band signals appear in the feedback path, their magnitude can be reduced by increasing the loop gain. One method to achieve the mentioned goal is to synthesize a notch using a Q-enhanced band-pass filter and an all-pass filter and obtain the notch by subtracting the output of the two filter. The synthesized notch then can be fed back to the input with a variable gain amplifier which controls the loop gain. The mentioned system is shown in Figure 3.1.

As depicted, the notch is synthesized at the node $V_{\text{notch}}$ and is fed back using the gain block of $A_V$. If all the blocks used in Figure 3.1 are ideal, by increasing the loop gain, the out of band signal will be rejected while the in band signal will remain unchanged. Using this method, the Q of the filter can be adjusted to the desired value. Q-enhancement can also be proved mathematically. If the transfer function of the band pass filter is assumed to be:
\[ H(S) = \frac{\omega_0 S}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2} \]  

(3.2.2)

Then the overall transfer function of the closed loop system of Figure 3.1 can be obtained as:

\[ H(S) = \frac{\omega_0}{Q(1 + A_V)} S \]  

\[ \frac{S^2 + \frac{\omega_0}{Q(1 + A_V)} S + \omega_0^2}{\omega_0^2} \]  

(3.2.3)

By comparing 3.2.2 with 3.2.3, it can be concluded that the Q of the new filter has been scaled by 1 + A_V without changing the pass band gain.

There are three main issues with the design mentioned in Figure 3.1. First, the gain of band pass and all pass filter should be perfectly matched. If any mismatch occurs, there will be interferer as well as signal in the feedback path. This will not only degrade the performance of filter in terms of Q but it also degrades the linearity of the system. This happens due to the fact that the band pass filter could experience a positive feedback if any gain mismatch occurs between all pass and band pass filters. Second, in the actual implementation of the filter, each node in the feedback path has its own parasitic capacitance. This can potentially lead the system to an unstable state since each pole degrades the phase margin of the system if it gets close to the operating frequency of the circuit. Third, as mentioned, in order to get higher Q, the loop gain of the filter has to be increased. This leads to an increase in the input-referred noise proportional to feedback. Therefore, with increasing the Q, the noise figure of the system degrades dramatically which also can be proven mathematically. If the output noise of the band pass filter is modelled as \( v_{n,BPF} \), the input referred noise of the system due to the band pass filter noise is going to be:

\[ \frac{v_{n,BPF,\text{in}}^2}{v_{n,BPF}^2} = \left| 1 + A_V \right|^2 \frac{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}{\omega_0^2} \]  

(3.2.4)

Since only the in-band noise is important, it can be concluded the input referred noise due to the band pass filter is increased by 1 + A_V factor. Moreover, the output noise of the variable gain amplifier directly appears at the input and it increases as its gain increases.

The short comings introduced make the system of Figure 3.1 not practical for high Q especially due to its noise behavior. The main source of the problem is the synthesized notch is not capable of completely decouple the band pass signal and its noise from the feedback path. A solution proposed to that problem is to use an LC notch instead of a synthesized one. The proposed solution is demonstrated in Figure 3.2.
For this system, the in band output noise of the band pass filter is suppressed by the notch. Moreover, if the depth of the notch is enough, there will be no signal in the feedback path and positive feedback does not occur. Therefore, the linearity does not get degraded. The system proposed in 3.2 still cannot reduce the noise effect caused by the amplifier in the feedback. In order to solve this issue, it is preferable to add the gain stage before the notch so that its noise gets cancelled. Therefore, a modified version of the system proposed in Figure 3.2 is introduced in Figure 3.3.

In the system proposed in Figure 3.3, the only important noise is the noise of the buffer which has to be minimized. The use of buffer is unavoidable since the output of the notch cannot be directly fed to the band pass filter. Another advantage of the system is that the output parasitic capacitance
of the variable gain amplifier and the input parasitic capacitance of the buffer can be resonated out using the notch. Moreover, the input parasitic capacitance of the variable gain amplifier and the output parasitic capacitance of the buffer can also be compensated in the band pass filter.

There are a few practical points to design the system mentioned in Figure 3.3 which has to be carefully considered to avoid the performance degradation of the system. First, the equation of 3.2.3 is not valid for the system. However, the Q of the system will still be increased by increasing the loop gain. Second, as it will be explained later, it is preferable to use a current amplifier instead of a voltage buffer at the output of the notch. Third, for the variable gain amplifier to have a large range of gain control, more than one stage is required. Therefore, there will be internal polls in the feedback loop. In order to avoid the stability issues, the bandwidth of each amplifier stage has to be designed far away from the operating frequency of the circuit. While the notch can suppress the noise of the band pass filter, it may introduce noise to the system. Therefore, the design of the notch is important to ensure minimum noise is added to the system.

3.2.2. Band-Stop Filter

As explained in section 2.2.1, a high Q LC notch is not possible by using only a series LC circuit due to the fact that the Q of the circuit is inversely proportional to the resistance requiring extremely low resistances. The basic idea of getting a high Q notch is to use a transconductance. A transconductance is defined as a two port element in which the output current is proportional to the voltage across its input. The transconductance is changed to a three terminal two port circuit by assuming common reference between the two port. If the common port is connected to ground, it works as a normal transconductor and if the common port is connected to a high impedance, the circuit cannot produce current at its output. In Figure 3.4, an ideal transconductance is shown with an impedance at its common terminal.

![Transconductor Diagram](image)

Figure 3.4 An ideal transconductor with an impedance in its common terminal

the out-input relationship of the mentioned circuit is:

$$\frac{i_{out}}{v_{in}} = \frac{G}{1+GZ_E}$$

(3.2.5)

Which proves the mentioned statement when $Z_E$ approaches zero and infinity. It can be shown the Thevenin band pass filter circuit shown in Figure 2.7 has the following input impedance:
The impedance of 3.2.6 approaches $R$ at the frequency of zero and infinity and goes to infinity at the center frequency of the tank, $1/\sqrt{LC}$. Moreover, as $RC$ gets larger, the transition from $R$ to infinity becomes more abrupt. It can be shown that if the tank is placed as $Z_E$ in Figure 3.4, a notch can be formed at the output current. The proposed notch is demonstrated in Figure 3.5.

![Figure 3.5 Proposed notch](image)

The output current in respect to the input voltage for the circuit of Figure 3.5 is:

$$
\frac{i_{out}}{v_{in}} = \frac{G}{1 + GR} \frac{S^2 + \frac{1}{LC}}{S^2 + \frac{\omega_0^2}{Q} S + \frac{\omega_0^2}{Q}}
$$

By assuming a large $G$ and comparing 3.2.7 with 2.1.2, the out of band gain of the circuit is $1/R$ and the $Q$ will be $R/(\sqrt{L/C})$. As an example, if $\sqrt{L/C}$ which is the characteristic impedance of the tank is 10, a resistance of 1 KΩ is needed to achieve the $Q$ of 100. Using this amount of resistance introduces two issues. First, a 1 KΩ resistance in an RF circuit can produce low frequency poles to the system. Second, the out of band gain in this case is going to be 1 mmho which requires a large resistance at the load to get larger than unity gain. Any load resistance smaller than 1 KΩ causes the circuit to be lossy which degrades the noise figure of the system.

In order to enhance the behavior of the system, a feedback based notch is introduced. The feedback is designed in a way it assists the circuit for large $Q$ and it can be turned off for low $Q$ to avoid stability and noise issues. The basic idea of the feedback is the same as band pass filter. By increasing the loop gain in the notch, the transition from its center frequency to pass band becomes more abrupt. The block diagram of the feedback based notch is illustrated in Figure 3.6.
The transfer function of the system of Figure 3.6 can be derived as:

\[
\frac{V_{out}}{V_{in}} = \frac{1}{1 + A_{V}} \frac{S^2 + \omega_0^2}{S^2 + \frac{\omega_0}{Q(1 + A_{V})} S + \omega_0^2}
\]

(3.2.8)

This equation states that the Q of the notch can be boosted by \(1 + A_{V}\) without having to change the resistance of it. While the system in Figure 3.6 is capable of Q boosting, its gain is reduced by \(1/(1 + A_{V})\). This is not desirable since the gain of smaller than unity increases the noise figure of the system. In order to address the issue, a Low Noise Amplifier (LNA) is added before the system. This system which is implemented in this thesis is demonstrated in Figure 3.7.

One issue with adding an LNA is, while it reduces the noise figure, it degrades the overall linearity of the system according to equation 2.1.4. However, since a feedback is used in this system, the amount of linearity degradation is compensated by the loop gain.

It will be explained in section 3.3 that it is easier to add and subtract signal in the current domain. Therefore, the subtraction in the system of Figure 3.7 is accomplished by subtracting the
output current of the LNA and variable gain amplifier. In consequence, the LNA and variable gain amplifier will be transconductance amplifiers with a shared load. This causes noise degradation of the system since LNA will not be able to suppress the noise imposed by the feedback path. In order to avoid excessive noise by the feedback path, it should not be used with a large gain. As can be concluded from the mentioned arguments, there exists a balance between the maximum Q obtained from the open loop and its Q boosting by the feedback path in order to maximize the noise performance.

It is also arguable that an adder in the voltage domain can solve the noise figure issue caused by the feedback variable gain amplifier. However, adding more elements will add more parasitic poles which is detrimental to a closed loop system in terms of stability. The design of the LNA is another important issue since the amplifier has to be able to provide enough gain (around 20 dB) while keeping a low noise figure and high linearity to have minimum negative impact on the overall system. As it will be discussed in section 3.3, since the circuit is implemented in the differential configuration which makes the signals available in both positive and negative signs, the subtracting block is embedded in the LNA and variable gain amplifier.

The block diagram of both of the systems designed in this work are explained in this section. Both of the systems use feedback techniques with slightly different block diagrams. While the implementation of the mentioned block diagrams may seem trivial, there are issues and different methods to implement them. This will be fully discussed in the next section. The band pass filter designed in this work operates in 4 to 8 GHz and is implemented using BiCMOS technology. The notch is designed to work in 4 to 8 GHz and is implemented fully in CMOS.

3.3 Circuit Details

In this section, the detailed schematic of each circuit will be discussed.

3.3.1. Band-Pass Filter

The band pass filter is an improvement to the design proposed in [5] by adding extra circuitry. A second order band pass filter is based on the schematic of Figure 2.7. In the integrated circuit implementation, the Q of the inductor in 4 to 8 GHz frequency range is limited to less than 10. While by increasing R in Figure 2.7, the Q can be controlled, its maximum is limited to less than 10 since all resistors need to be considered in determining the bandwidth. In order to overcome the problem, a negative resistance has to be added in parallel with the LC tank to increase the finite Q of the elements. A negative resistance can be as simple as a cross-coupled circuit. However, a Darlington negative resistance is preferred to achieve larger negative resistance and have better control resolution. The schematic of the Darlington negative resistance is demonstrated in Figure 3.8.
Based on the figure, there are two parts of fixed and variable resistances. The overall negative resistance on each side assuming the current of each transistor is high can be calculated as $R_{\text{fixed}}||R_{\text{var}}$ where $R_{\text{var}}$ can be varied to get the desired negative resistance depending on the required Q.

Driving the LC tank is another important factor. The band pass filter of Figure 2.7 can be voltage driven or current driven. When the circuit is voltage driven, the maximum achieved gain is 1 while the gain of the circuit can be variable using the current driven circuit. A large gain in the filter is important if a low noise figure is desired. This can be concluded from equation 2.1.6. If the current driven circuit is going to be implemented, a common emitter can be used to create the current. The current of the common emitter can be made variable by placing a variable resistance at the emitter of the transistor. It can be verified that there is a trade-off between the gain achieved by the transistor and its linearity. It is noteworthy to mention that the noise figure is not always the main target of the design. If the interferer level at the input of the filter is large, the circuit is required to have high linearity rather than a small noise figure. In this case, the voltage driven band pass filter is used. The voltage driven circuit can be implemented by driving the Thevenin equivalent of the tank with a common collector transistor. The common collector configuration is capable of providing high linearity if it is biased at a fairly large current. The circuit diagram of the band pass filter which is based on [5] is shown in Figure 3.9.
As seen from the figure, both voltage driven and current driven circuits are used and they can be adjusted to compromise noise figure in order to get higher linearity.

In order to design the circuit working in 4 - 8 GHz range, the inductor value is designed to be 650 pH differential meaning the circuit sees 325 pH on each side. The variable capacitor (varactor) is designed in a way that its value can be varied between 1.23 pF and 4.2 pF. In the design of the varactor, parasitic capacitance of the circuit has to be considered. The value of $R_Q$ is set to change from very small value up to 350 $\Omega$. While it is not considered in the schematic of Figure 3.9, the circuit cannot provide 50 $\Omega$ matching at its input since the input of a BJT transistor is a high impedance in this frequency range. In order to match the circuit for RF measurement, a 50 $\Omega$ resistance is placed between the base of input transistors and supply. This will significantly degrade the noise figure of the system. However, it is necessary in order to perform RF measurement. The size of the input transistors is also important in determining the noise figure of the system. Although increasing the size of the transistors would introduce parasitic capacitance at the input of the circuit which may degrade the performance, setting the size of them to the minimum possible size will cause a large base resistance which is detrimental to the noise figure of the system since it is on the first stage of the circuit.

If the finite resistance of the inductor and capacitor is fully compensated by the negative resistance, the Q of the circuit can be determined by $R_Q/\sqrt{L/C}$. By plugging the design numbers into the mentioned formula, the maximum Q achieved for this case ranges from 22 to 37. This is clearly not enough for the design requirements of this work. Increasing the size of $R_Q$ to about four times is not a practical solution. The only feasible solution is to increase the negative transconductance further to increase the effective $R_Q$. If the net negative resistance of the tank is assumed to be $-R_{tank}$, for the current driven path, the gain can be obtained by calculating the
parallel product of \( R_Q \) and \(-R_{\text{tank}}\) and multiplying that by the effective transconductance of the transistor. For the voltage driven, the gain can be calculated as:

\[
\frac{V_{\text{out}}}{V_{\text{in}}} = \frac{-R_{\text{tank}}}{R_Q - R_{\text{tank}}} 
\tag{3.3.1}
\]

The magnitude of 3.3.1 can be greater than unity meaning the voltage driven path can potentially provide gain in contrast to the case where the negative gm cell only cancels the tank resistance. While having a gain of larger than one is usually desirable, for this case, it causes nonlinearity since it is coming from the negative gm cell. Moreover, by increasing the strength of the negative gm, the noise of the system increases significantly by causing both the noise current and the effective resistance to rise. That is the main reason that a feedback is used to assist the circuit achieve high Qs without compromising noise figure and linearity.

The next step is to design each building block of Figure 3.3. Careful design of each block is necessary to avoid any negative impact on the performance of the band pass filter. Since the proposed system is a feedback based system, the first step to ensure stability is to isolate the feedback path from the feed forward. In order to achieve this, a buffer needs to be placed before the gain stage in Figure 3.3. A common collector is used as a buffer in the design. The next stage is going to be a voltage gain stage where the input resistance is relatively high. Therefore, a current of 1.35 mA is enough for the buffer to maintain its unity gain.

Since a high range of Q control is desired in this design, the variable gain amplifier has to provide a large high to low gain ratio. Another important issue is to avoid instability; the 3-dB gain cut-off frequency of the amplifier needs to be larger than 8 GHz which is the highest operating frequency of the circuit. In order to achieve the mentioned goals, a two stage amplifier is employed. In the amplifier schematic, two identical common emitters with variable currents are used. The overall gain of the two stage amplifier varies between \(-1.5 \text{ dB}\) and \(32 \text{ dB}\). In order to get the mentioned gain range, the current consumption of two stages varies between 0.65 mA and 5.9 mA. 3-dB cut-off frequency is 13.5 GHz. The schematic of the gain stage and buffer is highlighted in Figure 3.10.

![Figure 3.10 Buffer and gain stage in feedback](image)
As presented, the identical gain stages are used. In order to reduce the miller effect caused by the amplifier, a CASCODE configuration is employed.

The next stage following the variable gain amplifier is the band stop filter according to figure 3.3. This comes with practical issues. The notch which will be introduced later in this section has a low resistance. If the notch is directly connected to the variable gain amplifier, it significantly degrades the performance of the system. Therefore, buffers have to be added between the gain stage and the notch. The buffer would need to be biased with a large current since it has to be capable of driving a low resistance without a significant loss. Any loss in the feedback path will be translated into lower Q tuning range. The input resistance of a common emitter can be calculated as $\beta/g_m$. The value of $\beta$ in RF frequency can be approximated as $f_T/f$ where $f_T$ is the transit frequency of the BJT transistor and $f$ is its operating frequency. In order to get a rough estimation, if the transit frequency is assumed to be 200 GHz and the frequency of operation to be 5 GHz, the $\beta$ is going to be 40. In order to drive the notch, a current of around 2.5 mA is required. Therefore, the input resistance of the transistor is going to be $400 \Omega$. This value will degrade the gain of the variable gain amplifier by around 6 dB since it is in the order of $R_L$. In order to avoid the issue of gain reduction, two buffer stages have to be used. The first stage buffer can be designed with a lower current since it doesn’t need to drive a low resistance load. The schematic of the buffer stage is demonstrated in Figure 3.11.

![Buffer schematic](image)

**Figure 3.11 post VGA buffers in feedback**

For Buffer 1, the current is 0.7 mA using $R_{BUF1}$ of 600 $\Omega$. For Buffer 2, the circuit is biased so that it can provide 2.7 mA of current. With this values, the overall loss is about 3 dB. The loss could be reduced by increasing the current of the second buffer. However, that would lead to a very high current consumption.

The next stage is the notch. There are two choices of voltage driven and current driven notch. However, as it was explained in section 2.2.1, current driven cannot be a feasible choice due to its low gain for high Q cases. Therefore, the notch implemented as a part of band pass filter has to be a voltage driven notch. The basic schematic of a voltage driven notch has been demonstrated in Figure 2.9. The resistance in the circuit is the loading effect of the previous buffer which is preferred to be minimum to get a lower bandwidth notch. The capacitance at the notch needs to be made variable so that the frequency of it can be tuned to the frequency of the band pass
filter. Due to the use of real elements which have finite Q, the depth of the notch is not going to be infinity. If the equivalent resistance of the LC tank can be modelled as a series resistance of $R_{eq,LC}$ at the center frequency, the depth of the notch is going to be $R_{eq,LC}/(R_{eq,LC} + R_{previous \ stage})$. As it has been mentioned, it is desired that there is no signal in the feedback path in order to avoid performance degradation which requires a very deep notch. Therefore, $R_{eq,LC}$ has to be cancelled out. In order to achieve, a negative resistance can be employed.

As it has been explained in [3], a cross-coupled negative resistance is the best option to compensate a resistance with the minimum current consumption. However, it should be noted that a cross-coupled is only capable of cancelling the finite resistance for a low bandwidth since it can just be placed in parallel with the tank. In order to avoid any unnecessary noise penalty by the feedback path, the noise of the negative gm has to be suppressed. In an LC tank, the limiting Q factor is the inductor. Therefore, the negative transconductance cell can be placed in parallel with the inductor. The cross-coupled used in the feedback path is a non-Darlington two transistor version for simplicity. The value of the negative transconductance can be adjusted by changing the resistance at the emitter of each transistor. Depending at the frequency of the operation, the required negative gm varies. The value of the resistance at the emitters should be decreased until the minimum possible depth is reached. The schematic of the proposed notch as well as the negative transconductance is shown in Figure 3.12.

As observed from the figure, the noise of the negative gm is trapped in itself at the center frequency of the LC tank. The negative resistance of the circuit varies between 140 and 410 $\Omega$ while the current of each BJT varies between 0.9 and 7.67 mA.
The output of the notch has to go to a buffer so that the buffer can provide the necessary current to be subtracted from the input current of the circuit and the feedback loop becomes closed. The buffer can be a transconductance which provides current when a voltage is applied at its input. In order to succeed isolation between the feedforward and feedback path, a CASCODE stage is employed. It is necessary to mention that since the buffer is directly connected to the tank, the noise of each transistor directly appears at the output of the circuit. This is unavoidable. However, in order to minimize the noise effect of the circuit, it is desired that the least possible current is assigned to the buffer while preceding stages are designed to provide a large gain to get high Q. Depending on the design requirement, the designer can compromise Q for getting better noise figure. The schematic of the output buffer is shown in Figure 3.13.

![Figure 3.13 Output buffer of the feedback path](image)

The current of the circuit should be adjustable so that it can be turned off when the feedback path is not needed in order to avoid noise figure penalty. For this design, when the circuit is turned on, the current of each transistor is set to 1 mA.

As mentioned in this section, the proposed band stop filter employs two independent LC tanks. The center frequency of the tanks can be tuned automatically by monitoring the output of the band pass filter and notch and change the center frequency until highest possible Q is achieved while the circuit is stable. However, designing the automatic tuning circuit is beyond the scope of this research. The schematic simulation of the band pass filter as well as the layout and post layout simulation will be presented in next chapter.

### 3.3.2. Band-Stop Filter

The schematic of the band stop filter is based on Figure 3.5. For achieving a notch response, a band pass filter tank is connected to the source of a common source amplifier. If the circuit is ideal, the circuit output current will be a Q-tunable notch with the depth of infinity. However, due to the finite Q of the inductor and capacitor, the rejection of the notch is limited to the equivalent parallel resistance of the tank. Therefore, a negative resistance circuit can be used to compensate for that. If the negative resistance of the cell is tunable, the depth of the notch can be adjustable along its frequency range.

In order to implement a negative resistance, the cross-coupled circuit of Figure 3.12 can be used in CMOS. In the BJT cross-coupled, the assumption is that the transconductance of each
transistor is large enough so that the negative resistance is proportional to $R_{\text{var}}$. In CMOS, it is not always practical to assume large transconductance. Therefore, the CMOS version has to be implemented without the resistance on its source. In this case, the negative resistance of the circuit is inversely proportional to the transconductance of the transistors. This was not desirable in a BJT-based circuit due to its heavily nonlinear nature. However, in a CMOS circuit, it is acceptable not to use degeneration for cross-coupled linearization. The circuit diagram of the notch with the cross-coupled cell is demonstrated in Figure 3.14.

![Circuit Diagram](image)

Figure 3.14 Preliminary CMOS notch

From the circuit, the frequency of the notch can be varied by changing $C_{\text{var}}$ and its Q is controlled by $R_Q$. The negative resistance can also be controlled by changing $I_{\text{BIAS,VAR}}$.

The circuit in Figure 3.14 has practical issues which has to be addressed. First, if the biasing of $M_1$ and $M_2$ is accomplished using a current source, the depth of the notch will be limited by the output parasitic capacitance of the source. If the source is designed to provide a large current, that could significantly degrade the performance of the system. In order to avoid this issue, the gate of the transistor can be biased using the voltage applied at the center tap of the symmetric inductor. However, since the cross-coupled pair is also biased using the center tap of the inductor, the voltage needs to be fairly large to give headroom to the cross-coupled in order to avoid saturation. The voltage is usually set at the highest possible. This causes problem since it leaves no space for $M_1$ and $M_2$ to have positive gate to source bias. To solve bias problem, $M_3$ and $M_4$ can be changed to PMOS so that they can be biased with a zero voltage at the center tap of the inductor. This leaves space for the NMOS transistors of $M_1$ and $M_2$ to be biased at a positive voltage. In a CMOS transistor, the drain current with a square law model is:

$$I_D = \frac{\mu C_{\text{OX}} W}{2 L} (V_{GS} - V_{TH})^2$$

(3.3.2)

Where $\mu$ is the mobility of the channel, $C_{\text{OX}}$ is the oxide capacitance, $W$ and $L$ are the dimensions of the transistor, $V_{GS}$ is the gate to source voltage and $V_{TH}$ is the threshold voltage. Therefore, the transconductance of each transistor is going to be:
\[ g_m = \sqrt{2\mu C_{OX} \frac{W}{L} I_D} \]  

(3.3.3)

The value of \( \mu \) is larger for an NMOS transistor, therefore, in order to provide higher negative transconductance, an NMOS cross-coupled is preferred. Consequently, the transistors of \( M_1 \) and \( M_2 \) have to be changed to PMOS. Adding a load to the drain of PMOS transistor to get voltage gain the notch is modified in Figure 3.15.

In order to get a large range of negative resistance, \( I_{\text{BIAS, VAR}} \) has to be dramatically changed since the transconductance in a CMOS circuit is proportional to the square root of the bias current. This is unavoidable due to the physical nature of CMOS transistors. Another issue with this circuit, is in order to get a large \( Q \), \( R_Q \) has to be increased. This will lead to a large input referred noise and consequently large noise figure since \( R_Q \) directly appears at the input of the circuit. Moreover, since the gain of the circuit is proportional to \( R_D/R_Q \) if transconductance of the transistors is large enough, the overall gain is going to be small which causes the noise figure of next stages to be important as well. In order to address the issues mentioned, a low noise amplifier is added before the notch. The schematic of the proposed low noise amplifier is demonstrated in Figure 3.16.
The proposed LNA without $M_3$ and $M_4$ is called feed forward LNA and it is introduced at [20]. It can be shown the NF of the feedforward LNA of 3.16 without considering the load and $M_3$ and $M_4$ is $1 + \gamma/2$ while its NF is $1 + \gamma$ without using the feedforward technique. In this case, matching of 100 $\Omega$ is required for each transistor instead of 50 $\Omega$ which helps in the power consumption as well. Adding of $M_3$ and $M_4$ improves the noise performance further by providing a noise cancelling path to the circuit. The linearity of the circuit can be improved by adding resistors at the gate source of each common gate transistor. However, that degrades the noise figure of the system. In this design, no resistor is added due to the importance of noise figure for this work. The current consumption of each transistor in the LNA design is 1.5 mA while the supply of the circuit is 3.5 V to get more headroom. As it will be explained in the next chapter, the circuit can also work with the supply of 2.8 V.

The overall system is based on Figure 3.6 where a feedback is used to enhance the Q of the system. There are multiple options to implement a negative feedback. However, in order to make the loop gain and Q adjustable, a common source amplifier with variable bias current is used. The circuit is implemented using NMOS transistors. The overall schematic of the notch is shown in Figure 3.17.
Based on the figure, the use of differential structures can make it possible to implement a negative feedback without the need for a separate block for subtraction.

The feedback path and amplifier share the same load of $R_D$. Therefore, the noise of the feedback amplifiers cannot be suppressed by the LNA regardless of its gain. This adds an unavoidable noise penalty to the circuit when the feedback path is on. Therefore, the feedback current is adjustable so that it can be turned off in case the $Q$ that the feedforward path can provide is sufficient.
In order to perform RF testing, the circuits need to be matched to the impedance of the cables. Therefore, a matched buffer has to be added to the circuit for measurement purposes. Since linearity is an important factor in this design, the buffer has to be extremely linear. As the process used in this work is BiCMOS, high current common collector BJT circuits are used to prevent linearity degradation caused by the buffer. The output of the buffer has to be matched to 50 Ω. This can be done by adjusting the transconductance of the transistor. However, a more linear solution is to add a resistor in series with the emitter of the transistor and keep the transconductance as high as possible. Consequently, the output buffer circuit is designed in a way it consumes 16.4 mA of current which is equally assigned to each output terminal.

As mentioned, the circuit is designed to work at 3.5 V. However, it can also work with 2.8 V supply if a low power operation is desired. With 3.5 V supply, the negative transconductance branch consumes a current varied between 0 to 9.7 mA. The large range is due to the fact that the equivalent parallel resistance of the tank varies dramatically in 4 - 8 GHz range where the minimum is at lower frequencies and since the transconductance of a squared law model device is proportional to the square root of the current, the large current range is unavoidable. The current of the feedback is variable between 0 to 1.6 mA where the maximum is for the largest possible Q and it is off when Q enhancement provided by the feedforward is sufficient. In overall, current consumption varies between 30 mA and 41 mA where 41 mA is for the case when the lowest frequency range is desired and the feedback is at its maximum strength. It is important to mention that 16.4 mA current consumption of the output buffers have to be subtracted from the mentioned values in order to have a better estimation of current consumption.

The schematic of each proposed circuit has been explained in this chapter. The schematic simulation and layout and post layout simulations will be presented in next chapter. In the next section, the linearity of the LC tank as an important part of the linearity of the system is studied and nonlinear models will be developed in order to gain a better understanding of the nonlinear mechanisms.

3.4 Linearity Theory

The nonlinearity of the tank is a major issue in the nonlinearity of the systems using it. In a Q-enhanced filter, there are two major sources of nonlinearity. First, the cross-coupled negative transconductance cell is implemented by transistors as intrinsically nonlinear systems. The nonlinearity of the negative gm can be easily modelled by power series. Second, the varactor is a nonlinear element in nature. The nonlinearity of a varactor has a different characteristic than the nonlinearity of the cross-coupled cell. Since the voltage applied to the varactor determines its value, any nonlinear mechanism causes changes in varactor value which leads to changes in the center frequency of the tank. As a result, the circuit experiences a different impedance at the linear center frequency.

As mentioned, there are two nonlinear elements in a Q-enhanced nonlinear circuit. In this section, a nonlinear model based on nonlinear feedback is presented to describe the nonlinearity of the varactor which is also capable of demonstrating the nonlinearity of the negative gm cell. In order to verify the model, Volterra series nonlinear representation is also presented. There are two main assumptions in modelling the nonlinearity. First, the nonlinear model is only derived around the center frequency of the tank. It is assumed that all nonlinear elements not around the center frequency are rejected by the band pass filter. Second, it is assumed the negative gm cell
compensates all the finite equivalent resistance of the tank without changing the series resistance of it. This way, the tank can be simplified to an ideal tank with a nonlinear negative gm cell.

### 3.4.1. Nonlinear Feedback Model

A varactor is an element with nonlinear C-V characteristics. Without going into the physical details of it, there are two flat regions and one nonlinear transition region in the characteristic curve of a varactor. The most nonlinear regions of a varactor are in the transition region where a small voltage change can cause dramatic capacitance change. It is important to mention the concept of linearity here is completely different than the linearity of a varactor in a Voltage Controlled Oscillator (VCO) where the middle of the transition region is considered the most linear region. In order to characterize the nonlinearity of a varactor, it is necessary to write Taylor’s series representation of its characteristic curve. By writing the series around the bias point of the transistor, the first three terms can be represented as:

\[ C(v_{\text{cont}}) = C_0 + C_1 v_{\text{cont}} + C_2 v_{\text{cont}}^2 \]  

(3.4.1)

Where \( v_{\text{cont}} \) is the total voltage and \( v_{\text{cont}} \) is the small signal voltage across the capacitor, \( C_0 \) is the linear capacitor, \( C_1 \) is the first order nonlinear capacitance and \( C_2 \) is the second order with units of \( \text{F/V} \) and \( \text{F/V}^2 \).

The capacitors used as varactors are often small signal capacitors meaning their capacitance is defined as the change in charge in respect to change in voltage rather than the absolute value of charge and voltage. In this case, the capacitance is defined as \( \frac{dQ}{dV} \) where \( Q \) is the charge and \( V \) is the voltage across the capacitor. Consequently, the current of the capacitor of equation 3.4.1 can be obtained as:

\[ i_C(v_{\text{cont}}) = \frac{dQ_C(v_{\text{cont}})}{dt} = C(v_{\text{cont}}) \cdot \frac{dv_{\text{cont}}}{dt} \]

\[ = C_0 \cdot \frac{dv_{\text{cont}}}{dt} + C_1 \cdot \frac{d^2v_{\text{cont}}}{dt^2} + C_2 \cdot \frac{d^3v_{\text{cont}}}{dt^3} \]

(3.4.2)

As depicted, the equation consists of nonlinear terms of the control voltage and linear derivations operator. For the complete representation of the current, the series coefficients can be obtained by taking the derivatives of the C-V characteristics. The characteristic curve can be extracted from simulation. Using Cadence to run AC simulation and input a capacitor with a voltage or current source for a single frequency tone, the capacitance can be extracted by calculating \( i/v_{\omega} \) where \( \omega \) is the frequency of the simulation. The conceptual C-V characteristic of a varactor is shown in Figure 3.18.
As can be noticed from the figure, $C_1$ sign is always negative or positive (depending on the sign of $v_{\text{CONT}}$). However, the sign of $C_2$ changes over the control range. As it will be explained later, this could cause an improvement in the linearity as the coefficients can be set to cancel each other.

The nonlinear model of the capacitor can be applied to the following figure:

![Diagram of varactor nonlinear modeling of an LC tank](image)

Figure 3.19 Varactor nonlinear modeling of an LC tank

The output voltage in this model is the same as the small signal control voltage of the varactor. The linear impedance of the tank can be calculated as:

$$Z_{\text{tank}}(S) = R_P \frac{\omega_0 S}{S^2 + \frac{\omega_0}{Q} S + \omega_0^2}$$  \hspace{1cm} (3.4.3)

Where $\omega_0$ is the center frequency of the tank in the linear mode and $Q$ is its quality factor. For a nonlinear system, the output voltage and input current relationship can be modelled as following:

$$v_{\text{out}} = \alpha_1 i_s + \alpha_2 i_s^2 + \alpha_3 i_s^3$$  \hspace{1cm} (3.4.4)

Assuming that the input voltage-current relationship is $v_s = R_P i_s$ and by knowing $\alpha$ coefficients, the 1-dB compression point of the system can be calculated. The nonlinear feedback block diagram model of the system can be observed in Figure 3.20.
As seen from the figure, the nonlinearity of the varactor is modelled using a nonlinear negative feedback. It is important to gain an intuitive understanding of the nonlinear process before deriving formulas. Without the feedback, the system acts as a second order RLC network driven by a current with voltage as the output. If an element (varactor in this case) is nonlinear in the RLC tank, it starts to create current when a voltage is applied to its terminals and that current may increase or decrease with the amount of voltage applied to it. The nonlinear current will then be subtracted from the input current and it flows through the tank again and creates a new output voltage. This process continues until it reaches a steady state which is the point of interest in this study. At the steady state, the voltage is no longer equal to its linear case. This can cause gain compression if the feedback is degenerative. If the feedback is regenerative similar to a VCO, the nonlinear feedback process continues until it gets saturated, which may cause oscillation. In this study, it is assumed the strength of negative gm cell is not high enough to start an oscillation.

The nonlinear terms are caused by the interaction of higher order terms in the nonlinear polynomial equation of the system. If the input of the system is a single tone sinusoidal wave at the frequency of $\omega_0$, a second order term (or a squared term) can cause a tone at the frequency of $2\omega_0$. When the nonlinear terms are sampled at the output and fed back to the input, they see different impedances of the tank since they are at different frequencies. Therefore, the impedance of the tank is determined for different frequencies as:

$$Z_{\text{tank}}(\omega) = \begin{cases} R_P, & \text{at } 1\omega_0 \\ -j\frac{2}{3}R_P, & \text{at } 2\omega_0 \\ R_P, & \text{at } 3\omega_0 \end{cases}$$

(3.4.5)

It is important to mention that for the third order nonlinearity, only terms around $\omega_0$ are of interest; therefore, it is assumed that the third order terms will later create tones around $\omega_0$ by interacting with 2nd order terms.
The term of \( \frac{d}{dt} \) is a linear operator and can be replaced by \( j\omega_0 \). Applying this, the error current can be obtained as:

\[
i_e = i_s - \frac{j\omega_0 C_1}{2} v_{out}^2 - \frac{j\omega_0 C_2}{3} v_{out}^3 \tag{3.4.6}
\]

Placing 3.4.4 into 3.4.6 leads to:

\[
i_e = i_s - \frac{j\omega_0 C_1}{2} (\alpha_1 i_s + \alpha_2 i_s^2 + \alpha_3 i_s^3)^2 - \frac{j\omega_0 C_2}{3} (\alpha_1 i_s + \alpha_2 i_s^2 + \alpha_3 i_s^3)^3 \tag{3.4.7}
\]

In order to get input-output relationship, the following equation is used:

\[
v_{out} = i_e Z_{tank}(\omega) \tag{3.4.8}
\]

where \( Z_{tank} \) is obtained from the equation of 3.4.5. By placing 3.4.8 into 3.4.7, \( \alpha \) coefficients of equation 3.4.4 can be found.

When developing the equation for 1-dB compression point, it is important to avoid double counting of the same terms. If it is assumed the input of the circuit is a single tone current of \( e^{j\omega_0 t} + e^{-j\omega_0 t} \), the third order term can be calculated as:

\[
(e^{j\omega_0 t} + e^{-j\omega_0 t})^3 = e^{j3\omega_0 t} + e^{-j3\omega_0 t} + 3e^{j\omega_0 t} + 3e^{-j\omega_0 t} = 6 \cos \omega_0 t + \ldots \tag{3.4.9}
\]

where \( 6 \cos \omega_0 t \) is the undesired in-band tone created by \( i_s^3 \). The interaction between second order and first order can also create in-band tones. Assuming the second order term is \( e^{j2\omega_0 t} + e^{-j2\omega_0 t} \), the unwanted terms can be calculated as:

\[
(e^{j\omega_0 t} + e^{-j\omega_0 t})(e^{j2\omega_0 t} + e^{-j2\omega_0 t}) + (e^{j2\omega_0 t} + e^{-j2\omega_0 t})(e^{j\omega_0 t} + e^{-j\omega_0 t}) = 2e^{j\omega_0 t} + 2e^{-j\omega_0 t} + 2e^{j3\omega_0 t} + 2e^{-j3\omega_0 t} = 4 \cos \omega_0 t
\]

(3.4.10)

When the nonlinearity is not created through a feedback process, 3.4.10 terms will not appear. Therefore, in the new system, both 3.4.9 and 3.4.10 need to be normalized by 6 which leads to multiplying the second cosine term by 2/3 when calculating 1-dB compression point. Using 3.4.7 and 3.4.8 will lead to:

\[
v_{out} = R_p i_s - \frac{1}{3} (\omega_0 C_1 \frac{a_1 R_p}{Q}) i_s^2 - j \frac{2}{3} (\omega_0 C_1 \alpha_1 \alpha_2 R_p) i_s^3 + \frac{1}{3} (\omega_0 C_2 a_1 C_1 R_p) i_s^3 \tag{3.4.11}
\]

Comparing the above equation with 3.4.4 results in:
\[
\alpha_i = \begin{cases} 
\alpha_1 = R_p \\
\alpha_2 = \frac{-1}{3} \frac{R_p^3}{Q} (\omega_0 C_1) \\
\alpha_3 = j \left( \frac{2}{9} \frac{R_p^5}{Q} (\omega_0 C_1)^2 - \frac{1}{3} \left( \frac{R_p^4}{Q} \omega_0 C_2 \right) \right) 
\end{cases} 
\]  

(3.4.12)

By applying \( v_s = R_p i_s \) to 3.4.4, the input-output voltage relationship will be:

\[
v_{out} = \alpha_1' v_s + \alpha_2' v_s^2 + \alpha_3' v_s^3 = \frac{\alpha_1}{R_p} v_s + \frac{\alpha_2}{R_p^2} v_s^2 + \frac{\alpha_3}{R_p^3} v_s^3 
\]

(3.4.13)

By knowing \( Q = \omega_0 R_p C_0 \) and employing the 1-dB compression formula of \( 0.145 |\alpha_1'|/|\alpha_3'| \), the 1-dB compression point in terms of circuit parameters is going to be:

\[
v_{P-1dB}^2 = \frac{0.435 C_0}{Q C_2} \left| 1 - \frac{2}{3} \frac{C_1^2}{C_0 C_2} \right|^{-1} 
\]

(3.4.14)

In order to take the nonlinearity of the negative gm cell into account, the system of Figure 3.20 can be modified into the block diagram of Figure 3.21.

In the above figure, the voltage current relationship of the negative gm cell is assumed to be:
\[ i_{gm} = g_{m1}V_{out} + g_{m3}V_{out}^3 \]  \hspace{1cm} (3.4.15)

There are two assumptions in the modeling of equation 3.4.15 in Figure 3.21. First, the linear part is responsible for compensating the finite Q of the tank. If it completely cancels the equivalent resistance of the tank, it does not appear in the model. Second, the implementation of the circuit is differential. Therefore, there is no second order term in the nonlinear modeling of the negative gm cell. This assumption is not valid for the varactor as its characteristic is not symmetric and the circuit is not a fully differential pair.

By applying the same procedure as modeling the nonlinearity of the varactor, the nonlinearity equation of Figure 3.21 will be:

\[ V_{P-1dB}^2 = \frac{0.435}{Q} \frac{C_0}{C_2} \left[ \left( 1 - \frac{2}{3} \frac{C_1}{C_0C_2} \right)^2 + \left( \frac{3g_{m3}}{\omega_0C_2} \right)^2 \right]^{-0.5} \]  \hspace{1cm} (3.4.16)

In the next section, the same formula will be derived using Volterra series method. Moreover, verifying Cadence simulations will also be performed to validate the model. Lastly, tuning strategies will be suggested based on the formula of 3.4.16 to enhance the linearity of the system.

### 3.4.2. Volterra Series Model

The results obtained from the nonlinear feedback model can also be verified using Volterra series. A linear system is a system where the output is the scaled version of the input with a transfer function defined for the system. While the concept of transfer function is only defined for linear systems, Volterra series is a method to find functions with similar characteristics as a transfer function for nonlinear terms. Each transfer function is called kernel in Volterra series method. Since the series is an approximation of a nonlinear function, it is only valid for weakly nonlinear systems. The weakly nonlinear system is defined by the radius of convergence of the series which is beyond the scope of this research [21][22].

Without getting too much into the mathematical details of Volterra series, the aim of this session is to find kernels for the tank of Figure 3.19. The reason for finding kernels is to derive a closed loop formula for 1-dB compression point of the circuit. There are two major methods to calculate kernels of Volterra. In the first method, which is also called harmonic method, in order to find n-th order kernel, the input is assumed to be a linear combination of n single tone signals. The n tones are then applied to the differential equation of the system. By equating both sides of the differential equation, the n-th order kernel can be found. While this method is capable of finding any arbitrary kernel of the system, it may lead to lengthy calculations and it does not provide any intuition into the nonlinear process taking place in the system. The second method is called the method of nonlinear currents [23]. The method starts by calculating the first order Kernel using linear KVL and KCL equations. For higher order Kernels, the nonlinear element is modelled with a nonlinear current. KVL and KCL can then be written with the nonlinear current in the circuit to obtain higher order Kernels. The calculation details of this method will be discussed later in this section.

Starting from the 1st order kernel, it is the same as the linear transfer function. The equivalent circuit of the 1st order kernel calculation is shown in Figure 3.22.
As can be observed from the figure, the calculation is done for the Thevenin equivalent circuit of
the tank where $C_0$ is the linear portion of the tank and negative gm cell fully cancelled the
equivalent parasitic resistance of the tank and does not appear at the first order kernel calculations.
By assuming a single tone at the input around the center frequency of the tank $\omega_1$, KCL at the
output node leads to:

$$\frac{1 - H_1(j\omega_1)}{R_p} = H_1(j\omega_1)(j\omega_1 C_0) + \frac{H_1(j\omega_1)}{j\omega_0 L} \quad (3.4.17)$$

The voltages at this equation are normalized to the input voltage and $H_1(j\omega_1) = v_{out}/v_s$. The
same method will be used to calculate higher order kernels. At the center frequency of the tank,
first order kernel is going to be:

$$At \omega_1: j\omega_1 C_0 + \frac{1}{j\omega_1 L} = 0 \text{ therefore } H_1(j\omega_1) = 1 \quad (3.4.18)$$

This is same as the linear transfer function and it states the linear relationship of input and output
for an ideal thevenin second order LC circuit is 1.

In order to calculate the second order kernel, two tones of $\omega_1$ and $\omega_2$ have to be assumed
around the center frequency of the tank. The second order kernel equivalent circuit is shown in
Figure 3.23.
From the figure, the only non-linear term is $i_{C_1}$ since the negative gm cell is assumed to be perfectly differential, where even order nonlinearities are zero. The input does not appear in the circuit since only second order sources have to appear for the second order kernel calculation. The second order nonlinear current of the varactor can be calculated by applying to tones to the differential equation of the varactor as:

$$i_{C_1} = j(\omega_1 + \omega_2) \frac{C_1}{2} H_1(j\omega_1)H_1(j\omega_2) \tag{3.4.19}$$

KCL can then be written at the output node which will lead to:

$$\frac{H_2(j\omega_1,j\omega_2)}{R_P} + H_2(j\omega_1,j\omega_2)(\omega_1 + \omega_2)C_0 + \frac{H_2(j\omega_1,j\omega_2)}{j(\omega_1 + \omega_2)L} + i_{C_1} = 0 \tag{3.4.20}$$

By placing 3.4.19 into 3.4.20, the second order kernel can be calculated as:

$$H_2(j\omega_1,j\omega_2) = \frac{(\omega_1 + \omega_2)^2}{R_P - (\omega_1 + \omega_2)^2R_P L C_0 + j(\omega_1 + \omega_2)L} \frac{R_P L C_1}{2} \tag{3.4.21}$$

It is important to mention for the second order kernel calculation, the frequency is no longer the center frequency of the tank and inductor and capacitor are not going to resonate with each other.

For the third order kernel, the circuit of Figure 3.24 is used for the calculations.

From the figure, $i_{gm_3}$ is just $g_{m3}$ while $i_{C_2}$ can be calculated using the same method as $i_{C_1}$:

$$i_{C_2} = j(\omega_1 + \omega_2 + \omega_3) \frac{C_2}{3} + j(\omega_1 + \omega_2 + \omega_3) \frac{C_1}{2} [H_1(j\omega_1)H_2(j\omega_2) + H_1(j\omega_2)H_2(j\omega_1) + H_1(j\omega_3)H_2(j\omega_1,j\omega_2)] \tag{3.4.22}$$

By assuming all three tones are around center frequency of the tank, the third order kernel can be obtained as:
\[ H_3(j\omega_1, j\omega_2 = j\omega_1, j\omega_3 = -j\omega_2) \approx -R_p g_{m3} - j \left( R_p \omega_1 \frac{C_2}{3} - \frac{2}{9} R_p \omega_1^3 C_1^2 L \right) \]  

(3.4.23)

It is important to note the third order kernel is calculated for the specific case where the frequency is \(2\omega_1 - \omega_2\) rather than calculating it for the most general case since only the tones around the center frequency of the tank are of concern. 1-dB compression point can then be calculated by applying the following formula:

\[ v_{P-1\text{dB}}^2 = 0.145 \frac{|H_1(j\omega_1)|}{|H_3(j\omega_1,-j\omega_2)|} \]  

(3.4.24)

After simplification, 1-dB compression point will be:

\[ v_{P-1\text{dB}}^2 = \frac{0.435}{Q} \frac{C_0}{C_2} \left[ \left(1 - \frac{2}{3} \frac{C_1^2}{C_0 C_2} \right)^2 + \left( \frac{3g_{m3}}{\omega_0 C_2} \right)^2 \right]^{-0.5} \]  

(3.4.25)

which is the same as 3.4.16 where 1-dB compression point is derived by applying the nonlinear feedback modeling.

In order to verify varactor nonlinearity modeling, the nonlinearity of the tank used in the band pass filter design will be simulated using Cadence. When simulating, the negative \(g_m\) cell is assumed to be ideal and linear and it is assumed to compensate the tank in such a way that the voltage-gain from input to output becomes unity.

![Figure 3.25 verification of nonlinear model proposed in this work](image)

Figure 3.25 verification of nonlinear model proposed in this work

As seen from the figure, the nonlinear method can model the nonlinear behavior of the system.

Based on equation 3.4.25, two methods of tuning can be recommended. In method one, varactor tuning can be accomplished using two different control voltages. This can reduce
nonlinear coefficients if each of them is biased in a region where the coefficients can cancel each other. This method is used at [5]. In method 2, more than one control voltage can be used. For example, if four control voltages are used, three out of four can be biased at top or bottom flat regions while the fourth can be used to do continuous frequency tuning [13]. Cadence simulation for method one leads to the result of Figure 3.26.

![Figure 3.26 Dual varactor control simulation](image)

From the figure, up to 14 dB of improvement can be achieved using two varactor control voltages. The issue with this control scheme is the complexity of automatic tuning implementation since a look up table is needed in order for the tuning circuit to tune the varactor in order to get the best possible linearity performance. Four control voltage method can also be simulated. It can be shown using that method, the linearity of the system becomes limited by the negative gm cell rather than the varactor. However, using more control voltages is translated into more DC pads which increases the physical size of the circuit.

### 3.5 Chapter Summary

This chapter is about proposed designs of this work. The chapter starts by introducing the design requirements for each of the two proposed circuits. Then, the conceptual block diagram of each design is introduced. The circuit details of each block as well as component values are presented. At the end of the chapter, two linearity theories are presented to explain the nonlinear behavior of the LC tank. In the first theory, a nonlinear feedback model is presented using nonlinear block diagrams. In the second theory, Volterra series method is used to model the nonlinearity of the varactor as well as the negative gm cell. While the same results are obtained from both modeling methods, they both are validated by comparing the results extracted from the models with cadence simulations. Two recommendations are made based on the obtained formulas from the model.
Chapter 4

Implementation

This chapter is about the implementation of band pass and band stop filters proposed for this work. The chapter starts with schematic simulations. For the schematic simulations, both linear and nonlinear characteristics of the filter will be simulated to ensure feasibility of the design in schematic level. This step is critical in actual implementation since the implemented system performance can be optimized by comparing the simulations and optimizing the layout. Layout of the proposed systems using 0.13 μm BiCMOS technology is discussed after the schematic simulations. In this step, the overall size of the circuit is determined and the aim is to minimize the size while retaining the performance due to the fact that the size is proportional to the cost of the circuit. As it will be explained, the size is often determined by the number of pads and controlling signals. Parasitics (capacitive and resistive) in layout may introduce issues to the circuit. Those issues could be as important as instability or minor degradations of the performance. In order to maximize the performance of the implemented system, post layout simulations have to be accomplished. For this part, the type of simulations should be the same as schematic simulations and the performances should be compared to identify any potential implementation issue. Some issues caused by the layout can be avoided by trying different layers or different routings. However, some of them are unavoidable due to the fact that each line has its own parasitic capacitance and resistance. If post layout simulations are done carefully, it is expected that would result in the same performance during the measurement. Therefore, performance comparison will be discussed at the end of the chapter where the performance of the current system will be compared against state of the art designs.

4.1 Schematic Simulations

In this section, the schematic simulation of each system will be accomplished using Cadence Virtuoso and Analog Design Environment. S-parameter and noise simulations are done using SP simulation tool of cadence along with DC simulation and 1-dB compression point simulation as linearity simulation is performed using PSS tool of cadence. The detailed simulation steps will be discussed in next subsections.

4.1.1 S Parameter Simulation

The first step in S-parameter simulation is to ensure matching to 50 Ω. Matching is an important factor in RF circuits. It can be proved if the circuit is desired to get the maximum power from the source, its input impedance should be a complex conjugate of the source impedance. Power matching becomes important when a weak signal is received at the antenna and losing even a small portion of it would decrease the capability of the receiver to detect the signal. Even if the sensitivity of the receiver is not of main concern, the matching is important for measurement purposes. In a measurement setup, depending on the parameters needed to measure, the input and output of the circuit are connected to signal generators, network analyzers, spectrum analyzers, etc. Most of the mentioned equipment have the impedance of 50 Ω and the impedance of the cables connecting the device under test (DUT) to those equipment is often 50 Ω as well. Therefore, any
impedance other than 50 Ω would cause reflection and dependency of the system performance to the length of the cable. In order to avoid this issue, all ports of the system have to be matched. The quality of matching at any arbitrary port of “i” is determined by $S_{ii}$ and it is defined as following:

$$S_{ii} \text{(in dB)} = 10 \log \left( \frac{Z_{\text{in},i}-50\Omega}{Z_{\text{in},i}+50\Omega} \right)$$

(4.1.1)

Where $Z_{\text{in},i}$ is the input impedance seen at each port. It is usually desired to have $S_{ii}$ of better than -10 dB.

An issue which has to be addressed before looking into the s-parameter simulation of the circuit, is that the system designed for this work is a differential circuit, while the measurement setup will be single ended. Therefore, a single to differential module also called 180 degree hybrid coupler has to be placed between DUT and measurement instruments. A 180 degree hybrid coupler is a four terminal device where two of the terminals are connected to DUT, one of them is connected to a 50 Ω term and the fourth one is connected to the measurement instrument. The coupler would subtract the DUT signals and feed them to the measurement instrument. Each terminal of the coupler has to be matched. Therefore, a $1: \sqrt{2}$ transformer is used to model the coupler and realize matching at the input of the circuit in simulations. The schematic is illustrated in Figure 4.1.

![Differential Circuit Figure](image)

Figure 4.1 simulating hybrid coupler using an ideal transformer

As shown in the figure, using an ideal transformer, each port can be matched into 50 Ω.

For matching simulation of the band pass filter, according to the figure, there exist three ports in our system, port one is the input port, port two is the output port where the band pass response can be accomplished and port three is the notch monitoring port. As it has been explained, monitoring the notch is necessary for frequency adjustment to get the highest possible Q from the system. The matching s parameters of the system is shown in Figure 4.2. As it will be observed from the figure 4.2, port 1 and port 3 are perfectly matched while port 2 matching is slightly worse.
than 10 dB. However, since the stage coming after the filter, when implemented in a receiver chain may not need an output matching, this is not going to be a critical issue. It is also worth mentioning that the frequency of the notch seen for $S_{11}$ can vary depending on the frequency the circuit is tuned at. However, S parameters remain below -10 dB regardless of tuning condition.

![Graph](image)

**Figure 4.2** Schematic matching simulation of the band pass filter

For the matching of the band stop filter, there are two ports in contrast to the band pass filter where three ports existed in the system. Band stop filter of Figure 3.7 has two ports of input and output. At the input, an LNA is placed to reduce the noise figure of the system. Based on the noise and linearity performance, which will be explained in more details in next sections, another low noise amplifier may be placed before the current system to improve the noise. However, if the LNA of the proposed system is desired to be placed in direct contact with the antenna, the input matching will not only be important for measurement purposes, it will also be important to get the highest possible power from the antenna. Therefore, input matching is critical for this circuit and it has to be kept below -10 dB. For the output, same as the band pass filter, the matching may not be as critical as the input. However, for measurement, it is advised to be kept below -10 dB. In this setup, port 1 is going to be the input while port 2 is the output. The matching of band stop filter is demonstrated in Figure 4.3.
As can be observed from the figure, both input and output matching are below -10 dB.

Both systems designed as a part of this work are feedback-based systems. A feedback system with more than two poles has the potential to become unstable. For an analog system, phase margin is used to determine how stable a system is. Phase margin is defined as the difference of phase of the loop gain and -180 degrees where the circuit can become unstable. Larger phase margin is proportional to better stability condition. In RF and microwave circuits, it is more convenient to use $K$-stability factor and it is defined as:

$$K = \frac{1 - |S_{11}|^2 - |S_{22}|^2 + |\Delta|^2}{2|S_{11}S_{12}|}$$

(4.1.2)

Where $\Delta = S_{11}S_{22} - S_{12}S_{21}$. If $K$ is greater than 1, the circuit is stable [24]. From the formula, it can be understood that $K$ factor can be obtained from $S$ parameter simulation. It is important to define input and output for the system to get $K$ stability factor. For the band pass filter, input is going to be port 1. The output of notch is not the main point of concern. Therefore, $K$ factor is calculated assuming the input is port 1 and output is port 2 where the band pass response is achieved. The system has the potential to become unstable where feedback is on. Therefore, $K$ factor is simulated for only when the feedback is on with the highest possible loop gain which has the highest potential to become unstable. Moreover, the feedback of the band pass filter is frequency dependent since another LC tank is placed in the feedback loop to get the notch. Therefore, $K$ factor is simulated for three cases of low frequency which is around 4 GHz, mid frequency which is around 5-6 GHz and high frequency which is around 8 GHz, the highest operating frequency of the circuit. The $K$ factor of the band pass filter is depicted in Figure 4.4.
Figure 4.4 K stability factor for low frequency (left), mid frequency (middle) and high frequency (right) of the band pass filter

The low frequency case is where the center frequency of the tank is 4.63 GHz. For this case, minimum K factor is 50. For mid frequency case, the center frequency is 5.31 GHz and minimum K is 30. For high frequency case, the center frequency of the band pass filter is 7.62 GHz while the minimum K factor is 50. As can be concluded from the mentioned results, the circuit is stable for all cases.

For the band stop filter, the feedback path is not frequency dependent. Therefore, if K factor is only simulated for one frequency, it can be concluded the circuit will not be unstable. It is important to mention that the K factor simulation has been performed for all frequency range to ensure stability. However, only one of the frequencies will be brought here for example. The K factor simulation of the band stop filter is demonstrated in Figure 4.5.
The minimum K for the band stop filter is around 1200 which means the circuit is stable. The K factor is simulated for the case when the feedback is on and loop gain is at its maximum.

After ensuring the stability and matching, the functionality of each system has to be tested. For the band pass filter, as it has been explained and demonstrated in Figure 3.3, the Q can be increased by either increasing the negative transconductance cell in the main path or increasing the loop gain to increase the Q. For lower Q cases, it is more efficient to increase Q by using the main path since turning on the feedback path introduces a constant noise to the circuit. As a result, the Q is increased to until 25 using the main path and negative feedback is used after that to further increase the Q of the circuit. This test has to be performed for three frequency ranges the same as simulating the K stability factor. The low Q band pass filter response is shown for three cases of 4.5 GHz, 5.18 GHz and 7.83 GHz in Figure 4.6.

![Figure 4.6 Output response of the band pass filter for low Q cases of low frequency (left), mid frequency (middle) and high frequency (right)](image)

And the high Q response is shown in Figure 4.7.
Figure 4.7 Output response of the band pass filter for high Q cases of low frequency (left), mid frequency (middle) and high frequency (right)

From the figure, the center frequencies are 4.63 GHz, 5.31 GHz and 7.62 GHz respectively while the Qs are 500, 660 and 600. It will be shown in noise figure simulation in next section that adding the feedback path impacts the noise figure of the system in about 1 dB. However, this increase does not change when increasing the Q.

The same simulation for notch has to be done as well. For the first step, the notch has to be simulated for three frequency ranges as the band pass filter while the feedback path is completely off. This has been done in Figure 4.8.

Figure 4.8 Output response of the band stop filter for low Q cases of low frequency (left), mid frequency (middle) and high frequency (right)

And for the high Q case, the simulation results are:
Figure 4.9 Output response of the band stop filter for high Q cases of low frequency (left), mid frequency (middle) and high frequency (right)

The three frequencies are 4.4 GHz, 5.4 GHz and 8 GHz respectively. There is not much frequency difference between high Q and low Q cases in contrast to band pass filter. For the high Q case, the feedback is at its highest strength. For high Q-case, a small peaking is noticed. However, that is not of main concern since the stability of the circuit has already been checked.

As the last part of S parameter simulation, the depth of the notch has to be simulated. As mentioned previously, the notch is depth, frequency and Q tunable. When the level of the interferer is not high, a deep notch may not be needed. The depth of the notch can be adjusted by changing the strength of the negative gm cell. The response of the notch with different depth is highlighted in Figure 4.10.

Figure 4.10 Notch depth tuning
As can be observed from the figure, the depth of the notch is tunable. Notch depth is simulated for the case when feedback is off and center frequency is 5.4 GHz. The notch depth has been simulated for five cases of 0, 10, 20, 40 and 60 dB notch depth.

The functionality of the circuit is simulated in this section. In next section, noise figure will be simulated for band pass and band stop filters for different cases. This section along with the next section are linear type simulations where the circuit is assumed to be linear and small signal model is assumed to be valid.

4.1.2. Noise Simulation

In this section, noise figure simulation of the band pass and the band stop filters will be presented. As it has been mentioned, noise figure and s parameter simulations have been done at the same time using SP analysis of the cadence.

For the band pass filter, Same case as Figure 4.6 and 4.7 has to be simulated. The low Q case is demonstrated in Figure 4.11.

![Noisy Figure of the band pass filter for low Q cases of low frequency (left), mid frequency (middle) and high frequency (right)](image)

From the figure, as the center frequency increases, the noise figure slightly decreases. This happens because the parallel resistance of the tank is larger in higher frequencies. Therefore, in order to get a small Q of around 25, less negative gm is required which leads to less noise added by the negative gm cell as one of the main sources of the noise. The noise figure is less around the center frequency of the tank due to the existence of the signal which results in a higher signal to noise ratio. In overall, the noise figure of the circuit is approximately between 12 to 13 dB when the feedback loop is off. When the loop is turned on, a constant noise added by the output of the feedback circuit will degrade the noise figure. As mentioned in previous chapters, there is a trade-off between the highest achieved Q-boosting from feedback path and the noise penalty imposed by it. Same as Figure 4.7, the noise figure for high Q cases in three frequencies is simulated in Figure 4.12.
The noise figure for high Q cases ranges between 13 to 14 dB which turns into about 1 dB noise degradation caused by the feedback.

For simulating the noise figure of the notch, it is not necessary to have as many simulations as the band pass filter. For the band stop filter, the main source of the noise is feedback. There isn’t any frequency tunable element in the feedback path. Moreover, the in band noise of the negative gm cell goes to the ground, which is in contrast to the band pass filter. As it has been mentioned, the band stop filter employs a low noise amplifier at its input. Therefore, it is expected that the noise figure of the band stop filter would be smaller. The noise figure simulation of the band stop filter is shown in Figure 4.13. The simulation has been done for two cases of completely open loop system and maximum feedback strength. From the figure, the noise figure for the lower band ranges from 4 to 6.6 dB and the noise figure for higher band changes from 5.5 to 7.2 dB. This is because the CMOS transistors of the technology used are not high performance and consequently, their performance is not constant along the frequency of operation.
In the next sub-section, 1-dB compression point simulation of the circuit will be presented.

4.1.3. **Linearity Simulation**

The linearity of the system is simulated using PSS analysis of cadence. For linearity test, 1-dB compression point is simulated. The tone for 1-dB compression point simulation has to be placed at the center frequency of the filter. PSS analysis in contrast to SP analysis is a large signal analysis meaning the small signal models will no longer be valid.

For the linearity of the band pass filter, the tone is placed around the center frequency of the tank which is 4.63 GHz. The result is shown in Figure 4.14.
As seen from the figure, 1-dB compression point is around 6 dBm.

In order to simulate 1-dB compression point of the notch, the tone has to be placed out of the notch frequency. Linearity of the system is simulated when the feedback path is on as well. As the center frequency of the tank is set to mid frequency, the tone is placed at 2 and 4 GHz. While 2 GHz may seem far from the operating frequency of the system, it can be a good indication of the linearity of the system when there is no effect of the notch. The result of 1-dB compression point simulation is demonstrated in Figure 4.15.
From the figure, it can be concluded the input 1-dB compression point of the circuit for both 2 GHz and 4 GHz input is around -4 dBm.

In this section, the complete schematic simulation of both systems have been accomplished. In the next section, the layout of each design will be discussed. After completion of each layout, the post layout simulation has to be performed and compared to the schematic simulation of the circuit. This is an iterative process which may take couple of iterations to get the best layout. The results presented in this chapter are final results and the iterative result of each step will be skipped.

4.2 Layout of the Designs

The size of each layout is often determined by the number of the pads used. The pads are consisting of signal pads which could be differential and DC pads of supply, ground and control voltages. Therefore, the first step in each layout is floor planning. If the circuit has different building blocks, each block can be laid out and tested separately to avoid complexity in debugging of the system. In this section, the detailed layout of each design will be discussed and the related pictures will be presented.

4.2.1. Band Pass Filter Layout

As mentioned, the first step of the layout is floor planning. For the band pass filter, three ports are required. Since each port is differential, it has to be in Ground-Signal-Signal-Ground (GSSG) configuration. Based on the availability of the instruments, pitch of 100 μm is chosen for each GSSG. If the larger pitch is selected, the size of the circuit is going to be larger while it gives the benefit of easier probe landing and measurement. Since the input is always connected but port two and three may not be at the same time, port 1 is placed at the left side of the layout and port 2
and 3 will be placed at the right side. This way, each port of 2 and 3 can be measured without the need to change the measurement setup. Since port 2 and 3 are not going to be used simultaneously, they can share one common ground to shrink the size of the circuit.

For DC voltages, the frequency of the band pass filter has to be tuned. In order to avoid an increase in size, only one control voltage is assigned for controlling the varactor associated with the main path. The voltage of the varactor varies between 1.5 and 3.5 volts and is named $V_{\text{CAP,BPF}}$. If a very small Q is desired, the series resistance of the tank has to be tunable. Therefore, $V_{\text{RQ,BPF}}$ is assigned which can be changed from 2.5 to 3.5 volts. The lower voltage corresponds to open and higher series resistance. While it was not much focused on, there is a trade-off between linearity and noise for the main band pass filter and it can be adjusted by adjusting the gain. Therefore, a DC voltage is assigned to change the gain of the main band pass filter. This voltage is name $V_{\text{AV,BPF}}$ and it can vary between 0 to 1.8 volts where the highest gain is achieved when the voltage is set to 1.8. The circuit used as the main band pass filter is the same as [5]. Therefore, it has its own supply. The supply voltage of the circuit which is named $V_{\text{CC,BPF}}$ is set to 3.5 volts. The strength of the negative gm cell in the main path has to be controlled in order to tune the Q. Therefore, $V_{\text{GM,BPF}}$ is placed to change the amount of negative gm cell depending on the required Q from the main path. This voltage varies between 0 to 1.8 volts where 1.8 volts corresponds to the highest possible strength of the negative gm cell. As it has been mentioned in previous sections, feedback path may not be needed all the times especially when a low Q is sufficient. In this case, in order to avoid noise penalty imposed by the feedback path, the path has to be completely turned off. $V_{\text{ON,FB}}$ is designed to perform this task. This voltage is changed from 0 to 1.8 volts. The gain of the feedback path has to be tunable in order to achieve Q tunability, therefore, $V_{\text{AV,FB}}$ is put to accomplish the mentioned goal. This voltage changes from 0 to 1 volt where 0 corresponds to the highest possible gain. The feedback path has its own supply of 2.5 volts and its pad name is $V_{\text{CC,FB}}$. The tank of the feedback is also tunable. Since the same tank as the band pass filter is used with a slightly different configuration to get notch response, $V_{\text{CAP,FB}}$ is assigned to tune the frequency of the notch and its voltage varies from 1.5 to 3.5 volts which is similar to the main tank. Lastly, the notch has its own negative gm cell and its strength is controllable by $V_{\text{GM,FB}}$ which can be changed from 0 to 1,8 volts.

The configuration for signal pads is almost predefined. Therefore, three GSSG configurations are needed. However, for DC pads, it can have multiple configurations. As mentioned, 10 DC voltages are needed not considering the grounds. Since the left and right of the layout have already been occupied by GSSG pads, the DC pads have to be placed on top and bottom of the layout. In order to save space and ease the landing of the probes and avoid probe collision and based on the availability, a GPPPPPPPPPPG configuration (G for ground and P for power) is chosen and it is placed on top of the layout. The floor planning of band pass filter is shown in Figure 4.16.
As illustrated in the figure, the overall size of the circuit is 675 μm by 1430 μm. It is important to mention while using a GPPPPPPPPPPG probe facilitates the landing of the probes in terms of using only one DC probe instead of two, landing of it should be done carefully to ensure all pads are landed.

As mentioned, it is preferred to design the layout block by block so that the debugging after post extraction simulation will be more trivial. The layout of the band pass filter has been ready and it has not been redesigned except the grounding. The layout of the sub circuit of the Figure 3.10 is as following:

Figure 4.16 Floor planning of the band pass filter layout

Figure 4.17 The layout of the buffer and gain stage of the feedback path
The large capacitances are DC blocking capacitances and are large since the input impedance of the notch is small. The layout of the LC notch is as following:

![LC Notch]

Figure 4.18 The layout of the LC tank of the notch

After the layout of each sub circuit, the next step is to connect them together. After connecting, feedback path has to be established. It has to be laid out in the optimum way to avoid performance degradation. Then, the layout of band pass filter and notch has to be connected together. After connecting all the components, the circuit has to be connected to the pads. Then, the empty spaces have to be filled with fill cells connected to ground to pass both Design Rule Check (DRC) and have a perfect grounding to avoid potential difference in different grounds of the circuit. Exclude layers are also placed around LC tanks to avoid automatic metal fill by the foundry which degrades the performance of the system. After doing all the steps, the final layout of the band pass filter will be:

![Band pass filter final layout]

Figure 4.19 Band pass filter final layout
The distance between the output of the band pass filter and the output pad is around 600 \( \mu \text{m} \). This can cause problem if the line is not matched to 50 \( \Omega \). Therefore, by using Sonnet electromagnetic simulation tool, a 50 \( \Omega \) transmission line is designed between the output of the band pass filter and the pads. All adjacent ground pads are connected using the top metal.

### 4.2.2. Band Stop Filter Layout

The layout for the band stop filter, similar to the band pass filter, starts by floor planning. As it will be explained, the layout of the band stop filter is not as complex as the band pass filter. Therefore, it is not necessary to do the layout block by block.

For the band stop filter there are two ports of input and output and since both are differential, two GSSG pads are needed. With the same pitch as the pads of band pass filter, the input is placed on the right side of the layout while the output is placed on the left side.

For DC control voltages, \( V_{\text{Supply}} \) is needed. The supply voltage of the circuit varies between 2.8 and 3.5 volts. However, in order to minimize the power at the cost of worse noise figure and linearity, it is set to 2.8 volts. Since a negative gm cell is employed to control the depth of the notch, a control voltage is needed for that. Therefore, \( V_{\text{GM}} \) is assigned to accomplish this task and it changes from 0 to 2.5 volts. The Q of the system can be controlled by the series resistance of the LC tank similar to the band pass filter behavior. In order to tune Q, a variable resistance using an NMOS switch is placed in parallel to the series resistance of the tank and its value can be changed by changing a voltage called \( V_{\text{RQ}} \). This voltage can be changed from 0 to 1.8 volts. In order to tune the frequency, a voltage control is needed to change the voltage across the varactor. \( V_{\text{CAP}} \) is assigned to perform this task and is changeable from 2.5 to 4.5 volts if the supply is 3.5 volts and 1.8 to 3.8 if the supply is 2.8 volts. Lastly, since one way to control the Q is to change the loop gain, it has to be made variable. Using \( V_{\text{FB, Av}} \) and by changing it from 0 to 2.5 volts, the strength of the feedback path can be controlled.

So far, there has been two GSSG pads which are placed at the right and left side of the layout and five control voltages not considering the grounds. While all control voltages can be placed on top or bottom like the band pass filter, it leads to increase in the overall size of the circuit. Therefore, two pad sets are used at the top and bottom to shrink the overall size. On the top side, three of the DC pads are placed in GPPPG configuration. For the remaining DC pads, a GPPG configuration can be used. However, due to the availability of the probes in the measurement lab a second GPPPG pad is used. However, since only two control voltages are needed, it will be used as GGPPG. The floor plan of the band stop filter is shown in Figure 4.20.
Figure 4.20 Floor planning of the band pass filter layout

The overall size of the circuit is going to be 540 μm by 785 μm.

The circuit of the band stop filter consists of a low noise amplifier, a notch which is based on an LC tank and a feedback path. As mentioned, block by block of the design will not be explained since the circuit is significantly smaller than the band pass filter and doesn’t require block by block layout. The low noise amplifier is preferred to be closer to the input. Therefore, it is placed on the right side and the tank and notch are placed on the left side. Similar to the band pass filter, the feedback path needs to be carefully laid out. For the band stop filter the layout of the feedback becomes even more important. Since CMOS is used instead of HBT for the design of the band stop filter, the highest operating frequency of the CMOS transistors are significantly smaller than HBT transistors (100 GHz for CMOS compared to 200 GHz for HBT). Since both of the systems are design for 4 to 8 GHz frequency range, parasitic poles may impact the performance of the band stop filter in a more drastic way. After laying out the feedback and connecting all three parts together, grounding and exclude layer placing is completed and the final layout is going to be as following:
4.3 Post Layout Simulations

In this section, the simulation results after parasitic RC extraction of the layout will be presented. In order to have a fair comparison with the schematic part, same simulation steps will be followed and the results will be compared with the schematic. In addition to the results mentioned in the schematic simulation, the power consumption of the circuit will be simulated as well. After this section, a comparison will be made to the most recent designs in literature.

4.3.1 S Parameter Simulation

Same simulations as the schematic simulation will be done for this part. For the band pass filter, post layout matching is shown in Figure 4.22.
Comparing with Figure 4.2, input and notch matching are still below -10 dB. Output matching is degraded more is closed to -8 to -9 dB. However, as mentioned before, this is not of main concern.

The same simulations have to be done for the matching of the band stop filter. The results will be demonstrated in Figure 4.23. From the figure, and by comparing to Figure 4.3 which is the same simulation for schematic level, it can be concluded the overall matching of the circuit has not been degraded significantly after post layout simulation. The output matching of the circuit is slightly better than the input matching. However, as long as both of them are better than -10 dB, there will be no concerns regarding the matching.
Following the same steps as the schematic simulations, the stability of the systems has to be studied. It is expected that the stability gets worse for the post layout simulations due to the existence of layout parasitic poles.

For the stability of the band pass filter, the same simulations as Figure 4.4 has to be done in three different frequencies. This is shown in Figure 4.24. The simulations are for three different center frequencies of 4.58 GHz, 5.45 GHz and 7.45 GHz. These three frequencies are slightly higher than their schematic simulations counterpart. This is due to the unavoidable frequency shift imposed by the feedback path. As it will be explained, the values of Q are also degraded. The minimum K factor for the three cases are 5, 7 and 8 respectively. This was expected since the parasitic capacitance of the feedback play an important role in reducing the stability margin of the circuit. Although the layout has significantly degraded the minimum K factor of the circuit, the circuit is still stable since minimum K is larger than unity.

![Figure 4.24 K stability factor for low frequency (left), mid frequency (middle) and high frequency (right) of the band pass filter in post layout simulation](image)

Same as Figure 4.5, the K stability factor for the band stop filter is shown in Figure 4.25.
As compared to the K factor of Figure 4.5, the minimum of K stability factor has been degraded from 1200 to 28. However, the circuit is still stable.

The output response of the band pass filter for low Q after post layout is going to be:

And for the high Q case:
Comparing 4.26 with 4.6, the center frequency for low Q cases are 4.41, 5.2 and 7.37 GHz while the Q for all cases is 25. These frequencies are smaller than the schematic since there is more parasitic capacitance in the layout. However, frequency shift is in the other direction for high Q cases as the center frequencies are 4.58, 5.45 and 7.45 GHz for the Qs of 270, 285 and 270. The Q is almost degraded by half compared to the schematic simulation.

Following the same steps for the band stop filter, the output is going to be:

Figure 4.28 Output response of the band stop filter for low Q cases of low frequency (left), mid frequency (middle) and high frequency (right) for post layout
Figure 4.29 Output response of the band stop filter for high Q cases of low frequency (left), mid frequency (middle) and high frequency (right) for post layout

The center frequencies are not significantly different than the schematic. It is important to mention that there are multiple methods to define the bandwidth of a band stop filter. In order to compare the bandwidth in Figure 4.28 with Figure 4.29, it is assumed the bandwidth is defined at the points where the gain is 3 dB less than the pass band gain. By defining the bandwidth as mentioned, for Figure 4.28, bandwidth values from left to right are 180 MHz, 340 MHz and 710 MHz. These values would be boosted to 80 MHz, 160 MHz and 500 MHz respectively when the feedback is turned on. The reason the Q enhancement is higher for the lower frequencies is that the maximum gain the CMOS transistors can provide at higher frequency degrades. If a more advanced CMOS technology is employed, Q enhancement can be improved significantly.

As the last part of this sub section, the simulation of notch depth is shown in Figure 4.30.
As can be seen from the figure, the depth is adjustable from very small values up to about 55 dB.

4.3.2. Noise Simulation

The Noise Figure of the cases of Figures 4.26 and 4.27 is simulated in this section. The results will then be compared to Figures 4.11 and 4.12. It will be shown that the noise degradation due to post layout is not significant since it is still between 12 and 13 dB same as what has been observed from Figure 4.11 for the low Q case.

![Figure 4.31](image1.png)

Figure 4.31 Noise Figure of the band pass filter for low Q cases of low frequency (left), mid frequency (middle) and high frequency (right) for post layout

For the high Q case, the noise figure is shown in Figure 4.32.

![Figure 4.32](image2.png)

Figure 4.32 Noise Figure of the band pass filter for high Q cases of low frequency (left), mid frequency (middle) and high frequency (right) for post layout
From the Figure, the Noise Figure is between 13 to 14 dB which is the same as schematic simulation. In overall, it can be concluded there is no significant noise degradation in band pass filter after post layout simulation.

The noise figure simulation for the band stop filter for two cases of open loop and closed loop is shown in Figure 4.33.

![Figure 4.33 Schematic simulation of the Noise Figure of the band stop filter for open loop and closed loop cases for layout](image)

The Noise Figure is changing from 4.4 to 7.9 dB for open loop and 6.7 to 8.8 for closed loop simulations. While the Noise Figure degradation is negligible for low frequencies, it is higher than 1 dB for higher frequencies where 6.6 dB of schematic noise figure is compared to 7.9 dB of post layout for open loop and 7.2 dB of schematic noise figure compared to 8.8 dB of post layout for closed loop. The reason for this degradation is when more parasitic poles are added to the system, the gain path will degrade which causes degradation in noise figure since signal is going to be weaker. If the linearity is still high in post layout simulation, the noise figure can be reduced by compromising the linearity by adding another low noise amplifier to the system.

### 4.3.3. Linearity Simulation

Linearity simulation of the band pass filter leads to the following Figure for 1-dB compression point of the circuit.
For the band pass filter:

As can be seen the 1-dB compression point of band pass filter is around 2 dBm while this value is -4 dBm for the band stop filter.

4.3.4. Power Consumption

After post layout simulation, the main tank of band pass filter which has the voltage supply of 3.5 volts consumes between 13.16 mA and 26.8 mA of current while the current of the notch path varies between 0 to 30.83 mA and the supply of 2.5 volts.

For the band stop filter, DC current ranges from 14 mA to 25 mA and the supply voltage is 2.8 volts.
4.4 Performance Comparison

The comparison of the band stop filter proposed for this work and the state of the art is shown in Table 1.

Table 1 Comparison table for the state of the art band stop filters

<table>
<thead>
<tr>
<th></th>
<th>[14]</th>
<th>[15]</th>
<th>[17]</th>
<th>This work</th>
</tr>
</thead>
<tbody>
<tr>
<td>Process</td>
<td>65 nm CMOS</td>
<td>0.13 µm CMOS</td>
<td>0.13 µm BiCMOS</td>
<td>0.13 µm CMOS</td>
</tr>
<tr>
<td>Center Frequency (GHz)</td>
<td>0.1 - 1.2</td>
<td>5 - 6</td>
<td>4 - 8</td>
<td>4.4 – 7.8</td>
</tr>
<tr>
<td>Depth (dB)</td>
<td>21 - 24</td>
<td>35</td>
<td>50</td>
<td>55</td>
</tr>
<tr>
<td>NF (dB)</td>
<td>1.6 - 2.5</td>
<td>6.2</td>
<td>8 - 10.8</td>
<td>6.7 - 8.8</td>
</tr>
<tr>
<td>P1-dB (dBm)</td>
<td>6</td>
<td>-30</td>
<td>-9 to -6</td>
<td>-4</td>
</tr>
<tr>
<td>Power (mW)</td>
<td>3.5 - 30</td>
<td>32</td>
<td>66 - 91</td>
<td>39 - 70</td>
</tr>
<tr>
<td>Die Area (mm^2)</td>
<td>0.87</td>
<td>1.6</td>
<td>0.4</td>
<td>0.42</td>
</tr>
</tbody>
</table>

As can be observed from the table, the proposed work has the widest tuning range and highest depth tied with [17]. This work provides the best combination of linearity and noise figure except for the [14] where the operating frequency is significantly smaller. Power consumption is better than [17] and the area is slightly higher than [17]. In overall, the technique used is novel and the performance is acceptable compared to the most recent works.

For the band stop filter, the comparison table is demonstrated in Table 2.
Table 2 Comparison table for the state of the art band pass filters

<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Center Frequency (GHz)</td>
<td>0.1 - 1</td>
<td>2.25 - 4</td>
<td>0.8 - 2.4</td>
<td>0.6 - 0.85</td>
<td>0.4 - 1.2</td>
<td>0.1 - 1.2</td>
<td>2.03</td>
<td>4.4 – 7.45</td>
</tr>
<tr>
<td>Q</td>
<td>3 - 29</td>
<td>3 - 150</td>
<td>5.3 - 16</td>
<td>40 - 90</td>
<td>20 - 60</td>
<td>12.5 - 150</td>
<td>16</td>
<td>3 - 270</td>
</tr>
<tr>
<td>NF (dB)</td>
<td>3 - 5</td>
<td>10 - 18.5</td>
<td>19.26 - 21.24</td>
<td>8.6</td>
<td>10</td>
<td>2.8</td>
<td>15</td>
<td>10 - 14</td>
</tr>
<tr>
<td>P1-dB (dBm)</td>
<td>-8 to 9</td>
<td>-13 to -10</td>
<td>0</td>
<td>0</td>
<td>NA</td>
<td>-6.6</td>
<td>2</td>
<td></td>
</tr>
<tr>
<td>Power (mW)</td>
<td>2 - 16</td>
<td>43 - 66</td>
<td>350 - 400</td>
<td>75</td>
<td>21.4</td>
<td>15 - 48</td>
<td>16</td>
<td>46 - 171</td>
</tr>
<tr>
<td>Die Area (mm^2)</td>
<td>0.07</td>
<td>0.476</td>
<td>0.15</td>
<td>1.2</td>
<td>0.127</td>
<td>0.27</td>
<td>0.81</td>
<td>0.97</td>
</tr>
</tbody>
</table>

This work has the highest frequency range of all and its tuning range is tied with [5]. The tuning range of 3 to 270 is the highest of all designs and with the noise figure range of 10 dB to 14 dB and best case 1-dB compression point of 2 dBm, it provides a reasonable combination of linearity and noise. The reason for the large size is due to the using of 2 inductors and a complex circuit.

4.5 Chapter Summary

This chapter is mainly about the implementation of the two proposed systems of this work. The chapter starts with schematic simulations of the designs introduced in chapter 3. For each design, linear simulations of S-parameters, stability and Noise Figure are presented as well as nonlinearity simulations of 1-dB compression points. Following the schematic simulation, the layouts of both designs are discussed. For the layout sections, the details of floor planning and number of control voltages and input and outputs are reviewed. The final layout of each part is presented along with its overall size. After the layout, the same simulations as the schematic simulations are demonstrated and the results are compared to schematic simulations. At the end of the chapter, the performances are compared to the state of the art in band pass and band stop filter design.
Chapter 5

Conclusion

This work is based on designing interference cancelling systems for different wideband and narrowband applications. Filtering is a crucial part of RF communications. In the past, discrete and mechanical filters were used to accomplish the goal of filtering in high frequency. The new trend is to design integrated filters aiming to reduce the size and power consumption of the circuit. Moreover, integrating may provide room for software tuning of the characteristics of the filters. While current state of the art filter designs have been successful in achieving promising performances comparable to discrete and mechanical filters, the issue of frequency and bandwidth tunability is still an ongoing problem. The main purpose of this research is to design cutting edge filters with outstanding performances and to add frequency and tuning capability to them.

The first design introduced as a part of this work is a band pass filter. The main core of the filter is based on [5] where a second order RLC tank is employed along with a negative transconductance cell to enhance the Q of the filter. The issue with [5] is large noise penalty added to the system for high Q cases. The band pass filter of this research is based on feedback interference cancelling techniques where the Q of the system can be boosted with minimum noise penalty. Adding the feedback circuitry to [5] can provide both the advantage of an open loop system and high Q without excessive noise.

The second design of this work is a band stop filter. The circuit is based on a Q-enhanced band pass LC tank. The output current of the circuit is controlled by the LC tank and band stop response can be accomplished by using MOS transistors as transconductances. Feedback is also used for this design to get sharp transition from stop band to pass band. After final implementation of the filter, it has the capability of wide frequency tuning as well as depth tuning and bandwidth.

Since an LC tank using a varactor as a variable capacitor in the tank is the main core of both designs, the linearity of the varactor is a major focus of this study. Using two different techniques of nonlinear modeling, the nonlinearity of the tank is modelled and schematic simulations are performed to validate the developed models. After deriving a closed form formula, different tuning techniques are suggested to enhance the linearity of the system.

There are suggestions for future work that can be done. In this study, the band stop filter has been implemented using an old technology. Implementing it on a novel CMOS technology in future research would significantly improve the performance and make it possible to test the idea for higher frequency ranges. Second, none of the tuning techniques suggested in this work are implemented in the band stop and band pass filter. Using multiple control voltages or cancelling nonlinear coefficients by having more than one control voltage can significantly improve the linearity of the system. Third, there is room to improve the linearity of the negative gm cell. Using other negative gm generators, the noise and linearity performance of the system can be improved significantly. Finally, a low noise amplifier (LNA) can be added to the band pass filter. Successful implementation of an LNA with the band pass filter can give a practical low noise high linearity receiver.
References


