

SPIN PROJECTION OF SEMI-EMPIRICAL AND AB INITIO
UNRESTRICTED HARTREE-FOCK WAVEFUNCTIONS

by

Dana Alice Brewer

Dissertation submitted to the Graduate Faculty of the
Virginia Polytechnic Institute and State University
in partial fulfillment of the requirements for the degree of

DOCTOR OF PHILOSOPHY

in

Chemistry

APPROVED:

John C. Schug, Chairman

Jack D. Graybeal

Philip L. Hall

Larry T. Taylor

Jimmy W. Viers

July, 1977
Blacksburg, Virginia

II. ACKNOWLEDGMENTS

The author expresses her appreciation to Dr. John C. Schug for his support, patience and guidance during the completion of the research reported here. Gratitude is also expressed to Dr. Michael A. Ogliaruso for the collaboration on the research on homoconjugation and to Mr. Byron H. Lengsfield, III for helpful discussions and collaboration on the spin projection programs and applications. Finally, thanks is expressed to Mr. Lyle Evans for his outstanding aid as a consultant for the problems encountered in computer programming.

III. TABLE OF CONTENTS

CHAPTER	PAGE
I. TITLE	i
II. ACKNOWLEDGMENTS	ii
III. TABLE OF CONTENTS	iii
IV. LIST OF TABLES AND FIGURES	v
V. INTRODUCTION	1
VI. HARTREE-FOCK THEORY	7
VII. SPIN PROJECTION OPERATORS AND THE UNRESTRICTED HARTREE-FOCK WAVEFUNCTION	14
VIII. EXCITED ELECTRONIC STATES OF ALTERNANT PI-ELECTRON SYSTEMS	21
IX. ALL VALENCE ELECTRON CALCULATIONS	38
Homoconjugation in the Monohomocyclooctatetraene	
Anion Radical	42
Extension of INDO Calculations in Include	
d-Orbitals	53
X. AB INITIO UNRESTRICTED HARTREE-FOCK CALCULATIONS . .	57
Comparison of Spin Projection and MCSCF/CI	
Calculations on H ₂ O(+)	68
The Dissociation of CF ₂ O	74
XI. LITERATURE CITED	95
XII. APPENDIX A	100

CHAPTER	PAGE
XIII. VITA	209

IV. LIST OF TABLES AND FIGURES

TABLE	PAGE
I. Wavelengths(\AA) for the Ground to Excited State Transitions in Naphthalene	27
II. Wavelengths(\AA) for the Ground to Excited State Transitions in Anthracene	28
III. Wavelengths(\AA) for the Ground to Excited State Transitions in Naphthacene	29
IV. Wavelengths(\AA) for the Ground to Excited State Transitions in Pentacene	30
V. Projected Electronic Energies and Weighting Factors for the Open Shell Ground State in Pentacene	34
VI. Wavelengths(\AA) for Open Shell Ground to Excited State Transitions in Pentacene	35
VII. Proton Hyperfine Coupling Constants, a_H , for the Monohomocyclooctatetraene Anion Radical Obtained from Unprojected Wavefunctions	47
VIII. Proton Hyperfine Coupling Constants, a_H , for the Monohomocyclooctatetraene Anion Radical Obtained from Spin Projected Wavefunctions	48
IX. Unprojected and Projected Binding Energies(a.u.) and Weighting Factors for the Monohomocyclooctatetraene Anion Radical	50

TABLE	PAGE
X. Invariant Bond Orders for Calculated Geometries of Monohomocyclooctatetraene Anion Radical	52
XI. Atomic Energies(a.u.) for Third Row Atoms Calculated Using INDO Approximations	56
XII. Contracted Gaussian Basis Set for a (9s5p2d/4s1p) H ₂ O Primitive Basis Set	70
XIII. Unprojected and Projected Energies for the X ² B ₁ State of H ₂ O(+)	71
XIV. Unprojected and Projected Energies for the \tilde{B}^2B_2 State of H ₂ O(+)	72
XV. Comparison of MCSCF/CI and Spin Projection Energies for the Equilibrium Geometries of the X ² B ₁ and \tilde{B}^2B_2 States of H ₂ O(+)	73
XVI. Symmetry Orbitals for [4s3p] Basis Set of CF ₂ O Near the Equilibrium Geometry	80
XVII. Symmetry Orbitals for the [4s3p] Basis Set of CF ₂ + O	82
XVIII. Total Energies(a.u.) for the A ₁ State of CF ₂ O as a Function of the Carbon–Oxygen Bond Distance	84
XIX. Total Energies(a.u.) for the A ₂ State of CF ₂ O as a Function of the Carbon–Oxygen Bond Distance	85
XX. Total Energies(a.u.) for the B ₁ State of CF ₂ O as a Function of the Carbon–Oxygen Bond Distance	86
XXI. Total Energies(a.u.) for the B ₂ State of CF ₂ O as a Function of the Carbon–Oxygen Bond Distance	87

TABLE	PAGE
XXII. Total Energies(a.u.) as Functions of Molecular Symmetry for the Dissociated $\text{CF}_2 + \text{O}$	89
XXIII. Comparison of Experimental and Calculated Vertical Ionization Potentials for CF_2O	92
FIGURE	PAGE
1. Geometry of Monohomocyclooctatetraene Anion Radical . .	44
2. Geometry of CF_2O Molecule	78
3. Total Energy(a.u.) as a Function of Carbon-Oxygen Bond Distance(bohrs) in CF_2O	88

V. INTRODUCTION

The accurate description of molecular orbitals and molecular interactions has been a problem confronting chemists and physicists for many years. The problem would be straightforward if the electronic Schröedinger equation could be solved exactly. However, an exact solution of this equation is possible only for the hydrogen atom. Consequently, various approximation methods have been invoked. One of the most widely used methods is the variational theorem.

The variational theorem provides approximate solutions to the electronic Schröedinger equation,

$$\mathcal{H}_e \Psi_e = E_e \Psi_e \quad (1)$$

where \mathcal{H}_e is the electronic Hamiltonian operator, Ψ_e is an antisymmetrized product of molecular spin-orbitals, and E_e is the electronic energy. The spatial part of the spin orbitals, or molecular orbitals, are constructed as normalized linear combinations of atomic orbitals, ϕ_μ ,

$$\Phi_{\mu i} = \sum_{\mu} c_{\mu i} \phi_{\mu} \quad (2)$$

where the coefficients, $c_{\mu i}$, are allowed to vary in order to minimize the electronic energy of the molecule. However, because the variational theorem is an approximate technique, the expectation values of the energies derived from this method will always be

higher than the true energies of the ground state molecules.

A closed shell molecule is a system in which there is an equal number of spin up (α) and spin down (β) electrons and all orbitals are either empty or doubly occupied. The molecular orbitals for the α -electrons are the same as those for the β -electrons. Since the α - and β -wavefunctions are equal, the Hartree-Fock operator for the α -electrons is equal to the Hartree-Fock operator for the β -electrons. This is called a restricted calculation; i.e., the α - and β -wavefunctions are forced to be equal. This condition guarantees that the electronic wavefunction, Ψ , is an eigenfunction of the total spin operator, S^2 ,

$$S^2 \Psi = s(s + 1) \Psi . \quad (3)$$

An open shell molecule is a system in which either there is an unequal number of α - and β -electrons or there is an equal number of α - and β -electrons but some occupied orbitals are not doubly occupied. The treatment of such a system by a restricted calculation does not result in good approximations to the molecular energies; much closer values to the true energy are obtained when the α - and β -electrons are treated separately in an unrestricted calculation. In general, the orbitals for the α -electrons are not equal to the orbitals for the β -electrons. Unrestricted Hartree-Fock (UHF) theory or the method of different orbitals for different spins (DODS) provides much better approximations to the true energies than a restricted calculation.

Because UHF theory produces two different sets of molecular

orbitals, one set for the α - and one set for the β -electrons, the resultant single determinant wavefunction,

$$\Psi = | \phi_1^\alpha \phi_1^\beta \phi_2^\alpha \phi_2^\beta \cdots \phi_i^\alpha \phi_i^\beta \cdots | \quad (4)$$

is not guaranteed to be a state of pure spin multiplicity; that is,

$$S^2 \Psi \neq s(s+1) \Psi. \quad (5)$$

Since $[\mathcal{H}, S^2] = 0$, the correct electronic states will also be eigenfunctions of S^2 . This requirement can be satisfied by projecting from the single determinant various pure spin eigenfunctions.

One method of obtaining such wavefunctions is through the application of spin projection operators. Löwdin¹ has shown that it is a relatively simple procedure to construct spin projection operators which will project pure spin wavefunctions from wavefunctions with mixed multiplicity. Two methods of applying the spin projection operators have been explored, the Harriman-type UHF and the spin-projected extended Hartree-Fock (EHF) methods. Since the following chapters deal exclusively with the former method, the latter method will be briefly outlined, and the results obtained using the two methods will be briefly compared.

In the spin projected EHF method developed by Mayer,² single determinant wavefunctions are constructed using the DODS formalism and spin projected. Such a wavefunction is used as a trial function in the variational procedure. The one-electron orbitals are then optimized to obtain a minimum energy for the resulting projected wavefunction.

The spin projected UHF calculation differs from the EHF

method in that the energy minimization procedure is performed on the unprojected DODS wavefunction. Spin projection of the unprojected wavefunction follows the minimization procedure.

First inspection of the spin-projected EHF and UHF plus spin projection methods leads one to assume that the EHF method is superior to the UHF method since the projected pure spin state is dealt with in the former method. However, Mayer and Kertesz³ have examined the results of both methods using the Pariser-Pople-Parr (PPP) π -electron approximations for polyenes with two to 38 carbon atoms with surprising results. The EHF method is superior to the UHF method for the smallest systems up to approximately 15 carbon atoms; however, as the number of atoms increases further, the energy differences between the two methods decrease rapidly. Mayer concludes that, for larger systems, it is sufficient to perform UHF calculations with subsequent spin projection. From the standpoint of computational time involved, the UHF method is far superior.

The work described below is concerned exclusively with the UHF plus spin projection method. The electronic spectra of naphthalene, anthracene, naphthacene and pentacene were calculated using the PPP approximations and both UHF and configurational interaction (CI) techniques. The results of both techniques were compared to experimentally determined spectra when data were available. There was reasonable agreement between the CI and projected UHF results. While the CI calculations generally produced lower energies for the triplet states than the UHF calculations, the spectra from the UHF

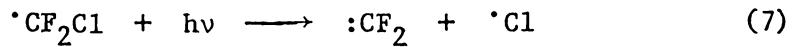
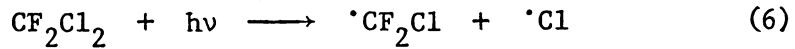
calculations were in somewhat better agreement with experiment. Anomalies encountered with degeneracies and the presence of open shell ground states are also discussed.

Monohomocyclooctatetraene anion radical (MHCOT) was studied using a DODS wavefunction with spin projection and the all-valence electron INDO approximations. The theoretical molecular geometry was varied until the experimental hyperfine coupling constants matched hyperfine constants obtained from using both projected and unprojected UHF wavefunctions. The two types of calculations resulted in slightly different energies and geometries with the projected calculations giving a higher energy for the doublet state; essentially no differences were noted in the bond orders obtained from the two types of calculations. The geometry from the projected calculations was a somewhat more strained conformation than the geometry from the unprojected calculation.

Ab initio UHF calculations with spin projection were performed on H₂O(+) using the POLYATOM (Version 2)⁴ system of programs. The purpose of the study was to compare the energies of pure spin states from ab initio multi-configurational self-consistent field with CI (MCSCF/CI)⁵ with those from spin projection. The MCSCF/CI calculations are superior to the UHF plus spin projection calculations. This result will always be observed when the UHF wavefunction is very close to a pure spin state before spin projection.

The dissociation of CF₂O was studied using ab initio wavefunctions. The molecule is of possible importance in the atmos-

pheric reaction scheme since it is a possible product from the dissociation of dichlorodifluoromethane,



The energies of the unprojected wavefunctions of CF_2O were examined along with those for the dissociated CF_2 and O fragments.

VI. HARTREE-FOCK THEORY

Since the work described below deals with spin projected Hartree-Fock wavefunctions and various approximations for terms in the Hartree-Fock equations, it is advantageous to review Hartree-Fock theory at this point.⁶

The nonrelativistic Hamiltonian, in atomic units, is

$$\begin{aligned} \mathcal{H} = & -\frac{1}{2} \sum_i v_i^2 + \sum_{i>j} \frac{1}{r_{ij}} - \sum_{\mu,i} \frac{z_\mu}{r_{\mu i}} - \frac{1}{2} \sum_\mu \frac{\nabla_\mu^2}{m_\mu} \\ & + \sum_{\mu>\nu} \frac{z_\mu z_\nu}{r_{\mu\nu}} \end{aligned} \quad (9)$$

where i and j denote electrons and μ and ν denote nuclei. When the Born-Oppenheimer approximation⁷ is applied, the fourth term describing the translational motion of the nuclei is ignored, and the fifth term, the nuclear repulsion energy operator, v_n , becomes a constant value. In other words, electronic states are examined in the "frozen-nuclei" approximation. The electronic Hamiltonian operator then reduces to

$$\mathcal{H} = -\frac{1}{2} \sum_i v_i^2 + \sum_{i>j} \frac{1}{r_{ij}} - \sum_{\mu,i} \frac{z_\mu}{r_{\mu i}} + v_n . \quad (10)$$

The electronic energy for an unrestricted wavefunction can be expressed as

$$\begin{aligned}
 E_e = & \sum_{r=1}^{B_{occ}} (T_r + V_r) + \frac{1}{2} \left(\sum_{r,s=1}^{B_{occ}} J_{rs} - \sum_{r,s=1}^{B_{occ}^\alpha} K_{rs}^\alpha \right. \\
 & \left. - \sum_{r,s=1}^{B_{occ}^\beta} K_{rs}^\beta \right)
 \end{aligned} \tag{11}$$

where B_{occ} is the total number of occupied orbitals, B_{occ}^α is the number of occupied α -molecular orbitals and B_{occ}^β is the number of occupied β -molecular orbitals. Letting r and s denote molecular orbitals, the first summation of one-electron terms is comprised of the kinetic and potential energy integrals, T_r and V_r , respectively,

$$T_r = \langle r(i) | -\frac{1}{2} \nabla_i^2 | r(i) \rangle \tag{12}$$

$$V_r = \langle r(i) | -\sum_\mu \frac{Z_\mu}{r_{\mu i}} | r(i) \rangle . \tag{13}$$

The two-electron integrals are described in the second term by the coulomb, J_{rs} , and the exchange integrals, K_{rs} ,

$$J_{rs} = \langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle \tag{14}$$

$$K_{rs} = \langle r(i) s(j) | \frac{1}{r_{ij}} | s(i) r(j) \rangle . \tag{15}$$

The molecular orbitals are described in terms of linear combinations of atomic orbitals (LCAO) with subscripts m , n , p , and q ,

$$| r^\alpha(i) \rangle = \sum_m c_{mr}^\alpha | m(i) \rangle \tag{16}$$

$$| r^\beta(i) \rangle = \sum_m c_{mr}^\beta | m(i) \rangle . \quad (17)$$

The distribution of the α - and β -electrons in the molecule is described by the α - and β -charge density and bond order matrices, P_m^α and P_m^β , with elements,

$$P_{mn}^\alpha = \sum_r^{B_{occ}^\alpha} c_{mr}^\alpha c_{nr}^\alpha \quad (18)$$

$$P_{mn}^\beta = \sum_r^{B_{occ}^\beta} c_{mr}^\beta c_{nr}^\beta . \quad (19)$$

The total density matrix, P , is the sum of the α - and β -density matrices,

$$P_{mn} = P_{mn}^\alpha + P_{mn}^\beta \quad (20)$$

The net unpaired electron density in the molecule is described by the spin density matrix, P_m^z ,

$$P_{mn}^z = P_{mn}^\alpha - P_{mn}^\beta . \quad (21)$$

The electronic energy can now be written in terms of the density matrices and integrals over atomic orbitals,

$$\begin{aligned} E = & \sum_{mn} P_{mn} (T_{mn} + V_{mn}) + \frac{1}{2} \sum_{mnpq} (P_{mn} P_{pq} - \\ & P_{mp}^\alpha P_{nq}^\alpha - P_{mp}^\beta P_{nq}^\beta) \langle m(i) p(j) | \frac{1}{r_{ij}} | n(i) q(j) \rangle . \end{aligned} \quad (22)$$

The variational principle is applied by using Lagrange's method of undetermined multipliers to insure that the orbitals are orthonormal. An extremum is sought in

$$\delta [E - \sum_{r,s=1}^B \lambda_{rs} (S_{rs} - S_{sr})] = 0, \quad (23)$$

where S_{rs} are the overlap integrals,

$$S_{rs} = \langle r(i) | s(i) \rangle, \quad (24)$$

and λ_{rs} are the undetermined multipliers. Equation 23 contains $N(N + 1)/2$ constraints; introduction of variations in the orbitals $|r(i)\rangle$ leads directly to the set of Hartree-Fock equations,

$$F^\alpha |r(i)\rangle = \sum_{s=1}^{B_\text{occ}^\alpha} \lambda_{rs} |s(i)\rangle \quad (25)$$

$$F^\beta |r(i)\rangle = \sum_{s=1}^{B_\text{occ}^\beta} \lambda_{rs} |s(i)\rangle \quad (26)$$

where F^α is the one-electron Fock operator for the α -electrons and F^β is the one-electron Fock operator for the β -electrons. The Fock operator may be expanded as

$$F^\alpha = T + V + \sum_{s=1}^{B_\text{occ}^\alpha} (J_s - K_s^\alpha) + \sum_{s=1}^{B_\text{occ}^\beta} J_s^\beta \quad (27)$$

$$F^\beta = T + V + \sum_{s=1}^{B_{occ}^\beta} (J_s - K_s^\beta) + \sum_{s=1}^{B_{occ}^\alpha} J_s^\alpha \quad (28)$$

and

$$T | r(i) \rangle = -\frac{1}{2} \nabla_i^2 | r(i) \rangle \quad (29)$$

$$V | r(i) \rangle = - \sum_{\mu} \frac{Z_{\mu}}{r_{\mu i}} | r(i) \rangle \quad (30)$$

$$J_s | r(i) \rangle = \langle s(j) | \frac{1}{r_{ij}} | s(j) r(i) \rangle \quad (31)$$

$$K_s | r(i) \rangle = \langle s(j) | \frac{1}{r_{ij}} | r(j) s(i) \rangle . \quad (32)$$

A unitary transformation of the Hartree-Fock equations can be carried out to bring the matrix of Lagrangian multipliers into diagonal form without affecting the operators F^α or F^β

$$F^\alpha | r(i) \rangle = \lambda_r^\alpha | r(i) \rangle \quad (33)$$

$$F^\beta | r(i) \rangle = \lambda_r^\beta | r(i) \rangle . \quad (34)$$

The molecular orbitals are eigenfunctions of the Fock operator, and the eigenvalues are

$$\lambda_r^\alpha = T_r^\alpha + V_r^\alpha + \sum_{s=1}^{B_{occ}^\alpha} (J_{rs} - K_{rs}^\alpha) + \sum_{s=1}^{B_{occ}^\beta} J_{rs}^\beta \quad (35)$$

$$\lambda_r^\beta = T_r^\beta + V_r^\beta + \sum_{s=1}^{B_{occ}^\beta} (J_{rs} - K_{rs}^\beta) + \sum_{s=1}^{B_{occ}^\alpha} J_{rs}^\alpha . \quad (36)$$

The electronic energy is then expressed as

$$\begin{aligned}
 E = & \sum_{r=1}^{B_{occ}^{\alpha}} \lambda_{rr}^{\alpha} + \sum_{r=1}^{B_{occ}^{\beta}} \lambda_{rr}^{\beta} - \sum_{r,s=1}^{B_{occ}^{\alpha}} (J_{rs} - K_{rs}^{\alpha}) - \\
 & \sum_{r,s=1}^{B_{occ}^{\beta}} (J_{rs} - K_{rs}^{\beta}) + \sum_{s=1}^{B_{occ}^{\alpha}} J_s^{\alpha} + \sum_{s=1}^{B_{occ}^{\beta}} J_s^{\beta}. \quad (37)
 \end{aligned}$$

When the LCAO molecular orbitals are used, two sets of coupled linear equations result,

$$\sum_{n=1}^{B_{occ}^{\alpha}} (F_{mn}^{\alpha} - \lambda_r^{\alpha} S_{mn}) c_{nk}^{\alpha} = 0 \quad (38)$$

$$\sum_{n=1}^{B_{occ}^{\beta}} (F_{mn}^{\beta} - \lambda_r^{\beta} S_{mn}) c_{nk}^{\beta} = 0. \quad (39)$$

Equations 38 and 39 are solved iteratively to obtain the SCF molecular orbital coefficients. The two Fock Hamiltonian matrices have elements given by

$$\begin{aligned}
 F_{mn}^{\alpha} = & T_{mn} + V_{mn} + \sum_{p,q} [P_{pq} \langle m(i) p(j) | \frac{1}{r_{ij}} | n(i) q(j) \rangle \\
 & - P_{pq}^{\alpha} \langle m(i) p(j) | \frac{1}{r_{ij}} | q(i) n(j) \rangle]. \quad (40)
 \end{aligned}$$

$$F_{mn}^{\beta} = T_{mn} + V_{mn} + \sum_{p,q} [P_{pq} \langle m(i) p(j) | \frac{1}{r_{ij}} | n(i) q(j) \rangle]$$

$$- \frac{P^\beta}{pq} \langle m(i) p(j) | \frac{1}{r_{ij}} | q(i) n(j) \rangle] . \quad (41)$$

The molecular orbital expansion coefficients are obtained by using a self-consistent field (SCF) procedure in the framework of the Hartree-Fock theory. An initial set of basis functions is assumed and the required integrals are calculated. The two Fock matrices are then constructed, one for α -electrons and one for β -electrons, and diagonalized yielding a new set of expansion coefficients. The electronic energy is then calculated using a new set of coefficients; if it differs from the energy using the previous set of coefficients by an amount greater than an accuracy threshold, the new coefficients are used to form a new Fock matrix in an iterative process. The procedure is repeated until the accuracy threshold is satisfied; i.e., self-consistency has been achieved.

VII. SPIN PROJECTION OPERATORS AND THE UNRESTRICTED HARTREE-FOCK WAVEFUNCTION

Unrestricted Hartree-Fock (UHF) theory⁸ is the simplest available method that allows the orbital rearrangement that is necessary to calculate excitation and ionization energies.⁹ However, the open-shell wavefunctions that result from application of the UHF theory are not pure spin states. It is therefore necessary to obtain pure spin states by using Löwdin's¹ spin projection operators. Harriman and coworkers¹⁰ have provided the basic equations for calculating the reduced one- and two-particle density matrices. Corrections to those expressions were later noted by Phillips and Schug.¹¹ The equations will be briefly reviewed, retaining the notation of the latter workers.

The nonrelativistic spin-free Hamiltonian can always be separated into one- and two-electron terms,

$$\mathcal{H} = \sum_i^N [T_i + V_i] + \sum_{i>j}^N \frac{1}{r_{ij}} \quad (42)$$

where N is the number of electrons in the molecule. The electronic energy can therefore be calculated from a knowledge of the first- and second-order charge density matrices. If r_i refers to spatial coordinates of the i^{th} electron, ζ_i the spin coordinates, and x_i the combined space and spin coordinates, then the second-order charge density matrix can be expressed as

$$\Gamma(r_1, r_2; r_1', r_2') = \frac{N!}{2! (N - 2)!} \int \Phi(x_1, x_2, \dots x_N) \times \\ \Phi^*(x_1', x_2', \dots x_N) d\zeta_1 d\zeta_2 dx_3 \dots dx_N \quad (43)$$

where $\Phi(x_1, x_2 \dots x_N)$ is any molecular wavefunction. If an additional integration is performed over the spatial coordinates of the second electron, the first-order charge density matrix results,

$$\gamma(r_1; r_1') = \int_{N-1}^2 \Gamma(r_1, r_2; r_1', r_2) dr_2 . \quad (44)$$

The expressions for spin projection are simplified if the charge density matrices are expressed in terms of the natural orbitals, $\{\phi\}$, which result when the density matrices are diagonalized. Letting B denote the number of basis functions, the first-order matrix is

$$\gamma(r_1; r_1') = \sum_{r=1}^B \gamma_r \phi_r(r_1) \phi_r^*(r_1') \quad (45)$$

while the second-order matrix is

$$\Gamma(r_1, r_2; r_1', r_2') = \sum_{r,s,t,v=1}^B \Gamma_{rstv} \phi_r(r_1) \phi_s(r_2) \times \\ \phi_t^*(r_1') \phi_v^*(r_2') . \quad (46)$$

The energy, in terms of the natural orbitals, is then expressed as

$$E = \sum_{r=1}^B \gamma_r \langle \phi_r | T_i + V_i | \phi_r \rangle + \\ \sum_{r,s,t,v=1}^B \Gamma_{rstv} \langle \phi_r \phi_s | \frac{1}{r_{ij}} | \phi_t \phi_v \rangle . \quad (47)$$

The coefficients that describe the charge density matrices in terms of the natural orbitals are γ_r and Γ_{rstv} . More specificity of the coefficients is gained by using the superscripts u and p to denote the unprojected and projected states, respectively.

The energy expression is most conveniently written in terms of natural orbitals, because only the numerical values of the coefficients multiplying the integrals, γ_r and Γ_{rstv} , change between the projected and unprojected states. The integrals over the natural orbitals remain constant.

A set of orbitals that facilitates the calculation of the numerical values of the coefficients multiplying the one- and two-electron natural orbitals is the set of corresponding orbitals, first introduced by Amos and Hall.¹² The alpha corresponding orbitals, {a}, are the eigenvectors of the product of the alpha and beta first-order charge density matrices, $P^\alpha P^\beta P^\alpha$, while the beta corresponding orbitals, {b}, are the eigenvectors of $P^\beta P^\alpha P^\beta$. The nonzero eigenvalues of the product matrices are identical and equal to the squares of the overlap integrals of the corresponding orbitals, d_r^2 . The overlap matrix, d, between the alpha and beta corresponding orbitals, is also in diagonal form,

$$\langle a_r | b_s \rangle = \langle a_s | b_r \rangle = d_r \delta_{rs} \quad (48)$$

$$\langle a_r | a_s \rangle = \langle b_r | b_s \rangle = \delta_{rs} \quad (49)$$

where δ_{rs} is the Kronecker delta.

The coefficients describing the first- and second-order charge density matrices are defined based on the classification of

the natural orbitals of charge. For a system with N^α alpha and N^β beta electrons, where N^α is greater than or equal to N^β , and where ordering occurs such that $\gamma_r^u > \gamma_{r+1}^u$, there are D doubly occupied orbitals. In this case, the unprojected and projected coefficients are equal,

$$\gamma_p^u = 2 = 1 + d_p \quad (p = 1, 2, \dots, D) \quad (50)$$

$$\gamma_p^p = 2 = 1 + d_p \quad (p = 1, 2, \dots, D) \quad (51)$$

This type of orbital always occurs when the number of basis functions, B, is less than the number of electrons, N, and may also occur other times.

The second type of natural orbitals, the i and i' set, has paired members, the sum of whose occupation numbers equals two in the unprojected space,

$$\gamma_i^u + \gamma_{i'}^u = 2. \quad (52)$$

The values of the γ_i and $\gamma_{i'}$ coefficients are

$$\gamma_i^u = 1 + d_i \quad (i = D+1, D+2, \dots) \quad (53)$$

$$\gamma_i^p = 1 + d_i \omega_i \quad (54)$$

$$\gamma_{i'}^u = \gamma_{N-i+1}^u = 1 - d_i \quad (55)$$

$$\gamma_{i'}^p = \gamma_{N-i+1}^p = 1 - d_i \omega_i ; \quad (56)$$

evaluation of the ω_i has been made by Harriman.¹⁰

Another type of natural orbital occurring in the space of singly occupied orbitals has no pairing properties. The coeffi-

cients in both the projected and unprojected states are equal,

$$\gamma_{v+j}^u = \gamma_{v+j}^p = 1 \quad (j = 1, 2, \dots 2m) \quad (57)$$

where $2m$ is equal to the difference between the number of alpha and beta electrons, $N^\alpha - N^\beta$.

The remaining orbitals, also having pairing properties, are empty; their occupation numbers are zero,

$$\gamma_{N+r}^u = \gamma_{N+r}^p = 0 \quad (r = 1, 2, \dots B). \quad (58)$$

Relationships between the natural orbitals of charge and the corresponding orbitals are necessary in order to test the consistency of the phases of both sets of orbitals and calculate the weighting factors for the projected spin states. The two sets of orbitals are related by

$$\phi_p = a_p = b_p \quad (p = 1, 2, \dots D) \quad (59)$$

$$\phi_i = [2(1 + d_i)]^{-1/2} (a_i + b_i) \quad (i = D+1, D+2, \dots N^\beta) \quad (60)$$

$$\phi_{i'} = \phi_{N-i+1} = [2(1 - d_i)]^{-1/2} (a_i - b_i) \quad (61)$$

$$\phi_{v+j} = a_{v+j} \quad (j = 1, 2, \dots 2m) . \quad (62)$$

The $N+r$ orbitals ($r = 1, 2, \dots B-N$) are undefined because no corresponding orbitals are defined in the empty space.

The inversion of equations 60 and 61 produce

$$a_i = t_i \phi_i + u_i \phi_{i'} \quad (i = D+1, D+2, \dots N^\beta) \quad (63)$$

$$b_i = t_i \phi_i - u_i \phi_{i'} \quad (64)$$

where

$$t_i = [(1 + d_i)/2]^{1/2} \quad (65)$$

$$u_i = [(1 - d_i)/2]^{1/2}. \quad (66)$$

The coefficients Γ_{rstv} that multiply the two-electron integrals occur in twenty distinct combinations of r , s , t , and v . Further combinations are obtained through the use of the permutation relationship

$$\Gamma_{rstv} = \Gamma_{tyrs} = \Gamma_{sryt} = \Gamma_{vtsr} \quad (67)$$

Since the expressions are quite complicated, the reader is referred to the paper by Phillips and Schug¹¹ for a listing of the equations. It should be noted that two Γ_{rstv} terms were in error, the Γ_{tutu} and Γ_{tuut} terms. The correct values for the coefficients are

$$\Gamma_{tutu} = 1/2 \quad (68)$$

$$\Gamma_{tuut} = -1/2 \quad (69)$$

It is important to note that the expressions were formulated by assuming that t_i and u_i are always greater than or equal to zero.

The spin density matrix, described by the difference between the α - and β -charge density matrices,

$$P^z = P^\alpha - P^\beta, \quad (70)$$

can also be used to obtain relationships between the projected and unprojected spin states. The natural orbitals of spin, $\{\phi^z\}$, diagonalize this matrix,

$$P^z(r_1; r_1') = \sum_{r=D+1}^N \lambda_r \phi_r^z(r_1) \phi_r^{z*}(r_1'). \quad (71)$$

The eigenvalues of the natural orbitals of spin, λ_k , are related

to the one-electron coefficients, γ_k , by

$$\lambda_i = (1 - d_i^2)^{1/2} = (\gamma_i \gamma_{i'})^{1/2} \quad (i = D+1, D+2, \dots N^\beta) \quad (72)$$

$$\lambda_{i'} = - (1 - d_{i'}^2)^{1/2} = - (\gamma_i \gamma_{i'})^{1/2} \quad (73)$$

$$\lambda_{j+v} = 1 \quad (j = 1, 2, \dots 2m) \quad (74)$$

and the eigenfunctions are related to the natural orbitals of charge by

$$\phi_i^z = (\phi_i + \phi_{i'})/\sqrt{2} \quad (i = D+1, D+2, \dots N^\beta) \quad (75)$$

$$\phi_{i'}^z = (\phi_i - \phi_{i'})/\sqrt{2} \quad (76)$$

$$\phi_{v+j}^z = \phi_{v+j} \quad (j = 1, 2, \dots 2m) . \quad (77)$$

The UHF wavefunction is not an eigenfunction of pure spin multiplicity. However, with the use of the spin projection operators presented above, the single determinant wavefunction of mixed multiplicity can be separated into a linear combination of wavefunctions with pure spin multiplicity,

$$\psi^u = \sum_{s=(N^\alpha-N^\beta)/2}^{(N^\alpha+N^\beta)/2} \omega_s \psi_s^p . \quad (78)$$

The work presented below is a series of applications of the spin projection techniques at various levels of approximate wavefunctions.

VIII. EXCITED ELECTRONIC STATES OF ALTERNANT PI-ELECTRON SYSTEMS

The Pariser-Pople-Parr (PPP) pi-electron approximations,¹³ applicable only to planar molecules, have been used previously with singly excited configurational interaction (CI) to calculate electronic spectra. The basic assumption in the PPP approximations is that the σ , or those orbitals in the molecular plane, and π orbitals, those orbitals perpendicular to the molecular plane, have no Hamiltonian matrix elements in common. The validity of this assumption is shown using group theory. The σ orbitals are symmetric with respect to reflections in the molecular plane while the π orbitals are antisymmetric. Since the Hamiltonian is a symmetric operator, no matrix elements (or combinations) between σ and π orbitals exist.

A CI calculation is quite different from a spin projection calculation.¹⁴ The calculation begins with the determination of the ground state wavefunction,

$$\psi_k = A | \Phi_1(1)\Phi_1(2) \dots \Phi_r(N) | . \quad (79)$$

A trial function for configuration interaction is then written as a linear combination of wavefunctions of the above for various configurations

$$\Psi = C_1 \psi_1 + C_2 \psi_2 + \dots + C_m \psi_m \quad (80)$$

where m is the number of configurations. The coefficients of the

atomic orbitals are held constant. The energy of Ψ is minimized with respect to all C_k by solving the secular equation

$$|\mathcal{H}_{mn} - \delta_{mn} E| = 0 \quad (81)$$

where each \mathcal{H}_{mn} is a Hamiltonian matrix element between configurations. The resultant multi-determinant wavefunction has pure spin multiplicity and spatial symmetry; the eigenvalues of the wavefunction correspond to excitation energies from the ground to the excited state.

The CI method was used by Pariser¹⁵ to calculate the electronic spectra of polyacenes and alternant hydrocarbons using the PPP pi-electron approximations. It was also desirable to apply spin projection techniques to pi-electron systems to compare the results from spin projection with both experimental and CI data. The molecules chosen for study were naphthalene, anthracene, naphthacene and pentacene since the symmetries of the transitions had been previously assigned to portions of the experimental spectra.

The PPP approximations include several empirical parameters that are used as substitutes for the rigorous expressions in the Hartree-Fock equations. They are worthy of review at this time.¹⁴

The greatest simplification of the Hartree-Fock equations occurs when the total zero differential overlap (TZDO) approximation,¹⁶

$$\phi_r \phi_s = |\phi_r|^2 \delta_{rs}, \quad (82)$$

is employed. This approximation leads to

$$\langle r(i) s(j) | \frac{1}{r_{ij}} | t(i) u(j) \rangle = \gamma_{rs} \delta_{rt} \delta_{su}. \quad (83)$$

A further simplification is obtained by setting

$$\langle r(i) | T + V | s(i) \rangle = 0 \quad (84)$$

if r and s are neither on the same atom nor near-neighbor atoms.

Using this approximation, the remaining core Hamiltonian matrix elements are

$$(T + V)_{rr} = -Z_r I_r + \sum_{s \neq r} \langle r(i) | v_{si}^{Zs}^+ | r(i) \rangle \quad (85)$$

$$(T + V)_{rs} = \beta_{rs} \quad (86)$$

where the kinetic energy is approximated by a product of the core charge, Z , and the ionization potential, I . The potential energy is approximated as an integral whose operator is $v_{si}^{Zs}^+$, the potential of an atom which has lost its pi-electrons. Using the approximation of Goeppert-Mayer and Sklar,¹⁷ the one-electron potential energy operator is

$$v_{sj}^+ = v_{sj} - Z \langle s(i) | \frac{1}{r_{ij}} | s(i) \rangle \quad (87)$$

where v_{sj} is the potential at atom j from a neutral atom s and is neglected; the integral represents the Coulomb potential due to a pi-electron on the atom s . The off-diagonal core Hamiltonian matrix elements are set equal to an empirical parameter, β_{rs} . The diagonal elements further reduce to

$$(T + V)_{rr} = -Z_r I_r - \sum_{s \neq r} Z_s \gamma_{rs}. \quad (88)$$

Using the above approximations including TZDO, the Hartree-Fock matrix elements are

$$\begin{aligned} F_{rr}^{\alpha} &= -Z_r I_r - P_{rr}^{\alpha} \gamma_{rr} - \sum_{s \neq r} Z_s \gamma_{rs} + \\ &\quad \sum_s P_{ss}^{\alpha} \gamma_{rs} + \sum_s P_{ss}^{\beta} \gamma_{rs} \end{aligned} \quad (89)$$

$$\begin{aligned} F_{rr}^{\beta} &= -Z_r I_r - P_{rr}^{\beta} \gamma_{rr} - \sum_{s \neq r} Z_s \gamma_{rs} + \\ &\quad \sum_s P_{ss}^{\beta} \gamma_{rs} + \sum_s P_{ss}^{\alpha} \gamma_{rs} \end{aligned} \quad (90)$$

$$F_{rs}^{\alpha} = \beta_{rs} - P_{rs}^{\alpha} \gamma_{rs} \quad (91)$$

$$F_{rs}^{\beta} = \beta_{rs} - P_{rs}^{\beta} \gamma_{rs} \quad (92)$$

The pi-electronic energy then is

$$\begin{aligned} E_{\pi} &= - \sum_r P_{rr} (I_r + \sum_{s \neq r} Z_s \gamma_{rs}) + \sum_r \sum_{s \neq r} P_{rs} \beta_{rs} \\ &\quad + \sum_r P_{rr}^{\alpha} P_{rr}^{\beta} \gamma_{rr} + \frac{1}{2} \sum_{s \neq r} (P_{rr} P_{ss} - \\ &\quad P_{rs}^{\alpha} P_{rs}^{\alpha} - P_{rs}^{\beta} P_{rs}^{\beta}) \gamma_{rs} \end{aligned} \quad (93)$$

where P_{rs} is a charge density matrix element. The two-center two-electron repulsion integrals, γ_{rs} , can be calculated using a variety of approximations, the Mataga-Nishimoto,¹⁸ the Pariser-Parr,¹⁹

the Nishimoto,²⁰ and the modified Mataga²¹ approximations. All are dependent on the distances between atoms, r_{rs} .

A wavefunction of a specific spatial symmetry can be obtained through a nonaufbau excitation. That is, the molecular orbitals are occupied so that the ground state electronic energy is not obtained, and the symmetries of the occupied alpha molecular orbitals are not equal to the symmetries of the occupied beta molecular orbitals. The occupation is reflected in the formation of the alpha and beta density matrices,

$$P_{rs}^{\alpha} = \sum_{k=1}^{B_{\alpha}} c_{rk}^{\alpha} c_{sk}^{\alpha} f_k^{\alpha} \quad (94)$$

$$P_{rs}^{\beta} = \sum_{k=1}^{B_{\beta}} c_{rk}^{\beta} c_{sk}^{\beta} f_k^{\beta} \quad (95)$$

where the f_k 's are arrays of occupation numbers for the orbitals. Using the equations of Brickstock and Pople, equations 89 through 92, the molecular orbitals are iterated in an SCF procedure until the energy convergence criterion is attained. Spin projection is then performed on the UHF wavefunction using the equations outlined in the previous chapter. A computer program incorporating the semi-empirical PPP pi-electron approximations with spin projection was developed and submitted to the Quantum Chemistry Program Exchange.²²

The calculation of the electronic spectra of naphthalene, anthracene, naphthacene and pentacene employed the theory outlined

above. All fused benzene rings were taken to be regular hexagons with sides of length 1.4 Angstroms. The off-diagonal core Hamiltonian matrix elements, β_{rs} , were empirically set equal to -2.395 electron volts.²³ The one-center electron repulsion integrals, γ_{rr} , were taken to be 11.13 electron volts and the two-center repulsion integrals were evaluated by the Mataga-Nishimoto approximation,¹⁸

$$\gamma_{rs} = \frac{14.397}{\frac{28.794}{\gamma_{rr} + \gamma_{ss}} + r_{rs}} . \quad (96)$$

The group theoretical notation is that suggested by IUPAC,²⁴ so that the molecules lie in the yz plane, the short molecular axis being in the z direction and the long axis, y . Since all molecules studied were members of the D_{2h} point group, no symmetry degenerate states existed. Both the spin projection and CI calculations employed the PPP approximations. The CI calculations that were done for comparison with the projected UHF calculations included all singly excited configurations.

The wavelengths for the ground to excited state transitions for naphthalene, anthracene, naphthacene and pentacene are listed in Tables I, II, III and IV, respectively. They are tabulated with the assumption that the ground state wavefunction is a closed shell. Both $m=0$ and $m=1$ calculations were performed for the purposes of comparison of the internal consistency of the spin projection technique; the $m=0$ state refers to an open shell system with an equal number of alpha and beta electrons while the $m=1$ system has two more alpha than beta electrons.

TABLE I

WAVELENGTHS (Å) FOR THE GROUND TO EXCITED
STATE TRANSITIONS IN NAPHTHALENE

<u>System</u>	<u>Calculated</u>			
	<u>Excited State</u>	<u>Projected UHF</u>	<u>CI</u>	<u>Experimental</u>
m=0	$^1\text{B}_{2u}$	3137	2991	3106 ^a
	$^1\text{B}_{1u}$	2724	2765	2757 ^b
	$^1\text{B}_{3g}$	2099	2115	
	$^3\text{B}_{2u}$	3319	3604	3353 ^b
	$^3\text{B}_{1u}$	5006	7264	4963 ^b
	$^3\text{B}_{3g}$	2708	4264	
m=1	$^3\text{B}_{2u}$	3148		3353 ^b
	$^3\text{B}_{1u}$	6720		4963 ^b
	$^3\text{B}_{3g}$	2924		

^aJ. R. Platt, J. Chem. Phys. 18, 1168 (1950).

^bR. G. Parr, "Quantum Theory of Molecular Electronic Structure", W. A. Benjamin Book Co., New York, 1964.

TABLE II

WAVELENGTHS (\AA) FOR THE GROUND TO EXCITED
STATE TRANSITIONS IN ANTHRACENE

<u>System</u>	<u>Calculated</u>			
	<u>Excited State</u>	<u>Projected UHF</u>	<u>CI</u>	<u>Experimental</u>
$m=0$	$^1\text{B}_{2u}$	3713	3342	3745 ^a
	$^1\text{B}_{1u}$	3493	3568	3649 ^b
	$^1\text{B}_{3g}$	2887	2630	
	$^3\text{B}_{2u}$	3711	3876	
	$^3\text{B}_{1u}$	7921	11488	7298 ^b
	$^3\text{B}_{3g}$	3286	5468	
$m=1$	$^3\text{B}_{2u}$	3473		
	$^3\text{B}_{1u}$	13393		7298 ^b
	$^3\text{B}_{3g}$	3673		

^aJ. R. Platt, J. Chem. Phys. 18, 1168 (1950).

^bR. G. Parr, "Quantum Theory of Molecular Electronic Structure", W. A. Benjamin Book Co., New York, 1964.

TABLE III

WAVELENGTHS (\AA) FOR THE GROUND TO EXCITED STATE TRANSITIONS IN NAPHTHACENE

<u>System</u>	<u>Calculated</u>			
	<u>Excited State</u>	<u>Projected UHF</u>	<u>CI</u>	<u>Experimental</u>
m=0	$^1\text{B}_{2u}$	4163	3568	3922 ^a
	$^1\text{B}_{1u}$	4239	4343	4278 ^b
	$^1\text{B}_{3g}$	3402	3182	
	$^3\text{B}_{2u}$	3969	3899	
	$^3\text{B}_{1u}$	11802	18859	10340 ^b
	$^3\text{B}_{3g}$	4121	7434	
m=1	$^3\text{B}_{2u}$	3582		
	$^3\text{B}_{1u}$	28788		10340 ^b
	$^3\text{B}_{3g}$	4901		

^aJ. R. Platt, J. Chem. Phys. 18, 1168 (1950).

^bR. G. Parr, "Quantum Theory of Molecular Electronic Structure", W. A. Benjamin Book Co., New York, 1964.

TABLE IV

WAVELENGTHS (Å) FOR THE GROUND TO EXCITED
STATE TRANSITIONS IN PENTACENE

<u>System</u>	<u>Calculated</u>			
	<u>Excited State</u>	<u>Projected UHF</u>	<u>CI</u>	<u>Experimental</u>
m=0	$^1\text{B}_{2u}$	4471	3711	4167 ^a
	$^1\text{B}_{1u}$	4915	4969	5755 ^b
	$^1\text{B}_{3g}$	4086	3696	
	$^3\text{B}_{2u}$	4130	3899	
	$^3\text{B}_{1u}$	16934	29078	
	$^3\text{B}_{3g}$	5002	8622	
m=1	$^3\text{B}_{2u}$	5191		
	$^3\text{B}_{1u}$	c		
	$^3\text{B}_{3g}$	6303		

^aJ. R. Platt, J. Chem. Phys. 18, 1168 (1950).

^bE. Clar, "The Aromatic Sextet," Wiley Book Co., London, 1972.

^cTriplet energy was lower than ground state RHF energy.

In all cases, the unprojected states were composed of almost 50 percent singlet and 50 percent triplet character. The weights of the states with multiplicity five were about 0.3 percent for B_{1u} symmetry, about one percent for B_{3g} symmetry and about five percent for B_{2u} symmetry. Much smaller, though nonvanishing contributions were also obtained for states of multiplicity seven for the larger molecules.

In most cases, there was reasonable agreement between the CI and the projected UHF results. The CI calculation generally produced appreciably lower energies for the triplet states than did the UHF treatment. However, for those cases where experimental data were available, the UHF results were in somewhat better agreement than the CI results.

A comparison of the wavelengths for the excitation from the ground states to the triplets between the $m=0$ and $m=1$ calculations is rather interesting. For the B_{2u} triplets, the $m=0$ calculations provided lower energy states than the $m=1$ calculations with the exception of pentacene, the largest molecule. For the B_{3g} and B_{1u} triplets, lower energies were obtained in all cases from the $m=1$ calculations. The difference between the $m=0$ and $m=1$ energies increased with the size of the molecule and was much greater for B_{1u} symmetry than for B_{3g} . The result of this was that the excitation energies for the ground state to the $^3B_{1u}$ states obtained from the $m=1$ calculation were much too small in comparison with available experimental data. The case of pentacene is extreme in

that the $^3\text{B}_{1u}$ ($m=1$) state was lower in energy than the closed shell ground state. This result implies that the ground state wavefunction may be an open rather than a closed shell.

Hartree-Fock instabilities are defined as cases where the ground state wavefunction determined using the UHF equations is an open shell that gives a lower energy than the closed shell.

Koutecký³⁰ showed that Hartree-Fock instabilities occurred for molecules as small as benzene and were a consequence of the parameterization used in the PPP calculation. He cites examples of the occurrence of open shell ground states in naphthalene, anthracene and pentacene when the Mataga parameterization is employed.

Koutecký's parameterization was slightly different from that employed in this work with $\beta = -2.318$ electron volts and $\gamma_{ii} = 10.84$ electron volts.

In an attempt to generate open shell ground states for the molecules under study, the SCF portion of the molecular orbital calculation was rewritten so that the alpha and beta molecular orbitals were calculated sequentially instead of concurrently. That is, in a usual SCF calculation, the alpha- and beta-electron Fock matrices are formed using the same set of starting orbitals and diagonalized to produce a new set of orbitals. Since the alpha- and beta-electron Fock matrices remain the same, the alpha and beta molecular orbitals stay the same. In the modified SCF calculation, the starting orbitals were used to form the alpha-electron Fock matrix, and the matrix was diagonalized to produce a new set

of alpha molecular orbitals; the new alpha orbitals were then used to form the beta-electron Fock matrix. By iterating back and forth to allow the alpha- and beta-electron Fock matrices to be different, it was hoped that sufficient differences would be introduced to produce open shell ground state molecular orbitals.

This procedure led to an open shell ground state for pentacene but closed shell solutions for naphthalene, anthracene and naphthacene. The projected energies and weighting factors for the open shell ground state of pentacene are listed in Table V while the electronic spectrum recalculated using the open shell ground state is presented in Table VI. The contributions to the open shell unprojected ground state energy by multiplicities greater than one are quite appreciable; also, the projected ground state energy is below the troublesome triplet energy obtained from the $m=1$ calculation.

The lack of open shell ground states in naphthalene, anthracene and naphthacene does not imply that such a solution does not exist but rather that the initial perturbation was not sufficient to produce an open shell solution.

The disparities between the $m=0$ and $m=1$ results can only be a consequence of the differences in the effective flexibility of the basis sets.²⁵ Since the $m=0$ results compared favorably with available experimental data on the whole, it must be concluded that the $m=0$ UHF basis set contained flexibility comparable to that of the closed shell calculation. The effective flexibility of the basis for the $m=1$ UHF calculations increased with molecular size

TABLE V

PROJECTED ELECTRONIC ENERGIES AND WEIGHTING
 FACTORS FOR THE OPEN SHELL GROUND
 STATE IN PENTACENE

<u>Multiplicity</u>	<u>Energy(eV)</u>	<u>Weight</u>
1	-932.54926	2.99489×10^{-1}
3	-931.48598	4.50627×10^{-1}
5	-929.41985	2.00174×10^{-1}
7	-926.66096	4.37340×10^{-2}
9	-923.41642	5.51858×10^{-3}
11	-919.78281	4.34172×10^{-4}
13	-915.79493	2.20764×10^{-5}
15	-911.45288	7.32055×10^{-7}
17	-906.73785	1.55937×10^{-8}
19	-901.62669	2.03853×10^{-10}
21	-896.11148	1.47624×10^{-12}

TABLE VI

WAVELENGTHS (\AA) FOR OPEN SHELL GROUND TO EXCITED
STATE TRANSITIONS IN PENTACENE

<u>System</u>	<u>Calculated</u>			
	<u>Excited State</u>	<u>Projected UHF</u>	<u>CI</u>	<u>Experimental</u>
$m=0$	$^1\text{B}_{2u}$	2162	3711	4167 ^a
	$^1\text{B}_{1u}$	2261	4969	5755 ^b
	$^1\text{B}_{3g}$	2068	3696	
	$^3\text{B}_{2u}$	2079	3899	
	$^3\text{B}_{1u}$	3356	29078	
	$^3\text{B}_{3g}$	2279	8622	
$m=1$	$^3\text{B}_{2u}$	1963		
	$^3\text{B}_{1u}$	5145		
	$^3\text{B}_{3g}$	2515		

^aJ. R. Platt, J. Chem. Phys. 18, 1168 (1950).

^bE. Clar, "The Aromatic Sextet", Wiley Book Co., London, 1972.

and was different for different spatial symmetries, increasing in the order $B_{3g} < B_{2u} < B_{1u}$. This order can be rationalized by comparing the available virtual orbitals for naphthalene in the three calculations. However, all observed variations cannot be rationalized without a considerable amount of additional study.

Several unexpected problems arose in the spin projection calculations. Although the resolution of these difficulties was relatively easily accomplished, the sources of the problems are worthy of some explanation and elaboration.

The first problem arose in trying to obtain wavefunctions with symmetries other than the ground state symmetry, A_g . In general, one nonaufbau excitation on the first SCF iteration is sufficient to retain the desired spatial symmetry of the wavefunction. However, since the orbital symmetries reordered and multiple excitations in the density matrices were required to retain the desired symmetry of the total wavefunction, an orbital symmetry search pattern was established for subsequent iterations. The search pattern determined the symmetries of every alpha and beta orbital. The orbitals were occupied based on a preselected list of the number of orbitals of each symmetry type in the total wavefunction. The total density matrix was then calculated using equations 94 and 95. The search pattern was repeated until self-consistency was achieved.

Multiple problems with degeneracies occurred during the calculations and are described elsewhere.²⁶

Based on the results presented above, the projected UHF

method is a viable alternative to CI for the calculation of excited electronic states provided that the UHF and closed shell restricted Hartree-Fock (RHF) treatments employ basis sets of comparable flexibility. It is indicated that the $m=0$ UHF calculation satisfies this requirement in most cases.

IX. ALL-VALENCE ELECTRON CALCULATIONS

The semi-empirical all-valence electron calculations as set forth by Pople and Beveridge⁶ employ either the complete neglect of differential overlap (CNDO) or the intermediate neglect of differential overlap (INDO) approximations. The difference between the CNDO and INDO methods lies in the manner in which the one-center two-electron repulsion integrals are treated. The CNDO approximations were originally parameterized for the first, second and third row atoms on the periodic table, hydrogen through chlorine, while the INDO segment included hydrogen through fluorine.

Both the INDO and CNDO parameterizations have been quite useful in the past⁶ in determining molecular structure, particularly equilibrium geometries of organic molecules, and properties such as dipole moments.

The work described below consists of three distinct segments: the application of the INDO approximations to determine the equilibrium geometry of monohomocyclooctatetraene anion radical (MHCOT); the inclusion of the spin projection in the INDO computer program; and, the extension of the INDO parameterizations to include the third row atoms, sodium through chlorine.

It is advantageous to review the INDO approximations at this time.

The diagonal core Hamiltonian matrix elements,

$$(T + V)_{rr} = \langle r(i) | -\frac{1}{2} v_i^2 - v_\mu | r(i) \rangle -$$

$$\sum_{v \neq \mu} \langle r(i) | v_v | r(i) \rangle , \quad (97)$$

are separated into contributions due to the interaction of the orbital $\langle r(i) |$ with the nucleus μ on which it resides and interactions with the other nuclei, v , in the molecule. The first integral, which is essentially an atomic term, is approximated semi-empirically by U_{rr} , an average of the ionization potential, I_r , and the electron affinity, A_r , and a term describing the number of valence electrons on the nucleus μ ,

$$\langle r(i) | -\frac{1}{2} v_i^2 - v_\mu | r(i) \rangle = U_{rr} \quad (98)$$

$$U_{rr} = -\frac{1}{2} (I_r + A_r) - (Z_\mu - \frac{1}{2}) \gamma_{\mu\mu} \quad (99)$$

where $\gamma_{\mu\mu}$ is a one-center two-electron coulomb integral of the form

$$\langle r(i) r(j) | \frac{1}{r_{ij}} | r(i) r(j) \rangle . \quad (100)$$

The second integral is approximated by

$$v_{\mu v} = \langle r(i) | v_v | r(i) \rangle = Z_v \gamma_{\mu v} . \quad (101)$$

These integrals are assumed to be the same for all orbitals $|r(i)\rangle$ on the atom μ .

The off-diagonal core Hamiltonian matrix elements are approximated by

$$(T + V)_{rs} = \beta_{\mu\nu}^0 S_{rs} \quad (102)$$

where S_{rs} is the overlap integral of equation 24 and $\beta_{\mu\nu}^0$ is composed

of empirical atomic bonding parameters of the form

$$\beta_{\mu\nu}^0 = \frac{1}{2} (\beta_{\mu}^0 + \beta_{\nu}^0) . \quad (103)$$

Orbitals r and s are required to be on different atoms, μ and ν .

The two-electron integrals are approximated using the zero differential overlap (ZDO) approximation,

$$\langle r(i) s(j) | \frac{1}{r_{ij}} | t(i) v(j) \rangle = \gamma_{rs} \delta_{rt} \delta_{sv} , \quad (104)$$

when r and s are on different atoms. When orbitals r and s are on the same atom, integrals of the form

$$\langle r(i) r(j) | \frac{1}{r_{ij}} | r(i) r(j) \rangle \quad (105)$$

$$\langle r(i) r(j) | \frac{1}{r_{ij}} | s(i) s(j) \rangle \quad (106)$$

$$\langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle \quad (107)$$

have nonvanishing values and are evaluated semi-empirically using Slater-Condon parameters.³¹ Other one-center two-electron integrals vanish by symmetry; one-center integrals involving more than two orbitals are neglected.

The basis set used for the INDO calculation contains pure s and p atomic orbitals (no hybrids). They are Slater type orbitals of the form

$$x_i = A \exp (-\zeta_i r_i) Y_{lm}(\theta, \phi) \quad (108)$$

where ζ_i is the orbital exponent, r_i the distance from the nucleus on which the orbital resides, and $Y_{lm}(\theta, \phi)$ a spherical harmonic.

Using the above approximations, the open shell Fock matrix

elements are

$$\begin{aligned}
 F_{rr}^{\alpha} = & U_{rr} + \sum_{s \text{ on } \mu} [P_{ss} \langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle \\
 & - P_{ss}^{\alpha} \langle r(i) r(j) | \frac{1}{r_{ij}} | s(i) s(j) \rangle] \\
 & + \sum_{v \neq \mu} (P_{vv} - z_v) \gamma_{\mu v}
 \end{aligned} \tag{109}$$

$$\begin{aligned}
 F_{rr}^{\beta} = & U_{rr} + \sum_{s \text{ on } \mu} [P_{ss} \langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle \\
 & - P_{ss}^{\beta} \langle r(i) r(j) | \frac{1}{r_{ij}} | s(i) s(j) \rangle] \\
 & + \sum_{v \neq \mu} (P_{vv} - z_v) \gamma_{\mu v}
 \end{aligned} \tag{110}$$

$$\begin{aligned}
 F_{rs}^{\alpha} = & (2 P_{rs} - P_{rs}^{\alpha}) \langle r(i) r(j) | \frac{1}{r_{ij}} | s(i) s(j) \rangle \\
 & - P_{rs}^{\alpha} \langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle
 \end{aligned} \tag{111}$$

$$\begin{aligned}
 F_{rs}^{\beta} = & (2 P_{rs} - P_{rs}^{\beta}) \langle r(i) r(j) | \frac{1}{r_{ij}} | s(i) s(j) \rangle \\
 & - P_{rs}^{\beta} \langle r(i) s(j) | \frac{1}{r_{ij}} | r(i) s(j) \rangle
 \end{aligned} \tag{112}$$

where the orbital $|r(i)\rangle$ is on atom μ .

The molecular orbital calculation is performed in an SCF procedure similar to that described in the preceding chapter.

Homoconjugation in the Monohomocyclooctatetraene
Anion Radical

The concept of homoconjugation was introduced by Winstein³² to describe the high stability of certain molecules and ions in which conjugation is interrupted in one or more places by aliphatic groups. Winstein, et. al.³³ view this phenomenon as due to delocalization across the interruption through the carbon p-orbitals which are twisted relative to the π -orbitals of the remaining system because of the inserted aliphatic group. For the specific case of methylene insertion, Hehre³⁴ has described how this picture could be rationalized by using the known valence orbitals of the cyclopropane ring.

Various homoaromatic compounds have been studied theoretically using specially-parameterized Hückel and minimum basis set ab initio calculations. The molecules studied were primarily compounds with an even number of pi-electrons including the unsubstituted and substituted cations and anions of bicyclo[3.1.0]-hexene^{35,36} and homotropylium.^{36,37} The compounds were studied both for their formation and rearrangement processes. The Hückel ($4n + 2$) rule for aromaticity can be applied to these compounds. The rule predicts aromaticity for those compounds that have an even number of pi-electrons equal to $(4n + 2)$ where n is an integer; those compounds that contain an even number of electrons not equal to $(4n + 2)$ are predicted to be antiaromatic. No prediction is made for compounds containing an odd number of pi-electrons; apparently homodelocalization through single bonds occurs in such cases.

Monohomocyclooctatetraene anion radical (MHCOT) is a system containing an odd number of pi-electrons and has not been examined theoretically by other workers. However, the formation reaction was studied and the electron spin resonance (ESR) hyperfine coupling constants for MHCOT were measured.^{38,39} No molecular geometry was available, a requirement for a bonding study. It was, therefore, necessary to determine the structure of MHCOT by systematically varying the geometry. The structure was determined by comparing the experimental hyperfine constants with those calculated by using a hypothetical geometry in an INDO calculation.

MHCOT is an eight-membered ring with a methylene group attached to two adjacent carbon atoms in the ring. Two hydrogen atoms, H1 and H8, are bonded to the carbon atoms that join the methylene group to the eight-membered ring (for example, see Figure 1). The ESR data^{38,39} indicate that the anion radical has only a single plane of symmetry which contains the entire methylene group. A number of possible geometries for the eight-membered ring were investigated including a cis-fused chair, a cis-fused boat and a planar ring with the methylene group in the perpendicular plane of symmetry. The boat and chair conformations contained alternant single and double bonds of lengths 1.54 and 1.35 Angstroms (\AA), respectively. In all possible geometries, the angles between the methylene group and the adjacent plane of the eight-membered ring, and between H1 and H8 and the adjacent plane of the ring were varied. Specific details of the INDO calculations are presented elsewhere.⁴⁰

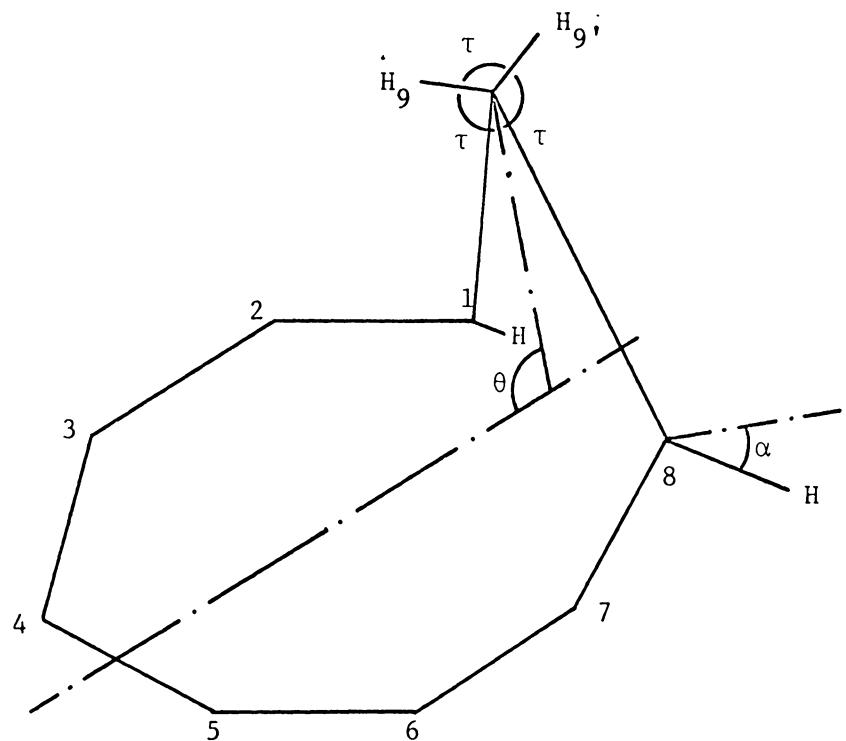


Figure 1. - Geometry of Monohomocyclooctatetraene Anion Radical

The exponents for the Slater orbitals used in both the INDO and spin projection calculations were derived from Burn's rules.⁴¹ That is, the s-orbital exponent for hydrogen was 1.2, the s-orbital exponent for carbon was 1.55, and the p-orbital exponent for carbon was 1.325.

The hyperfine coupling constants, a_H , were obtained directly from the calculated hydrogen 1s orbital spin densities, and did not involve the use of McCennell's relation⁴³ or any variation thereof.

The geometry from the INDO calculations that provided the best comparison between the calculated and experimental coupling constants was a uniform octagonal ring illustrated in Figure 1. The in-plane carbon-carbon bonds had lengths of 1.40 Å while the out-of-plane C₁-C₉ and C₈-C₉ bonds were set at 1.54 Å; all carbon-hydrogen bonds were assumed to be 1.084 Å. The carbon-hydrogen bonds at carbons two through seven were assumed to lie in the plane of the eight-membered ring, bisecting the external carbon-carbon-carbon angles. The hydrogens at carbons one and eight were similarly located, but then the carbon-hydrogen bonds were allowed to tilt below the plane by an angle α . The best comparison with experimental coupling constants was obtained when α was equal to 0° and θ , the angle between the octagonal plane and the cyclopropyl ring, was 83.5°. This angle, θ , is close to those determined by Hehre^{34,35} by ab initio calculations on the bicyclo[3.1.0]-hex-3-en-2-yl cation and the homotropylium cation. It should be noted that, in comparison to other possible geometries, this geometry did not produce the lowest binding energy, E_B, the difference between the

energy of the molecule and the energies of the atoms separated at an infinite distance.

In order to measure the amount of spin contamination in the calculated geometry of MHCOT, it was necessary to obtain a wavefunction of pure spin multiplicity. To this end, a computer program was developed to perform spin projection calculations on CNDO and INDO wavefunctions. The program has been submitted to the Quantum Chemistry Program Exchange.⁴²

Spin projection calculations were performed on the planar uniform octagonal structure of the eight-membered ring of MHCOT. Only the angle that the cyclopropyl group made with the plane of the ring, θ , and the angle that H1 and H8 tilted below the plane of the ring, α , were varied.

The best fit between the projected hyperfine coupling constants and experiment occurred when $\theta = 76.7^\circ$ and $\alpha = 0^\circ$. This geometry, too, did not produce the lowest binding energy compared to other possible geometries that were tested.

The comparisons between the unprojected hyperfine constants and experiment are presented in Table VII while the comparison between the projected hyperfine constants for the two geometries are shown in Table VIII. The unprojected hyperfine coupling constants showed better agreement with experiment than the projected hyperfine constants. In most geometries tested, the calculated hyperfine constants for H1 and H8 were greater than the hyperfine constant for H9. Since the experimental data showed the reverse situation to be true, a major requirement for the calculated

TABLE VII

PROTON HYPERFINE COUPLING CONSTANTS, a_H , FOR THE
MONOHOMOCYCLOCHECTATETRAENE ANION RADICAL
OBTAINED FROM UNPROJECTED WAVEFUNCTIONS

Protons	Calculated a_H (Gauss)		Experimental a_H (Gauss) ^a
	$\theta = 83.5^\circ$	$\theta = 76.7^\circ$	
	$\alpha = 0^\circ$	$\alpha = 0^\circ$	
H ₁ , H ₈	4.21	1.92	±5.72
H ₂ , H ₇	-1.57	1.48	±0.87
H ₃ , H ₆	2.62	2.37	±5.12
H ₄ , H ₅	-2.03	-1.86	±1.99
H ₉	-7.55	-9.17	±12.18
H _{9'}	-3.71	-3.86	±4.54

^aS. Winstein, G. Moshuk, R. Rieke and M. A. Ogliaruso, J. Amer. Chem. Soc. 95, 2624 (1973).

TABLE VIII

PROTON HYPERFINE COUPLING CONSTANTS, a_H , FOR THE
 MONOHOMOCYCLOCHECTATETRAENE ANION RADICAL
 OBTAINED FROM SPIN PROJECTED
 WAVEFUNCTIONS

Protons	Calculated a_H (Gauss)		Experimental a_H (Gauss) ^a
	$\theta = 83.5^\circ$	$\theta = 76.7^\circ$	
	$\alpha = 0^\circ$	$\alpha = 0^\circ$	
H ₁ , H ₈	2.72	1.15	±5.72
H ₂ , H ₇	0.78	2.84	±0.87
H ₃ , H ₆	1.34	1.17	±5.12
H ₄ , H ₅	-0.59	-0.51	±1.99
H ₉	-2.49	-3.02	±12.18
H _{9'}	-1.21	-1.26	±4.54

^aS. Winstein, G. Moshuk, R. Rieke and M. A. Ogliaruso, J. Amer. Chem. Soc. 95, 2624 (1973).

hyperfine constants was that the magnitude of H9 be greater than H1. This requirement was satisfied only within a relatively small range of change for the angle θ . It is interesting to note that a further decrease in the angle θ in the optimized projected geometry from 76.7° to 76.65° produced an increase in the hyperfine constants for H9, H9' and H1 to 184.51, 35.12 and 21.22. This sharp increase is apparently the result of H9 interfering with the conjugated pi-electron cloud of the eight-membered ring.

The unprojected energies, projected energies and weighting factors for the geometries producing the best match with experiment are presented in Table IX. As is evident from Table IX, the unprojected doublet ground state had about 1.5 percent spin contamination from the quartet and sextet states. With both geometries, an energy lowering for the doublet of 0.05 atomic units was obtained upon projection.

The calculations were performed using the common convention of a uniform right-handed coordinate system. In the planar eight-membered ring, there occurs one p-orbital on each carbon atom which is oriented perpendicular to the plane of the ring. In the absence of the methylene group, these orbitals would be designated as pi-orbitals and the associated bond orders as $P(\pi r, \pi s)$.

In order to get a more complete picture of the overall bonding, it is necessary to obtain Mulliken bond orders for the in-plane components of the carbon-carbon bonds. This was done by transforming⁴⁴ the orbitals for each carbon-carbon pair into a local coordinate system in which the p_σ -orbital of each carbon

TABLE IX

UNPROJECTED AND PROJECTED BINDING ENERGIES(A.U.)
 AND WEIGHTING FACTORS FOR THE MONOHOMOCYCLO-
 OCTATETRAENE ANION RADICAL

<u>Geometry</u>	<u>Unprojected Energy</u>	<u>Multiplicity</u>	<u>Weight</u>	<u>Binding Energy</u>
$\theta = 83.5^\circ$, $\alpha = 0^\circ$	-9.710	2	9.86×10^{-1}	-9.715
		4	1.35×10^{-2}	-9.346
		6	4.27×10^{-5}	-8.036
$\theta = 76.7^\circ$, $\alpha = 0^\circ$	-9.707	2	9.85×10^{-1}	-9.712
		4	1.44×10^{-2}	-9.353
		6	4.75×10^{-5}	-9.032

points toward the other carbon, the p_{π} -orbitals are perpendicular to the ring as described above, and the p_{π} -orbitals are in the plane of the ring perpendicular to the bond. For each pair, $C_r C_s$, this produces a set of bond orders, $P(\pi_i; \pi_j)$, $P(s_i; s_j)$, $P(\sigma_i; \sigma_j)$ [$P(\sigma_i; s_j + P(s_i; \sigma_j))$], $P(\pi'i; \pi'j)$, which are invariant to the coordinate system used in the calculation and hereafter referred to as invariant bond orders. The invariant bond orders for the best geometries of MHCOT are presented in Table X. It should be noted that the projected density matrices are very close to the unprojected density matrices within the accuracies of the calculations.

As is evident from Table X, only a negligible difference in bond orders occurs between the two geometries and leads to the conclusion that the invariant bond orders are insensitive to relatively small changes in geometry.

An examination of the magnitude of the $P(\pi_i; \pi_j)$ bond orders shows close to aromatic pi-bond orders around the entire ring between carbons two and seven. The 1,2 and 7,8 pi-bond orders are understandably reduced because of the attached methylene group. The values of 0.416 and 0.422 associated with the C_1-C_8 bond are surprisingly large and imply that homoconjugation as envisioned by Winstein^{32,33} does occur.

The C_1-C_8 σ -bond order is reduced by ten to twenty percent relative to the other σ -bond orders in the ring; a similar reduction in strength occurs for the $P(s_i; s_j)$, $P(\sigma_i; \sigma_j)$ and [$P(\sigma_i; s_j + P(s_i; \sigma_j))$] bond orders. The conclusion that must be drawn from the reduction of about twenty percent in the total C_1-C_8 bond strength is that the

TABLE X

 INVARIANT BOND ORDERS FOR CALCULATED GEOMETRIES
 OF MONOHOMOCYCLOCHECTATETRAENE ANION RADICAL

<u>Bond Order</u>	<u>Geometry</u>	
	$\theta = 83.5^\circ$	$\theta = 76.7^\circ$
	$\alpha = 0^\circ$	$\alpha = 0^\circ$
$P(\pi_1; \pi_8)$	0.416	0.422
$P(\pi_1; \pi_2)$	0.384	0.388
$P(\pi_2; \pi_3)$	0.669	0.661
$P(\pi_3; \pi_4)$	0.609	0.615
$P(\pi_4; \pi_5)$	0.602	0.598
$P(s_1; s_8)$	0.270	0.270
$P(s_1; s_2)$	0.318	0.313
$P(s_2; s_3)$	0.340	0.340
$P(s_3; s_4)$	0.344	0.344
$P(s_4; s_5)$	0.344	0.344
$P(\sigma_1; \sigma_8)$	0.477	0.477
$P(\sigma_1; \sigma_2)$	0.511	0.104
$P(\sigma_2; \sigma_3)$	0.511	0.511
$P(\sigma_3; \sigma_4)$	0.510	0.510
$P(\sigma_4; \sigma_5)$	0.510	0.509
$P(\sigma_1; s_8) + P(s_1; \sigma_8)$	0.896	0.894
$P(\sigma_1; s_2) + P(s_1; \sigma_2)$	1.036	1.028
$P(\sigma_2; s_3) + P(s_2; \sigma_3)$	1.068	1.067
$P(\sigma_3; s_4) + P(s_3; \sigma_4)$	1.070	1.070
$P(\sigma_4; s_5) + P(s_4; \sigma_5)$	1.070	1.070
$P(\pi'_1; \pi'_8)$	0.246	0.249
$P(\pi'_1; \pi'_2)$	0.266	0.264
$P(\pi'_2; \pi'_3)$	0.275	0.273
$P(\pi'_3; \pi'_4)$	0.275	0.275
$P(\pi'_4; \pi'_5)$	0.275	0.275

bond has not been opened upon formation of the anion radical from cis-bicyclo[6.1.0]-nona-2,4,6-triene.

The conclusion is in good agreement with the rationalization of the cyclopropyl ring-opening process on the basis of the Woodward-Hoffman rules for the conservation of orbital symmetry.⁴⁵ When the reaction to form the nine pi-electron MHCOT is considered, both the disrotatory and conrotatory ring openings are disallowed processes since the symmetries of the starting material and product are different. However, similar considerations lead to the conclusion that the cis-bicyclo[6.1.0]-nona-2,4,6-triene dianion may undergo a symmetry allowed disrotatory cyclopropyl ring-opening process. Once obtained, the ring-opened dianion is then capable of establishing an equilibrium between the radical anion and the dianion.

Extension of INDO Calculations to Include d-Orbitals

The INDO formalism was used previously to describe the bonding in molecules comprised of the atoms hydrogen through fluorine. Kaufman and Predney⁴⁶ developed the equations necessary to extend the INDO calculations to include d-orbitals on the atoms sodium through chlorine, but a computer program to perform the INDO calculations with d-orbitals was not previously available. The program would be particularly useful in studying sulfur heterocycles and compounds containing the -N=SF₆ group.⁴⁷ For this reason, work was begun to extend the INDO calculation to include d-orbitals.

The Fock matrix elements that included d-orbitals were

available from the work of Kaufman and Predney⁴⁶ along with a complete set of Slater-Condon parameters, F's and G's, that were calculated from Slater-type orbitals. However, two errors in the Fock matrix elements were noted. Abbreviating the d_z^2 , d_{xz} , d_{yz} , $d_{x^2-y^2}$ and d_{xy} orbitals by σ , π , π' , δ and δ' , the correct expressions are

$$\begin{aligned}
F_{\delta\delta}^{\alpha} \text{ (INDO)} &= F_{\delta\delta}^{\alpha} \text{ (CNDO)} - (9 P_{\sigma\sigma}^{\alpha} + 24 P_{\pi\pi}^{\alpha} + 24 P_{\pi'\pi'}^{\alpha}) \\
&- 69 P_{\delta'\delta'}^{\alpha} - 6 P_{\sigma\sigma}^{\beta} + 4 P_{\pi\pi}^{\beta} + 4 P_{\pi'\pi'}^{\beta} - 36 P_{\delta\delta}^{\beta} + \\
&34 P_{\delta'\delta'}^{\beta} F^4(\text{dd})/441 - (P_{xx}^{\alpha} + P_{yy}^{\alpha}) G^1(\text{pd})/5 \\
&- (8 P_{xx}^{\alpha} + 8 P_{yy}^{\alpha} + 5 P_{zz}^{\alpha}) 3 G^3(\text{pd})/245 - P_{ss}^{\alpha} G^2(\text{sd})/5 \\
&- (2 P_{zz}^{\alpha} - P_{xx}^{\alpha} - P_{yy}^{\alpha} + 2 P_{zz}^{\beta} - P_{xx}^{\beta} - P_{yy}^{\beta}) 2 F^2(\text{pd})/35
\end{aligned} \tag{113}$$

$$F_{x\pi^+} \text{ (INDO)} = F_{x\pi^+} \text{ (CNDO)} + 4 P_{x\pi^+}^\alpha F^2(\text{pd})/35 \\ + (P_{x\pi^+} + 2 P_{x\pi^+}) 3 G^3(\text{pd})/49 . \quad (114)$$

It was also necessary to recognize the equivalence of several two-electron integrals.

$$\begin{aligned}
 & \langle \pi \ \pi' | \frac{1}{r_{ij}} | \ \pi \ \pi' \rangle = \langle \pi' \ \delta | \frac{1}{r_{ij}} | \ \pi' \ \delta \rangle = \\
 & \langle \pi' \ \delta' | \frac{1}{r_{ij}} | \ \pi' \ \delta' \rangle = \langle \pi \ \delta | \frac{1}{r_{ij}} | \ \pi \ \delta \rangle = \\
 & \langle \pi \ \delta' | \frac{1}{r_{ij}} | \ \pi \ \delta' \rangle
 \end{aligned} \tag{115}$$

The binding energy, E_B , is the difference between the total

energy of a molecule and the energies of the atoms separated at an infinite distance. The ground state energies of third row atoms in the INDO approximation can be calculated using

$$\begin{aligned}
 E(m, n) = & -\frac{m}{2} (I + A)_S - \frac{n}{2} (I + A)_P + \\
 & (m + n)(m + n - 1) F^0 - \frac{1}{6} m n G^1(sp) - \\
 & \frac{1}{25} n(n - 1) F^2(pp)
 \end{aligned} \tag{116}$$

where m is the number of s-orbital electrons and n is the number of p-orbital electrons in the ground state configuration $(3s)^m(3p)^n$. The atomic energies are listed in Table XI.

The computer program was transferred to Mr. John M. Fildes; results from the use of this program will be forthcoming.

TABLE XI

ATOMIC ENERGIES (A.U.) FOR THIRD ROW ATOMS
CALCULATED USING INDO APPROXIMATIONS

<u>Atom</u>	<u>Total Energy(a.u.)</u>
Na	-0.1461713
Mg	-0.6501658
Al	-1.5838907
Si	-3.1385524
P	-5.5635470
S	-9.0512034
Cl	-13.501409

X. AB INITIO UNRESTRICTED HARTREE-FOCK CALCULATIONS

Ab initio molecular orbital calculations are based on first principles and, as such, contain no empirical parameters. All one- and two-electron integrals are calculated explicitly. However, the fact that the calculations can be done with the current high speed computers does not guarantee that the predicted molecular properties will be reliable, i.e., in agreement with experiment.⁴⁹ The primary consideration in the reliability of the electronic structure calculation is the choice of a basis set.

The basis functions used in molecular calculations are usually atom-centered and either exponential or Gaussian functions. Slater⁵⁰ first suggested the use of exponential functions of the type

$$x_i = A r^{n-1} \exp(-\zeta_i r_i) Y_{lm}(\theta, \phi) \quad (117)$$

where A is a normalization factor, n is the principle quantum number and ζ_i is the orbital exponent or screening factor. The angular dependence of the orbital is introduced with a spherical harmonic, $Y_{lm}(\theta, \phi)$, while r is the distance from the atom on which the Slater function is centered.

Boys⁵¹ first proposed the use of Gaussian functions which, in comparison with the Slater functions, may be written as

$$x_i = B r^n \exp(-\alpha_i r_i^2) Y_{lm}(\theta, \phi) . \quad (118)$$

More frequently, however, the angular dependence of Gaussian functions is introduced by

$$x_i = C x^l y^m z^n \exp(-\alpha_i r_i^2) \quad (119)$$

where l , m and n are integers. Such functions are called cartesian Gaussians. A linear combination of Gaussian-type orbitals (GTO's) can be found to match a Slater-type orbital (STO) with $\zeta_i = 1$. Then a scale factor, κ , can be introduced to relate the STO to the linear combination of GTO's. The scaled STO with $\zeta_i' = \kappa$ is represented by the same linear combination of GTO's with exponents equal to $\kappa^2 \zeta_i$.

The size of a basis set is an important factor in the reliability of molecular calculations. The work described in the previous chapter dealt with a valence orbital minimum basis set. Ab initio calculations, by their very nature, deal with both core and valence electrons. SCF energies obtained using minimum basis sets are far above the Hartree-Fock energies; for this reason, larger basis sets are usually used. A Slater basis set that receives wide use is the double zeta set, comprised of twice as many functions as the minimum basis set. For the carbon atom, the notation used to describe such a basis set is (4s2p); that is, the atom is described by two 1s and two 2s Slater functions, all with different orbital exponents. In addition, there are two sets (p_x , p_y and p_z) of 2p functions.

Extended basis sets, those larger than double zeta, are used when it is necessary to obtain SCF energies very close to the Hartree-Fock limit. Further, when molecular dissociations and properties

are studied, it is frequently necessary to employ polarization functions,⁵³ functions which have angular quantum numbers, ℓ , greater than the highest ℓ value generally found occupied in the ground state wavefunction. For example, the polarization functions for the carbon atom would include 3d orbitals.

As the size of the basis set increases, the amount of computational time increases accordingly. It is advantageous, then, to weigh the amount of increased accuracy obtained by increasing the size of the basis set against the increased time requirements to reach a balance between the two factors. Two portions of an ab initio molecular orbital calculation consume great quantities of time, the multi-centered two-electron integral evaluation and the diagonalization of the Hartree-Fock matrices to give the molecular orbitals.

The primary advantage of Gaussian over Slater orbitals is the speed with which integral evaluation can be accomplished. Multi-centered two-electron integrals over Gaussian functions can be evaluated in closed form while those over Slater functions cannot; thus, it has been shown⁵⁴ that integral evaluation can proceed at a rate of ten times more rapidly when Gaussian functions are used instead of Slater functions. One disadvantage of the use of Gaussian functions is that many more Gaussian than Slater functions are necessary to obtain comparable SCF energies. In a comparison of sizes of basis sets versus SCF energies obtained for oxygen and fluorine, Schaefer⁴⁹ has shown that a (10s6p) Gaussian basis set is necessary to match double zeta Slater results.

The second time consuming portion of the molecular orbital calculation, the solution of the SCF equations, requires an amount of time proportional to the fourth power of the number of basis functions. Further, large basis sets may slow convergence necessitating more iterations.⁴⁹ Therefore, the use of primitive Gaussians (equation 119) is uneconomical because of the computational time requirements.

The use of contracted Gaussian functions, linear combinations of Gaussians with fixed coefficients,^{55,56} partially alleviates the problem of large basis sets. When contracted functions are used, only the coefficients of each contracted function in an SCF orbital are determined. Whitten⁵⁶ first made effective use of contracted Gaussians by optimizing a (10s5p) basis set to a contracted [3s1p] set, where brackets denote a contracted basis set. Dunning^{57,58} continued the work in contraction schemes by optimizing various atomic basis sets and polarization functions for hydrogen through krypton. Generally, when forming a contracted basis set, the greatest number of primitives per contracted function are found in orbitals used to describe the core region of the atom. Relatively few primitives per contracted function are located in the more diffuse region of the atom; this freeing of orbitals allows a better description of the bonding region when an atom is present in a molecule than when a large number of primitives comprise a contracted function in the bonding region.

The contraction scheme thus far described does not allow the

primitive functions to have nonzero contributions in more than one contracted orbital; this type of contraction is referred to as a segmented contraction scheme. The disadvantage of this scheme is that, since atomic schemes are used in molecular calculations, they fail to adequately describe the internuclear region.

Raffenetti⁵⁹ proposed the use of a general contraction scheme to remedy this failure. In his scheme, each contracted function can have nonzero contribution from each primitive Gaussian. In addition, the most diffuse primitive Gaussian is allowed to float as a separate contracted function. Calculations on H₂O showed that 96 to 98 percent of the available energy relative to the completely uncontracted basis set was obtained.

The time required for diagonalization of the SCF matrices is dependent on the method of matrix diagonalization and roughly proportional to the fourth power of the size of the matrix. A reduction in computational time requirements can be realized when the secular determinant is symmetry-restricted. Like orbitals in other SCF calculations, each orbital must transform according to one of the irreducible representations of the molecular point group.⁶⁰ The molecular orbitals can then be grouped by symmetry; matrix elements between orbitals of different symmetry groups are zero. Using this information, the matrix diagonalization problem reduces from the diagonalization of one matrix of size B by B to the diagonalization of several smaller matrices, realizing a considerable savings in computational time.

The SCF procedure is performed using the Hartree-Fock

equations outlined in Chapter VI. One complication that is usually ignored in semi-empirical calculations and is therefore unique to ab initio calculations is the nonorthogonality of the atomic basis set.

The direct consequence of the nonorthogonality of the atomic orbitals is that one- and two-electron integrals, equations 29 through 32, are evaluated and the SCF matrices are formed in the nonorthogonal representation. The orthogonal molecular orbitals can be expressed in two forms, as a linear combination of nonorthogonal atomic functions,

$$\phi_r = \sum_{\rho} n_{\rho} Y_{\rho r} \quad (120)$$

or as a set of orthogonal symmetry functions,

$$\sigma_r = \sum_{\rho} n_{\rho} R_{\rho r} . \quad (121)$$

The former expression is preferable in relating bonding parameters to specific portions of a molecule but results in nonorthogonal density matrices.

Matrices in a nonorthogonal representation can be put into an orthogonal basis through a transformation using the symmetry blocking transformation matrix. The transformation results from the fact that the overlap matrix, S, is in diagonal form,

$$\langle \phi_r | \phi_s \rangle = \delta_{rs} = \sum_{\rho, \tau} Y_{\rho r}^* \langle n_{\rho} | n_{\tau} \rangle Y_{\tau s} \quad (122)$$

or

$$\langle \phi_r | \phi_s \rangle = \sum_{\rho, \tau} \tilde{Y}_{r\rho} S_{\rho\tau} Y_{\tau s} \quad (123)$$

leading directly to

$$\underline{\tilde{Y}} \underline{S} \underline{Y} = \underline{1}. \quad (124)$$

Solving for $\underline{\tilde{Y}}^{-1}$ leads to

$$\underline{\tilde{Y}}^{-1} = \underline{S} \underline{Y} \quad (125)$$

Equation 124 applies for any orthogonal basis, whether the basis is the molecular orbitals from a previous iteration or other orbitals such as natural orbitals.

The Hartree-Fock problem is solved using Roothaan's equation⁶¹ which is

$$\underline{F} \underline{Y} = \underline{S} \underline{Y} \underline{E} \quad (126)$$

where the Fock matrix, \underline{F} , the matrix of eigenvectors, \underline{Y} , and the overlap matrix, \underline{S} , are in the nonorthogonal representation and \underline{E} is a diagonal matrix of orbital eigenvalues. The Fock, overlap and eigenvector matrices are transformed into the orthogonal basis by

$$\underline{F}' = \underline{\tilde{R}} \underline{F} \underline{R} \quad (127)$$

$$\underline{S}' = \underline{\tilde{R}} \underline{S} \underline{R} \quad (128)$$

$$\underline{W} = \underline{\tilde{R}}^{-1} \underline{Y} \quad (129)$$

giving a Fock equation of

$$\underline{\tilde{R}} \underline{F} \underline{R} \underline{R}^{-1} \underline{Y} = \underline{\tilde{R}} \underline{S} \underline{R} \underline{R}^{-1} \underline{Y} \underline{E} \quad (130)$$

which, when equation 124 is used, takes the appearance of a standard eigenvalue problem,

$$\underline{F}' \underline{W} = \underline{W} \underline{E}. \quad (131)$$

The solution of the standard Hartree-Fock equations yields molecular orbitals in the orthogonal basis; the transformation to the nonorthogonal basis is accomplished with

$$\underline{Y} = \underline{R} \underline{W}. \quad (132)$$

The POLYATOM (Version 2)⁴ system of programs is a series of programs designed to calculate ab initio molecular orbital wavefunctions using Gaussian basis functions. In order to provide maximum flexibility, the system contains a number of independent main programs. Computer memory requirements are minimized by utilizing off-line tape storage to the fullest possible extent. The main programs include PA20A and PA20B which list one- and two-electron integrals respectively, and PA30A and PA30B which evaluate those integrals. The open shell SCF calculation is performed using PA43. Several supplemental programs which perform a variety of SCF calculations and compute molecular properties are also available.

The initial set of molecular orbitals in POLYATOM can be obtained from two sources, from a set of molecular orbitals from a previous calculation or from the diagonalization of the core Hamiltonian.

Spin projection of ab initio wavefunctions requires the formation of the corresponding orbitals and the natural orbitals of charge and spin. As was stated earlier, the density matrices are expressed in a nonorthogonal basis but may be transformed to the orthogonal representation using equation 125 by

$$\underline{P}' = \underline{Y}^{-1} \underline{P} \tilde{\underline{Y}}^{-1} . \quad (133)$$

The diagonalization of \underline{P}' by

$$\underline{P}' \underline{C} = \underline{N} \underline{C} \quad (134)$$

gives the natural orbitals, $\{m_r\}$,

$$m_r = \sum_{s,\rho} n_\rho Y_{\rho r} \tilde{c}_{sr} = \sum_\rho n_\rho (\tilde{\underline{Y}} \underline{C})_{\rho s} . \quad (135)$$

The natural orbitals are expressed in the atomic orbital basis by the transformation

$$\underline{X} = \underline{Y} \underline{C} . \quad (136)$$

The alpha corresponding orbitals are formed in a manner similar to that for the natural orbitals with one noteworthy exception. The product matrix $\underline{P}^\alpha \underline{P}^\beta \underline{P}^\alpha$ cannot be transformed to the orthogonal representation as a single matrix, but rather \underline{P}^α and \underline{P}^β must be separately transformed before the product matrix is formed. The reason for the necessity of separate transformations lies in the lack of orthonormality of the orbitals. This can best be seen by examining the effect of \underline{P}^α operating on an arbitrary vector, A.

The alpha density matrix is

$$\underline{P}^\alpha = \sum_r^{B_{occ}^\alpha} |r^\alpha\rangle \langle r^\alpha| \quad (137)$$

where $|r\rangle$ is a molecular orbital. Each molecular orbital is a linear combination of atomic orbitals, $|m\rangle$,

$$| r \rangle = \sum_m c_{rm} | m \rangle . \quad (138)$$

The alpha density matrix, then, in terms of atomic orbitals, is

$$\begin{aligned} \underline{P}^\alpha &= \sum_r \sum_{m,n} c_{rm}^\alpha | m \rangle \langle n | c_{nr}^{\alpha*} \\ &= \sum_{m,n} P_{mn}^\alpha | m \rangle \langle n | \end{aligned} \quad (139)$$

where P_{mn}^α is a density matrix coefficient. When the density matrix is used as an operator operating on an arbitrary vector, \underline{A} ,

$$\underline{A} = \sum_p | p \rangle c_p , \quad (140)$$

the resultant equation is

$$\underline{P}^\alpha \underline{A} = \sum_{m,n,p} P_{mn}^\alpha | m \rangle \langle n | | p \rangle c_p \quad (141)$$

where $\langle n | p \rangle$ are overlap integrals. When orthonormal orbitals are used, the overlap matrix is diagonal with elements $S_{nn} = 1$. However, the overlap matrix in the nonorthogonal representation is not diagonal but can be used to bring nonorthogonal orbitals into the orthogonal representation,

$$\underline{P}^\alpha \underline{A} = \sum_{m,n,p} P_{mn}^\alpha | m \rangle S_{np} c_p . \quad (142)$$

The overlap matrix can also be expressed, using equation 124, as

$$\underline{S} = \underline{\tilde{Y}}^{-1} \underline{Y}. \quad (143)$$

Using these arguments, then, the matrix equation for the determination of the alpha corresponding orbitals becomes

$$\underline{Y}^{-1} \underline{P}^\alpha \underline{\tilde{Y}}^{-1} \underline{Y}^{-1} \underline{P}^\beta \underline{\tilde{Y}}^{-1} \underline{Y}^{-1} \underline{P}^\alpha \underline{\tilde{Y}}^{-1} \underline{A} = \underline{\Delta} \underline{A} \quad (144)$$

or

$$\underline{Y}^{-1} \underline{P}^\alpha \underline{S} \underline{P}^\beta \underline{S} \underline{P}^\alpha \underline{\tilde{Y}}^{-1} \underline{A} = \underline{\Delta} \underline{A} \quad (145)$$

where $\Delta_i = d_i^2$, an eigenvalue of the alpha corresponding orbital.

The spin projection calculation for ab initio wavefunctions derived from the POLYATOM (Version 2)⁴ system of programs was written to conform as closely as possible to the original system of programs and is listed in Appendix A. Documentation for the manner in which the data is input is provided in the program comments. The program utilizes an integral tape that was generated by the POLYATOM integral evaluation programs; in addition, an open shell molecular orbital wavefunction obtained from the POLYATOM UHF SCF package must be provided in either card or tape format. The desire to minimize the computer region requirements was accomplished by utilizing scratch disk to as great an extent as possible.

The program calculates the alpha corresponding orbitals and natural orbitals of charge in the manner just described. Appropriate replacements of the singly-occupied natural orbitals of charge by natural orbitals of spin are made as was described in equations 75 and 76. All orbitals are then transformed to the nonorthogonal basis in order to conform to the integral tape which is in the nonorthogonal basis; further, the orbitals are completely

reordered, breaking the symmetry blocking, so that the lowest orbital has the highest occupation number. The purpose of the reordering is to properly classify the orbitals based on occupation numbers during the spin projection calculation.

**Comparison of Spin Projection and MCSCF/CI
Calculations on H₂O(+)**

The water cation was studied by several groups of workers using a variety of theoretical techniques. Dunning, Pitzer and Aung⁶² obtained near Hartree-Fock vertical ionization potentials of ground state H₂O, and Meyer,⁶³ using CI calculations, obtained vertical and adiabatic ionization potentials along with SCF equilibrium geometries for selected ion states. LeClerc, Horsley and Lorquet⁶⁴ studied the asymmetric dissociation and potential energy surfaces for the ground and excited states of H₂O(+) while Smith, Jørgensen and Øhrn⁶⁵ and Fortune, Rosenberg and Wahl⁵ carried out a vibrational analysis of selected low-lying states.

The purpose of the study described below was to compare the degree of energy lowering obtained with spin projection and MCSCF/CI calculations. Spin projection has been described as a viable alternative to the time-consuming MCSCF/CI calculations. An adequate assessment of spin projection can be made only when as many parameters as possible, such as the basis set and geometry, are held constant. An evaluation of the spin projection technique was most easily made by comparing spin projection data with MCSCF/CI calculations⁵ on the X²B₁ and \tilde{B}^2B_2 states of H₂O(+).

The basis set chosen for study was one where the polarization functions were specially optimized for H₂O by Dunning.⁵⁷ It consisted of a set of (9s5p2d) orbitals contracted to [4s3p1d] for oxygen and a (4s1p) set contracted to [2s1p] for hydrogen. It is listed in Table XII.

The geometries chosen for study were equilibrium geometries obtained from the potential energy surface of Fortune, et. al.⁵ The H₂O(+) molecule lies in the xz plane with oxygen at the origin (0.0, 0.0, 0.0). The equilibrium geometry of the X²B₁ state located the hydrogens at (± 1.54499 , 0.0, 1.11224) bohrs giving an oxygen-hydrogen bond length of 1.90 bohrs and an angle, <HOH, of 47.88°; the hydrogens were located at (± 0.99428 , 0.0, 1.91128) bohrs (an oxygen-hydrogen length of 2.15 bohrs and angle, <HOH, of 54.97°) for the equilibrium \tilde{B}^2B_2 state. The convergence criterion for the total energy for both calculations was 1.0×10^{-6} atomic units.

The unprojected and projected energies for the X²B₁ and \tilde{B}^2B_2 states are presented in Tables XIII and XIV, respectively; a comparison of this work with MCSCF/CI and RHF calculations is available in Table XV.

An energy lowering of 0.0046 and 0.0008 atomic units for the X²B₁ and \tilde{B}^2B_2 states, respectively, is obtained when an UHF rather than a RHF wavefunction is used. Very little additional energy lowering was obtained upon spin projection of the UHF wavefunction, 0.002 atomic units for the \tilde{B}^2B_2 and 0.003 atomic units for the X²B₁ state. This lack of considerable energy lowering is attributed to the fact that the UHF wavefunction is so close to being a pure

TABLE XII

CONTRACTED GAUSSIAN BASIS SET FOR A (9s5p2d/4s1p)
 H_2O PRIMITIVE BASIS SET^a

<u>Atom</u>	<u>Orbital Type</u>	<u>Contracted Orbital No.</u>	<u>Exponent</u>	<u>Coefficient</u>
O	s	1	7816.5400	0.002031
O	s	1	1175.8200	0.015436
O	s	1	273.1880	0.073771
O	s	1	81.1696	0.247606
O	s	1	27.1836	0.611832
O	s	1	3.4136	0.241205
O	s	2	9.5322	1.000000
O	s	3	0.9398	1.000000
O	s	4	0.2846	1.000000
O	p	5	35.1832	0.040023
O	p	5	7.9040	0.253849
O	p	5	2.3051	0.806842
O	p	6	0.7171	1.000000
O	p	7	0.2137	1.000000
O	d	8	1.3220	0.357851
O	d	8	0.3916	0.759561
H	s	9	21.7208	0.032828
H	s	9	3.2729	0.231208
H	s	9	0.7377	0.817238
H	s	10	0.2004	1.000000
H	p	11	1.1592	1.000000

^aT. H. Dunning, J. Chem. Phys. 53, 2823 (1970); T. H. Dunning, J. Chem. Phys. 55, 3958 (1971).

TABLE XIII

UNPROJECTED AND PROJECTED ENERGIES FOR
 THE X^2B_1 STATE OF $H_2O(+)$

Unprojected Energies(a.u.)

Kinetic Energy, T	75.749684
One-Electron Potential Energy, V(1)	-192.949513
Two-Electron Potential Energy, V(1,2)	33.021498
Electronic Energy, E(E)	-84.378330
Nuclear Repulsion Energy, V(N)	8.728339
Total Energy, E	-75.649992

Projected Energies(a.u.)

<u>Multiplicity</u>	<u>Weight, w_i</u>	<u>Total Energy, E_i</u>
2	9.9737×10^{-1}	-75.65323
4	2.6255×10^{-3}	-74.42535
6	1.6888×10^{-6}	-73.49101
8	2.882×10^{-10}	-72.58397

TABLE XIV

UNPROJECTED AND PROJECTED ENERGIES FOR
 THE $\tilde{B}^2_{B_2}$ STATE OF $H_2O(+)$

Unprojected Energies(a.u.)

Kinetic Energy, T	75.40146
One-Electron Potential Energy, V(1)	-191.25650
Two-Electron Potential Energy, V(1,2)	32.44855
Electronic Energy, E(E)	-83.40648
Nuclear Repulsion Energy, V(N)	7.92953
Total Energy, E	-75.47695

Projected Energies(a.u.)

Multiplicity	Weight, w_i	Total Energy, E_i
2	9.9868×10^{-1}	-75.47908
4	1.3204×10^{-3}	-73.86906
6	2.6566×10^{-7}	-72.84159
8	1.3743×10^{-11}	-71.85666

TABLE XV

COMPARISON OF MCSCF/CI^a AND SPIN PROJECTION
 ENERGIES FOR THE EQUILIBRIUM GEOMETRIES
 OF THE X²B₁ AND \tilde{B}^2B_2 STATES OF H₂O(+)

<u>Type of Wavefunction</u>	<u>Total Energies(a.u.)</u>	
	<u>X²B₁</u>	<u>\tilde{B}^2B_2</u>
RHF SCF	-75.64565 ^a	-75.47629 ^b
RHF Plus MCSCF/CI	-75.72328 ^a	-75.55451 ^b
UHF SCF	-75.64999	-75.47695
UHF Plus Spin Projection	-75.65323	-75.47908

^aP. J. Fortune, B. J. Rosenberg and A. C. Wahl, J. Chem. Phys. 65, 2201 (1976).

^bData from cubic fit of Fortune, et. al.

doublet state.

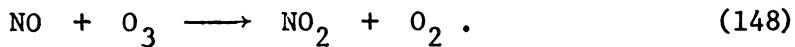
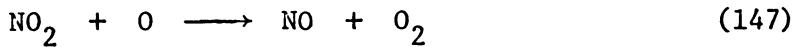
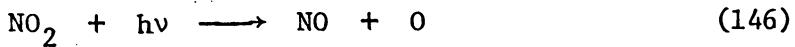
In contrast to the spin projection results, the MCSCF/CI calculations which used 20 configurations produced a much greater energy lowering of 0.078 atomic units relative to the RHF energy for both the \tilde{B}^2B_2 and X^2B_1 states. The conclusion that must be reached from this study is that the MCSCF/CI calculation is superior to spin projection when the weighting factor for the spin projected state of lowest multiplicity is very close to unity. However, studies using semi-empirical techniques^{25,26} indicated that useful results from spin projection can be obtained when the weight for the state of lowest multiplicity is much different from one. Since spin projection calculations using small basis sets are more economical in terms of computational time than MCSCF/CI calculations, further investigation into cases where weighting factors are different from unity is certainly warranted. In any case, weighting factors obtained from spin projection calculations should be examined before the more costly MCSCF/CI calculation is attempted.

The Dissociation of CF_2O

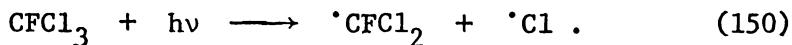
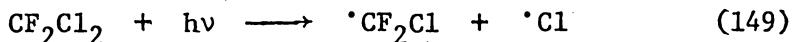
The study of the dissociation of carbonyl fluoride, CF_2O , was initiated from the desire to better understand the possible reaction pathways that could occur in the stratosphere, particularly the reactions involving chlorofluoromethanes.

Any decrease in the amount of stratospheric ozone is likely to have extreme environmental consequences.⁶⁶ The most important mode of ozone destruction at the present time is the nitrogen oxide

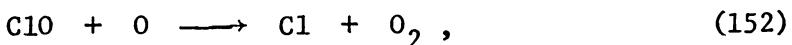
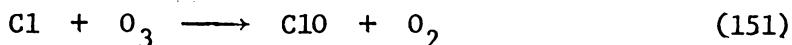
catalyzed cycle,⁶⁷



However, Rowland and Molina⁶⁸ indicate that if the use of chlorofluoromethanes, CF_2Cl_2 and CFCl_3 , continues at the present rate, the chlorine oxide catalyzed cycle will overtake the nitrogen oxide cycle in importance within several years. The chlorofluoromethanes are a starting point in the chlorine oxide cycle when they are photolytically dissociated by ultraviolet solar radiation,



The chlorine atoms then deplete the odd oxygen content by

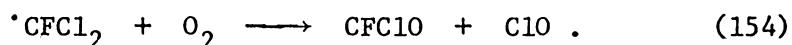
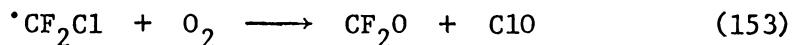


giving the same net effect as reactions 147 and 148.

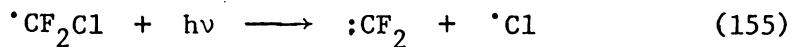
Rowland and Molina⁶⁸ point out many other reactions related to 151 and 152 that require study or are currently under study. Rowland is studying some photolytic reactions;⁶⁹ Watson is investigating the reactions of ClO with a range of atmospheric species;⁷⁰ Kaufmann's research group is studying a variety of reactions involving Cl and ClO;⁷¹ and Heicklen⁷² is researching the photo-dissociation of the chlorofluoromethanes.

The reactions of the chlorofluoromethyl radicals produced

in reactions 149 and 150 have been largely ignored. Rowland and Molina⁶⁸ indicate that, and some experimental data^{69,72} supports, the primary reaction of the chlorofluoromethyl radicals with oxygen is

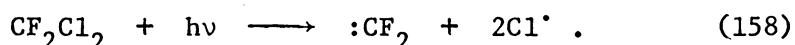
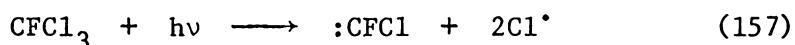


The possibility also exists that substituted methyl radicals can absorb another photon and dissociate to produce carbenes,



Either reaction 155 or 156 produces chlorine atoms which can initiate the chlorine oxide catalyzed destruction of ozone.

The possibility of direct production of carbenes from the photolysis of chlorofluoromethanes was noted at the August 1975 meeting of the American Chemical Society by Ausloos and Rebbert⁷³ who found evidence to support the reactions



The focus of this work is on the reaction of difluorocarbene with oxygen to produce carbonyl fluoride,



Available thermochemical data⁷⁴ show that CF_2O is a fairly stable molecule with a standard heat of formation at 298°K of -152.0 kcal/mole. Three possible modes of dissociation for CF_2O

can be envisioned,



with standard heats of reaction, ΔH_{298}° , of 130.6, 168.8 and 126.3 kcal/mole, respectively. The dissociation of CF_2O by reaction 161 was chosen for study.

The study of the dissociation of carbonyl fluoride was begun using two geometries, the equilibrium geometry for CF_2O determined by Laurie, Pence and Jackson⁷⁵ and illustrated in Figure 2 and the equilibrium geometry for CF_2 determined by Powell, Lide and Mathews.⁷⁶ Both molecules are members of the C_{2v} point group and were chosen to lie in the yz plane. The carbon atom was located at the origin (0.0, 0.0, 0.0) in both geometries. In the equilibrium geometry for CF_2O , the oxygen atom was located at (0.0, 0.0, -2.21858) bohrs and the fluorines at (0.0, ±1.92806, 1.40082) bohrs giving a carbon-fluorine bond distance of 2.38 bohrs and an angle, $\angle FCF$, of 108°. The carbon-oxygen bond length was varied in increments of 0.20000 bohrs in the z direction from 1.81858 to 2.61858 bohrs in order to obtain data on the behavior of CF_2O near the equilibrium geometry. The geometry for CF_2 located the fluorines at (0.0, ±1.94876, 1.52802) bohrs giving a carbon-fluorine bond distance of 2.48 bohrs and an angle, $\angle FCF$, of 103.8°; an oxygen atom was placed at (0.0, 0.0, -18.90359) bohrs in order to approximate the dissociated CF_2O molecule.

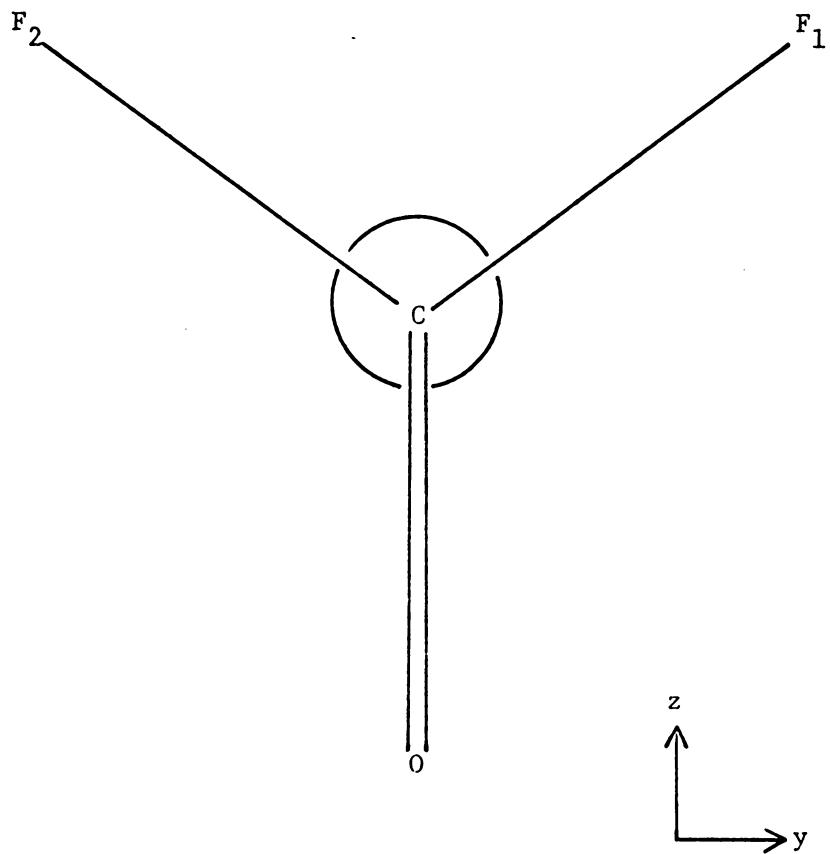


Figure 2.- Geometry of CF_2O molecule.

The POLYATOM (Version 2) system of programs⁴ discussed earlier in this chapter was used to obtain wavefunctions for all geometries of CF_2O . All two-electron integrals whose values were less than 1.0×10^{-9} atomic units were taken to be exactly zero. The criterion for energy convergence was 1.0×10^{-6} atomic units.

The basis set used in all calculations was Dunning's (9s5p) set contracted to $[4s3p]^{58}$ for each atom in CF_2O or a total of 52 contracted orbitals. Symmetry orbitals were formed to the fullest possible extent, giving 502,627 two-electron integrals, 261,910 of which were unique.

Symmetry factoring of the secular determinant in the SCF portion of the molecular orbital calculation was performed differently for the geometry where the carbon-oxygen bond distance was 18.90359 bohrs than for the remainder of the geometries. The factoring of the latter will be discussed first.

The 52 atomic orbitals of CF_2O near the equilibrium geometry can be combined into 52 symmetry orbitals, 24 a_1 , 3 a_2 , 9 b_1 and 16 b_2 which are presented in Table XVI. The atomic orbitals p_x , p_y and p_z are abbreviated x, y and z. Since all symmetry types in the point group contain orbitals, all molecular symmetry states, A_1 , A_2 , B_1 and B_2 , in the point group are accessible. A preliminary examination of the symmetry orbitals showed the m=0 ground state orbital occupation in the A_1 molecular symmetry state was 8 a_1 , 1 a_2 , 2 b_1 and 5 b_2 for both the alpha and beta orbitals. A RHF calculation was performed on the A_1 state of the equilibrium geometry in order to determine the lowest energy excitations and

TABLE XVI

SYMMETRY ORBITALS FOR [4s3p] BASIS SET OF CF_2O
NEAR THE EQUILIBRIUM GEOMETRY

<u>Orbital Symmetry</u>	<u>Symmetry Orbital</u>	<u>Number of Orbitals</u>
a_1	s_0	4
a_1	s_c	4
a_1	$s_{F1} + s_{F2}$	4
a_1	$y_{F1} - y_{F2}$	3
a_1	z_0	3
a_1	z_c	3
a_1	$z_{F1} + z_{F2}$	3
a_2	$x_{F1} - x_{F2}$	3
b_1	x_0	3
b_1	x_c	3
b_1	$x_{F1} + x_{F2}$	3
b_2	$s_{F1} - s_{F2}$	4
b_2	y_0	3
b_2	y_c	3
b_2	$y_{F1} + y_{F2}$	3
b_2	$z_{F1} - z_{F2}$	3

thus the occupation of symmetry orbitals necessary to form the A_2 , B_1 and B_2 states. The lowest energy excitations were obtained when the following alpha-electron symmetry orbitals were occupied: 8 a_1^α , 1 a_2^α , 3 b_1^α , and 4 b_2^α for the A_2 state; 9 a_1^α , 1 a_2^α , 1 b_1^α and 5 b_2^α for the B_1 state; and 9 a_1^α , 1 a_2^α , 2 b_1^α and 4 b_2^α for the B_2 state. In all cases, the occupation of the beta symmetry orbitals was equal to that for the A_1 state.

An attempt was made to treat all geometries in the same manner with respect to symmetry factoring. However, the geometry where the carbon-oxygen distance equalled 18.90359 bohrs produced wide oscillations in the total energy when an SCF calculation was attempted. In addition, the orbitals attributed to the oxygen atom showed very little interaction with those orbitals associated with the CF_2 fragment. In order to obtain SCF convergence, it was necessary to separate by symmetry factoring the oxygen orbitals from the difluorocarbene orbitals. The symmetry factoring for this geometry is shown in Table XVII. By using such symmetry factoring, this geometry approached CF_2O dissociated into CF_2 and O at an infinite separation.

Eight molecular symmetry states were considered for the dissociated $\text{CF}_2 + \text{O}$, four symmetries in the C_{2v} point group for CF_2 , A_1 , A_2 , B_1 and B_2 and two atomic states for oxygen, ^3P and ^1D . The occupation of symmetry orbitals for CF_2 was determined using $\text{CF}_2(\text{A}_1) + \text{O}(^3\text{P})$ in a manner similar to that described previously for the CF_2O geometries near equilibrium. The occupation of the beta-electron symmetry orbitals for all states was set equal

TABLE XVII

SYMMETRY ORBITALS FOR THE [4s3p] BASIS
SET OF $\text{CF}_2 + \text{O}$

<u>Orbital Symmetry</u>	<u>Symmetry Orbital</u>	<u>Number of Orbitals</u>
a_1	s_C	4
a_1	$s_{F1} + s_{F2}$	4
a_1	$y_{F1} - y_{F2}$	3
a_1	z_C	3
a_1	$z_{F1} + z_{F2}$	3
a_2	$x_{F1} - x_{F2}$	3
b_1	x_C	3
b_1	$x_{F1} + x_{F2}$	3
b_2	y_C	3
b_2	$y_{F1} + y_{F2}$	3
b_2	$z_{F1} - z_{F2}$	3
b_2	$s_{F1} - s_{F2}$	4
a'_1	s_0	4
a'_1	z_0	3
b'_1	x_0	3
b'_2	y_0	3

to that for the A_1 alpha-electron orbitals in all molecular symmetries considered; the alpha orbital occupations for CF_2 were: 6 a_1^α , 1 a_2^α , 1 b_1^α and 4 b_2^α for the A_1 state; 6 a_1^α , 1 a_2^α , 2 b_1^α and 3 b_2^α for the A_2 state; 5 a_1^α , 1 a_2^α , 2 b_1^α and 4 b_2^α for the B_1 state; and 5 a_1^α , 1 a_2^α , 1 b_1^α and 5 b_2^α for the B_2 state. The 3P state of oxygen was generated by occupying 3 a_1^α' , 1 b_1^α' , and 1 b_2^α' while the occupation for the $O(^1D)$ was 3 a_1' and 1 b_2' .

The existence of an open shell ground state in pentacene was discussed previously. In order to allow for the possibility of open shell ground states in CF_2O , the B_1 states were obtained, and the open shell orbitals from the B_1 state were used as starting orbitals for the generation of the A_1 states; the A_1 orbitals were used as starting points for the A_2 states and orbitals from the A_2 state used as starting points for the B_2 states. This procedure not only allowed for the possibility of open shell ground states but had the added advantage of saving the computational time that would have been required had the starting point for each state been the core Hamiltonian.

The total energies with respect to carbon-oxygen bond distances for the A_1 , A_2 , B_1 and B_2 states are listed in Tables XVIII, XIX, XX and XXI, respectively, and presented graphically in Figure 3. First inspection leads to the conclusion that the A_2 , B_1 and B_2 states are dissociative; that is, no possibility of bonding occurs in any of those states. However, upon viewing these data together with those for the dissociated $CF_2 + O$ presented in Table XXII, only one state is truly dissociative, the B_1 state.

TABLE XVIII

TOTAL ENERGIES(A.U.) FOR THE A₁ STATE OF CF₂O
AS A FUNCTION OF THE CARBON-OXYGEN
BOND DISTANCE

Carbon-Oxygen Bond Distance (bohrs)	<u>Total Energy(a.u.)</u>
1.81858	-311.422091
2.01858	-311.533835
2.21858	-311.560185
2.41858	-311.543846
2.61858	-311.508605

TABLE XIX

TOTAL ENERGIES(A.U.) FOR THE A₂ STATE OF CF₂O
AS A FUNCTION OF THE CARBON-OXYGEN
BOND DISTANCE

<u>Carbon-Oxygen Bond Distance (bohrs)</u>	<u>Total Energy(a.u.)</u>
1.81858	-311.076288
2.01858	-311.270210
2.21858	-311.366903
2.41858	-311.409140
2.61858	-311.421066

TABLE XX

TOTAL ENERGIES(A.U.) FOR THE B_1 STATE OF CF_2O
AS A FUNCTION OF THE CARBON-OXYGEN
BOND DISTANCE

Carbon-Oxygen Bond Distance <u>(bohrs)</u>	Total Energy(a.u.)
1.81858	-310.882854
2.01858	-311.043688
2.21858	-311.123940
2.41858	-311.166386
2.61858	-311.202223

TABLE XXI

TOTAL ENERGIES(A.U.) FOR THE B_2 STATE OF CF_2O
AS A FUNCTION OF THE CARBON-OXYGEN
BOND DISTANCE

Carbon-Oxygen Bond Distance (bohrs)	Total Energy(a.u.)
1.81858	-310.941836
2.01858	-311.091515
2.21858	-311.160894
2.41858	-311.195404
2.61858	-311.226302

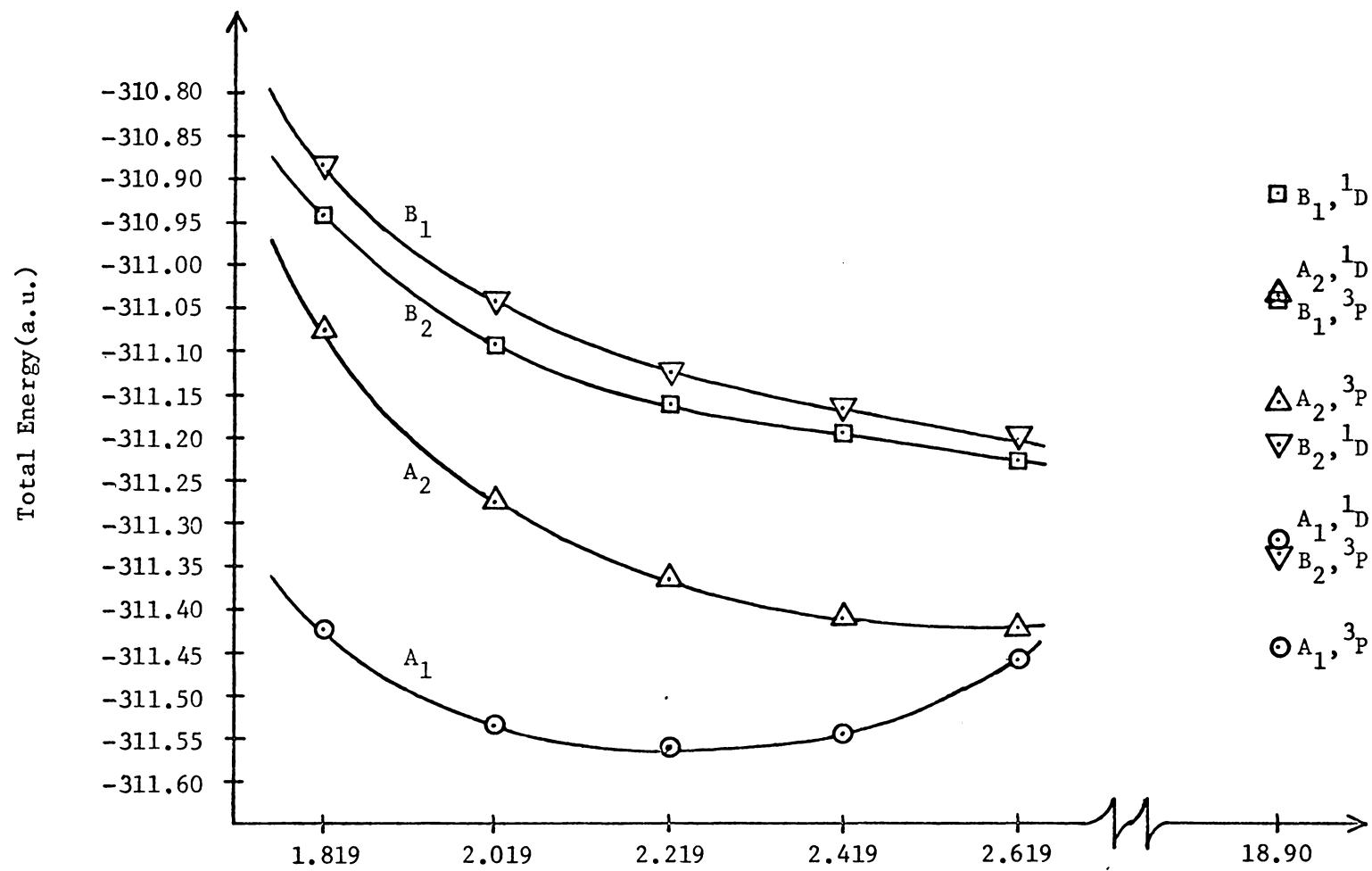


Figure 3.- Total Energy(a.u.) as a Function of Carbon-Oxygen Bond Distance(bohrs) in CF_2O^0

TABLE XXII

TOTAL ENERGIES (A.U.) AS FUNCTIONS OF MOLECULAR
SYMMETRY FOR THE DISSOCIATED $\text{CF}_2 + \text{O}$

Molecular Symmetry State of CF_2	Atomic Symmetry Of O	Total Energy (a.u.)
A_1	^3P	-311.443844
A_1	^1D	-311.319693
A_2	^3P	-311.160710
A_2	^1D	-311.036568
B_1	^3P	-311.332431
B_1	^1D	-311.208280
B_2	^3P	-311.039037
B_2	^1D	-310.914880

The energy minima for the A_2 and B_2 states were not reached with the geometries considered; it is necessary to calculate wavefunctions at additional carbon-oxygen bond distances, but the lack of computer time prevented these additional calculations. Also additional curves should be calculated to correspond to every state for the dissociated $\text{CF}_2 + \text{O}$ geometry.

The attempts to generate the A_1 open shell ground states for the near equilibrium geometries produced surprising results. Closed shell wavefunctions resulted for all geometries with the exception of the case where the carbon-oxygen bond distance equalled 2.21858 bohrs, the equilibrium geometry. Exactly the reverse situation was anticipated since, as the carbon-oxygen bond was stretched or contracted from its equilibrium position, the electrons forming the bond should begin to take on some atomic nature, producing open shell wavefunctions. The fact that an open shell wavefunction was produced at equilibrium leads to the conclusions that open shell ground states for the A_1 symmetry should certainly exist and that an alternate procedure must be used to produce such wavefunctions. Such a procedure might be to begin a calculation using the orbitals from $\text{CF}_2 + \text{O}$ as a starting point.

Koopman's theorem⁷⁸ can be used to compare the observed ionization potentials of Thomas and Thompson³² and those calculated for the closed shell A_1 state of the equilibrium geometry. Koopman's theorem states that orbital energies or eigenvalues can be associated with the vertical ionization potentials of a molecule for which the SCF wavefunction has been obtained. The association

is made by using the highest occupied eigenvalue of the positive ion, or, alternately, multiplying the highest doubly occupied orbital eigenvalue of a given symmetry by 0.92⁷⁹ to account for the correlation energy⁸⁰ obtained on forming the positive ion. Correlation energy is the energy difference between the RHF energy and the exact nonrelativistic energy of a particular system. In the Hartree-Fock approximation scheme, the motion of each electron is solved in the presence of the average rather than the instantaneous motion of the remaining electrons. The factor of 0.92 is an attempt to empirically compensate for the lack of correlation energy in the Hartree-Fock orbitals.

Table XXIII provides a comparison between the experimental and calculated vertical ionization potentials together with the symmetries of the orbitals used to approximate the positive ion; experimental and calculated data show good agreement both numerically and in the assignments of orbital symmetries to the ionizations. However, some disagreement exists in the assignments of specific orbitals to the ionizations. The discrepancies arise because molecular orbital calculations, by their very nature, produce eigenvectors that are linear combinations of several atomic orbitals; the calculations do not restrict an eigenvector to a specific atom.

Thomas and Thompson⁷⁷ assigned the lowest experimental ionization at 13.62 electron volts (eV) to an oxygen lone pair orbital; the calculations showed this orbital was a combination of a p_y orbital on oxygen and p_z orbitals on the fluorines, z₁ - z₂.

TABLE XXIII

COMPARISON OF EXPERIMENTAL AND CALCULATED
VERTICAL IONIZATION POTENTIALS FOR CF_2^0

<u>Experimental Ionization Potential^a(eV)</u>	<u>Orbital Eigenvalue (eV)</u>	<u>Calculated Ionization Potential (eV)</u>	<u>Symmetry of Orbital</u>
13.62	-15.40	14.17	b_2
14.62	-15.67	14.42	b_1
16.6	-19.10	17.57	a_1
17.0	-20.21	18.59	a_2

^aR. K. Thomas and H. Thompson, Proc. Royal Soc. (London) A327, 13 (1972).

The ionization at 14.62 electron volts, attributed to a carbon-oxygen π bonding orbital, was shown to be a combination of carbon and oxygen p_x orbitals, $x_C + x_0$, and p_x orbitals on the fluorines, $x_1 + x_2$. The assignment of an ionization from an a_1 orbital to a nonbonding orbital on fluorine also disagreed; the calculations point to combinations of p_z orbitals on carbon and oxygen, $z_C - z_0$, and p_z orbitals on fluorine, $z_1 + z_2$. The ionization at 17.0 electron volts and attributed to a $b_1 \pi$ orbital on fluorine agrees with the calculated combination of p_x orbitals on fluorine, $x_1 - x_2$.

Relatively few calculations have been carried out on difluorocarbene. The starting point for our calculations of the dissociated CF_2O , $\text{CF}_2 + \text{O}$, was the core Hamiltonian. The first state generated was $\text{CF}_2(\text{A}_1) + \text{O}({}^3\text{P})$. Since all occupied orbitals comprising the A_1 state of CF_2 contained two electrons, no opportunity existed for the solution of an open shell ground state. An attempt was made to begin the $\text{CF}_2(\text{A}_1)$ calculation with the B_1 orbitals from the CF_2O calculation at 2.21858 bohrs; however, this attempt failed for the lack of proper symmetry blocking of the dissociated CF_2O molecule that was discussed earlier.

The initial purpose of this work was to study the dissociation of CF_2O using spin projection of the ab initio wavefunctions. When the use of the computer program for spin projection was attempted, however, it was estimated that the spin projection calculation would take ten hours for each wavefunction on the IBM 370/158 JES2/VM machine. In comparison, the spin projection calculations for the $\text{H}_2\text{O}(+)$ wavefunctions required 5.5 minutes. Clearly the

large time requirements were unacceptable.

The computer program was then modified to provide more efficient calculation of the two-electron integrals over natural orbitals; those modifications are included in the computer program listed in Appendix A. Lack of sufficient computer time made it impossible to complete the examination of the dissociation of CF_2O at this time.

The completed study of the dissociation of CF_2O will provide electronic spectra for CF_2 and CF_2O , the dissociation energy for carbonyl fluoride and, hopefully, a reasonable picture of the potential energy surface for CF_2O . Additional curves corresponding to all states of $\text{CF}_2 + \text{O}$ are expected. The potential energy surface will further provide a good test of the utility of the spin projection technique.

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XII. APPENDIX A

C PA90 - SPIN PROJECTION OF UNRESTRICTED AB INITIO WAVEFUNCTIONS DAN00010
C WRITTEN FOR AN IBM 370/158 JES2/VM (VIRTUAL MACHINE) DAN00020
C COMPUTER BY DANA A. BREWER, JOHN C. SCHUG AND BYRON H. DAN00030
C LENGSFIELD AT VIRGINIA POLYTECHNIC INSTITUTE AND STATE DAN00040
C UNIVERSITY. DAN00050
DAN00060
DAN00070
C THIS PROGRAM CONTAINS EFFICIENCY MODIFICATIONS THAT HAVE DAN00080
C BEEN TESTED FOR A MOLECULE WITH C2V SYMMETRY. DAN00090
DAN00100
C THIS SPIN PROJECTION PACKAGE IS DESIGNED TO BE COMPATIBLE DAN00110
C WITH THE POLYATOM SYSTEM OF PROGRAMS. IT REQUIRES THAT AN DAN00120
C INTEGRAL TAPE BE PROVIDED IN THE FORMAT GENERATED BY THE DAN00130
C POLYATOM INTEGRAL EVALUATION PROGRAMS. DAN00140
DAN00150
C THE OPEN SHELL MOLECULAR ORBITALS GENERATED FROM PA43 ARE ALSO DAN00160
C REQUIRED. THESE MUST BE AVAILABLE IN ONE OF THREE FORMS: DAN00170
C 1) AS CARD INPUT; 2) ON FILE 5 OF THE INTEGRAL TAPE (THE DAN00180
C INTEGRAL TAPE IS NOT FILE PROTECTED IN PA43); 3) ON A SEPARATED DAN00190
C FILE (THE INTEGRAL FILE WAS FILE PROTECTED IN PA43). DAN00200
DAN00210
C THE FINAL OUTPUT OF THE PROGRAM CONSISTS OF THE WEIGHTING DAN00220
C FACTORS FOR THE PROJECTED STATES, THE ALPHA CORRESPONDING DAN00230
C ORBITALS, THE NATURAL ORBITALS OF CHARGE AND SPIN, THE DAN00240
C PROJECTED ATOMIC SPIN DENSITIES, THE DIAGONAL COMPONENTS OF DAN00250
C THE SECOND ORDER PROJECTED CHARGE DENSITY MATRIX, AND THE DAN00260
C PROJECTED STATE ENERGIES. DAN00270
DAN00280
C THE PROGRAM MAKES USE OF A MINIMUM OF TWO TAPES. IF THE DAN00290
C INTEGRAL TAPE IS FILE PROTECTED, ONE ADDITIONAL FILE (TAPE OR DAN00300
C DISK) IS NEEDED. DAN00310
DAN00320

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C THE SUBROUTINES USED ARE - DAN00330
C PURELY FOR THE SPIN PROJECTION... DAN00340
C PA90, WATE, F, CK, SWITCH, NOINTS DAN00350
C MATRIX MANIPULATION... DAN00360
C MTBSYM, MBTSYM, MMBAT2, MULT2, MMOVE, MMATB1, MCLEAR, MCLRT, DAN00370
C MABAT DAN00380
C MATRIX OUTPUT... DAN00390
C MWRITT, MWRITE, MWRITB, MPRY1, MPRY2 DAN00400
C FILE HANDLING... DAN00410
C LAB, SEC, FILE, FOLLOW, EFSKIP, ABT, TEST2, ADDT DAN00420
C ADDITIONAL MATRIX MANIPULATION... DAN00430
C HDIAG, FMUHF, FMJUHF, FMEXTB, REORD, FMDMB, FMDTB, MOOBLK, DAN00440
C ORDREI DAN00450
C DAN00460
C DAN00470
C THE CARD INPUT IS AS FOLLOWS: DAN00480
C (1) ONE CARD (12A6) WITH THE LABEL OF THE PROBLEM DAN00490
C (2) ONE CARD (24I3) WITH THE INPUT/OUTPUT OPTIONS, ICON(1-24). DAN00500
C           ICON(3) .LT. 0 READ MOLECULAR ORBITALS FROM CARDS DAN00510
C           .EQ. 0 READ MOLECULAR ORBITALS FROM INTEGRAL TAPE DAN00520
C           .GT. 0 READ MOLECULAR ORBITALS FROM FILE 12 (INTEGRAL DAN00530
C                         TAPE IS FILE PROTECTED) DAN00540
C           ICON(4) .EQ. 0 CALCULATES A GROUND STATE WAVEFUNCTION DAN00550
C           ICON(9) .NE. 0 PRINT CHECKSUMS FROM READING TWO-ELECTRON DAN00560
C                         INTEGRALS DAN00570
C           ICON(10) .NE. 0 PRINTS FILE HANDLING INFORMATION DAN00580
C (3) ONE CARD (A6) WITH THE NAME OF THE INTEGRAL TAPE DAN00590
C (4) ONE CARD (D15.7) WITH CUT. TWO ELECTRON INTEGRALS WHOSE DAN00600
C                         DAN00610
C                         DAN00620
C                         DAN00630
C                         DAN00640

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C ABSOLUTE VALUE IS LESS THAN CUT ARE IGNORED IN FORMING THE DAN00650
C FOCK AND NATURAL ORBITAL INTEGRAL MATRICES. DAN00660
C IF ICON(3) .LT. 0 GO TO 8 DAN00670
C
C (5) ONE OR MORE CARDS (26I3) WITH ISYM, (NS(I), I=1,ISYM). ISYM DAN00680
C IS THE NUMBER OF SYMMETRY BLOCKS IN THE MOLECULAR ORBITAL DAN00690
C MATRIX. NS IS THE NUMBER OF MOLECULAR ORBITALS IN EACH DAN00700
C SYMMETRY BLOCK. DAN00710
C
C (6) AS MANY CARDS AS NEEDED (8F10.5) TO GIVE THE OCCUPATION DAN00720
C NUMBERS OF THE ALPHA MOLECULAR ORBITALS. FULL OCCUPANCY OF AND DAN00730
C ORBITAL IS 0.5. FRACTIONAL OCCUPANCY OTHER THAN 0.5 AND 0.0 DAN00740
C IS ALLOWED. DAN00750
C
C (7) AS MANY CARDS AS NEEDED (8F10.5) TO GIVE THE OCCUPATION DAN00760
C NUMBERS OF THE BETA MOLECULAR ORBITALS. FULL OCCUPANCY DAN00770
C OF AN ORBITAL IS 0.5. FRACTIONAL OCCUPANCY OTHER THAN 0.5 AND DAN00780
C 0.0 IS ALLOWED. DAN00790
C
C GO TO STEP 13. DAN00800
C
C (8) ONE CARD (2I3) WITH THE TOTAL NUMBER OF SYMMETRY ORBITALS, NR, DAN00810
C AND THE NUMBER OF BASIS FUNCTIONS, NC. DAN00820
C
C CARDS (9) AND (10) ARE REPEATED FOR EACH ITH ALPHA MOLECULAR DAN00830
C ORBITAL. DAN00840
C
C (9) ONE CARD (4X,I4,12X,D15.8,F15.8) WITH IS, EA, FR. IS IS THE DAN00850
C NUMBER OF THE ORBITAL IN THE SYMMETRY BLOCK. EA IS THE EIGEN-DAN00860
C VALUE OF THE ORBITAL AND FR IS THE OCCUPATION NUMBER OF THE DAN00870
C ORBITAL. FRACTIONAL OCCUPANCY OTHER THAN 0.5 AND 0.0 IS DAN00880

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C ALLOWED. DAN00970
C DAN00980
C (10) AS MANY ACRDS AS NEEDED (4D15.8) TO SPECIFY THE COEFFICIENTS DAN00990
C OF THE ITH MOLECULAR ORBITAL. (THESE ARE COEFFICIENTS OF A DAN01000
C NORMALIZED BASIS FUNCTION). THE EIGENVECTORS ARE READ IN AS DAN01010
C ROWS. DAN01020
C DAN01030
C CARDS (11) AND (12) ARE REPEATED FOR EACH JTH BETA MOLECULAR DAN01040
C ORBITAL. DAN01050
C DAN01060
C (11) ONE CARD (20X,D15.8,F15.8) WITH EB AND FR. EB IS THE EIGEN- DAN01070
C VALUE OF THE JTH BETA ORBITAL. FR IS THE OCCUPANCY OF THAT DAN01080
C ORBITAL. FULL OCCUPANCY IS 0.5. FRACTIONAL OCCUPANCY OTHER DAN01090
C THAN 0.5 AND 0.0 IS ALLOWED. DAN01100
C DAN01110
C (12) AS MANY CARDS AS NEEDED (4D15.8) TO SPECIFY THE COEFFICIENTS DAN01120
C OF THE JTH BETA MOLECULAR ORBITAL. (THESE ARE COEFFICIENTS DAN01130
C OF A NORMALIZED BASIS FUNCTION.) THE MOLECULAR ORBITAL DAN01140
C COEFFICIENTS ARE READ IN AS ROWS. DAN01150
C DAN01160
C (13) ONE CARD (3I5) WITH KIKMAX, THE MAXIMUM NUMBER OF PROJECTED DAN01170
C STATES THAT WILL BE CALCULATED. DAN01180
C DAN01190
C (14) ONE CARD (2I3) WITH THE ORBITAL NUMBERS FOR THE SINGLY DAN01200
C OCCUPIED ORBITALS, ASSUMING THAT THE FIRST ORBITAL OCCUPIED DAN01210
C IS NUMBERED ONE. DAN01220
C DAN01230
C DIMENSION STATEMENTS DAN01240
C DAN01250
C IMPLICIT REAL*8(A-H,O-Z) DAN01260
REAL*8 ILBL,ILAB,INTNAM,INAME(6),ILABL(12) DAN01270
C DAN01280

C LABELLED COMMON DAN01290
C DAN01300
COMMON/ZEIT/LAPSE,LAPST DAN01310
COMMON/LABELS/ILBL(12),ILAB(12) DAN01320
COMMON/IOIND/ICON(24) DAN01330
C DAN01340
C DIMENSION STATEMENTS DAN01350
C DAN01360
DIMENSION R(60,60),S(60,60),T(60,60),TT(60,60) DAN01370
DIMENSION PKD(636),VAL(636) DAN01380
DIMENSION FR(60) DAN01390
DIMENSION RR(60,60),SS(60,60) DAN01400
DIMENSION TENO(3000) DAN01410
DIMENSION NS(60),IS(60) DAN01420
DIMENSION EA(60),EB(60) DAN01430
INTEGER D2TAPE DAN01440
DATA NTAPE, D2TAPE, ITAPE/10,11,12/ DAN01450
DATA INAME/6HETA+VL,6HG-INTS,6HT-INTS,6HV-MATX,6HM-INTS/ DAN01460
C SET MISCELLANEOUS PARAMETERS DAN01470
C DAN01480
CALL ERRSET(208,500,-1,1) DAN01490
NRX=60 DAN01500
NIN=636 DAN01510
NTOP=3000 DAN01520
AD=1.00/DSQRT(2.00) DAN01530
ITR=1 DAN01540
XNA=0.00 DAN01550
XNB=0.00 DAN01560
C DAN01570
C DAN01580
READ LABEL OF PROBLEM AND INPUT/OUTPUT OPTIONS DAN01590
C DAN01600

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CALL LAB                               DAN01610
READ(5,189)INTNAM                      DAN01620
CALL TEST2(NTAPE,INTNAM)                 DAN01630
IF(ICON(3).EQ.0)ITAPE=NTAPE             DAN01640
READ(5,49)CUT                           DAN01650
WRITE(6,59)CUT                          DAN01660
IPTI=ICON(9)                           DAN01670
C                                         DAN01680
C     DA=R      DB=S      DT=T      NC=NBFNS DAN01690
C                                         DAN01700
C                                         DAN01710
C                                         DAN01720
C                                         DAN01730
C                                         DAN01740
C                                         DAN01750
C                                         DAN01760
15 CALL FILE(INAME(5),NTAPE,ILABL)       DAN01770
35 READ(ITAPE)                         DAN01780
    READ(ITAPE)                         DAN01790
    READ(ITAPE)NR,(EA(I),I=1,NR)          DAN01800
    READ(ITAPE)NRR,NC,((S(I,J),J=1,NC),I=1,NRR) DAN01810
    READ(ITAPE)NRR,(EB(I),I=1,NRR)         DAN01820
    READ(ITAPE)NRR,NCC,((TT(I,J),J=1,NCC),I=1,NRR) DAN01830
    READ(5,199)ISYM,(NS(I),I=1,ISYM)       DAN01840
    READ(5,179){FR(I),I=1,NR}              DAN01850
    DO 70 I=1,NR                         DAN01860
70 XNA=XNA+2.D0*FR(I)                   DAN01870
    NA=XNA+0.01                          DAN01880
    GO TO 45                            DAN01890
5  READ(5,199)NR,NC                     DAN01900
    DO 10 I=2,NRX                        DAN01910
10 NS(I)=0                             DAN01920

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DO 60 I=1,NR                               DAN01930
READ(5,249)IS(I),EA(I),FR(I)             DAN01940
60 READ(5,219)(S(I,J),J=1,NC)           DAN01950
      WRITE(D2TAPE)((S(I,J),J=1,NC),I=1,NR) DAN01960
      ISYM=1                                DAN01970
      NS(1)=1                                DAN01980
      DO 40 I=1,NR                           DAN01990
      XNA=XNA+2.D0*FR(I)                   DAN02000
      NA=XNA+0.01                          DAN02010
      DO 50 I=2,NR                           DAN02020
      IM=I-1                                DAN02030
      IF(IS(I).LE.IS(IM))GO TO 55          DAN02040
      NS(ISYM)=NS(ISYM)+1                  DAN02050
      GO TO 50                                DAN02060
55 ISYM=ISYM+1                            DAN02070
      NS(ISYM)=NS(ISYM)+1                  DAN02080
50 CONTINUE                                DAN02090
45 CALL MPRY1(S,EA,FR,6HALPHA ,6HORBITA,6HLS      ,1,NC,NR,NRX) DAN02100
C
C          FORM ALPHA DENSITY MATRIX, DA        DAN02110
C
C          CALL FMDMB(S,R,FR,2.0,NR,NC,NRX)      DAN02120
C          CALL MCLEAR(T,NC,NC,NRX)              DAN02130
C
C          FORM SYMMETRY BLOCKING TRANSFORMATION MATRIX DAN02140
C
C          CALL ADDT(INAME(2),NTAPE,ILABL,T,NRX,PKD,VAL,NIN) DAN02150
C          CALL MTBSYM(T,NC,NRX)                 DAN02160
C          CALL MMBAT2(T,S,NC,NC,NR,EA,NRX)       DAN02170
C          WRITE(D2TAPE)NR,NC,((S(I,J),J=1,NC),I=1,NR) DAN02180
C
C          READ BETA MOLECULAR ORBITALS          DAN02190
C
C          CALL FMDMB(S,R,FR,2.0,NR,NC,NRX)      DAN02200
C          CALL MCLEAR(T,NC,NC,NRX)              DAN02210
C          CALL MMBAT2(T,S,NC,NC,NR,EA,NRX)       DAN02220
C          WRITE(D2TAPE)NR,NC,((S(I,J),J=1,NC),I=1,NR) DAN02230
C
C          READ BETA MOLECULAR ORBITALS          DAN02240

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C
      IF(ICON(3))85,95,95
85  DO 90 I=1,NR
      READ(5,209)EA(I),FR(I)
90  READ(5,219)(T(I,J),J=1,NC)
      GO TO 105
95  DO 100 I=1,NR
      EA(I)=EB(I)
      DO 100 J=1,NC
100 T(I,J)=TT(I,J)
      READ(5,179)(FR(I),I=1,NR)
105 DO 75 I=1,NR
75  XNB=XNB+2.00*FR(I)
      NB=XNB+0.01

C
C          FORM BETA DENSITY MATRIX, DB
C
      CALL MPRY1(T,EA,FR,6HBETA ,6HORBITA,6HLS      ,1,NC,NR,NRX)      DAN02250
      CALL FMDMB(T,S,FR,2.0,NR,NC,NRX)           DAN02260
      CALL FMDTB(R,S,T,1.0,NC,NRX)             DAN02270
      WRITE(D2TAPE)NC,((R(I,J),J=1,I),I=1,NC)   DAN02280
      WRITE(D2TAPE)NC,((S(I,J),J=1,I),I=1,NC)   DAN02290
      WRITE(D2TAPE)NC,((T(I,J),J=1,I),I=1,NC)   DAN02300
      DO 30 I=1,NRX
30  FR(I)=1.00
      CALL MBTSYM( R,NC,NRX)                   DAN02310
      CALL MBTSYM( S,NC,NRX)                   DAN02320
      CALL MBTSYM( T,NC,NRX)                   DAN02330
      CALL MWRITB(R,6HALPHA ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02340
      CALL MWRITB(S,6HBETA D,6HENSTITY,6H MATRX,0,NC,NRX)      DAN02350
      CALL MWRITB(T,6HTOTAL ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02360
      CALL SEC(6HREAD D,6HENSTITY,6H MATRX)       DAN02370
      NB=XNB+0.01

C
C          FORM BETA DENSITY MATRIX, DB
C
      CALL MPRY1(T,EA,FR,6HBETA ,6HORBITA,6HLS      ,1,NC,NR,NRX)      DAN02380
      CALL FMDMB(T,S,FR,2.0,NR,NC,NRX)           DAN02390
      CALL FMDTB(R,S,T,1.0,NC,NRX)             DAN02400
      WRITE(D2TAPE)NC,((R(I,J),J=1,I),I=1,NC)   DAN02410
      WRITE(D2TAPE)NC,((S(I,J),J=1,I),I=1,NC)   DAN02420
      WRITE(D2TAPE)NC,((T(I,J),J=1,I),I=1,NC)   DAN02430
      DO 30 I=1,NRX
30  FR(I)=1.00
      CALL MBTSYM( R,NC,NRX)                   DAN02440
      CALL MBTSYM( S,NC,NRX)                   DAN02450
      CALL MBTSYM( T,NC,NRX)                   DAN02460
      CALL MWRITB(R,6HALPHA ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02470
      CALL MWRITB(S,6HBETA D,6HENSTITY,6H MATRX,0,NC,NRX)      DAN02480
      CALL MWRITB(T,6HTOTAL ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02490
      CALL SEC(6HREAD D,6HENSTITY,6H MATRX)       DAN02500
      NB=XNB+0.01

C
C          FORM BETA DENSITY MATRIX, DB
C
      CALL MPRY1(T,EA,FR,6HBETA ,6HORBITA,6HLS      ,1,NC,NR,NRX)      DAN02510
      CALL FMDMB(T,S,FR,2.0,NR,NC,NRX)           DAN02520
      CALL FMDTB(R,S,T,1.0,NC,NRX)             DAN02530
      WRITE(D2TAPE)NC,((R(I,J),J=1,I),I=1,NC)   DAN02540
      WRITE(D2TAPE)NC,((S(I,J),J=1,I),I=1,NC)   DAN02550
      WRITE(D2TAPE)NC,((T(I,J),J=1,I),I=1,NC)   DAN02560
      DO 30 I=1,NRX
30  FR(I)=1.00
      CALL MBTSYM( R,NC,NRX)                   DAN02570
      CALL MBTSYM( S,NC,NRX)                   DAN02580
      CALL MBTSYM( T,NC,NRX)                   DAN02590
      CALL MWRITB(R,6HALPHA ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02600
      CALL MWRITB(S,6HBETA D,6HENSTITY,6H MATRX,0,NC,NRX)      DAN02610
      CALL MWRITB(T,6HTOTAL ,6HDENSIT,6HY MATX,0,NC,NRX)      DAN02620
      CALL SEC(6HREAD D,6HENSTITY,6H MATRX)       DAN02630
      NB=XNB+0.01

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C
C      FORM KINETIC ENERGY MATRIX IN TT          DAN02570
C                                              DAN02580
C                                              DAN02590
C
C      CALL MCLRT(TT,NC,NRX)                      DAN02600
C      CALL ADDT(INAME(3),NTAPE,ILABL,TT,NRX,PKD,VAL,NIN) DAN02610
C
C          CALCULATE EXPECTATION VALUE OF T WITH DT; DAN02620
C          EXPECTATION VALUE STORED IN XK           DAN02630
C
C      CALL FMEXTB(TT,T,NC,NRX,1.0,XK)            DAN02640
C
C          ADD POTENTIAL ENERGY TO KINETIC ENERGY DAN02650
C
C      CALL ADDT(INAME(4),NTAPE,ILABL,TT,NRX,PKD,VAL,NIN) DAN02660
C
C          CALCULATE EXPECTATION VALUE OF T+V WITH DT DAN02670
C          STORE THIS VALUE IN XH                  DAN02680
C
C      CALL FMEXTB(TT,T,NC,NRX,1.0,XH)            DAN02690
C      CALL SEC(6HREAD 1,6H-ELEC ,6HINTS )        DAN02700
C          XKE=XH-XK                           DAN02710
C
C          READ (FROM INTEGRAL TAPE) THE NUCLEAR REPULSION ENERGY DAN02720
C          STORED IN EN                         DAN02730
C
C          CALL FILE(INAME(1),NTAPE,ILABL)          DAN02740
C          READ(NTAPE)                            DAN02750
C          READ(NTAPE)                            DAN02760
C          READ(NTAPE)                            DAN02770
C          READ(NTAPE)EN                         DAN02780
C
C          FORM MATRIX FT IN TT BY FORMING AND ADDING JT TO H ALREADY IN DAN02880

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C      TT. ALSO FORM KA IN RR AND KB IN SS.          DAN02890
C      FT=H+JT                                         DAN02900
C      JT(I,J)=SUM(OVER K,L) DT(K,L) * (IJ,KL)        DAN02910
C      KA(I,J)=SUM (OVER K,L) DA(K,L) * (IK,JL)        DAN02920
C      KB(I,J)=SUM (OVER K,L) DB(K,L) * (IK,JL)        DAN02930
C      FIRST RETAIN THE CORE HAMILTONIAN               DAN02940
C
C      WRITE(D2TAPE)NC,((TT(I,J),I=1,J),J=1,NC)       DAN02950
C      CALL MCLRT(RR,NC,NRX)                           DAN02970
C      CALL MCLRT(SS,NC,NRX)                           DAN02980
C      CALL FMJUHF(TT,RR,SS,T,R,S,NC,NRX,I NAME(6),NTAPE,ILABL,PKD,VAL,NINDAN02990
1,IPTI,CUT,IX)
C      CALL SEC(6HREAD 2,6H-ELEC ,6HINTS )             DAN03000
C      CALL MWRITT(TT,6H JT+H,6H FT MA,6HTRIX ,ITR,NC,NRX) DAN03020
C      CALL MWRITT(RR,6HKALPHA,6H KA MA,6HTRIX ,ITR,NC,NRX) DAN03030
C      CALL MWRITT(SS,6H KBETA,6H KB MA,6HTRIX ,ITR,NC,NRX) DAN03040
C
C      FORM ALPHA AND BETA UHF HAMILTONIAN MATRICES, FA AND FB,   DAN03050
C      IN RR AND SS RESPECTIVELY                         DAN03060
C      FA = FT - KA = H + JT - KA                      DAN03070
C      FB = FT - KB = H + JT - KB                      DAN03080
C
C      CALL FMFUHF(RR,SS,TT,NC,NRX)                     DAN03090
C
C      COMPUTE EXPECTATION VALUES OF FA WITH DA AND FB WITH DB   DAN03100
C
C      CALL FMEXTB(RR,R,NC,NRX,1.0,XFA)                 DAN03110
C      CALL FMEXTB(SS,S,NC,NRX,1.0,XFB)                 DAN03120
C      XF=XFA+XFB                                     DAN03130
C      WRITE(6,9)XK                                     DAN03140
C      WRITE(6,29)XKE                                    DAN03150
C      WRITE(6,19)XH                                     DAN03160

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EPI2=0.5D0*(XF-XH)          DAN03210
WVE33=XKE+EPI2              DAN03220
WE33=XH+EPI2                DAN03230
WV33=XKE+EPI2+EN            DAN03240
W33=WE33+EN                 DAN03250
WRITE(6,69)EPI2              DAN03260
WRITE(6,79)WVE33              DAN03270
WRITE(6,89)WE33              DAN03280
WRITE(6,39)EN                 DAN03290
WRITE(6,129)WV33              DAN03300
WRITE(6,149)W33               DAN03310
C
C          OBTAIN SYMMETRY BLOCKING TRANSFORMATION MATRIX.
C          STORE IN RR                         DAN03320
C
C          REWIND D2TAPE                         DAN03330
IF(ICON(3))165,175,175          DAN03340
165 READ(D2TAPE)                DAN03350
175 READ(D2TAPE)NRR,NCC,((RR(I,J),J=1,NCC),I=1,NRR)
      READ(D2TAPE)NCC,((R(J,I),J=1,I),I=1,NCC)          DAN03380
C
C          SYMMETRY BLOCK DA AND DB             DAN03390
C
READ(D2TAPE)NCC,((S(J,I),J=1,I),I=1,NCC)          DAN03400
CALL MABAT(RR,R,NR,NC,TT,NRX)                      DAN03410
CALL MABAT(RR,S,NR,NC,TT,NRX)                      DAN03420
CALL MTBSYM(R,NR,NRX)                            DAN03430
CALL MTBSYM(S,NR,NRX)                            DAN03440
C
C          FORM DA*DB*DA IN ORTHOGONAL BASIS REPRESENTATION.
C
CALL MULT2(S,R,TT,NR,NRX)                      DAN03450

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CALL MULT2(R,TT,SS,NR,NRX) DAN03530
C
C      FORM SPIN DENSITY MATRIX IN ORTHOGONAL BASIS DAN03540
C
DO 80 I=1,NR DAN03550
DO 80 J=1,NR DAN03560
80 T(I,J)=R(I,J)-S(I,J) DAN03570
IF(ICON(3))115,125,135 DAN03580
135 REWIND ITAPE DAN03590
GO TO 145 DAN03600
125 CALL FILE(INAME(5),NTAPE,ILABL) DAN03610
145 READ(ITAPE) DAN03620
READ(ITAPE)
READ(ITAPE)
READ(ITAPE)
READ(ITAPE)NRR,NCC,((S(I,J),J=1,NCC),I=1,NRR) DAN03630
GO TO 155 DAN03640
115 REWIND D2TAPE DAN03650
READ(D2TAPE)((S(I,J),J=1,NC),I=1,NR) DAN03660
READ(D2TAPE)
READ(D2TAPE)
READ(D2TAPE) DAN03670
155 CONTINUE DAN03680
C
C      FORM ALPHA CORRESPONDING ORBITALS DAN03690
C
CALL MODBLK(RR,SS,TT,NS,EA,EB,S,NR,NC,NRX,6HA.C.D.,0,0) DAN03700
CALL REORD(SS,TT,EB,EA,NR,NC,NRX) DAN03710
CALL MMOVE(SS,TT,NR,NC,NRX) DAN03720
CALL MPRY1(TT,EB,FR,6HALPHA ,6HCORR. ,6HORBS. ,0,NC,NR,NRX) DAN03730
CALL SEC(6HCALC A,6HLFA CO,6HRR ORB) DAN03740
C
C      FORM NATURAL ORBITALS OF SPIN AND STORE IN TENO DAN03750
DAN03760
DAN03770
DAN03780
DAN03790
DAN03800
DAN03810
DAN03820
DAN03830
DAN03840

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C		DAN03850
CALL MODBLK(RR,T,R,NS,FR,EA,S,NR,NC,NRX,6HN.O.S.,0,0)		DAN03860
CALL REORD(T,R,EA,FR,NR,NC,NRX)		DAN03870
CALL MPRY1(T,EA,FR,6HNATL 0,6HRBS OF,6H SPIN ,0,NC,NR,NRX)		DAN03880
CALL SEC(6HCALC N,6HATL OR,6HB SPIN)		DAN03890
AD=1.00/DSQRT(2.00)		DAN03900
DO 20 I=1,NC		DAN03910
TENO(I)=AD*(T(NC,I)+T(I,I))		DAN03920
20 TENO(NC+I)=AD*(T(NC,I)-T(I,I))		DAN03930
C		DAN03940
C FORM NATURAL ORBITALS OF CHARGE		DAN03950
C		DAN03960
READ(D2TAPE)NCC,((T(J,I),J=1,I),I=1,NCC)		DAN03970
CALL MABAT(RR,T,NR,NC,SS,NRX)		DAN03980
CALL MODBLK(RR,T,R,NS,FR,EA,S,NR,NC,NRX,6HN.O.C.,0,0)		DAN03990
CALL REORD(T,R,EA,FR,NR,NC,NRX)		DAN04000
CALL MMOVE(T,R,NR,NC,NRX)		DAN04010
CALL MPRY1(R,EA,FR,6HNATL 0,6HRBS OF,6H CHG ,0,NC,NR,NRX)		DAN04020
CALL SEC(6HCALC N,6HATL OR,6HBS CHG)		DAN04030
C		DAN04040
C SWITCH ROWS AND COLUMNS.		DAN04050
C THE SPIN PROJECTION IS PERFORMED WITH THE ORBITALS AS		DAN04060
C COLUMNS.		DAN04070
C		DAN04080
CALL SWITCH(TT,T,NR,NC,NRX)		DAN04090
CALL SWITCH(R,T,NR,NC,NRX)		DAN04100
CALL MCLEAR(S,NRX,NRX,NRX)		DAN04110
CALL MCLEAR(T,NRX,NRX,NRX)		DAN04120
CALL MCLEAR(SS,NRX,NRX,NRX)		DAN04130
READ(D2TAPE)NCC,((RR(I,J),J=1,I),I=1,NCC)		DAN04140
CALL MWRITB(RR,6HCORE H,6HAMILTO,6HNIAN ,1,NC,NRX)		DAN04150
CALL MBTSYM(RR,NC,NRX)		DAN04160

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REWIND D2TAPE DAN04170
C
C      READY TO PERFORM SPIN PROJECTION DAN04180
C      MATRIX OCCUPATION (IN ATOMIC BASIS): DAN04190
C      TT = A.C.O. EIGENVECTORS DAN04200
C      EB = A.C.O. EIGENVALUES DAN04210
C      R = N.O.C. EIGENVECTORS DAN04220
C      EA = N.O.C. EIGENVALUES DAN04230
C      T = EMPTY DAN04250
C      X = EMPTY DAN04260
C      S = EMPTY DAN04270
C      RR = CORE HAMILTONIAN DAN04280
C      SS = EMPTY DAN04290
C      X1 = EMPTY DAN04300
C                                         DAN04310
C
CALL WATE(S,SS,R,TT,RR,TENO,EB,T(1,1),T(1,2),T(1,3),T(1,4),EA,T(1,DAN04320
15),T(1,6),T(1,7),T(1,8),T(1,9),T(1,10),PKD,VAL,CUT,EN,INAME,NTAPE,DAN04330
1NRX,NTOP,NIN,NC,NA,NB,NR) DAN04340
CALL FOLLOW DAN04350
9 FORMAT(' ','' KINETIC ENERGY, T = ',30X,1PD20.10) DAN04360
19 FORMAT(' ','' ONE ELECTRON ENERGY, H = T+V(1) = ',16X,1PD20.10) DAN04370
29 FORMAT(' ','' ONE ELECTRON POTENTIAL ENERGY, V(1) = ',12X,1PD20.10) DAN04380
39 FORMAT(' ','' NUCLEAR REPULSION ENERGY, V(N) = ',17X,1PD20.10) DAN04390
49 FORMAT(D15.7) DAN04400
59 FORMAT('0',''TWO-ELECTRON INTEGRAL CUTOFF = ',1PD12.4) DAN04410
69 FORMAT(' ','' TWO ELECTRON POTENTIAL ENERGY, V(1,2) = ',10X,
11PD20.10) DAN04420
79 FORMAT(' ','' ELECTRONIC PCTENTIAL ENERGY, VIE) = V(1)+V(1,2) = ', DAN04430
11PD20.10) DAN04440
89 FORMAT(' ','' ELECTRONIC ENERGY, E(E) = H+V(1,2) = ',13X,1PD20.10) DAN04450
129 FORMAT(' ','' POTENTIAL ENERGY, V = V(E)+V(N) = ',16X,1PD20.10) DAN04460
149 FORMAT(' ','' TOTAL ENERGY, E = E(E)+V(N) = ',20X,1PD20.10) DAN04470

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169 FORMAT('0','READ ERROR ON D2TAPE') DAN04490
179 FORMAT(8F10.5) DAN04500
189 FORMAT(A6) DAN04510
199 FORMAT(26I3) DAN04520
209 FORMAT(20X,D15.8,F15.8) DAN04530
219 FORMAT(4D15.8) DAN04540
229 FORMAT('0','NUMBER OF ROWS IN BETA MOLECULAR ORBITALS .NE. NUMBER DAN04550
    10F ROWS IN ALPHA MOLECULAR ORBITALS') DAN04560
239 FORMAT('0','NUMBER OF COLUMNS IN BETA MOLECULAR ORBITALS .NE. NO 0DAN04570
    1F COLUMNS IN ALPHA MOLECULAR ORBITALS') DAN04580
249 FORMAT(4X,I4,12X,D15.8,F15.8) DAN04590
STOP DAN04600
END DAN04610
BLOCK DATA DAN04620
REAL*8 ILAB,ILBL DAN04630
COMMON/LABELS/ILBL(12),ILAB(12) DAN04640
DATA ILAB/6H PA90 ,6H UNRE,6HSTRICT,6HED HAR,6HTREE-F,6HOCK SP,6HDAN04650
1IN PRO,6HJECTIO,6HN METH,6HOD L.C,6H.A.O. ,6HTEST / DAN04660
END DAN04670
CNOINTS      SUBROUTINE NPOINTS DAN04680
SUBROUTINE NPOINTS(EA,PKLABL,VALUEM,C,T,CUTLO,INAME,NB,MNM,MO,M,NINDAN04690
1TS,NINMAX,NRX,NTOP,NTAPE) DAN04700
IMPLICIT REAL *8(A-H,O-Z) DAN04710
DIMENSION PKLABL(NINMAX),VALUEM(NINMAX),C(NRX,NRX),T(NTOP) DAN04720
DIMENSION EA(NRX) DAN04730
DIMENSION IPRT(36) DAN04740
REAL *8 INTNAM,INAME,ILAB,ILBL(12) DAN04750
COMMON/IOIND/ICON(24) DAN04760
COMMON/LABELS/ILBL(12),ILAB(12) DAN04770
DIMENSION INAME(6) DAN04780
NRECNT=0 DAN04790
NMINNW=0 DAN04800

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IRC=1 DAN04810
IFLAG=0 DAN04820
IPTI=ICON(9) DAN04830
C DAN04840
C PRINT HEADER IF CHECK SUM FLAG IS ON DAN04850
C DAN04860
C IF(IPTI.EQ.0)GO TO 70 DAN04870
WRITE(6,19) DAN04880
70 CONTINUE DAN04890
READ(5,59)NSING1,NSING2 DAN04900
59 FORMAT(2I3) DAN04910
DO 40 I=1,NTOP DAN04920
40 T(I)=0.00 DAN04930
C DAN04940
C POSITION TAPE TO READ TWO-ELECTRON INTEGRALS DAN04950
C DAN04960
CALL FILE(INAME(6),NTAPE,ILABL) DAN04970
20 IF(IFLAG)21,21,76 DAN04980
21 READ(NTAPE)NINTS,LSTRCD,PKLABL,VALUEM DAN04990
IF(LSTRCD.NE.0)IFLAG=1 DAN05000
NRECNT=NRECNT+1 DAN05010
NMINNW=NMINNW+NINTS DAN05020
IF(IPTI.EQ.0)GO TO 75 DAN05030
IF(IRC.EQ.1)IPRT(1)=NRECNT DAN05040
CALL UNPACK(PKLABL(1),IA,JA,KA,LA,IZ,ITA) DAN05050
CALL UNPACK (PKLABL(NINTS),IB,JB,KB,LB,IZ,ITB) DAN05060
IPRT(IRC+1)=JA DAN05070
IPRT(IRC+2)=LA DAN05080
IPRT(IRC+3)=NINTS DAN05090
IPRT(IRC+4)=JB DAN05100
IPRT(IRC+5)=LB DAN05110
IRC=IRC+5 DAN05120

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IF(IRC.LT.36)GO TO 75                               DAN05130
WRITE(6,29)(IPRT(MN),MN=1,IRC)                   DAN05140
IRC=1                                              DAN05150
75 IF(NINTS.GT.NINMAX.OR.NINTS.LE.0)GO TO 30      DAN05160
MN1=1                                              DAN05170
55 XI=VALUEM(MN1)                                 DAN05180
JCTR=1                                              DAN05190
CALL UNPACK(PKLABL(MN1),I1,J1,K1,L1,MU,I2)       DAN05200
52 IF(MN1.EQ.NINTS)GO TO 50                         DAN05210
53 IF(MN1.GE.NINTS)GO TO 50                         DAN05220
CALL UNPACK(PKLABL(MN1+1),I2,J2,K2,L2,MU2,I2Z)    DAN05230
IF(I2Z)51,50,51                                     DAN05240
51 JCTR=JCTR+1                                       DAN05250
MN1=MN1+1                                         DAN05260
GO TO 53                                           DAN05270
50 IF(DABS(XI).LT.CUTLG)GO TO 10                  DAN05280
XI=XI*jctr                                         DAN05290
DAN05300
C          SKIP THE INTEGRAL IF ITS VALUE IS SMALL   DAN05310
C
X2=2.D0*XI                                         DAN05320
X4=4.D0*XI                                         DAN05330
X8=8.D0*XI                                         DAN05340
GO TO (1100,200,300,400,500,700,600,600,100,100,100,100,100,100), DAN05350
1MU
100 J=0
DO 140 K=1,NB
KP=M-K+1
A1=C(I1,K)
A2=C(J1,K)
A3=C(K1,K)
A4=C(L1,K)

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118 IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING1)	DAN05450
1GO TO 116	DAN05460
IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING2)	DAN05470
1GO TO 116	DAN05480
IF(DABS(A3).LE.1.D-08.OR.DABS(A4).LE.1.D-08.AND.K.NE.NSING2)	DAN05490
1GO TO 115	DAN05500
IF(DABS(A3).LE.1.D-08.OR.DABS(A4).LE.1.D-08.AND.K.NE.NSING1)	DAN05510
1GO TO 115	DAN05520
GO TO 117	DAN05530
116 J=J+1	DAN05540
P1=0.D0	DAN05550
P2=A3*A4	DAN05560
IF(K.LT.MNN)GO TO 110	DAN05570
IF(EA(K).GT.1.999999)GO TO 110	DAN05580
J=J+3	DAN05590
A5=C(I1,KP)	DAN05600
A6=C(J1,KP)	DAN05610
A7=C(K1,KP)	DAN05620
A8=C(L1,KP)	DAN05630
P3=0.D0	DAN05640
P4=A7*A8	DAN05650
P31=0.D0	DAN05660
P32=0.D0	DAN05670
P33=A3*A8	DAN05680
P34=A4*A7	DAN05690
GO TO 110	DAN05700
115 J=J+1	DAN05710
P1=A1*A2	DAN05720
P2=0.D0	DAN05730
IF(K.LT.MNN)GO TO 110	DAN05740
IF(EA(K).GT.1.999999)GO TO 110	DAN05750
J=J+3	DAN05760

A5=C(I1,KP)	DAN05770
A6=C(J1,KP)	DAN05780
A7=C(K1,KP)	DAN05790
A8=C(L1,KP)	DAN05800
P3=A5*A6	DAN05810
P4=0.00	DAN05820
P31=A1*A6	DAN05830
P32=A2*A5	DAN05840
P33=0.00	DAN05850
P34=0.00	DAN05860
GO TO 110	DAN05870
117 P1=A1*A2	DAN05880
P2=A3*A4	DAN05890
J=J+1	DAN05900
T(J)=T(J)+X8*P1*p2	DAN05910
IF(K.LT.MNM)GO TO 110	DAN05920
IF(EA(K).GT.1.999999)GO TO 110	DAN05930
A5=C(I1,KP)	DAN05940
A6=C(J1,KP)	DAN05950
A7=C(K1,KP)	DAN05960
A8=C(L1,KP)	DAN05970
P3=A5*A6	DAN05980
P4=A7*A8	DAN05990
P31=A1*A6	DAN06000
P32=A2*A5	DAN06010
P33=A3*A8	DAN06020
P34=A4*A7	DAN06030
Q=(P31+P32)*(P33+P34)	DAN06040
J=J+1	DAN06050
T(J)=X8*P3*p4+T(J)	DAN06060
J=J+1	DAN06070
T(J)=T(J)+X4*Q	DAN06080

J=J+1	DAN06090
T(J)=T(J)+X8*(P1*p4+p2*p3)	DAN06100
110 KAND=K+1	DAN06110
IF(K.EQ.NB)GO TO 130	DAN06120
DO 120 LN=KAND,NB	DAN06130
LP=M-LN+1	DAN06140
A9=C(I1,LN)	DAN06150
A10=C(J1,LN)	DAN06160
A11=C(K1,LN)	DAN06170
A12=C(L1,LN)	DAN06180
P7=A11*A12	DAN06190
P8=A9*A10	DAN06200
P13=A1*A10	DAN06210
P14=A2*A9	DAN06220
P15=A11*A4	DAN06230
P16=A12*A3	DAN06240
J=J+1	DAN06250
T(J)=T(J)+X8*(P1*p7+p2*p8)	DAN06260
J=J+1	DAN06270
T(J)=T(J)+X4*(P13+P14)*(P15+P16)	DAN06280
IF(LN.LT.MNM)GO TO 120	DAN06290
IF(EA(LN).GT.1.999999)GO TO 120	DAN06300
A13=C(I1,LP)	DAN06310
A14=C(J1,LP)	DAN06320
A15=C(K1,LP)	DAN06330
A16=C(L1,LP)	DAN06340
P5=A15*A16	DAN06350
P6=A13*A14	DAN06360
P9=A1*A14	DAN06370
P10=A13*A2	DAN06380
P11=A15*A4	DAN06390
P12=A16*A3	DAN06400

P17=A7*A16	DAN06410
P18=A8*A15	DAN06420
P19=A13*A6	DAN06430
P20=A5*A14	DAN06440
J=J+1	DAN06450
T(J)=T(J)+X8*(P1*P5+P2*P6)	DAN06460
J=J+1	DAN06470
T(J)=T(J)+X4*(P9+P10)*(P11+P12)	DAN06480
IF(K.LT.MNM)GO TO 120	DAN06490
IF(EA(K).GT.1.999999)GO TO 120	DAN06500
P35=A9*A6	DAN06510
P36=A5*A10	DAN06520
P37=A7*A12	DAN06530
P38=A8*A11	DAN06540
J=J+1	DAN06550
T(J)=T(J)+X8*(P8*P4+P7*P3)	DAN06560
J=J+1	DAN06570
T(J)=T(J)+X4*(P35+P36)*(P37+P38)	DAN06580
J=J+1	DAN06590
T(J)=T(J)+X8*(P3*P5+P4*P6)	DAN06600
J=J+1	DAN06610
T(J)=T(J)+X4*(P19+P20)*(P17+P18)	DAN06620
J=J+1	DAN06630
T(J)=T(J)+X4*((P9+P10)*(P37+P38)+(P12+P11)*(P35+P36))	DAN06640
J=J+1	DAN06650
T(J)=T(J)+X4*((P13+P14)*(P17+P18)+(P15+P16)*(P19+P20))	DAN06660
120 CONTINUE	DAN06670
130 IF(MO.LE.0)GO TO 140	DAN06680
DO 135 LQ=1,MO	DAN06690
LN=LQ+NB	DAN06700
A9=C(I1,LN)	DAN06710
A10=C(J1,LN)	DAN06720

A11=C(K1,LN)	DAN06730
A12=C(L1,LN)	DAN06740
P21=A11*A12	DAN06750
P22=A9*A10	DAN06760
P23=A1*A10	DAN06770
P24=A9*A2	DAN06780
P27=A11*A4	DAN06790
P28=A12*A3	DAN06800
J=J+1	DAN06810
T(J)=T(J)+X8*(P1*P21+P2*P22)	DAN06820
J=J+1	DAN06830
T(J)=T(J)+X4*(P23+P24)*(P27+P28)	DAN06840
IF(K.LT.MNM)GO TO 135	DAN06850
IF(EA(K).GT.1.999999)GO TO 135	DAN06860
P25=A11*A8	DAN06870
P26=A7*A12	DAN06880
P29=A5*A10	DAN06890
P30=A6*A9	DAN06900
J=J+1	DAN06910
T(J)=T(J)+X8*(P3*P21+P4*P22)	DAN06920
J=J+1	DAN06930
T(J)=T(J)+X4*(P29+P30)*(P25+P26)	DAN06940
J=J+1	DAN06950
T(J)=T(J)+X4*[(P23+P24)*(P25+P26)+(P27+P28)*(P29+P30)]	DAN06960
135 CONTINUE	DAN06970
140 CONTINUE	DAN06980
IF(MO.LE.1)GO TO 160	DAN06990
DO 150 KQ=1,MO	DAN07000
K=KQ+N6	DAN07010
IF(KQ.EQ.MO)GO TO 150	DAN07020
KQ1=KQ+1	DAN07030
DO 145 LQ=KQ1,MO	DAN07040

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LN=LQ+NB          DAN07050
A1=C(I1,K)        DAN07060
A2=C(J1,K)        DAN07070
A3=C(K1,K)        DAN07080
A4=C(L1,K)        DAN07090
A9=C(I1,LN)       DAN07100
A10=C(J1,LN)      DAN07110
A11=C(K1,LN)      DAN07120
A12=C(L1,LN)      DAN07130
J=J+1             DAN07140
T(J)=T(J)+X8*(A1*A2*A11*A12+A3*A4*A9*A10)  DAN07150
J=J+1             DAN07160
145 T(J)=T(J)+X4*(A1*A10+A9*A2)*(A11*A4+A12*A3)  DAN07170
150 CONTINUE       DAN07180
160 GO TO 6000     DAN07190
200 J=0             DAN07200
DO 240 K=1,NB      DAN07210
KP=M-K+1           DAN07220
A1=C(I1,K)         DAN07230
A2=C(J1,K)         DAN07240
218 IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING1)  DAN07250
1GO TO 216          DAN07260
IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING2)  DAN07270
1GO TO 216          DAN07280
GO TO 217          DAN07290
216 J=J+1           DAN07300
P1=0.D0             DAN07310
IF(K.LT.MNM)GO TO 210  DAN07320
IF(EA(K).GT.1.999999)GO TO 210  DAN07330
J=J+3               DAN07340
A5=C(I1,KP)         DAN07350
A6=C(J1,KP)         DAN07360

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P3=0.D0	DAN07370
P31=0.D0	DAN07380
P32=0.D0	DAN07390
GO TO 210	DAN07400
217 P1=A1*A2	DAN07410
J=J+1	DAN07420
T(J)=T(J)+X4*P1*P1	DAN07430
IF(K.LT.MNM)GO TO 210	DAN07440
IF(EA(K).GT.1.999999)GO TO 210	DAN07450
A5=C(I1,KP)	DAN07460
A6=C(J1,KP)	DAN07470
P3=A5*A6	DAN07480
P31=A1*A6	DAN07490
P32=A2*A5	DAN07500
Q=(P31+P32)**2	DAN07510
J=J+1	DAN07520
T(J)=T(J)+X4*P3*P3	DAN07530
J=J+1	DAN07540
T(J)=T(J)+X2*Q	DAN07550
J=J+1	DAN07560
T(J)=T(J)+X8*P1*P3	DAN07570
210 KAND=K+1	DAN07580
IF(K.EQ.NB)GO TO 230	DAN07590
DO 220 LN=KAND,NB	DAN07600
LP=M-LN+1	DAN07610
A9=C(I1,LN)	DAN07620
A10=C(J1,LN)	DAN07630
P7=A9*A10	DAN07640
P13=A1*A10	DAN07650
P14=A2*A9	DAN07660
J=J+1	DAN07670
T(J)=T(J)+X8*P1*P7	DAN07680

J=J+1	DAN07690
T(J)=T(J)+X2*(P13+P14)**2	DAN07700
IF(LN.LT.MNM)GO TO 220	DAN07710
IF(EA(LN).GT.1.999999)GO TO 220	DAN07720
A13=C(I1,LP)	DAN07730
A14=C(J1,LP)	DAN07740
P5=A13*A14	DAN07750
P9=A1*A14	DAN07760
P10=A13*A2	DAN07770
P17=A5*A14	DAN07780
P18=A6*A13	DAN07790
J=J+1	DAN07800
T(J)=T(J)+X8*p1*p5	DAN07810
J=J+1	DAN07820
T(J)=T(J)+X2*(P9+P10)**2	DAN07830
IF(K.LT.MNM)GO TO 220	DAN07840
IF(EA(K).GT.1.999999)GO TO 220	DAN07850
P35=A9*A6	DAN07860
P36=A5*A10	DAN07870
J=J+1	DAN07880
T(J)=T(J)+X8*p3*p7	DAN07890
J=J+1	DAN07900
T(J)=T(J)+X2*(P35+P36)**2	DAN07910
J=J+1	DAN07920
T(J)=T(J)+X8*p3*p5	DAN07930
J=J+1	DAN07940
T(J)=T(J)+X2*(P17+P18)**2	DAN07950
J=J+1	DAN07960
T(J)=T(J)+X4*(P9+P10)*(P35+P36)	DAN07970
J=J+1	DAN07980
T(J)=T(J)+X4*(P13+P14)*(P17+P18)	DAN07990
220 CONTINUE	DAN08000

230 IF(MO.LE.0)GO TO 240	DAN08010
DO 235 LQ=1,MO	DAN08020
LN=LQ+NB	DAN08030
A9=C(I1,LN)	DAN08040
A10=C(J1,LN)	DAN08050
P21=A10*A9	DAN08060
P23=A1*A10	DAN08070
P24=A9*A2	DAN08080
J=J+1	DAN08090
T(J)=T(J)+X8*P1*P21	DAN08100
J=J+1	DAN08110
T(J)=T(J)+X2*(P23+P24)**2	DAN08120
IF(K.LT.MNM)GO TO 235	DAN08130
IF(EA(K).GT.1.999999)GO TO 235	DAN08140
P25=A9*A6	DAN08150
P26=A5*A10	DAN08160
J=J+1	DAN08170
T(J)=T(J)+X8*P3*P21	DAN08180
J=J+1	DAN08190
T(J)=T(J)+X2*(P25+P26)**2	DAN08200
J=J+1	DAN08210
T(J)=T(J)+X4*(P23+P24)*(P25+P26)	DAN08220
235 CONTINUE	DAN08230
240 CONTINUE	DAN08240
IF(MO.LE.1)GO TO 260	DAN08250
DO 250 KQ=1,MO	DAN08260
K=KQ+NB	DAN08270
IF(KQ.EQ.MO)GO TO 250	DAN08280
KQ1=KQ+1	DAN08290
DO 245 LQ=KQ1,MO	DAN08300
LN=LQ+NB	DAN08310
A1=C(I1,K)	DAN08320

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A2=C(J1,K)                               DAN08330
A9=C(I1,LN)                             DAN08340
A10=C(J1,LN)                            DAN08350
J=J+1                                    DAN08360
T(J)=T(J)+X8*A1*A2*A9*A10               DAN08370
J=J+1                                    DAN08380
245 T(J)=T(J)+X2*(A1*A10+A2*A9)**2      DAN08390
250 CONTINUE                            DAN08400
260 GO TO 6000                           DAN08410
1100 J=0                                 DAN08420
      DO 1140 K=1,NB                     DAN08430
      KP=M-K+1                           DAN08440
      A1=C(I1,K)                         DAN08450
1118 IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING1)GO TO 1116   DAN08460
      IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING2)GO TO 1116   DAN08470
      GO TO 1117                           DAN08480
1116 J=J+1                               DAN08490
      P1=0.D0                            DAN08500
      IF(K.LT.MNM)GO TO 1110             DAN08510
      IF(EA(K).GT.1.999999)GO TO 1110   DAN08520
      J=J+3                               DAN08530
      A5=0.D0                            DAN08540
      P3=0.D0                            DAN08550
      P31=0.D0                           DAN08560
      GO TO 1110                          DAN08570
1117 P1=A1*A1                           DAN08580
      J=J+1                               DAN08590
      T(J)=T(J)+XI*P1*P1                 DAN08600
      IF(K.LT.MNM)GO TO 1110             DAN08610
      IF(EA(K).GT.1.999999)GO TO 1110   DAN08620
      A5=C(I1,KP)                         DAN08630
      P3=A5*A5                           DAN08640

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P31=A1*A5	DAN08650
J=J+1	DAN08660
T(J)=T(J)+X1*P3*P3	DAN08670
J=J+1	DAN08680
T(J)=T(J)+X2*P31*P31	DAN08690
J=J+1	DAN08700
T(J)=T(J)+X2*P1*P3	DAN08710
1110 KAND=K+1	DAN08720
IF(K.EQ.NB)GO TO 1130	DAN08730
DO 1120 LN=KAND,NB	DAN08740
LP=M-LN+1	DAN08750
A9=C(I1,LN)	DAN08760
P7=A9*A9	DAN08770
P13=A1*A9	DAN08780
J=J+1	DAN08790
T(J)=T(J)+X2*P1*P7	DAN08800
J=J+1	DAN08810
T(J)=T(J)+X2*P13**2	DAN08820
IF(LN.LT.MNM)GO TO 1120	DAN08830
IF(EA(LN).GT.1.999999)GO TO 1120	DAN08840
A13=C(I1,LP)	DAN08850
P5=A13*A13	DAN08860
P9=A1*A13	DAN08870
P17=A5*A13	DAN08880
J=J+1	DAN08890
T(J)=T(J)+X2*P1*P5	DAN08900
J=J+1	DAN08910
T(J)=T(J)+X2*P9**2	DAN08920
IF(K.LT.MNM)GO TO 1120	DAN08930
IF(EA(K).GT.1.999999)GO TO 1120	DAN08940
P35=A9*A5	DAN08950
J=J+1	DAN08960

T(J)=T(J)+X2*P3*p7	DAN08970
J=J+1	DAN08980
T(J)=T(J)+X2*p35**2	DAN08990
J=J+1	DAN09000
T(J)=T(J)+X2*p3*p5	DAN09010
J=J+1	DAN09020
T(J)=T(J)+X2*p17**2	DAN09030
J=J+1	DAN09040
T(J)=T(J)+X4*p9*p35	DAN09050
J=J+1	DAN09060
T(J)=T(J)+X4*p13*p17	DAN09070
1120 CONTINUE	DAN09080
1130 IF(M0.LE.0)GO TO 1140	DAN09090
DO 1135 LQ=1,M0	DAN09100
LN=LQ+N8	DAN09110
A9=C(I1,LN)	DAN09120
P21=A9*A9	DAN09130
P23=A1*A9	DAN09140
J=J+1	DAN09150
T(J)=T(J)+X2*p1*p21	DAN09160
J=J+1	DAN09170
T(J)=T(J)+X2*p23**2	DAN09180
IF(K.LT.MNM)GO TO 1135	DAN09190
IF(EA(K).GT.1.999999)GO TO 1135	DAN09200
P25=A9*A5	DAN09210
J=J+1	DAN09220
T(J)=T(J)+X2*p3*p21	DAN09230
J=J+1	DAN09240
T(J)=T(J)+X2*p25**2	DAN09250
J=J+1	DAN09260
T(J)=T(J)+X4*p23*p25	DAN09270
1135 CONTINUE	DAN09280

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1140 CONTINUE                               DAN09290
    IF(M0.LE.1)GO TO 1160                   DAN09300
    DO 1150 KQ=1,M0                         DAN09310
    K=KQ+NB                                 DAN09320
    IF(KQ.EQ.M0)GO TO 1150                   DAN09330
    KQ1=KQ+1                                DAN09340
    DO 1145 LQ=KQ1,M0                         DAN09350
    LN=LQ+NB                                 DAN09360
    A1=C(I1,K)                                DAN09370
    A9=C(I1,LN)                                DAN09380
    J=J+1                                     DAN09390
    T(J)=T(J)+X2*(A1**2)*(A9**2)             DAN09400
    J=J+1                                     DAN09410
1145 T(J)=T(J)+X2*(A1**2)*(A9**2)           DAN09420
1150 CONTINUE                               DAN09430
1160 GO TO 6000                            DAN09440
300  J=0                                     DAN09450
    DO 340 K=1,NB                           DAN09460
    KP=M-K+1                                DAN09470
    A1=C(I1,K)                                DAN09480
    A3=C(K1,K)                                DAN09490
318  IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING1)GO TO 316   DAN09500
    IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING2)GO TO 316   DAN09510
    IF(DABS(A3).LE.1.D-08.AND.K.NE.NSING1)GO TO 315   DAN09520
    IF(DABS(A3).LE.1.D-08.AND.K.NE.NSING2)GO TO 315   DAN09530
    GO TO 317                                DAN09540
316  J=J+1                                     DAN09550
    P1=0.D0                                    DAN09560
    P2=A3*A3                                  DAN09570
    IF(K.LT.MNM)GO TO 310                    DAN09580
    IF(EA(K).GT.1.999999)GO TO 310          DAN09590
    J=J+3                                     DAN09600

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A5=0.D0	DAN09610
A7=C(K1,KP)	DAN09620
P3=0.D0	DAN09630
P4=A7*A7	DAN09640
P31=0.D0	DAN09650
P33=A3*A7	DAN09660
GO TO 310	DAN09670
315 J=J+1	DAN09680
P1=A1*A1	DAN09690
P2=0.D0	DAN09700
IF(K.LT.MNM)GO TO 310	DAN09710
IF(EA(K).GT.1.999999)GO TO 310	DAN09720
J=J+3	DAN09730
A5=C(I1,KP)	DAN09740
A7=0.D0	DAN09750
P3=A5*A5	DAN09760
P4=0.D0	DAN09770
P31=A1*A5	DAN09780
P33=0.D0	DAN09790
GO TO 310	DAN09800
317 P1=A1*A1	DAN09810
P2=A3*A3	DAN09820
J=J+1	DAN09830
T(J)=T(J)+X2*P1*P2	DAN09840
IF(K.LT.MNM)GO TO 310	DAN09850
IF(EA(K).GT.1.999999)GO TO 310	DAN09860
A5=C(I1,KP)	DAN09870
A7=C(K1,KP)	DAN09880
P3=A5*A5	DAN09890
P4=A7*A7	DAN09900
P31=A1*A5	DAN09910
P33=A3*A7	DAN09920

J=J+1	DAN09930
T(J)=X2*p3*p4+t(j)	DAN09940
J=J+1	DAN09950
T(J)=T(J)+X4*p31*p33	DAN09960
J=J+1	DAN09970
T(J)=T(J)+X2*(P1*p4+p2*p3)	DAN09980
310 KAND=K+1	DAN09990
IF(K.EQ.NB)GO TO 330	DAN10000
DO 320 LN=KAND,NB	DAN10010
LP=M-LN+1	DAN10020
A9=C(I1,LN)	DAN10030
A11=C(K1,LN)	DAN10040
P7=A11*A11	DAN10050
P8=A9*A9	DAN10060
P13=A1*A9	DAN10070
P15=A11*A3	DAN10080
J=J+1	DAN10090
T(J)=T(J)+X2*(P1*p7+p2*p8)	DAN10100
J=J+1	DAN10110
T(J)=T(J)+X4*p13*p15	DAN10120
IF(LN.LT.MNM)GO TO 320	DAN10130
IF(EA(LN).GT.1.999999)GO TO 320	DAN10140
A13=C(I1,LP)	DAN10150
A15=C(K1,LP)	DAN10160
P5=A15*A15	DAN10170
P6=A13*A13	DAN10180
P9=A1*A13	DAN10190
P11=A15*A3	DAN10200
P17=A7*A15	DAN10210
P19=A13*A5	DAN10220
J=J+1	DAN10230
T(J)=T(J)+X2*(P1*p5+p2*p6)	DAN10240

J=J+1	DAN10250
T(J)=T(J)+X4*P9*P11	DAN10260
IF(K.LT.MNM)GO TO 320	DAN10270
IF(EA(K).GT.1.999999)GO TO 320	DAN10280
P35=A9*A5	DAN10290
P37=A7*A11	DAN10300
J=J+1	DAN10310
T(J)=T(J)+X2*(P8*P4+P7*P3)	DAN10320
J=J+1	DAN10330
T(J)=T(J)+X4*P35*P37	DAN10340
J=J+1	DAN10350
T(J)=T(J)+X2*(P3*P5+P4*P6)	DAN10360
J=J+1	DAN10370
T(J)=T(J)+X4*P19*P17	DAN10380
J=J+1	DAN10390
T(J)=T(J)+X4*(P9*P37+P11*P35)	DAN10400
J=J+1	DAN10410
T(J)=T(J)+X4*(P13*P17+P15*P19)	DAN10420
320 CONTINUE	DAN10430
330 IF(MO.LE.0)GO TO 340	DAN10440
DO 335 LQ=1,MO	DAN10450
LN=LQ+NB	DAN10460
A9=C(I1,LN)	DAN10470
A11=C(K1,LN)	DAN10480
P21=A11*A11	DAN10490
P22=A9*A9	DAN10500
P23=A1*A9	DAN10510
P27=A11*A3	DAN10520
J=J+1	DAN10530
T(J)=T(J)+X2*(P1*P21+P2*P22)	DAN10540
J=J+1	DAN10550
T(J)=T(J)+X4*P23*P27	DAN10560

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IF(K.LT.MNM)GO TO 335          DAN10570
IF(EA(K).GT.1.999999)GO TO 335   DAN10580
P25=A11*A7                      DAN10590
P29=A5*A9                        DAN10600
J=J+1                            DAN10610
T(J)=T(J)+X2*(P3*P21+P4*P22)    DAN10620
J=J+1                            DAN10630
T(J)=T(J)+X4*P25*P29            DAN10640
J=J+1                            DAN10650
T(J)=T(J)+X4*(P23*P25+P27*P29)  DAN10660
335 CONTINUE                      DAN10670
340 CONTINUE                      DAN10680
IF(MO.LE.1)GO TO 360            DAN10690
DO 350 KQ=1,MO                  DAN10700
K=KQ+N8                         DAN10710
IF(KQ.EQ.MO)GO TO 350            DAN10720
KQ1=KQ+1                         DAN10730
DO 345 LQ=KQ1,MO                DAN10740
LN=LQ+N8                         DAN10750
A1=C(I1,K)                       DAN10760
A3=C(K1,K)                       DAN10770
A9=C(I1,LN)                       DAN10780
A11=C(K1,LN)                      DAN10790
J=J+1                            DAN10800
T(J)=T(J)+X2*(A1*A1*A11*A11+A3*A3*A9*A9)  DAN10810
J=J+1                            DAN10820
345 T(J)=T(J)+X4*A1*A9*A3*A11  DAN10830
350 CONTINUE                      DAN10840
360 GO TO 6000                  DAN10850
400 J=0                           DAN10860
DO 440 K=1,N8                  DAN10870
KP=M-K+1                         DAN10880

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A1=C(I1,K)	DAN10890
A4=C(L1,K)	DAN10900
418 IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING1)GO TO 416	DAN10910
IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING2)GO TO 416	DAN10920
IF(DABS(A4).LE.1.D-08.AND.K.NE.NSING1)GO TO 415	DAN10930
IF(DABS(A4).LE.1.D-08.AND.K.NE.NSING2)GO TO 415	DAN10940
GO TO 417	DAN10950
416 J=J+1	DAN10960
P1=0.D0	DAN10970
P2=0.D0	DAN10980
IF(K.LT.MNM)GO TO 410	DAN10990
IF(EA(K).GT.1.999999)GO TO 410	DAN11000
J=J+3	DAN11010
A5=0.D0	DAN11020
A3=C(L1,KP)	DAN11030
P3=0.D0	DAN11040
P4=0.D0	DAN11050
P31=0.D0	DAN11060
P33=0.D0	DAN11070
P34=0.D0	DAN11080
GO TO 410	DAN11090
415 J=J+1	DAN11100
P1=A1*A1	DAN11110
P2=0.D0	DAN11120
IF(K.LT.MNM)GO TO 410	DAN11130
IF(EA(K).GT.1.999999)GO TO 410	DAN11140
J=J+3	DAN11150
A5=C(I1,KP)	DAN11160
A8=0.D0	DAN11170
P3=A5*A5	DAN11180
P4=0.D0	DAN11190
P31=A1*A5	DAN11200

P33=0.D0	DAN11210
P34=0.D0	DAN11220
GO TO 410	DAN11230
417 P1=A1*A1	DAN11240
P2=A1*A4	DAN11250
J=J+1	DAN11260
T(J)=T(J)+X4*P1*P2	DAN11270
IF(K.LT.MNM)GO TO 410	DAN11280
IF(EA(K).GT.1.999999)GO TO 410	DAN11290
A5=C(I1,KP)	DAN11300
A8=C(L1,KP)	DAN11310
P3=A5*A5	DAN11320
P4=A5*A8	DAN11330
P31=A1*A5	DAN11340
P33=A1*A8	DAN11350
P34=A4*A5	DAN11360
Q=2.D0*P31*(P33+P34)	DAN11370
J=J+1	DAN11380
T(J)=X4*P3*P4+T(J)	DAN11390
J=J+1	DAN11400
T(J)=T(J)+X2*Q	DAN11410
J=J+1	DAN11420
T(J)=T(J)+X4*(P1*P4+P2*P3)	DAN11430
410 KAND=K+1	DAN11440
IF(K.EQ.NB)GO TO 430	DAN11450
DO 420 LN=KAND,NB	DAN11460
LP=M-LN+1	DAN11470
A9=C(I1,LN)	DAN11480
A12=C(L1,LN)	DAN11490
P7=A9*A12	DAN11500
P8=A9*A9	DAN11510
P13=A1*A9	DAN11520

P15=A9*A4	DAN11530
P16=A12*A1	DAN11540
J=J+1	DAN11550
T(J)=T(J)+X4*(P1*P7+P2*P8)	DAN11560
J=J+1	DAN11570
T(J)=T(J)+X4*P13*(P15+P16)	DAN11580
IF(LN.LT.MNM)GO TO 420	DAN11590
IF(EA(LN).GT.1.999999)GO TO 420	DAN11600
A13=C(I1,LP)	DAN11610
A16=C(L1,LP)	DAN11620
P5=A13*A16	DAN11630
P6=A13*A13	DAN11640
P9=A1*A13	DAN11650
P11=A13*A4	DAN11660
P12=A16*A1	DAN11670
P17=A5*A16	DAN11680
P18=A8*A13	DAN11690
P19=A13*A5	DAN11700
J=J+1	DAN11710
T(J)=T(J)+X4*(P1*P5+P2*P6)	DAN11720
J=J+1	DAN11730
T(J)=T(J)+X4*P9*(P11+P12)	DAN11740
IF(K.LT.MNM)GO TO 420	DAN11750
IF(EA(K).GT.1.999999)GO TO 420	DAN11760
P35=A9*A5	DAN11770
P38=A8*A9	DAN11780
P37=A5*A12	DAN11790
J=J+1	DAN11800
T(J)=T(J)+X4*(P8*P4+P7*P3)	DAN11810
J=J+1	DAN11820
T(J)=T(J)+X4*P35*(P37+P38)	DAN11830
J=J+1	DAN11840

T(J)=T(J)+X4*(P3*P5+P4*P6)	DAN11850
J=J+1	DAN11860
T(J)=T(J)+X4*P19*(P17+P18)	DAN11870
J=J+1	DAN11880
T(J)=T(J)+X4*(P9*(P37+P38)+P35*(P11+P12))	DAN11890
J=J+1	DAN11900
T(J)=T(J)+X4*(P13*(P17+P18)+P19*(P15+P16))	DAN11910
420 CONTINUE	DAN11920
430 IF(M0.LE.0)GO TO 440	DAN11930
DO 435 LQ=1,MO	DAN11940
LN=LQ+NB	DAN11950
A9=C(I1,LN)	DAN11960
A12=C(L1,LN)	DAN11970
P21=A9*A12	DAN11980
P22=A9*A9	DAN11990
P23=A1*A9	DAN12000
P27=A9*A4	DAN12010
P28=A12*A1	DAN12020
J=J+1	DAN12030
T(J)=T(J)+X4*(P1*P21+P2*P22)	DAN12040
J=J+1	DAN12050
T(J)=T(J)+X4*P23*(P27+P28)	DAN12060
IF(K.LT.MNN)GO TO 435	DAN12070
IF(EA(K).GT.1.999999)GO TO 435	DAN12080
P25=A9*A8	DAN12090
P26=A5*A12	DAN12100
P29=A5*A9	DAN12110
J=J+1	DAN12120
T(J)=T(J)+X4*(P3*P21+P4*P22)	DAN12130
J=J+1	DAN12140
T(J)=T(J)+X4*P29*(P25+P26)	DAN12150
J=J+1	DAN12160

T(J)=T(J)+X4*(P23*(P25+P26)+P29*(P27+P28))	DAN12170
435 CONTINUE	DAN12180
440 CONTINUE	DAN12190
IF(M0.LE.1)GO TO 460	DAN12200
DO 450 KQ=1,M0	DAN12210
K=KQ+NB	DAN12220
IF(KQ.EQ.M0)GO TO 450	DAN12230
KQ1=KQ+1	DAN12240
DO 445 LQ=KQ1,M0	DAN12250
LN=LQ+NB	DAN12260
A1=C(I1,K)	DAN12270
A4=C(L1,K)	DAN12280
A9=C(I1,LN)	DAN12290
A12=C(L1,LN)	DAN12300
J=J+1	DAN12310
T(J)=T(J)+X4*A1*A9*(A1*A12+A4*A9)	DAN12320
J=J+1	DAN12330
445 T(J)=T(J)+X4*A1*A9*(A4*A9+A1*A12)	DAN12340
450 CONTINUE	DAN12350
460 GO TO 6000	DAN12360
500 J=0	DAN12370
DO 540 K=1,NB	DAN12380
KP=M-K+1	DAN12390
A1=C(I1,K)	DAN12400
A3=C(K1,K)	DAN12410
A4=C(L1,K)	DAN12420
518 IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING1)GO TO 516	DAN12430
IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING2)GO TO 516	DAN12440
IF(DABS(A3).LE.1.D-08.OR.DABS(A4).LE.1.D-08.AND.K.NE.NSING1)	DAN12450
1GO TO 515	DAN12460
IF(DABS(A3).LE.1.D-08.OR.DABS(A4).LE.1.D-08.AND.K.NE.NSING2)	DAN12470
1GO TO 515	DAN12480

GO TO 517	DAN12490
516 J=J+1	DAN12500
P1=0.D0	DAN12510
P2=A3*A4	DAN12520
IF(K.LT.MNM)GO TO 510	DAN12530
IF(EA(K).GT.1.999999)GO TO 510	DAN12540
J=J+3	DAN12550
A5=0.D0	DAN12560
A7=C(K1,KP)	DAN12570
A8=C(L1,KP)	DAN12580
P3=0.D0	DAN12590
P4=A7*A8	DAN12600
P31=0.D0	DAN12610
P33=A3*A8	DAN12620
P34=A4*A7	DAN12630
GO TO 510	DAN12640
515 J=J+1	DAN12650
P1=A1*A1	DAN12660
P2=0.D0	DAN12670
IF(K.LT.MNM) GO TO 510	DAN12680
IF(EA(K).GT.1.999999)GO TO 510	DAN12690
J=J+3	DAN12700
A5=C(I1,KP)	DAN12710
A7=C(K1,KP)	DAN12720
A8=C(L1,KP)	DAN12730
P3=A5*A5	DAN12740
P4=0.D0	DAN12750
P31=A1*A5	DAN12760
P33=0.D0	DAN12770
P34=0.D0	DAN12780
GO TO 510	DAN12790
517 P1=A1*A1	DAN12800

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P2=A3*A4                               DAN12810
J=J+1                                   DAN12820
T(J)=T(J)+X4*P1*P2                     DAN12830
IF(K.LT.MNM)GO TO 510                  DAN12840
IF(EA(K).GT.1.999999)GO TO 510          DAN12850
A5=C(I1,KP)                            DAN12860
A7=C(K1,KP)                            DAN12870
A8=C(L1,KP)                            DAN12880
P3=A5*A5                              DAN12890
P4=A7*A8                              DAN12900
P31=A1*A5                             DAN12910
P33=A3*A8                             DAN12920
P34=A4*A7                             DAN12930
Q=2.D0*(P33+P34)*P31                  DAN12940
J=J+1                                   DAN12950
T(J)=X4*P3*P4+T(J)                      DAN12960
J=J+1                                   DAN12970
T(J)=T(J)+X2*Q                          DAN12980
J=J+1                                   DAN12990
T(J)=T(J)+X4*(P1*P4+P2*P3)            DAN13000
510 KAND=K+1                           DAN13010
IF(K.EQ.NB)GO TO 530                  DAN13020
DO 520 LN=KAND,NB                      DAN13030
LP=M-LN+1                             DAN13040
A9=C(I1,LN)                            DAN13050
A11=C(K1,LN)                           DAN13060
A12=C(L1,LN)                           DAN13070
P7=A11*A12                            DAN13080
P8=A9*A9                              DAN13090
P13=A1*A9                             DAN13100
P15=A11*A4                            DAN13110
P16=A12*A3                            DAN13120

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J=J+1                               DAN13130
T(J)=T(J)+X4*(P1*P7+P2*P8)          DAN13140
J=J+1                               DAN13150
T(J)=T(J)+X4*P13*(P15+P16)          DAN13160
IF(LN.LT.MNM)GO TO 520              DAN13170
IF(EA(LN).GT.1.999999)GO TO 520      DAN13180
A13=C(I1,LP)                         DAN13190
A15=C(K1,LP)                         DAN13200
A16=C(L1,LP)                         DAN13210
P5=A15*A16                           DAN13220
P6=A13*A13                           DAN13230
P9=A1*A13                            DAN13240
P11=A15*A4                           DAN13250
P12=A16*A3                           DAN13260
P17=A7*A16                           DAN13270
P18=A8*A15                           DAN13280
P19=A13*A5                           DAN13290
J=J+1                               DAN13300
T(J)=T(J)+X4*(P1*P5+P2*P6)          DAN13310
J=J+1                               DAN13320
T(J)=T(J)+X4*P9*(P11+P12)           DAN13330
IF(K.LT.MNM)GO TO 520              DAN13340
IF(EA(K).GT.1.999999)GO TO 520      DAN13350
P35=A9*A5                           DAN13360
P37=A7*A12                           DAN13370
P38=A8*A11                           DAN13380
J=J+1                               DAN13390
T(J)=T(J)+X4*(P8*P4+P7*P3)          DAN13400
J=J+1                               DAN13410
T(J)=T(J)+X4*P35*(P37+P38)          DAN13420
J=J+1                               DAN13430
T(J)=T(J)+X4*(P3*P5+P4*P6)          DAN13440

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J=J+1	DAN13450
T(J)=T(J)+X4*(P17+P18)	DAN13460
J=J+1	DAN13470
T(J)=T(J)+X4*(P9*(P37+P38)+P35*(P11+P12))	DAN13480
J=J+1	DAN13490
T(J)=T(J)+X4*(P13*(P17+P18)+P19*(P15+P16))	DAN13500
520 CONTINUE	DAN13510
530 IF(MO.LE.0)GO TO 540	DAN13520
DO 535 LQ=1,MD	DAN13530
LN=LQ+N8	DAN13540
A9=C(I1,LN)	DAN13550
A11=C(K1,LN)	DAN13560
A12=C(L1,LN)	DAN13570
P21=A11*A12	DAN13580
P22=A9*A9	DAN13590
P23=A1*A9	DAN13600
P27=A11*A4	DAN13610
P28=A12*A3	DAN13620
J=J+1	DAN13630
T(J)=T(J)+X4*(P1*P21+P2*P22)	DAN13640
J=J+1	DAN13650
T(J)=T(J)+X4*P23*(P27+P28)	DAN13660
IF(K.LT.MNM)GO TO 535	DAN13670
IF(EA(K).GT.1.999999)GO TO 535	DAN13680
P25=A11*A8	DAN13690
P26=A7*A12	DAN13700
P29=A5*A9	DAN13710
J=J+1	DAN13720
T(J)=T(J)+X4*(P3*P21+P4*P22)	DAN13730
J=J+1	DAN13740
T(J)=T(J)+X4*P29*(P25+P26)	DAN13750
J=J+1	DAN13760

T(J)=T(J)+X4*(P23*(P25+P26)+P29*(P27+P28))	DAN13770
535 CONTINUE	DAN13780
540 CONTINUE	DAN13790
IF(MO.LE.1)GO TO 560	DAN13800
DO 550 KQ=1,MO	DAN13810
K=KQ+NB	DAN13820
IF(KQ.EQ.MO)GO TO 550	DAN13830
KQ1=KQ+1	DAN13840
DO 545 LQ=KQ1,MO	DAN13850
LN=LQ+NB	DAN13860
A1=C(I1,K)	DAN13870
A3=C(K1,K)	DAN13880
A4=C(L1,K)	DAN13890
A9=C(I1,LN)	DAN13900
A11=C(K1,LN)	DAN13910
A12=C(L1,LN)	DAN13920
J=J+1	DAN13930
T(J)=T(J)+X4*(A1*A1*A11*A12+A3*A4*A9*A9)	DAN13940
J=J+1	DAN13950
545 T(J)=T(J)+X4*A1*A9*(A4*A11+A3*A12)	DAN13960
550 CONTINUE	DAN13970
560 GO TO 6000	DAN13980
700 J=0	DAN13990
DO 740 K=1,NB	DAN14000
KP=M-K+1	DAN14010
A1=C(I1,K)	DAN14020
A2=C(J1,K)	DAN14030
718 IF(DABS(A2).LE.1.D-08.AND.K.NE.NSING1)GO TO 715	DAN14040
IF(DABS(A2).LE.1.D-08.AND.K.NE.NSING2)GO TO 715	DAN14050
IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING1)GO TO 716	DAN14060
IF(DABS(A1).LE.1.D-08.AND.K.NE.NSING2)GO TO 716	DAN14070
GO TO 717	DAN14080

716	P1=0.00	DAN14090
	P2=A2*A2	DAN14100
	J=J+1	DAN14110
	IF(K.LT.MNM)GO TO 710	DAN14120
	IF(EA(K).GT.1.999999)GO TO 710	DAN14130
	J=J+3	DAN14140
	A5=0.00	DAN14150
	A6=C(J1,KP)	DAN14160
	P3=0.00	DAN14170
	P4=A6*A6	DAN14180
	P31=0.00	DAN14190
	P32=0.00	DAN14200
	P33=A2*A6	DAN14210
	GO TO 710	DAN14220
715	J=J+1	DAN14230
	P1=0.00	DAN14240
	P2=0.00	DAN14250
	IF(K.LT.MNM)GO TO 710	DAN14260
	IF(EA(K).GT.1.999999)GO TO 710	DAN14270
	J=J+3	DAN14280
	A5=C(I1,KP)	DAN14290
	A6=0.00	DAN14300
	P3=0.00	DAN14310
	P4=0.00	DAN14320
	P31=0.00	DAN14330
	P32=0.00	DAN14340
	P33=0.00	DAN14350
	GO TO 710	DAN14360
717	P1=A1*A2	DAN14370
	P2=A2*A2	DAN14380
	J=J+1	DAN14390
	T(J)=T(J)+X4*P1*P2	DAN14400

IF(K.LT.MNM)GO TO 710	DAN14410
IF(EA(K).GT.1.999999)GO TO 710	DAN14420
A5=C(I1,KP)	DAN14430
A6=C(J1,KP)	DAN14440
P3=A5*A6	DAN14450
P4=A6*A6	DAN14460
P31=A1*A6	DAN14470
P32=A2*A5	DAN14480
P33=A2*A6	DAN14490
Q=2.D0*P33*(P31+P32)	DAN14500
J=J+1	DAN14510
T(J)=X4*P3*P4+T(J)	DAN14520
J=J+1	DAN14530
T(J)=T(J)+X2*Q	DAN14540
J=J+1	DAN14550
T(J)=T(J)+X4*(P1*P4+P2*P3)	DAN14560
710 KAND=K+1	DAN14570
IF(K.EQ.NB)GO TO 730	DAN14580
DO 720 LN=KAND,NB	DAN14590
LP=M-LN+1	DAN14600
A9=C(I1,LN)	DAN14610
A10=C(J1,LN)	DAN14620
P7=A10*A10	DAN14630
P8=A9*A10	DAN14640
P13=A1*A10	DAN14650
P14=A2*A9	DAN14660
P15=A10*A2	DAN14670
J=J+1	DAN14680
T(J)=T(J)+X4*(P1*P7+P2*P8)	DAN14690
J=J+1	DAN14700
T(J)=T(J)+X4*P15*(P13+P14)	DAN14710
IF(LN.LT.MNM)GO TO 720	DAN14720

IF(EA(LN).GT.1.999999)GO TO 720	DAN14730
A13=C(I1,LP)	DAN14740
A14=C(J1,LP)	DAN14750
P5=A14*A14	DAN14760
P6=A13*A14	DAN14770
P9=A1*A14	DAN14780
P10=A13*A2	DAN14790
P11=A14*A2	DAN14800
P17=A6*A14	DAN14810
P19=A13*A6	DAN14820
P20=A5*A14	DAN14830
J=J+1	DAN14840
T(J)=T(J)+X4*(P1*P5+P2*P6)	DAN14850
J=J+1	DAN14860
T(J)=T(J)+X4*P11*(P9+P10)	DAN14870
IF(K.LT.MNM)GO TO 720	DAN14880
IF(EA(K).GT.1.999999)GO TO 720	DAN14890
P35=A9*A6	DAN14900
P36=A5*A10	DAN14910
P37=A6*A10	DAN14920
J=J+1	DAN14930
T(J)=T(J)+X4*(P8*P4+P7*P3)	DAN14940
J=J+1	DAN14950
T(J)=T(J)+X4*P37*(P35+P36)	DAN14960
J=J+1	DAN14970
T(J)=T(J)+X4*(P3*P5+P4*P6)	DAN14980
J=J+1	DAN14990
T(J)=T(J)+X4*P17*(P19+P20)	DAN15000
J=J+1	DAN15010
T(J)=T(J)+X4*(P37*(P9+P10)+P11*(P35+P36))	DAN15020
J=J+1	DAN15030
T(J)=T(J)+X4*(P17*(P13+P14)+P15*(P19+P20))	DAN15040

720	CONTINUE	DAN15050
730	IF(M0.LE.0)GO TO 740	DAN15060
	DO 735 LQ=1,M0	DAN15070
	LN=LQ+NB	DAN15080
	A9=C(I1,LN)	DAN15090
	A10=C(J1,LN)	DAN15100
	P21=A10*A10	DAN15110
	P22=A9*A10	DAN15120
	P23=A1*A10	DAN15130
	P24=A9*A2	DAN15140
	P27=A10*A2	DAN15150
	J=J+1	DAN15160
	T(J)=T(J)+X4*(P1*P21+P2*P22)	DAN15170
	J=J+1	DAN15180
	T(J)=T(J)+X4*P27*(P23+P24)	DAN15190
	IF(K.LT.MNM)GO TO 735	DAN15200
	IF(EA(K).GT.1.999999)GO TO 735	DAN15210
	P25=A10*A6	DAN15220
	P29=A5*A10	DAN15230
	P30=A6*A9	DAN15240
	J=J+1	DAN15250
	T(J)=T(J)+X4*(P3*P21+P4*P22)	DAN15260
	J=J+1	DAN15270
	T(J)=T(J)+X4*P25*(P29+P30)	DAN15280
	J=J+1	DAN15290
	T(J)=T(J)+X4*(P25*(P23+P24)+P27*(P29+P30))	DAN15300
735	CONTINUE	DAN15310
740	CONTINUE	DAN15320
	IF(M0.LE.1)GO TO 760	DAN15330
	DO 750 KQ=1,M0	DAN15340
	K=KQ+NB	DAN15350
	IF(KQ.EQ.M0)GO TO 750	DAN15360

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KQ1=KQ+1                               DAN15370
DO 745 LQ=KQ1,M0                      DAN15380
LN=LQ+NB                                DAN15390
A1=C(I1,K)                                DAN15400
A2=C(J1,K)                                DAN15410
A9=C(I1,LN)                                DAN15420
A10=C(J1,LN)                               DAN15430
J=J+1                                     DAN15440
T(J)=T(J)+X4*A2*A10*(A1*A10+A2*A9)    DAN15450
J=J+1                                     DAN15460
745 T(J)=T(J)+X4*A2*A10*(A1*A10+A2*A9) DAN15470
750 CONTINUE                               DAN15480
760 GO TO 6000                            DAN15490
600 J=0                                    DAN15500
DO 640 K=1,NB                            DAN15510
KP=M-K+1                                 DAN15520
A1=C(I1,K)                                DAN15530
A2=C(J1,K)                                DAN15540
A3=C(K1,K)                                DAN15550
618 IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING1) DAN15560
1GO TO 616                                DAN15570
IF(DABS(A1).LE.1.D-08.OR.DABS(A2).LE.1.D-08.AND.K.NE.NSING2) DAN15580
1GO TO 616                                DAN15590
IF(DABS(A3).LE.1.D-08.AND.K.NE.NSING1)GO TO 615 DAN15600
IF(DABS(A3).LE.1.D-08.AND.K.NE.NSING2)GO TO 615 DAN15610
GO TO 617                                DAN15620
616 J=J+1                                 DAN15630
P1=0.00                                   DAN15640
P2=A3*A3                                 DAN15650
IF(K.LT.MNM)GO TO 610                   DAN15660
IF(EA(K).GT.1.999999)GO TO 610          DAN15670
J=J+3                                    DAN15680

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A5=C(I1,KP)	DAN15690
A6=C(J1,KP)	DAN15700
A7=C(K1,KP)	DAN15710
P3=0.D0	DAN15720
P4=A7*A7	DAN15730
P31=0.D0	DAN15740
P32=0.D0	DAN15750
P33=A3*A7	DAN15760
GO TO 610	DAN15770
615 J=J+1	DAN15780
P1=A1*A2	DAN15790
P2=0.D0	DAN15800
IF(K.LT.MNM)GO TO 610	DAN15810
IF(EA(K).GT.1.999999)GO TO 610	DAN15820
J=J+3	DAN15830
A5=C(I1,KP)	DAN15840
A6=C(J1,KP)	DAN15850
A7=0.D0	DAN15860
P3=A5*A6	DAN15870
P4=0.D0	DAN15880
P31=A6*A1	DAN15890
P32=A2*A5	DAN15900
P33=0.D0	DAN15910
GO TO 610	DAN15920
617 P1=A1*A2	DAN15930
P2=A3*A3	DAN15940
J=J+1	DAN15950
T(J)=T(J)+X4*P1*P2	DAN15960
IF(K.LT.MNM)GO TO 610	DAN15970
IF(EA(K).GT.1.999999)GO TO 610	DAN15980
A5=C(I1,KP)	DAN15990
A6=C(J1,KP)	DAN16000

A7=C(K1,KP)	DAN16010
P3=A5*A6	DAN16020
P4=A7*A7	DAN16030
P31=A1*A6	DAN16040
P32=A2*A5	DAN16050
P33=A3*A7	DAN16060
Q=2.00*P33*(P31+P32)	DAN16070
J=J+1	DAN16080
T(J)=X4*P3*P4+T(J)	DAN16090
J=J+1	DAN16100
T(J)=T(J)+X2*Q	DAN16110
J=J+1	DAN16120
T(J)=T(J)+X4*(P1*P4+P2*P3)	DAN16130
610 KAND=K+1	DAN16140
IF(K.EQ.NB)GO TO 630	DAN16150
DO 620 LN=KAND,NB	DAN16160
LP=M-LN+1	DAN16170
A9=C(I1,LN)	DAN16180
A10=C(J1,LN)	DAN16190
A11=C(K1,LN)	DAN16200
P7=A11*A11	DAN16210
P8=A9*A10	DAN16220
P13=A1*A10	DAN16230
P14=A2*A9	DAN16240
P15=A11*A3	DAN16250
J=J+1	DAN16260
T(J)=T(J)+X4*(P1*P7+P2*P8)	DAN16270
J=J+1	DAN16280
T(J)=T(J)+X4*P15*(P13+P14)	DAN16290
IF(LN.LT.MNM)GO TO 620	DAN16300
IF(EA(LN).GT.1.999999)GO TO 620	DAN16310
A13=C(I1,LP)	DAN16320

A14=C(J1,LP)	DAN16330
A15=C(K1,LP)	DAN16340
P5=A15*A15	DAN16350
P6=A13*A14	DAN16360
P9=A1*A14	DAN16370
P10=A13*A2	DAN16380
P11=A15*A3	DAN16390
P17=A7*A15	DAN16400
P19=A13*A6	DAN16410
P20=A5*A14	DAN16420
J=J+1	DAN16430
T(J)=T(J)+X4*(P1*P5+P2*P6)	DAN16440
J=J+1	DAN16450
T(J)=T(J)+X4*P11*(P9+P10)	DAN16460
IF(K.LT.MNM)GO TO 620	DAN16470
IF(EA(K).GT.1.999999)GO TO 620	DAN16480
P35=A9*A6	DAN16490
P36=A5*A10	DAN16500
P37=A7*A11	DAN16510
J=J+1	DAN16520
T(J)=T(J)+X4*(P8*P4+P7*P3)	DAN16530
J=J+1	DAN16540
T(J)=T(J)+X4*P37*(P35+P36)	DAN16550
J=J+1	DAN16560
T(J)=T(J)+X4*(P3*P5+P4*P6)	DAN16570
J=J+1	DAN16580
T(J)=T(J)+X4*P17*(P19+P20)	DAN16590
J=J+1	DAN16600
T(J)=T(J)+X4*(P37*(P9+P10)+P11*(P35+P36))	DAN16610
J=J+1	DAN16620
T(J)=T(J)+X4*(P17*(P13+P14)+P15*(P19+P20))	DAN16630
620 CONTINUE	DAN16640

630 IF(MO.LE.0)GO TO 640	DAN16650
DO 635 LQ=1,MO	DAN16660
LN=LQ+NB	DAN16670
A9=C(I1,LN)	DAN16680
A10=C(J1,LN)	DAN16690
A11=C(K1,LN)	DAN16700
P21=A11*A11	DAN16710
P22=A9*A10	DAN16720
P23=A1*A10	DAN16730
P24=A9*A2	DAN16740
P27=A11*A3	DAN16750
J=J+1	DAN16760
T(J)=T(J)+X4*(P1*P21+P2*P22)	DAN16770
J=J+1	DAN16780
T(J)=T(J)+X4*P27*(P23+P24)	DAN16790
IF(K.LT.MNN)GO TO 635	DAN16800
IF(EA(K).GT.1.999999)GO TO 635	DAN16810
P25=A11*A7	DAN16820
P29=A5*A10	DAN16830
P30=A6*A9	DAN16840
J=J+1	DAN16850
T(J)=T(J)+X4*(P3*P21+P4*P22)	DAN16860
J=J+1	DAN16870
T(J)=T(J)+X4*P25*(P29+P30)	DAN16880
J=J+1	DAN16890
T(J)=T(J)+X4*(P25*(P23+P24)+P27*(P29+P30))	DAN16900
635 CONTINUE	DAN16910
640 CONTINUE	DAN16920
IF(MO.LE.1)GO TO 660	DAN16930
DO 650 KQ=1,MO	DAN16940
K=KQ+NB	DAN16950
IF(KQ.EQ.MQ)GO TO 650	DAN16960

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KQ1=KQ+1                               DAN16970
DO 645 LQ=KQ1,MD                      DAN16980
LN=LQ+NB                                DAN16990
A1=C(I1,K)                                DAN17000
A2=C(J1,K)                                DAN17010
A3=C(K1,K)                                DAN17020
A9=C(I1,LN)                                DAN17030
A10=C(J1,LN)                               DAN17040
A11=C(K1,LN)                               DAN17050
J=J+1                                     DAN17060
T(J)=T(J)+X4*(A1*A2*A11*A11+A3*A3*A9*A10) DAN17070
J=J+1                                     DAN17080
645 T(J)=T(J)+X4*A3*A11*(A1*A10+A2*A9)   DAN17090
650 CONTINUE                               DAN17100
660 GO TO 6000                            DAN17110
6000 CONTINUE                            DAN17120
10 IF(NINTS-MN1)30,20,54                  DAN17130
54 MN1=MN1+1                            DAN17140
GO TO 55                                 DAN17150
C                                         DAN17160
C     IF THIS WAS NOT THE LAST RECORD, GO BACK INTO THE LOOP AND DAN17170
C     READ ANOTHER RECORD OF INTEGRALS.          DAN17180
C     IF CHECKSUM PRINT FLAG IS ON, AND THERE ARE NO MORE CHECKSUMSDAN17190
C     PRINT THEM                                DAN17200
C                                         DAN17210
C     76 IF(IPTI.EQ.0.AND.IRC.EQ.1)GO TO 78    DAN17220
C                                         DAN17230
C     PRINT THE CHECKSUMS OBTAINED ON THIS RUN THROUGH THE LOOP DAN17240
C                                         DAN17250
C     WRITE(6,39)NMINNW                         DAN17260
78 CONTINUE                               DAN17270
19 FORMAT(1H1///37X,                      DAN17280

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16IINTERNAL CHECK SUMS, ETC. FROM READING TWO ELECTRON INTEGRALS//DAN17290
16H REC ,7(1X,17H FIRST NOS LAST )/ DAN17300
16H NOS ,7(1X,17H LABEL OF LABEL )/ DAN17310
16X,7(1X,17H J L INTS J L )) DAN17320
29 FORMAT (1X,I4,1X,7(I3,I3,1X,I4,I3,I3,1X)) DAN17330
39 FORMAT(12X, DAN17340
118H THIS NOS. OF INTS,I12) DAN17350
      RETURN DAN17360
C DAN17370
C     ERROR EXIT FOR INCORRECT VALUE OF NINTS (POSSIBLE TAPE READ DAN17380
C     ERROR) DAN17390
C DAN17400
30 WRITE(6,9) DAN17410
 9 FORMAT('0','ERROR IN NOINTS') DAN17420
  CALL ABT DAN17430
  STOP DAN17440
  END DAN17450
CWATE   SUBROUTINE WATE DAN17460
        SUBROUTINE WATE( FA,H,CA,CB,BETA,TENO,EB,SOMEGA,B,AX,A,EA,BX, DED DAN17470
        1W,BE,SPIN,ED,A2IJ,PKD,VAL,CUT,EN,INAME,NTAPE,NRX,NTOP,NIN,NBFNS, DAN17480
        1NA,NB,NR) DAN17490
C DAN17500
C     REFERENCES: (1) PHILLIPS AND SCHUG, J.CHEM.PHYS. 61, 1031 DAN17510
C     (1974); (2) HARRIMAN, IBID. 40, 2827(1964); (3) HARDISSON AND DAN17520
C     HARRIMAN, IBID. 46, 3639(1967); (4) SANDO AND HARRIMAN, IBID. DAN17530
C     47,180(1967); (5) SASAKI AND OHNO, J. MATH. PHYS. 7, 1140 DAN17540
C     (1963). DAN17550
C     ERRATUM FOR REFERENCE (1): EQN. (24) SHOULD READ DAN17560
C     E(I)=(1-D(I)**2)**0.5 = 2*T(I)*U(I) DAN17570
C     THIS IS A TYPOGRAPHICAL ERROR. THE CORRECT FORM WAS USED IN DAN17580
C     THE CALCULATIONS. DAN17590
C DAN17600

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IMPLICIT REAL*8(A-H,O-Z)                               DAN17610
REAL*8 ILBL,ILAB,ILABL,INTNAM,INAME                DAN17620
COMMON/ZEIT/LAPSE,LAPST                           DAN17630
COMMON/LABELS/ILBL(12),ILAB(12)                   DAN17640
COMMON/ICIND/ICON(24)                            DAN17650
DIMENSION FA(NRX,NRX),H(NRX,NRX),CA(NRX,NRX),CB(NRX,NRX),BETA(NRX,DAN17660
1NRX)                                              DAN17670
DIMENSION INAME(6)                                DAN17680
DIMENSION TEND(NTOP)                            DAN17690
DIMENSION EB(NRX),SOMEGA(NRX),B(NRX),AX(NRX),A(NRX),EA(NRX),BX(NRX,DAN17700
1),DELW(NRX),BE(NRX),SPIN(NRX),ED(NRX),A2IJ(NRX)   DAN17710
DIMENSION PKD(NIN),VAL(NIN)                      DAN17720
REAL*8 ILBL,ILAB                                 DAN17730
EXTERNAL F,CK                                     DAN17740
C
C          SET CONSTANTS
C
NTI=5                                              DAN17750
NTO=6                                              DAN17760
READ(NTI,169)KIKMAX                           DAN17770
XNA=DFLOAT(NA)                                DAN17780
XNB=DFLOAT(NB)                                DAN17790
XM=0.500*(XNA-XNB)                           DAN17800
XN=0.500*(XNA+XNB)                           DAN17810
S2=XM                                         DAN17820
NBP=NB+1                                       DAN17830
M=NA+NB                                      DAN17840
NC=NBFNS                                     DAN17850
N=NR                                         DAN17860
NTT=(N*(N+1))/2                                DAN17870
NP=N+1                                         DAN17880
NM=N-1                                         DAN17890

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NAP=NA+1                               DAN17930
NAM=NA-1                               DAN17940
NBM=NB-1                               DAN17950
N2=N/2                                 DAN17960
N2P=N2+1                               DAN17970
MP=M+1                                 DAN17980
MU=NA-NB+1                            DAN17990
MD=NA-NB                             DAN18000
WRITE(NT0,209)                         DAN18010
WRITE(NT0,299)NA,NB                   DAN18020
DAN18030
C
C          INITIALIZE ARRAYS AND INVERT ORDER OF BETA EIGENVALUES(EB'S)
C
DO 10 I=1,N                           DAN18040
SOMEWA(I)=EB(N-I+1)                  DAN18050
10 A(I)=0.D0                           DAN18060
DO 20 I=1,N                           DAN18070
IF(SOMEWA(I).LT.0.)SOMEWA(I)=0.D0   DAN18080
IF(SOMEWA(I).GT.1.)SOMEWA(I)=1.D0   DAN18090
20 EB(I)=SOMEWA(I)                   DAN18100
DAN18110
DAN18120
DAN18130
DAN18140
DAN18150
DAN18160
DAN18170
DAN18180
DAN18190
DAN18200
DAN18210
DAN18220
DAN18230
DAN18240
C
C          THE EB(I) ARE THE D(I)**2 OF REF. (1).
C          THE EA(I) ARE EQUAL TO E(I)**2 OF REF. (1).
C
DO 30 I=1,NB                         DAN18140
B(I)=0.D0                            DAN18150
30 AX(I)=1.D0-EB(I)                  DAN18160
I=1
B(I)=1.D0                            DAN18170
A(I)=1.D0                            DAN18180
B(NBP)=1.D0                           DAN18190
A(NBP)=1.D0                           DAN18200

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      WRITE(NTO,9)                               DAN18250
      WRITE(NTO,19)(EB(I),I=1,N)                 DAN18260
C
C          CALCULATE SUMS OF CONTINUING PRODUCTS
C
      FA(1,1)=EB(1)                            DAN18270
      FA(2,1)=0.D0                            DAN18280
      IF(NB.LE.1)GO TO 221                     DAN18290
      DO 50 J=2,NB                           DAN18300
      JM=J-1                                DAN18310
      FA(1,J)=FA(1,JM)+EB(J)                  DAN18320
      DO 40 K=2,J                           DAN18330
      40 FA(K,J)=FA(K,JM)+EB(J)*FA(K-1,JM)   DAN18340
      FA(J+1,J)=0.D0                          DAN18350
      50 CONTINUE                            DAN18360
      221 DO 60 I=1,NB                      DAN18370
      60 A(I+1)=FA(I,NB)                     DAN18380
C
C          THESE ARE HARRIMAN'S ASUBK. SEE EQN. (21) OF REF. (2)
C
      WRITE(NTO,29)                            DAN18390
      WRITE(NTO,19)(A(I),I=1,NBP)              DAN18400
      FA(1,1)=AX(1)                            DAN18410
      FA(2,1)=0.D0                            DAN18420
      IF(NB.LE.1)GO TO 222                     DAN18430
      DO 80 J=2,NB                           DAN18440
      JM=J-1                                DAN18450
      FA(1,J)=FA(1,JM)+AX(J)                  DAN18460
      DO 70 K=2,J                           DAN18470
      70 FA(K,J)=FA(K,JM)+AX(J)*FA(K-1,JM)   DAN18480
      FA(J+1,J)=0.D0                          DAN18490
      80 CONTINUE                            DAN18500

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222 DO 90 I=1,NB DAN18570
  90 B(I+1)=FA(I,NB) DAN18580
C DAN18590
C      THESE ARE BSUBK OF REFS. (1), (2), AND (3). DAN18600
C DAN18610
C      WRITE(NTO,119) DAN18620
  WRITE(NTO,19)(B(I),I=1,NBP) DAN18630
C DAN18640
C      CALCULATION OF WEIGHTS FROM EQN. (26) OF REF. (1). DAN18650
C DAN18660
DO 110 I=1,NBP DAN18670
SI=XM+I-1.00 DAN18680
XZ=XN-SI DAN18690
MM=XZ+1.01 DAN18700
IS=2.*SI+0.01 DAN18710
MS=SI+XM+0.01 DAN18720
NS=SI-XM+0.01 DAN18730
XS=DFLOAT(IS) DAN18740
SOMEWA(I)=0.00 DAN18750
DO 100 J=1,MM DAN18760
JM=J-1 DAN18770
100 SOMEWA(I)=SOMEWA(I)+(-1.00)**JM*(F(NS+JM,1)**2*B(NS+J))/(F(IS+J,1)*F(JM,1)) DAN18780
  SOMEWA(I)=(XS+1.00)*F(MS,1)*SOMEWA(I)/F(NS,1) DAN18800
  IM=I-1 DAN18810
  110 WRITE(NTO,39)SI,SOMEWA(I) DAN18820
C DAN18830
C      INVERT THE ORDER OF THE NATURAL ORBITAL OF CHARGE EIGENVALUES DAN18840
C      SO THAT THE LOWEST ORBITAL HAS THE HIGHEST OCCUPATION DAN18850
C DAN18860
DO 120 I=1,N DAN18870
AX(I)=EA(N-I+1) DAN18880

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DO 120 J=1,NC                               DAN18890
120 H(J,I)=CA(J,N-I+1)                     DAN18900
      DO 130 J=1,NR                         DAN18910
      EA(J)=AX(J)                           DAN18920
      DO 130 I=1,NC                         DAN18930
130 CA(I,J)=H(I,J)                         DAN18940
      DO 1200 I=1,N                          DAN18950
      DO 1200 J=1,NC                         DAN18960
1200 H(J,I)=CB(J,N-I+1)                     DAN18970
      DO 1210 I=1,NC                         DAN18980
      DO 1210 J=1,N                          DAN18990
1210 CB(I,J)=H(I,J)                         DAN19000
      IF(NA.NE.NB.OR.ICON(4).EQ.0)GO TO 5   DAN19010
      DO 140 I=1,NC                         DAN19020
      CA(I,NA)=TENO(I)                      DAN19030
140 CA(I,NBP)=TENO(N+I)                     DAN19040
      CALL MPRY2(CA,EA,B,6HMCDIFJ,6HED N.O,6HRBS CG,O,NR,NC,NRX)
      5 CONTINUE                                DAN19050
C                                         DAN19060
C                                         DAN19070
C                                         DAN19080
C                                         DAN19090
      DO 150 I=1,N                          DAN19100
      H(1,I)=1.00                           DAN19110
150 FA(1,I)=1.00                           DAN19120
      IF(NB.LE.1)GO TO 223                  DAN19130
      DO 170 I=2,NB                         DAN19140
      IM=I-1                               DAN19150
      DO 160 J=1,NB                         DAN19160
C                                         DAN19170
C                                         DAN19180
C                                         DAN19190
160 FA(I,J)=A(I)-EB(J)*FA(IM,J)           DAN19200

```

170 CONTINUE
 C
 C FA(K,L) IS ASUBK(L) OF REF. (2)
 C
 223 WRITE(NTO,129)
 CALL MWRITE(FA,6HFA(K,L,6H) = AS,6HUBK(L),1,NB,NB,NRX)
 C
 C CORRECT PHASES OF NATURAL ORBITALS TO INSURE THAT TSUBI AND
 C USUBI ARE POSITIVE. SEE EQNS. (14), AND (15) OF REF. (1).
 C
 NBMM=NB-1
 IF(NA.NE.NB.OR.ICON(4).EQ.0)NBMM=NB
 DO 210 I=1,NBMM
 JI=M-I+1
 IF(JI.GT.N)GO TO 210
 XV=1.D-06
 KK=1
 1875 IF(DABS(CA(KK,I)).GE.XV.AND.DABS(CA(KK,JI)).GE.XV.AND.
 1 DABS(CB(KK,I)).GE.XV) GO TO 1900
 KK=KK+1
 GO TO 1875
 1900 LL=KK+1
 1905 IF(DABS(CA(LL,I)).GE.XV.AND.DABS(CA(LL,JI)).GE.XV.AND.
 1 DABS(CB(LL,I)).GE.XV) GO TO 1910
 1906 LL=LL+1
 GO TO 1905
 1910 XXV=CA(LL,JI)*CA(KK,I)-CA(LL,I)*CA(KK,JI)
 IF(DABS(XXV).LT.1.D-06)GO TO 1906
 XV=CA(LL,JI)/CA(KK,JI)
 AX(I)=(CB(LL,I)-CB(KK,I)*XV)/(CA(LL,I)-CA(KK,I)*XV)
 XV=CA(LL,I)/CA(KK,I)
 BX(I)=(CB(LL,I)-CB(KK,I)*XV)/(CA(KK,JI)*XV-CA(LL,JI))

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IF(AX(I).GT.0.)GO TO 15                               DAN19530
DO 190 J=1,NC                                         DAN19540
190 CA(J,I)=-1.D0*CA(J,I)                           DAN19550
15 IF(BX(I).LE.0.)GO TO 210                          DAN19560
DO 200 J=1,NC                                         DAN19570
200 CA(J,JI)=-1.D0*CA(J,JI)                         DAN19580
210 CONTINUE                                           DAN19590
      CALL MPRY2(CA,EA,B,6HNATL D,6HRBS OF,6H CHG ,0,NR,NC,NRX) DAN19600
C
C          NATURAL ORBITALS OF SPIN CALCULATION
C
      DO 213 I=1,M                                     DAN19610
      BX(I)=0.D0                                       DAN19620
213 AX(I)=0.D0                                       DAN19630
      DO 240 I=1,N                                     DAN19640
      DELW(I)=DSQRT(1.D0-EB(I))                      DAN19650
240 BE(I)=DSQRT(EB(I))                            DAN19660
      E1UP=0.D0                                       DAN19670
      E2UP=0.D0                                       DAN19680
      XA1=0.D0                                         DAN19690
      MNM=M-N+1                                       DAN19700
C
C          ATOMIC SPIN DENSITIES CALCULATION
C          SEE TABLE II IN REF. (2)
C
C          CALCULATE INTEGRALS OVER NATURAL ORBITALS
C
      CALL NOINTS(EA,PKD,VAL,CA,TENO,CUT,INAME,NB,MNM,MO,M,NINTS,NIN,NRX) DAN19810
1,NTOP,NTAPE)                                         DAN19820
      DO 470 KIK=1,KIKMAX                           DAN19830
      IF(SOMEGA(KIK).LE.1.D-16)GO TO 470           DAN19840

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XKIK=KIK-1.D0          DAN19850
S2=XM+XKIK              DAN19860
WRITE(NT0,59)S2          DAN19870
IF(MU.EQ.1)GO TO 65      DAN19880
CALL MCLEAR(H,NRX,NRX,NRX) DAN19890
AD=1.D0/DSQRT(2.D0)       DAN19900
DO 220 I=1,NB             DAN19910
N1=M-I+1                  DAN19920
DO 220 J=1,NC              DAN19930
IF(N1.GT.N)GO TO 25        DAN19940
H(J,N1)=AD*(CA(J,I)-CA(J,N1)) DAN19950
H(J,I)=AD*(CA(J,I)+CA(J,N1)) DAN19960
GO TO 220                  DAN19970
25 H(J,I)=CA(J,I)          DAN19980
220 CONTINUE                DAN19990
IF(NA.EQ.NB)GO TO 35        DAN20000
DO 230 I=NBP,NA              DAN20010
DO 230 J=1,NC              DAN20020
230 H(J,I)=CA(J,I)          DAN20030
35 CONTINUE                  DAN20040
P=0.D0                      DAN20050
DO 250 K=1,NB              DAN20060
KM=K-1                      DAN20070
250 P=P+(-1.D0)**K*CK(KM,1,NA,NB,KIK)*A(K+1)*K DAN20080
B(I)=0.D0                    DAN20090
IF(NB.LE.1)GO TO 45          DAN20100
DO 260 I=1,NB              DAN20110
B(I)=0.D0                    DAN20120
DO 260 K=1,NBM              DAN20130
KM=K-1                      DAN20140
KP=K+1                      DAN20150
260 B(I)=B(I)+(-1.D0)**K*CK(KM,2,NA,NB,KIK)*FA(KP,I)*K DAN20160

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45 CONTINUE DAN20170
DO 270 I=1,NB DAN20180
BX(I)=0.D0 DAN20190
DO 270 K=1,NB DAN20200
KM=K-1 DAN20210
270 BX(I)=BX(I)+(-1.D0)**KM*CK(KM,1,NA,NB,KIK)*FA(K,I) DAN20220
DO 290 I=1,NA DAN20230
JI=M-I+1 DAN20240
IF(JI.GT.N)GO TO 61 DAN20250
SS=XM/(S2*(S2+1.D0)) DAN20260
IF(I.GT.NB)GO TO 55 DAN20270
AA=SS+SS*(XN*SOMEGA(KIK)+P-XN*BX(I)-B(I))/SOMEGA(KIK) DAN20280
BB=SS*XN*BX(I)*DELW(I)/SOMEGA(KIK) DAN20290
EA(I)=AA+BB DAN20300
EA(JI)=AA-BB DAN20310
GO TO 290 DAN20320
55 EA(I)=SS*(XM+1.) DAN20330
DO 280 J=1,NB DAN20340
280 EA(I)=EA(I)+SS*(1.D0-BX(J)/SOMEGA(KIK)) DAN20350
GO TO 290 DAN20360
61 EA(I)=0.D0 DAN20370
290 CONTINUE DAN20380
DO 300 I=1,NC DAN20390
SPIN(I)=0.D0 DAN20400
DO 300 K=1,M DAN20410
IF(K.GT.N.OR.K.LT.MNM)GO TO 300 DAN20420
SPIN(I)=SPIN(I)+EA(K)*H(I,K)**2 DAN20430
300 CONTINUE DAN20440
WRITE(NT0,69)S2 DAN20450
WRITE(NT0,19)(SPIN(I),I=1,NC) DAN20460
65 CONTINUE DAN20470
CALL MCLEAR(H,NRX,NRX,NRX) DAN20480

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C
C      CALCULATION OF D PARAMETERS          DAN20490
C      UPPER HALF OF H MATRIX=D2(I,J)        DAN20500
C      LOWER HALF OF H MATRIX=D0(I,J)        DAN20510
C      UPPER HALF OF BETA = CORE HAMILTONIAN DAN20520
C      LOWER HALF OF BETA MATRIX=D1(I,J)      DAN20530
C      ED(I)=D1(I); AX(I)=D0(I)            DAN20540
C      SEE REF. (3), TABLE V AND EQN. (9) OF REF. (4) DAN20550
C
DO 360 I=1,NB
  AX(I)=0.00
  ED(I)=0.00
  DO 310 J=1,NB
    JM=J-1
    AX(I)=AX(I)+(-1.00)**JM*CK(JM,0,NA,NB,KIK)*FA(J,I)
310 CONTINUE
  AX(I)=AX(I)/SOMEGA(KIK)
  IM=I-1
  DO 320 K=1,NB
320 ED(I)=ED(I)+(-1.00)**K*CK(K,0,NA,NB,KIK)*FA(K,I)
  ED(I)=ED(I)/SOMEGA(KIK)
  IF(I.EQ.1) GO TO 360
  DO 350 J=1,IM
    A2IJ(1)=1.00
    IF(NB.LE.1)GO TO 224
    DO 324 K=2,NB
324 A2IJ(K)=FA(K,I)-EB(J)*A2IJ(K-1)
C
C      A2IJ(K) IS ASUBK(I,J) OF REF. (2)      DAN20760
C
224 H(I,J)=0.00
  H(J,I)=0.00

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IF(NB.LE.1)GO TO 225                               DAN20810
DO 330 K=1,NBM                                     DAN20820
  KM=K-1                                         DAN20830
330 H(I,J)=H(I,J)+(-1.00)**KM*CK(KM,0,NA,NB,KIK)*A2IJ(K) DAN20840
340 H(I,J)=H(I,J)/SOMEGA(KIK)                   DAN20850
225 BETA(I,J)=(AX(I)-H(I,J))/EB(J)             DAN20860
  H(J,I)=(ED(I)-BETA(I,J))/EB(J)               DAN20870
350 CONTINUE                                       DAN20880
360 CONTINUE                                       DAN20890
C
C          PROJECTED CHARGE DENSITY CALCULATION   DAN20900
C          SEE TABLE II OF REF. (2)                DAN20910
C
C          DO 380 I=1,NC                           DAN20920
C          DO 380 J=1,I                            DAN20930
C            CB(I,J)=0.00                         DAN20940
C            DO 370 K=1,M                          DAN20950
C              IF(K.LE.NB)GO TO 75                 DAN20960
C              IF(K.LE.NA)GO TO 85                 DAN20970
C              IF(K.GT.N)GO TO 370                 DAN20980
C              IF(K.GT.NA)GO TO 95                 DAN20990
C 75    CB(I,J)=  CB(I,J)+(1.00+DSQRT(EB(K)))*(AX(K)+ED(K))*CA(I,K)*CA(J,DAN21020
C        1,K)                                     DAN21030
C        GO TO 370                                DAN21040
C 85    CB(I,J)=  CB(I,J)+CA(I,K)*CA(J,K)      DAN21050
C        GO TO 370                                DAN21060
C 95    II=M-K+1                                 DAN21070
C          CB(I,J)=  CB(I,J)+(1.00-DSQRT(EB(II)))*(AX(II)+ED(II))*CA(I,K)*CDAN21080
C        1A(J,K)                                 DAN21090
C 370  CONTINUE                                     DAN21100
C 380  CB(J,I)=CB(I,J)                           DAN21110
C          WRITE(NT0,79)S2                         DAN21120

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CALL MWRITE(CB,6HPROJ.,6HCHARGE,6HDENS.,0,NC,NC,NRX) DAN21130
E1P=CB(1,1)*BETA(1,1) DAN21140
DO 390 I=2,NC DAN21150
E1P=E1P+CB(I,I)*BETA(I,I) DAN21160
IM=I-1 DAN21170
DO 390 J=1,IM DAN21180
390 E1P=E1P+(CB(I,J)+CB(J,I))*BETA(J,I) DAN21190
WRITE(6,89)E1P DAN21200
E1UP=E1UP+SOMEGA(KIK)*E1P DAN21210
E2P=0.D0 DAN21220
QM=0 DAN21230
J=0 DAN21240
DO 430 K=1,NB DAN21250
KP=M-K+1 DAN21260
C      CALCULATE IIII DAN21270
J=J+1 DAN21280
GX=0.25D0*((1.D0+BE(K))**2)*(AX(K)+ED(K)) DAN21290
QM=QM+GX*TEND(J) DAN21300
IF(K.LT.MNM)GO TO 115 DAN21310
IF(BE(K).GT.0.999999)GO TO 115 DAN21320
C      CALCULATE I'I'I'I' DAN21330
J=J+1 DAN21340
GX=0.25D0*((1.D0-BE(K))**2)*(AX(K)+ED(K)) DAN21350
QM=QM+GX*TEND(J) DAN21360
C      CALCULATE III'I' DAN21370
J=J+1 DAN21380
GX=-0.25D0*(DELW(K)**2)*(AX(K)+ED(K)) DAN21390
QM=QM+GX*TEND(J) DAN21400
C      CALCULATE II'II' DAN21410
J=J+1 DAN21420
GX=0.25D0*(DELW(K)**2)*(AX(K)-ED(K)) DAN21430
QM=QM+GX*TEND(J) DAN21440

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C      CALCULATE II'I'I           DAN21450
GX=-0.25D0*(DELW(K)**2)*(AX(K)-ED(K))
QM=QM+GX*TENO(J-1)                      DAN21460
IF(K.EQ.NB)GO TO 125                    DAN21470
115 KAND=K+1                           DAN21480
DO 410 LN=KAND,NB                      DAN21490
LP=M-LN+1                            DAN21500
C      CALCULATE IJIJ             DAN21510
J=J+1                                 DAN21520
GX=0.5D0*(1.D0+BE(K))*(1.D0+BE(LN))*(H(LN,K)+(BE(K)+BE(LN))*BETA(L
IN,K)+BE(K)*BE(LN)*H(K,LN))          DAN21530
QM=QM+GX*TENO(J)                      DAN21540
C      CALCULATE IJJI             DAN21550
J=J+1                                 DAN21560
GX=-0.25D0*(1.D0+BE(K))*(1.D0+BE(LN))*(H(LN,K)-BETA(LN,K)+2.D0*(BE
L(K)+BE(LN))*BETA(LN,K)-BE(K)*BE(LN)*(BETA(LN,K)-H(K,LN)))        DAN21570
QM=QM+GX*TENO(J)                      DAN21580
IF(LN.LT.MNM)GO TO 116                DAN21590
IF(BE(LN).GT.0.999999)GO TO 116      DAN21600
C      CALCULATE IJ'IJ'           DAN21610
J=J+1                                 DAN21620
GX=0.5D0*(1.D0+BE(K))*(1.D0-BE(LN))*(H(LN,K)+(BE(K)-BE(LN))*BETA(L
IN,K)-BE(K)*BE(LN)*H(K,LN))          DAN21630
QM=QM+GX*TENO(J)                      DAN21640
C      CALCULATE IJ'J'I            DAN21650
J=J+1                                 DAN21660
GX=-0.25D0*(1.D0+BE(K))*(1.D0-BE(LN))*(H(LN,K)-BETA(LN,K)+2.D0*(BE
L(K)-BE(LN))*BETA(LN,K)+BE(K)*BE(LN)*(BETA(LN,K)-H(K,LN)))        DAN21670
QM=QM+GX*TENO(J)                      DAN21680
C      CALCULATE IJ'JI'           DAN21690
J=J+1                                 DAN21700
GX=-0.25D0*(1.D0+BE(K))*(1.D0-BE(LN))*(H(LN,K)-BETA(LN,K)+2.D0*(BE
L(K)-BE(LN))*BETA(LN,K)+BE(K)*BE(LN)*(BETA(LN,K)-H(K,LN)))        DAN21710
QM=QM+GX*TENO(J)                      DAN21720
116 IF(K.LT.MNM)GO TO 410            DAN21730
IF(BE(K).GT.0.999999)GO TO 410      DAN21740
C      CALCULATE JI'JI'           DAN21750

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J=J+1                                              DAN21770
GX=0.5D0*(1.D0+BE(LN))*(1.D0-BE(K))*(H(LN,K)+(BE(LN)-BE(K))*BETA(LN)  DAN21780
1N,K)-BE(LN)*BE(K)*H(K,LN))                      DAN21790
QM=QM+GX*TENO(J)                                  DAN21800
C      CALCULATE JI'I'J                           DAN21810
J=J+1                                              DAN21820
GX=-0.25D0*(1.D0+BE(LN))*(1.D0-BE(K))*(H(LN,K)-BETA(LN,K)+2.D0*(BEDAN21830
1(LN)-BE(K))*BETA(LN,K)+BE(LN)*BE(K)*(BETA(LN,K)-H(K,LN)))          DAN21840
QM=QM+GX*TENO(J)                                  DAN21850
C      CALCULATE I'J'I'J                           DAN21860
J=J+1                                              DAN21870
GX=0.5D0*(1.D0-BE(K))*(1.D0-BE(LN))*(H(LN,K)-(BE(K)+BE(LN))*BETA(LN)  DAN21880
1N,K)+BE(K)*BE(LN)*H(K,LN))                      DAN21890
QM=QM+GX*TENO(J)                                  DAN21900
C      CALCULATE I'J'I'J'I'                         DAN21910
J=J+1                                              DAN21920
GX=-0.25D0*(1.D0-BE(K))*(1.D0-BE(LN))*(H(LN,K)-BETA(LN,K)-2.D0*(BEDAN21930
1(K)+BE(LN))*(BETA(LN,K))-BE(K)*BE(LN)*(BETA(LN,K)-H(K,LN)))          DAN21940
QM=QM+GX*TENO(J)                                  DAN21950
C      CALCULATE IJJ'I'                           DAN21960
J=J+1                                              DAN21970
GX=-0.25D0*DELW(K)*DELW(LN)*(H(LN,K)+BETA(LN,K)+BE(K)*BE(LN)*(BETADAN21980
1(LN,K)+H(K,LN)))                      DAN21990
QM=QM+GX*TENO(J)                                  DAN22000
C      CALCULATE IJ'JI'                           DAN22010
J=J+1                                              DAN22020
GX=-0.25D0*DELW(K)*DELW(LN)*(H(LN,K)+BETA(LN,K)-BE(K)*BE(LN)*(BETADAN22030
1(LN,K)+H(K,LN)))                      DAN22040
QM=QM+GX*TENO(J)                                  DAN22050
410 CONTINUE                                         DAN22060
125 IF(MQ.LE.0) GO TO 430                         DAN22070
DO 425 LQ=1,MO                                     DAN22080

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LN=LQ+NB DAN22090
C   CALCULATE ITIT DAN22100
J=J+1 DAN22110
GX=0.500*(1.00+BE(K))*(AX(K)+BE(K)*ED(K)) DAN22120
QM=QM+GX*TEND(J) DAN22130
C   CALCULATE ITTI DAN22140
J=J+1 DAN22150
GX=-0.500*(1.00+BE(K))*(0.500*(AX(K)-ED(K))+BE(K)*ED(K)) DAN22160
QM=QM+GX*TEND(J) DAN22170
IF(K.LT.MNM)GO TO 425 DAN22180
IF(BE(K).GT.0.999999)GO TO 425 DAN22190
C   CALCULATE I'TI'I' DAN22200
J=J+1 DAN22210
GX=0.500*(1.00-BE(K))*(AX(K)-BE(K)*ED(K)) DAN22220
QM=QM+GX*TEND(J) DAN22230
C   CALCULATE I'TTI' DAN22240
J=J+1 DAN22250
GX=-0.500*(1.00-BE(K))*(0.500*(AX(K)-ED(K))-BE(K)*ED(K)) DAN22260
QM=QM+GX*TEND(J) DAN22270
C   CALCULATE ITTI' DAN22280
J=J+1 DAN22290
GX=-.2500*(DELW(K)*(AX(K)+ED(K))) DAN22300
420 QM=QM+GX*TEND(J) DAN22310
425 CONTINUE DAN22320
430 CONTINUE DAN22330
421 IF(MO.LE.1)GO TO 441 DAN22340
DO 440 KQ=1,MO DAN22350
K=KQ+NB DAN22360
IF(KQ.EQ.MO)GO TO 440 DAN22370
KQ1=KQ+1 DAN22380
DO 435 LQ=KQ1,MO DAN22390
LN=LQ+NB DAN22400

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C      CALCULATE TUTU          DAN22410
      J=J+1                      DAN22420
      GX=.500                     DAN22430
      QM=QM+GX*TEND(J)           DAN22440
C      CALCULATE TUUT          DAN22450
      J=J+1                      DAN22460
      GX=-.500                    DAN22470
435   QM=QM+GX*TEND(J)         DAN22480
440   CONTINUE                  DAN22490
441   CONTINUE                  DAN22500
      E2P=E2P+QM                 DAN22510
5030  CONTINUE                  DAN22520
6000  CONTINUE                  DAN22530
      ETP=E1P+E2P                DAN22540
      E2UP=E2UP+SOMEGA(KIK)*E2P  DAN22550
      WRITE(6,259)E2P             DAN22560
259   FORMAT('0',3X,'TWO-ELECTRON PART OF ENERGY = ',1PD14.6) DAN22570
      WRITE(6,99)S2,ETP            DAN22580
      XA12=ETP*SOMEGA(KIK)        DAN22590
      WRITE(6,139)XA12            DAN22600
      ETP1=ETP1+XA12              DAN22610
      WRITE(6,149)ETP1             DAN22620
      WRITE(NT0,279)E1UP            DAN22630
      WRITE(NT0,269)E2UP            DAN22640
470   CONTINUE                  DAN22650
      9 FORMAT('0','EB')           DAN22660
      19 FORMAT(' ',5(1PD15.6,2X)) DAN22670
      29 FORMAT('0','A')            DAN22680
      39 FORMAT('-', 'THE WEIGHTING FACTOR FOR THE S=',F6.4,', STATE =',1PD15DAN22690
      1.7)                         DAN22700
      49 FORMAT('0','NATURAL ORBITALS OF CHARGE') DAN22710
      59 FORMAT('1',25X,'RESULTS OF PROJECTION FOR S=',F6.4) DAN22720

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69 FORMAT('0','ATOMIC SPIN DENSITIES FOR S=',F6.4) DAN22730
79 FORMAT('0','PROJECTED CHARGE DENSITY FOR S=',F6.4) DAN22740
89 FORMAT('0','ONE-ELECTRON PART OF ENERGY =',1PD14.6) DAN22750
99 FORMAT('0','FOR S=',F8.4,5X,'ENERGY =',1PD14.6) DAN22760
119 FORMAT('0','B') DAN22770
129 FORMAT('0','A(K+1)') DAN22780
139 FORMAT('0','THE WEIGHTED ENERGY FOR THIS PROJECTION =',1PD14.6) DAN22790
149 FORMAT('0','THE SUM OF THE WEIGHTED ENERGIES FOR THE ABOVE PROJECT DAN22800
    IONS INCLUDING THIS'/5X,'PROJECTION=',1PD14.6) DAN22810
169 FORMAT(3I5) DAN22820
179 FORMAT(' ','MODIFIED NATURAL ORBITALS OF CHARGE') DAN22830
209 FORMAT('1','BEGINNING OF HARRIMAN PROJECTION TREATMENT') DAN22840
269 FORMAT('0','UNPROJECTED TWO-ELECTRON ENERGY =',1PD15.8) DAN22850
279 FORMAT('0','UNPROJECTED ONE-ELECTRON ENERGY =',1PD15.8) DAN22860
299 FORMAT('0','CALCULATION FOR ',I5,' ALPHA ELECTRONS AND ',I5,'BETA DAN22870
    ELECTRONS') DAN22880
      RETURN DAN22890
      END DAN22900
CF      FUNCTION F DAN22910
FUNCTION F(INM,MNR) DAN22920
C
C      CALCULATES FACTORIAL(INM)/FACTORIAL(MNR-1) DAN22930
C
IMPLICIT REAL*8 (A-H,O-Z) DAN22940
XF=1.00 DAN22950
IF(INM.LE.1) GO TO 5 DAN22960
DO 10 J=MNR,INM DAN22970
XJ=J DAN22980
10 XF=XF*XJ DAN22990
5 F=XF DAN23000
      RETURN DAN23010
      END DAN23020
DAN23030
DAN23040

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```

CCK      FUNCTION CK          DAN23050
FUNCTION CK(I,NLM,NA,NB,KIK) DAN23060
C
C      SUMS FACTORIALS USING EQUATION (20) OF REFERENCE (2) DAN23070
C      CSUBK(S,M,NP) WHERE K=I, 2S=NA-NB+2*(KIK-1), 2M=NA-NB, DAN23080
C      2*NP=NA+NBNL*2 DAN23090
C
C      IMPLICIT REAL*8 (A-H,O-Z) DAN23100
IB=NB-KIK+2-NLM DAN23110
IS=KIK-1 DAN23120
JS=NA-NB+KIK-1 DAN23130
NS=NBNL DAN23140
IS2=NA-NB+2*KIK-2 DAN23150
XSX=DFLOAT(IS2) DAN23160
WY=0.D0 DAN23170
IF(IB.LE.0)GO TO 45 DAN23180
IF((NS-I).LT.0)GO TO 45 DAN23190
DO 10 J=1,IB DAN23200
JM=J-1 DAN23210
IF((IB-JM-1).LT.0)GO TO 10 DAN23220
I1=J DAN23230
I2=IS+JM DAN23240
IF(IS.GT.0)GO TO 5 DAN23250
ZZ=1.D0 DAN23260
GO TO 15 DAN23270
5 ZZ=F(I2,I1) DAN23280
15 I1=IS+J-I DAN23290
I2=IS+JM DAN23300
IF((I1-1).LT.0)GO TO 10 DAN23310
IF(I.EQ.0)GO TO 25 DAN23320
YY=F(I2,I1) DAN23330
GO TO 35 DAN23340
DAN23350
DAN23360

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25 YY=1.D0 DAN23370
35 WY=(-1.D0)**JM*ZZ*YY*F(NS-I,2)/(F(IB-JM-1,2)*F1IS2+J,2))+WY DAN23380
10 CONTINUE DAN23390
    CK=(XSX+1.D0)*F(JS,1)/F1IS,1)*WY DAN23400
    RETURN DAN23410
45 CK=0.D0 DAN23420
    RETURN DAN23430
    END DAN23440
CMTBSYM      SUBROUTINE MTBSYM DAN23450
SUBROUTINE MTBSYM(A,N,NMAX) DAN23460
IMPLICIT REAL*8(A-H,O-Z) DAN23470
DIMENSION A(NMAX,NMAX) DAN23480
C      THIS SUBROUTINE SYMMETRIZES THE MATRIX A. DAN23490
C      A IS ORIGINALLY STORED IN THE TOP HALF OF A. DAN23500
C      A(J,I)=A(I,J) DAN23510
C
DO 1 J=2,N DAN23520
JM=J-1 DAN23530
DO 1 I=1,JM DAN23540
A(J,I)=A(I,J) DAN23550
1 CONTINUE DAN23560
RETURN DAN23570
END DAN23580
CMBTSYM      SUBROUTINE MBTSYM DAN23600
SUBROUTINE MBTSYM(A,N,NMAX) DAN23610
IMPLICIT REAL*8(A-H,O-Z) DAN23620
DIMENSION A(NMAX,NMAX) DAN23630
C      THIS SUBROUTINE SYMMETRIZES THE MATRIX A. DAN23640
C      A IS ORIGINALLY STORED IN THE LOWER HALF OF A. DAN23650
C      A(I,J)=A(J,I) DAN23660
DO 1 J=2,N DAN23670
JM=J-1 DAN23680

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DO 1 I=1,JM          DAN23690
A(I,J)=A(J,I)        DAN23700
1 CONTINUE           DAN23710
RETURN              DAN23720
END                 DAN23730
CSWITCH      SUBROUTINE SWITCH          DAN23740
SUBROUTINE SWITCH(A,B,NR,NC,NRX)        DAN23750
IMPLICIT REAL*8(A-H,O-Z)               DAN23760
DIMENSION A(NRX,NRX),B(NRX,NRX)        DAN23770
C          SUBROUTINE SWITCHES ROWS FOR COLUMNS IN MATRIX A.   DAN23780
C          B IS A DUMMY MATRIX USED TO SWITCH ROWS FOR COLUMNS   DAN23790
DO 10 I=1,NC          DAN23800
DO 10 J=1,NR          DAN23810
10 B(I,J)=A(J,I)      DAN23820
DO 20 I=1,NC          DAN23830
DO 20 J=1,NR          DAN23840
20 A(I,J)=B(I,J)      DAN23850
RETURN              DAN23860
END                 DAN23870
CMMBAT2      SUBROUTINE MMBAT2          DAN23880
SUBROUTINE MMBAT2(A,B,NCA,NR,NCB,X,NBMX) DAN23890
IMPLICIT REAL*8(A-H,O-Z)               DAN23900
DIMENSION A(NBMX,NBMX),B(NBMX,NBMX),X(NBMX) DAN23910
C
C          THIS SUBROUTINE COMPUTES THE MATRIX PRODUCT          DAN23920
C          C = B * AT                                         DAN23930
C          WHERE AT IS THE TRANPOSE OF A, A IS NR BY NCA, B IS NCB BY NRDAN23950
C          AND THE RESULT C IS NCB BY NCA (ROWS BY COLUMNS)       DAN23960
C          ON RETURN FROM THIS SUBROUTINE B CONTAINS C, A CONTAINS AT. DAN23970
C          TAKE THE TRANPOSE OF A. STORE RESULTS IN A.          DAN23980
DOUBLE PRECISION SUM          DAN23990
NMAX=NR            DAN24000

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IF(NCA.GT.NR)NMAX=NCA                               DAN24010
DO 3 J=2,NMAX                                      DAN24020
IHI=J-1                                            DAN24030
DO 3 I=1,IHI                                       DAN24040
FT=A(I,J)                                         DAN24050
A(I,J)=A(J,I)                                     DAN24060
A(J,I)=FT                                         DAN24070
3 CONTINUE                                         DAN24080
C                                                 DAN24090
C         COMPUTE C ONE ROW AT A TIME.  STORE THE ROW IN X.  THEN STORE DAN24100
C         X IN B.                                    DAN24110
C                                                 DAN24120
C         DO 7 I=1,NCB                           DAN24130
C                                                 DAN24140
C         COMPUTE A ROW OF C. STORE IT IN X       DAN24150
C                                                 DAN24160
C         DO 5 K=1,NCA                           DAN24170
SUM=0.D0                                           DAN24180
DO 4 J=1,NR                                         DAN24190
SUM=SUM+B(I,J)*A(J,K)                           DAN24200
4 CONTINUE                                         DAN24210
X(K)=SUM                                         DAN24220
5 CONTINUE                                         DAN24230
C                                                 DAN24240
C         STORE ROW IN B                         DAN24250
DO 6 K=1,NCA                                      DAN24260
B(I,K)=X(K)                                       DAN24270
6 CONTINUE                                         DAN24280
7 CONTINUE                                         DAN24290
RETURN                                            DAN24300
END                                              DAN24310
CMULT2    SUBROUTINE MULT2                      DAN24320

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C SUBROUTINE MULT2(A,B,C,N,NRX) DAN24330
C MATRIX MULTIPLICATION ROUTINE FOR SQUARE MATRICES. DAN24340
C C = A * B DAN24350
C IMPLICIT REAL*8(A-H,O-Z) DAN24360
C DIMENSION A(NRX,NRX),B(NRX,NRX),C(NRX,NRX) DAN24370
DO 10 I=1,N DAN24380
DO 10 J=1,N DAN24390
C(I,J)=0.D0 DAN24400
DO 10 M=1,N DAN24410
10 C(I,J)=C(I,J)+A(I,M)*B(M,J) DAN24420
      RETURN DAN24430
      END DAN24440
CLAB          SUBROUTINE LAB DAN24450
SUBROUTINE LAB DAN24460
COMMON/LABELS/ILBL(12),ILAB(12) DAN24470
COMMON/ZEIT/LAPSE,LAPST DAN24480
REAL*8 ILBL,ILAB DAN24490
REAL*4 LAPSE,LAPST DAN24500
COMMON/IOIND/ICON(24) DAN24510
WRITE(6,101)ILAB DAN24520
READ(5,100)ILBL DAN24530
WRITE(6,102)ILBL DAN24540
READ(5,200) (ICON(I),I=1,24) DAN24550
WRITE(6,201) (I,I=1,24),(ICON(I),I=1,24) DAN24560
LAPSN=0.0 DAN24570
CALL STIME(ITIME) DAN24580
LAPSE=(FLOAT(ITIME))*0.36 DAN24590
LAPST=LAPSE DAN24600
      RETURN DAN24610
100 FORMAT(12A6) DAN24620
101 FORMAT(1H1///29X,12A6//) DAN24630
102 FORMAT(29X,12A6//) DAN24640

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200 FORMAT(24I3) DAN24650
201 FORMAT(51X,28H** INPUT - OUTPUT OPTIONS **/29X,24I3/29X,24I3) DAN24660
END DAN24670
CFILE SUBROUTINE FILE (NAMFIL,NTAPE,LABLE) DAN24680
SUBROUTINE FILE(NAMFIL,NTAPE,LABLE) DAN24690
C THE SUBROUTINE FILE SEARCHES THE FILE UNIT NTAPE FOR THE DATA DAN24700
C FILE NAMED NAMFIL. IF IT FINDS IT THE FILE UNIT IS POSITIONED TO DAN24710
C READ THE FILE. DAN24720
REAL*8 NAMFIL,LABLE,NAMTAP DAN24730
EQUIVALENCE (NOFILE,XNOMFIL) DAN24740
COMMON /IOIND/ ICON(24) DAN24750
DIMENSION LABLE(1) DAN24760
NT=NTAPE DAN24770
IF(ICON(10).GT.0) WRITE(6,100) NT,NAMFIL DAN24780
M=3 DAN24790
1 CALL EFSKIP (NT,1) DAN24800
READ(NT) NAMTAP,NOFILE,(LABLE(I),I=3,NOFILE) DAN24810
C SEARCH FOR FILE NAME DAN24820
DO3I=M,NOFILE DAN24830
II=I DAN24840
IF(LABLE(I).EQ.NAMFIL) GOTO6 DAN24850
3 CONTINUE DAN24860
IF(LABLE(NOFILE).EQ.0) GOTO10 DAN24870
M=NOFILE+1 DAN24880
GOTO1 DAN24890
C FOUND FILE NAME DAN24900
6 IF(ICON(10).GT.0) WRITE(6,105) DAN24910
IF(NOFILE.EQ.I) GOTO9 DAN24920
C CALL EFSKIP(NT,(I-NOFILE-1)) DAN24930
C CALL EFSKIP(NT,1) DAN24940
REWIND NT DAN24950
CALL EFSKIP ( NT,I-2) DAN24960

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        READ(NT) NAMTAP,NOFILE,(LABLE(I),I=3,NOFILE)
        IF(LABLE(NOFILE).EQ.NAMFIL) GOT09
10      WRITE(6,107)NT,NAMFIL
107     FORMAT(33H0FILE LABELLED WRONG ON FILE NO. I3/
112H0FILE LABEL A6,17H CAN NOT BE FOUND)
        CALL ABT
9       LABLE(1)=NAMTAP
        LABLE(2)=XNOFIL
        RETURN
100    FORMAT(70X,4HTAPE,I3, 19H SEARCHED FOR FILE A6)
105    FORMAT(70X,15HFILE NAME FOUND  )
        END

CSEC          SUBROUTINE SEC
        SUBROUTINE SEC(A,B,C)
        COMMON/ZEIT/LAPSE,LAPST
        REAL*4 LAPSE,LAPST,LAPSN
        REAL*8 A,B,C
        CALL STIME(ITIME)
        LAPSN=(FLOAT(ITIME))*0.36
        TIM=LAPSN-LAPSE
        LAPSE=LAPSN
        WRITE(6,100) A,B,C, TIM
        RETURN
100    FORMAT(/50X,3A6,15H ELAPSED TIME =,F9.3,8H SECONDS )
        END

CMMOVE          SUBROUTINE MMOVE
        SUBROUTINE MMOVE(A,B,NR,NC,NMAX)
        IMPLICIT REAL*8 (A-H,O-Z)
        DIMENSION A(NMAX,NMAX),B(NMAX,NMAX)
C...THIS SUBROUTINE SETS THE NR BY NC ELEMENTS OF A EQUAL TO THE
C...CORRESPONDING ELEMENTS OF B.
        DO 1 I=1,NR

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      DO 1 J=1,NC                               DAN25290
      B(I,J)=A(I,J)                           DAN25300
1   CONTINUE                                 DAN25310
      RETURN                                  DAN25320
      END                                     DAN25330
CMWRITT          SUBROUTINE MWRITT           DAN25340
      SUBROUTINE MWRITT(A,WA,WB,WC,ITR,NC,NRX) DAN25350
      IMPLICIT REAL*8 (A-H,O-Z)               DAN25360
C...THIS SUBROUTINE PRINTS OUT THE UPPER TRIANGULAR HALF (INCLUDING THE DAN25370
C...DIAGONAL) OF THE MATRIX A.                DAN25380
      DIMENSION A(NRX,NRX)                   DAN25390
      REAL*8 WA,WB,WC,ILBL,ILAB              DAN25400
      COMMON/LABELS/ILBL(12),ILAB(12)        DAN25410
      WRITE(6,100) (ILBL(I),I=1,12),WA,WB,WC DAN25420
      IF(ITR.GT.0) WRITE(6,101) ITR          DAN25430
      WRITE(6,102) (M,M=1,10)                 DAN25440
      DO 1 I=1,NC                           DAN25450
      WRITE(6,104) I,(A(J,I),J=1,I)         DAN25460
1   CONTINUE                                 DAN25470
      RETURN                                  DAN25480
100  FORMAT(1H1//31X,12A6/58X,3A6)          DAN25490
101  FORMAT(61X,10HITERATION ,I3)          DAN25500
102  FORMAT(4HOROW,5X,I2,9(10X,I2))       DAN25510
104  FORMAT(14,10F12.7/(4X,10F12.7))     DAN25520
      END                                     DAN25530
CMMATB1          SUBROUTINE MMATB1           DAN25540
      SUBROUTINE MMATB1(A,B,NCA,NR,NCB,X,NBMX) DAN25550
      IMPLICIT REAL*8 (A-H,O-Z)               DAN25560
      DIMENSION A(NBMX,NBMX),B(NBMX,NBMX),X(1) DAN25570
C...THIS SUBROUTINE COMPUTES THE MATRIX PRODUCT - DAN25580
C...          C = AT * B                  DAN25590
C...WHERE AT IS THE TRANPOSE OF A, A IS NR BY NCA, B IS NR BY NCB, DAN25600

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C...AND THE RESULT, C, IS NCA BY NCB. ( ROWS BY COLUMNS) DAN25610
C...ON RETURN FROM THIS SUBROUTINE A CONTAINS C, B IS UNAFFECTED. DAN25620
C...THE VECTOR X IS USED FOR TEMPORARY STORAGE. DAN25630
C...TAKE TRANSPOSE OF A. STORE RESULT IN A. DAN25640
    DOUBLE PRECISION SUM DAN25650
    NMAX=NR DAN25660
    IF(NCA.GT.NR) NMAX=NCA DAN25670
    DO3J=2,NMAX DAN25680
    IH1=J-1 DAN25690
    DO3I=1,IH1 DAN25700
    FT=A(I,J) DAN25710
    A(I,J)=A(J,I) DAN25720
    A(J,I)=FT DAN25730
3  CONTINUE DAN25740
C...COMPUTE C ONE ROW AT A TIME. STORE THE ROW IN X. THEN STORE X BACK DAN25750
C...IN A. DAN25760
    DO 7 I=1,NCA DAN25770
C...COMPUTE A ROW OF C. STORE IT IN X. DAN25780
    DO 5 K=1,NCB DAN25790
    SUM=0.000 DAN25800
    DO 4 J=1,NR DAN25810
    SUM=SUM+A(I,J)*B(J,K) DAN25820
4  CONTINUE DAN25830
    X(K)=SUM DAN25840
5  CONTINUE DAN25850
C...STORE THE ROW BACK IN A. DAN25860
    DO 6 K=1,NCB DAN25870
    A(I,K)=X(K) DAN25880
6  CONTINUE DAN25890
7  CONTINUE DAN25900
    RETURN DAN25910
    END DAN25920

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CMCLR	SUBROUTINE MCLR	DAN25930
	SUBROUTINE MCLR(A,N,NMAX)	DAN25940
	IMPLICIT REAL*8 (A-H,O-Z)	DAN25950
	DIMENSION A(NMAX,NMAX)	DAN25960
C...THIS SUBROUTINE SETS ALL THE ELEMENTS IN THE UPPER TRIANGULAR HALF		DAN25970
C... (INCLUDING THE DIAGONAL) OF A EQUAL TO 0.0 THE POSITION OF THE		DAN25980
C... 1,1 ELEMENT OF A IS DEFINED BY THE CALLING PROGRAM.		DAN25990
DO 1 J=1,N		DAN26000
DO 1 I=1,J		DAN26010
A(I,J)=0.0		DAN26020
1 CONTINUE		DAN26030
RETURN		DAN26040
END		DAN26050
CMCLEAR	SUBROUTINE MCLEAR	DAN26060
	SUBROUTINE MCLEAR(A,NR,NC,NMAX)	DAN26070
	IMPLICIT REAL*8 (A-H,O-Z)	DAN26080
	DIMENSION A(NMAX,NMAX)	DAN26090
C...THIS SUBROUTINE SETS THE NR BY NC ELEMENTS OF A EQUAL TO 0.0		DAN26100
C... THE 1,1 ELEMENT OF A IS DEFINED BY THE CALLING PROGRAM.		DAN26110
DO 1 J=1,NC		DAN26120
DO 1 I=1,NR		DAN26130
A(I,J)=0.0		DAN26140
1 CONTINUE		DAN26150
RETURN		DAN26160
END		DAN26170
CHDIAG	SUBROUTINE HDIAG	DAN26180
	SUBROUTINE HDIAG(H,U,X,IQ,N,NBMX,IEGEN,NR)	DAN26190
	IMPLICIT REAL*8 (A-H,O-Z)	DAN26200
C	FORTRAN IV DIAGONALIZATION OF A REAL SYMMETRIC MATRIX BY THE	DAN26210
C	JACOBI METHOD.	DAN26220
C	MAY 19,1959,REVISED TO FORTRAN IV AUG 17,1966	DAN26230
C	CALLING SEQUENCE FOR DIAGONALIZATION	DAN26240

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C           CALL HDIAG(H,U,X,IQ,N,NBMX,IEGEN,NR)          DAN26250
C           WHERE H IS THE ARRAY TO BE DIAGONALIZED.        DAN26260
C           N IS THE ORDER OF THE MATRIX, H.                 DAN26270
C           IEGEN MUST BE SET UNEQUAL TO ZERO IF ONLY EIGENVALUES ARE DAN26280
C           TO BE COMPUTED.                                DAN26290
C           IEGEN MUST BE SET EQUAL TO ZERO IF EIGENVALUES AND EIGENVECTORS DAN26300
C           ARE TO BE COMPUTED.                            DAN26310
C           U IS THE UNITARY MATRIX USED FOR FORMATION OF THE EIGENVECTORS. DAN26320
C           NR IS THE NUMBER OF ROTATIONS.                DAN26330
C           NBMX IS THE MAXIMUM ORDER OF THE MATRIX H TO BE DIAGONALISED DAN26340
C           X,IQ ARE ADDITIONAL ARRAYS BOTH ARE OF LENGTH AT LEAST NBMX DAN26350
C           THE SUBROUTINE OPERATES ONLY ON THE ELEMENTS OF H THAT ARE TO THE DAN26360
C           RIGHT OF THE MAIN DIAGONAL.  THUS, ONLY A TRIANGULAR DAN26370
C           SECTION NEED BE STORED IN THE ARRAY H.          DAN26380
C           DIMENSION H(NBMX,NBMX),U(NBMX,NBMX),X(1),IQ(1) DAN26390
C           SET INDICATOR FOR SHUT OFF RAP IS APPROX 2**-45. DAN26400
C           SPECIFICALLY FOR THE CDC6600 48 BIT MANTISSA DAN26410
C           DATA RAPS/2.0E-13/,HDTES/1.0E38/               DAN26420
C           IF(IEGEN.NE.0) GO TO 15                         DAN26430
C           DO 10 I=1,N                                     DAN26440
C           DO 10 J=1,N                                     DAN26450
C           U(I,J)=0.                                    DAN26460
C           IF(I.EQ.J) U(I,J)=1.                          DAN26470
10            CONTINUE                                     DAN26480
15            NR=0                                       DAN26490
C           IF(N.LE.1) RETURN                           DAN26500
C           SCAN FOR LARGEST OFF DIAGONAL ELEMENT IN EACH ROW DAN26510
C           X(I) CONTAINS LARGEST ELEMENT IN ITH ROW       DAN26520
C           IQ(I) HOLDS SECOND SUBSCRIPT DEFINING POSITION OF ELEMENT DAN26530
C           NM1=N-1                                      DAN26540
C           DO 30 I=1,NM1                               DAN26550
C           X(I)=0.                                    DAN26560

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IPL1=I+1                               DAN26570
DO 30 J=IPL1,N                         DAN26580
IF(X(I).GT.DABS(H(I,J))) GO TO 30    DAN26590
X(I)=DABS(H(I,J))                     DAN26600
IQ(I)=J                                DAN26610
30 CONTINUE                             DAN26620
C   SET UP ZERO CUT OFF (RAP) , INITIALIZE HDTEST.      DAN26630
RAP=7.45058060E-9                      DAN26640
HTEST=1.0E38                            DAN26650
C   FIND MAXIMUM OF X(I) S FOR PIVOT ELEMENT AND TEST FOR END OF PROB DAN26660
40 DO 70 I=1,NMII1                     DAN26670
IF(I.LE.1) GO TO 60                     DAN26680
IF(XMAX.GE.X(I)) GO TO 70             DAN26690
60 XMAX=X(I)                           DAN26700
IPIV=I                                 DAN26710
JPIV=IQ(I)                            DAN26720
70 CONTINUE                            DAN26730
C   IS MAX. X(I) EQUAL TO ZERO, IF LESS THAN HDTEST, REVISE HDTEST      DAN26740
IF(XMAX.LE.0.0) RETURN                 DAN26750
IF(HTEST.LE.0.0) GO TO 90              DAN26760
IF(XMAX.GT.HTEST) GO TO 148           DAN26770
90 HDIMIN=DABS(H(1,1))                DAN26780
DO 110 I= 2,N                         DAN26790
IF(HDIMIN.GT.DABS(H(I,I))) HDIMIN=DABS(H(I,I))          DAN26800
110 CONTINUE                            DAN26810
HTEST=HDIMIN*RAP                      DAN26820
C   RETURN IF MAX.H(I,J)LESS THAN RAP*ABS(MIN(H(K,K)))      DAN26830
IF(HTEST.GE.XMAX) RETURN               DAN26840
148 NR = NR+1                          DAN26850
C   COMPUTE TANGENT, SINE AND COSINE,H(I,I),H(J,J)      DAN26860
150 TANG=DSIGN(2.00,(H(IPIV,IPIV)-H(JPIV,JPIV))*H(IPIV,JPIV)/(DABS DAN26870
     1(H(IPIV,IPIV)-H(JPIV,JPIV))+DSQRT((H(IPIV,IPIV)-H(JPIV,JPIV))**2 DAN26880

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2 +4.0*H(IPIV,JPIV)**2))
COSINE=1./DSQRT(1.+TANG**2)
SINE=TANG*COSINE
HII=H(IPIV,IPIV)
H(IPIV,IPIV)=COSINE**2*(HII+TANG*(2.*H(IPIV,JPIV)+TANG*H(JPIV,JPIV)
1)))
H(JPIV,JPIV)=COSINE**2*(H(JPIV,JPIV)-TANG*(2.*H(IPIV,JPIV)-TANG*H
1II))
H(IPIV,JPIV)=0.
C PSEUDO RANK THE EIGENVALUES DAN26970
C ADJUST SINE AND COS FOR COMPUTATION OF H(IK) AND U(IK) DAN26980
IF(H(IPIV,IPIV).GE.H(JPIV,JPIV)) GO TO 153 DAN26990
HTEMP=H(IPIV,IPIV)
H(IPIV,IPIV)=H(JPIV,JPIV)
H(JPIV,JPIV)=HTEMP DAN27000
C RECOMPUTE SINE AND COS DAN27010
HTEMP=DSIGN(1.0,-SINE)*COSINE DAN27020
COSINE=DABS(SINE)
SINE=HTEMP DAN27030
153 CONTINUE DAN27040
C THE I OR J ROW. DAN27050
DO 350 I=1,NMII DAN27060
IF(I.EQ.IPIV.OR.I.EQ.JPIV) GO TO 350 DAN27070
IF(IQ(I).NE.IPIV.AND.IQ(I).NE.JPIV) GO TO 350 DAN27080
K=IQ(I)
HTEMP=H(I,K)
H(I,K)=0.
IPL1=I+1 DAN27090
X(I)=0.
C SEARCH IN DEPLETED ROW FOR NEW MAXIMUM DAN27100
DO 320 J=IPL1,N DAN27110
IF(X(I).GT.DABS(H(I,J))) GO TO 320 DAN27120

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X(I)=DABS(H(I,J))                               DAN27210
IQ(I)=J                                         DAN27220
320 CONTINUE                                     DAN27230
H(I,K)=HTEMP                                    DAN27240
350 CONTINUE                                     DAN27250
X(IPIV)=0.                                      DAN27260
X(JPIV)=0.                                      DAN27270
DO 530 I=1,N                                    DAN27280
IF(I-IPIV)370,530,420                           DAN27290
370 HTEMP = H(I,IPIV)                           DAN27300
H(I,IPIV) = COSINE*HTEMP + SINE*H(I,JPIV)     DAN27310
IF(X(I).GE.DABS(H(I,IPIV))) GO TO 390        DAN27320
X(I)=DABS(H(I,IPIV))                          DAN27330
IQ(I)=IPIV                                     DAN27340
390 H(I,JPIV) = -SINE*HTEMP + COSINE*H(I,JPIV) DAN27350
IF(X(I).GE.DABS(H(I,JPIV))) GO TO 530        DAN27360
X(I)=DABS(H(I,JPIV))                          DAN27370
IQ(I)=JPIV                                     DAN27380
GO TO 530                                     DAN27390
420 IF(I-JPIV)430,530,480                      DAN27400
430 HTEMP = H(IPIV,I)                           DAN27410
H(IPIV,I) = COSINE*HTEMP + SINE*H(I,JPIV)     DAN27420
IF(X(IPIV).GE.DABS(H(IPIV,I))) GO TO 450      DAN27430
X(IPIV)=DABS(H(IPIV,I))                      DAN27440
IQ(IPIV)=I                                     DAN27450
450 H(I,JPIV) = -SINE*HTEMP + COSINE*H(I,JPIV) DAN27460
IF(X(I).GE.DABS(H(I,JPIV))) GO TO 530        DAN27470
X(I)=DABS(H(I,JPIV))                          DAN27480
IQ(I)=JPIV                                     DAN27490
GO TO 530                                     DAN27500
480 HTEMP = H(IPIV,I)                           DAN27510
H(IPIV,I) = COSINE*HTEMP + SINE*H(IPIV,I)      DAN27520

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IF(X(IPIV).GE.DABS(H(IPIV,I))) GO TO 500          DAN27530
X(IPIV)=DABS(H(IPIV,I))                          DAN27540
IQ(IPIV)=I                                      DAN27550
500 H(JPIV,I) = -SINE*HTEMP + COSINE*H(JPIV,I)    DAN27560
IF(X(JPIV).GT.DABS(H(JPIV,I))) GO TO 530        DAN27570
X(JPIV)=DABS(H(JPIV,I))                          DAN27580
IQ(JPIV)=I                                      DAN27590
530 CONTINUE                                     DAN27600
C TEST FOR COMPUTATION OF EIGENVECTORS           DAN27610
IF(IEGEN.NE.0) GO TO 40                          DAN27620
DO 550 I=1,N                                     DAN27630
HTEMP=U(I,IPIV)                                 DAN27640
U(I,IPIV)=COSINE*HTEMP+SINE*U(I,JPIV)          DAN27650
550 U(I,JPIV)=-SINE*HTEMP+COSINE*U(I,JPIV)      DAN27660
GO TO 40                                         DAN27670
END
CFOLLOW      SUBROUTINE FOLLOW                  DAN27680
SUBROUTINE FOLLOW                               DAN27690
COMMON /ZEIT/ LAPSE,LAPST                      DAN27700
COMMON /LABELS/ ILBL(12),ILAB(12)                DAN27710
REAL*8 ILBL,ILAB                                DAN27720
REAL*4 LAPSE,LAPST                             DAN27730
LAPSE = LAPST                                    DAN27740
WRITE (6,100) ILAB                            DAN27750
WRITE (6,101) ILBL                            DAN27760
CALL SEC (6HFINISH,6HED PRO,6HBLEM      )     DAN27770
STOP
100 FORMAT( 1H1 //// 15X 12A6)                  DAN27780
101 FORMAT ( 15X 12A6)                         DAN27790
END
CFMFUHF      SUBROUTINE FMFUHF                  DAN27800
SUBROUTINE FMFUHF(A,B,C,NC,NRX)                 DAN27810
                                                DAN27820
                                                DAN27830
                                                DAN27840

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IMPLICIT REAL*8 (A-H,O-Z) DAN27850
DIMENSION A(NRX,NRX),B(NRX,NRX),C(NRX,NRX) DAN27860
C...THIS SUBROUTINED FORMS THE UNRESTRICTED HARTREE FOCK HAMILTONIAN DAN27870
C...MATICES, FA AND FB. DAN27880
C... FA = H + JT - KA DAN27890
C... FB = H + JT - KB DAN27900
C...ON ENTRY C CONTAINS THE MATRIX FT, FT = H + JT, A CONTAINS KA, AND DAN27910
C...B CONTAINS KB. ON EXIT A CONTAINS FA, AND B CONTAINS FB. ONLY THE DAN27920
C...UPPER TRIANGULAR HALF (INCLUDING THE DIAGONAL) OF A, B, AND C IS DAN27930
C...USED IN THIS ROUTINE AS ALL THE MATRICES ARE SYMMETRIC. DAN27940
DO 2 J=1,NC DAN27950
DO 1 I=1,J DAN27960
A(I,J)= C(I,J)-A(I,J) DAN27970
B(I,J)= C(I,J)-B(I,J) DAN27980
1 CONTINUE DAN27990
2 CONTINUE DAN28000
RETURN DAN28010
END DAN28020
CFMJUHF SUBROUTINE FMJUHF DAN28030
SUBROUTINE FMJUHF(T,R,S,TT,RR,SS,NBFNS,NBMX,NAM,NITAPE,ILABL, DAN28040
1 PKLABL,VALUEM,NINMAX,IPTI,CUTLO,IX) DAN28050
IMPLICIT REAL*8 (A-H,O-Z) DAN28060
REAL*8 INTNAM,ILABL,ILAB,ILBL,NAM DAN28070
DIMENSION T(NBMX,NBMX),TT(NBMX,NBMX),R(NBMX,NBMX), DAN28080
1 RR(NBMX,NBMX),S(NBMX,NBMX),SS(NBMX,NBMX), DAN28090
1 PKLABL(NINMAX),VALUEM(NINMAX), DAN28100
1 IPRT(36),ILABL(1) DAN28110
DAN28120
C...INITIALIZE COUNTERS. DAN28130
NRECNT=0 DAN28140
LSUMNW=0 DAN28150
NMINNW=0 DAN28160
IRC=1

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C...PRINT HEADER IF CHECK SUM FLAG IS ON.	DAN28170
IF(IPTI.EQ.0) GO TO 70	DAN28180
WRITE(6,100)	DAN28190
70 CONTINUE	DAN28200
C...POSITION TAPE TO READ TWO ELECTRON INTEGRALS.	DAN28210
CALL FILE(NAM,NITAPE,ILABL)	DAN28220
C...LOOP UNTIL LAST RECORD OF TWO ELECTRON INTEGRALS IS REACHED	DAN28230
C...READ A RECORD OF INTEGRALS.	DAN28240
72 READ(NITAPE) NINTS,LSTRCD,PKLABL,VALUEM	DAN28250
C...UP RECORD COUNTER.	DAN28260
NRECNT=NRECNT+1	DAN28270
C...SET UP AND PRINT CHECKSUMS IF CHECKSUM PRINT FLAG IS ON.	DAN28280
IF(IPTI.EQ.0) GO TO 75	DAN28290
IF(IRC.EQ.1) IPRT(1)=NRECNT	DAN28300
CALL UNPACK(PKLABL(1),IA,JA,KA,LA,IZ,ITA)	DAN28310
CALL UNPACK(PKLABL(NINTS),IB,JB,KB,LB,IZ,ITB)	DAN28320
IPRT(IRC+1)=JA	DAN28330
IPRT(IRC+2)=LA	DAN28340
IPRT(IRC+3)=NINTS	DAN28350
IPRT(IRC+4)=JB	DAN28360
IPRT(IRC+5)=LB	DAN28370
IRC=IRC+5	DAN28380
IF(IRC.NE.36) GO TO 75	DAN28390
WRITE(6,103) IPRT	DAN28400
IRC=1	DAN28410
C...CHECK FOR ERRONEOUS VALUES OF NINTS.	DAN28420
75 IF(NINTS.GT.NINMAX.OR.NINTS.LE.0) GO TO 500	DAN28430
C...LOOP ON EACH INTEGRAL.	DAN28440
C...PLACE EACH INTEGRAL WITH ITS PROPER MULTIPLIER IN THE MATRICES.	DAN28450
DO 29 M=1,NINTS	DAN28460
V=VALUEM(M)	DAN28470
CALL UNPACK(PKLABL(M),I,J,K,L,MU,IZ)	DAN28480

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C...SKIP THE INTEGRAL IF ITS VALUE IS SMALL.          DAN28490
  IF(DABS(V).LT.CUTL) GO TO 29                     DAN28500
  LSUMNW=LSUMNW+L                                     DAN28510
  NMINNW=NMINNW+1                                     DAN28520
C...DEPENDING ON THE TYPE OF LABEL OF THE INTEGRAL AS GIVEN BY THE DAN28530
C...INDEX MU, MULTIPLY THE VALUE OF THE INTEGRAL BY ITS PROPER DAN28540
C...DENSITY MATRIX PREFACTORS AND ADD THE PRODUCTS TO THE PROPER ELEMENT DAN28550
C...OF THE MATRICES TO BE FORMED.                   DAN28560
  GOTO(12,13,14,15,16,17,18,19,20,21,22,23,24,25),MU   DAN28570
C...I/I/I/I..
  12  T(I,I)=T(I,I)+TT(I,I)*V                      DAN28580
      R(I,I)=R(I,I)+RR(I,I)*V                      DAN28590
      S(I,I)=S(I,I)+SS(I,I)*V                      DAN28600
      GO TO 29                                      DAN28610
C...I/J/I/J...I.GT.J                               DAN28630
  13  T(J,I)=T(J,I)+2.*TT(I,J)*V                  DAN28640
      R(J,I)=R(J,I)+RR(I,J)*V                      DAN28650
      S(J,I)=S(J,I)+SS(I,J)*V                      DAN28660
      R(I,I)=R(I,I)+RR(J,J)*V                      DAN28670
      S(I,I)=S(I,I)+SS(J,J)*V                      DAN28680
      R(J,J)=R(J,J)+RR(I,I)*V                      DAN28690
      S(J,J)=S(J,J)+SS(I,I)*V                      DAN28700
      GO TO 29                                      DAN28710
C...I/I/K/K...I.GT.K                               DAN28720
  14  T(I,I)=T(I,I)+TT(K,K)*V                      DAN28730
      T(K,K)=T(K,K)+TT(I,I)*V                      DAN28740
      R(K,I)=R(K,I)+RR(I,K)*V                      DAN28750
      S(K,I)=S(K,I)+SS(I,K)*V                      DAN28760
      GO TO 29                                      DAN28770
C...I/I/I/L...I.GT.L                               DAN28780
  15  T(L,I)=T(L,I)+TT(I,I)*V                      DAN28790
      T(I,I)=T(I,I)+2.*TT(I,L)*V                  DAN28800

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R(L,I)=R(L,I)+RR(I,I)*V	DAN28810
S(L,I)=S(L,I)+SS(I,I)*V	DAN28820
R(I,I)=R(I,I)+2.*RR(I,L)*V	DAN28830
S(I,I)=S(I,I)+2.*SS(I,L)*V	DAN28840
GO TO 29	DAN28850
C...I/I/K/L...I.GT.K.GT.L	
16 T(L,K)=T(L,K)+TT(I,I)*V	DAN28860
T(I,I)=T(I,I)+2.*TT(K,L)*V	DAN28870
R(L,I)=R(L,I)+RR(I,K)*V	DAN28880
S(L,I)=S(L,I)+SS(I,K)*V	DAN28890
R(K,I)=R(K,I)+RR(I,L)*V	DAN28900
S(K,I)=S(K,I)+SS(I,L)*V	DAN28910
GO TO 29	DAN28920
C...I/J/J/J...I.GT.J	
17 T(J,J)=T(J,J)+2.*TT(I,J)*V	DAN28930
T(J,I)=T(J,I)+TT(J,J)*V	DAN28940
R(J,J)=R(J,J)+2.*RR(I,J)*V	DAN28950
S(J,J)=S(J,J)+2.*SS(I,J)*V	DAN28960
R(J,I)=R(J,I)+RR(J,J)*V	DAN28970
S(J,I)=S(J,I)+SS(J,J)*V	DAN28980
GO TO 29	DAN28990
C...I/J/K/K...I.GT.J.GT.K	
18 T(K,K)=T(K,K)+2.*TT(I,J)*V	DAN29000
T(J,I)=T(J,I)+TT(K,K)*V	DAN29010
R(K,J)=R(K,J)+RR(I,K)*V	DAN29020
S(K,J)=S(K,J)+SS(I,K)*V	DAN29030
R(K,I)=R(K,I)+RR(J,K)*V	DAN29040
S(K,I)=S(K,I)+SS(J,K)*V	DAN29050
GO TO 29	DAN29060
C...I/J/K/K...I.GT.K.GT.J	
19 T(K,K)=T(K,K)+2.*TT(I,J)*V	DAN29070
T(J,I)=T(J,I)+TT(K,K)*V	DAN29080
	DAN29090
	DAN29100
	DAN29110
	DAN29120

R(J,K)=R(J,K)+RR(I,K)*V	DAN29130
S(J,K)=S(J,K)+SS(I,K)*V	DAN29140
R(K,I)=R(K,I)+RR(K,J)*V	DAN29150
S(K,I)=S(K,I)+SS(K,J)*V	DAN29160
GO TO 29	DAN29170
C...I/J/J/L...I.GT.J.GT.L	DAN29180
20 T(J,I)=T(J,I)+2.*TT(J,L)*V	DAN29190
T(L,J)=T(L,J)+2.*TT(I,J)*V	DAN29200
R(J,J)=R(J,J)+2.*RR(I,L)*V	DAN29210
S(J,J)=S(J,J)+2.*SS(I,L)*V	DAN29220
R(J,I)=R(J,I)+RR(J,L)*V	DAN29230
S(J,I)=S(J,I)+SS(J,L)*V	DAN29240
R(L,J)=R(L,J)+RR(I,J)*V	DAN29250
S(L,J)=S(L,J)+SS(I,J)*V	DAN29260
R(L,I)=R(L,I)+RR(J,J)*V	DAN29270
S(L,I)=S(L,I)+SS(J,J)*V	DAN29280
GO TO 29	DAN29290
C...I/J/I/L...I.GT.J.GT.L	DAN29300
21 T(J,I)=T(J,I)+2.*TT(I,L)*V	DAN29310
T(L,I)=T(L,I)+2.*TT(I,J)*V	DAN29320
R(I,I)=R(I,I)+2.*RR(J,L)*V	DAN29330
S(I,I)=S(I,I)+2.*SS(J,L)*V	DAN29340
R(J,I)=R(J,I)+RR(I,L)*V	DAN29350
S(J,I)=S(J,I)+SS(I,L)*V	DAN29360
R(L,J)=R(L,J)+RR(I,I)*V	DAN29370
S(L,J)=S(L,J)+SS(I,I)*V	DAN29380
R(L,I)=R(L,I)+RR(I,J)*V	DAN29390
S(L,I)=S(L,I)+SS(I,J)*V	DAN29400
GO TO 29	DAN29410
C...I/J/K/J...I.GT.K.GT.J	DAN29420
22 T(J,I)=T(J,I)+2.*TT(K,J)*V	DAN29430
T(J,K)=T(J,K)+2.*TT(I,J)*V	DAN29440

R(J,J)=R(J,J)+2.*RR(I,K)*V	DAN29450
S(J,J)=S(J,J)+2.*SS(I,K)*V	DAN29460
R(J,K)=R(J,K)+RR(I,J)*V	DAN29470
S(J,K)=S(J,K)+SS(I,J)*V	DAN29480
R(J,I)=R(J,I)+RR(K,J)*V	DAN29490
S(J,I)=S(J,I)+SS(K,J)*V	DAN29500
R(K,I)=R(K,I)+RR(J,J)*V	DAN29510
S(K,I)=S(K,I)+SS(J,J)*V	DAN29520
GO TO 29	DAN29530
C...I/J/K/L...I.GT.J.GT.K.GT.L	
23 T(J,I)=T(J,I)+2.*TT(K,L)*V	DAN29540
T(L,K)=T(L,K)+2.*TT(I,J)*V	DAN29550
R(K,I)=R(K,I)+RR(J,L)*V	DAN29560
S(K,I)=S(K,I)+SS(J,L)*V	DAN29570
R(K,J)=R(K,J)+RR(I,L)*V	DAN29580
S(K,J)=S(K,J)+SS(I,L)*V	DAN29590
R(L,J)=R(L,J)+RR(I,K)*V	DAN29600
S(L,J)=S(L,J)+SS(I,K)*V	DAN29610
R(L,I)=R(L,I)+RR(J,K)*V	DAN29620
S(L,I)=S(L,I)+SS(J,K)*V	DAN29630
GO TO 29	DAN29640
C...I/J/K/L...I.GT.K.GT.J.GT.L	
24 T(J,I)=T(J,I)+2.*TT(K,L)*V	DAN29650
T(L,K)=T(L,K)+2.*TT(I,J)*V	DAN29660
R(K,I)=R(K,I)+RR(J,L)*V	DAN29670
S(K,I)=S(K,I)+SS(J,L)*V	DAN29680
R(J,K)=R(J,K)+RR(I,L)*V	DAN29690
S(J,K)=S(J,K)+SS(I,L)*V	DAN29700
R(L,J)=R(L,J)+RR(I,K)*V	DAN29710
S(L,J)=S(L,J)+SS(I,K)*V	DAN29720
R(L,I)=R(L,I)+RR(K,J)*V	DAN29730
S(L,I)=S(L,I)+SS(K,J)*V	DAN29740
	DAN29750
	DAN29760

GO TO 29 DAN29770
 C...I/J/K/L...I.GT.K.GT.L.GT.J DAN29780
 25 T(J,I)=T(J,I)+2.*TT(K,L)*V DAN29790
 T(L,K)=T(L,K)+2.*TT(I,J)*V DAN29800
 R(K,I)=R(K,I)+RR(L,J)*V DAN29810
 S(K,I)=S(K,I)+SS(L,J)*V DAN29820
 R(J,K)=R(J,K)+RR(I,L)*V DAN29830
 S(J,K)=S(J,K)+SS(I,L)*V DAN29840
 R(J,L)=R(J,L)+RR(I,K)*V DAN29850
 S(J,L)=S(J,L)+SS(I,K)*V DAN29860
 R(L,I)=R(L,I)+RR(K,J)*V DAN29870
 S(L,I)=S(L,I)+SS(K,J)*V DAN29880
 29 CONTINUE DAN29890
 C...IF THIS WAS NOT THE LAST RECORD GO BACK INTO THE LOOP AND READ DAN29900
 C...ANOTHER RECORD OF INTEGRALS IN. DAN29910
 IF(LSTRCD.EQ.0) GO TO 72 DAN29920
 C...IF CHECK SUM PRINT FLAG IS ON AND THERE ARE MORE CHECKSUMS THEN DAN29930
 C...PRINT THEM. DAN29940
 IF(IPTI.EQ.0.AND.IRC.EQ.1) GO TO 76 DAN29950
 WRITE(6,103) (IPRT(MN),MN=1,IRC) DAN29960
 C...COMPARE THE CHECKSUMS OBTAINED ON THIS RUN THROUGH THIS ROUTINE DAN29970
 C...WITH THOSE OBTAINED ON THE PREVIOUS RUN THROUGH. IN CASE OF ERROR DAN29980
 C...ABORT. ALSO PRINT CHECK SUMS IF PRINT FLAG IS SET. DAN29990
 76 IF(IX.EQ.0) GO TO 79 DAN30000
 IF(LSUM.NE.LSUMNW.OR.NOSINT.NE.NMINNW) GO TO 500 DAN30010
 IF(IPTI.EQ.0) GO TO 79 DAN30020
 WRITE(6,102) LSUM,LSUMNW,NOSINT,NMINNW DAN30030
 C...STORE THE CHECK SUMS OF THIS RUN THROUGH FOR CHECKING LATER ON NEXT DAN30040
 C...PASS DAN30050
 79 LSUM=LSUMNW DAN30060
 NOSINT=NMINNW DAN30070
 C...SET FLAG TO INDICATE THAT A PASS THROUGH THIS ROUTINE HAS BEEN MADE.DAN30080

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IX=1 DAN30090
C...RETURN TO SCFUHF PROGRAM. DAN30100
    RETURN DAN30110
C...ERROR EXIT. DAN30120
500  WRITE(6,501) DAN30130
    CALL ABT DAN30140
    STOP DAN30150
100  FORMAT(1H1///37X, DAN30160
161INTERNAL CHECK SUMS, ETC. FROM READING TWO ELECTRON INTEGRALS// DAN30170
    1      6H REC ,7(1X,17H FIRST NOS LAST )/ DAN30180
    1      6H NOS ,7(1X,17H LABEL OF LABEL )/ DAN30190
    1      6X,7(1X,17H J L INTS J L )) DAN30200
102  FORMAT(1X,10HLAST L SUM,I12,11H THIS L SUM,I12/1X,17HLAST NOS. OF DAN30210
    1INTS,I12,18H THIS NOS. OF INTS,I12) DAN30220
103  FORMAT(1X,I4,1X,7(I3,I3,1X,I4,I3,I3,1X)) DAN30230
501  FORMAT(22HREAD ERROR IN FMJUHF ) DAN30240
    END DAN30250
CFMEXTB          SUBROUTINE FMEXTB DAN30260
    SUBROUTINE FMEXTB(A,P,NBFNS,NBMX,PRE,EX) DAN30270
    IMPLICIT REAL*8 (A-H,O-Z) DAN30280
    DIMENSION A(NBMX,NBMX),P(NBMX,NBMX) DAN30290
    DOUBLE PRECISION EY DAN30300
C...SUBROUTINE FMEXTB COMPUTES THE TRACE OF THE PRODUCT OF THE DAN30310
C...SYMMETRIC MATRICES A AND P. FURTHER IT MULTIPLIES THE VALUE DAN30320
C...OF THE TRACE BY THE FACTOR PRE. THE UPPER TRIANGULAR HALF (INCLUDING DAN30330
C...THE DIAGONAL) OF A IS USED AND THE LOWER TRIANGULAR HALF (INCLUDING DAN30340
C...THE DIAGONAL) OF P IS USED. THUS DAN30350
C...
    EX = PRE*TRACE(A * P) DAN30360
    EY=0.0D0 DAN30370
    DO 2 I=1,NBFNS DAN30380
    DO 1 J=1,I DAN30390
    COD=2.0 DAN30400

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IF(I.EQ.J) COD=1.0                               DAN30410
EY=EY+COD*A(J,I)*P(I,J)
1 CONTINUE                                         DAN30420
2 CONTINUE                                         DAN30430
EX=PRE*EY                                         DAN30440
RETURN                                            DAN30450
END                                              DAN30460
DAN30470
CEFSKIP      SUBROUTINE EFSKIP(NTAPE,NFILS)       DAN30480
              SUBROUTINE EFSKIP(NTAPE,NFILS)
C   THIS SUBROUTINE MOVES TAPE NO. NTAPE JUST OVER NFILS NUMBER OF
C   END-OF-FILE MARKS, EITHER FORWARD OR BACKWARDS DEPENDING ON THE
C   SIGN OF NFILS. IFNFILS=0, THE SUBROUTINE DOES NOTHING.
REAL*8 EOF,WORD1
DATA EOF/6H***EOF/
NT=NTAPE
IF(NFILS) 20,18,10
C   FORWARD SPACE OVER NFILS END-OF-FILES ON TAPE NTAPE
10 D016K=1,NFILS                                 DAN30570
12 READ(NT) WORD1                                DAN30580
14 IF(WORD1.NE.EOF) GOTO12                         DAN30590
16 CONTINUE                                         DAN30600
18 RETURN                                           DAN30610
20 N=-NFILS                                         DAN30620
C   BACKSPACE FILE UNIT NTAPE OVER NFILS FILE MARKS
D030K=1,N
KOUNT=0
32 BACKSPACE NT                                    DAN30630
KOUNT=KOUNT+1                                     DAN30640
READ(NT) WORD1                                    DAN30650
BACKSPACE NT                                     DAN30660
IF(KOUNT.GT.50) GO TO 40                         DAN30670
IF(WORD1.NE.EOF) GOTO32                           DAN30680
DAN30690
DAN30700
DAN30710
DAN30720

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30  CONTINUE                               DAN30730
    RETURN                                 DAN30740
40  WRITE(6,99) K                         DAN30750
    CALL ABT                                DAN30760
99  FORMAT(7HO FILE I3,30H CONTAINS MORE THAT 50 RECORDS) DAN30770
    END                                     DAN30780
CADDT          SUBROUTINE ADDT             DAN30790
    SUBROUTINE ADDT(NAM,NITAPE,ILABL,ARRAY,NBMX,PKDLBL,VALINT,NINMAX) DAN30800
    IMPLICIT REAL*8 (A-H,O-Z)               DAN30810
    DIMENSION PKDLBL(NINMAX),VALINT(NINMAX) DAN30820
    DIMENSION ARRAY(NBMX,NBMX),ILABL(1)     DAN30830
    REAL*8 NAM,ILABL                        DAN30840
C...POSITION TAPE, NITAPE, TO READ THE FILE WHOSE NAME IS NAM. DAN30850
C...FILE NAM CONTAINS BINARY RECORDS OF INTEGRAL LABELS AND VALUES. DAN30860
    CALL FILE(NAM,NITAPE,ILABL)             DAN30870
C...READ A RECORD OF INTEGRAL LABELS AND VALUES. DAN30880
    1 READ (NITAPE) NINTS,LSTRCD,PKDLBL,VALINT DAN30890
        IF(NINTS.GT.NINMAX.OR.NINTS.LE.0) GO TO 500 DAN30900
C...LOOP OVER THE NINTS LABELS AND VALUES IN THE RECORD JUST READ IN. DAN30910
    DO 2 M=1,NINTS                         DAN30920
C...UNPACK A LABEL.                      DAN30930
    CALL UNPACK(PKDLBL(M),I,J,IZ,IZ,IZ,IZ) DAN30940
C...PUT VALUE INTO CORRECT POSITION IN ARRAY (UPPER TRIANGULAR HALF) DAN30950
    ARRAY(J,I)=ARRAY(J,I)+VALINT(M)         DAN30960
    2 CONTINUE                               DAN30970
C...IF THE RECORD JUST READ IN WAS NOT THE LAST GO TO 1 AND READ ANOTHER DAN30980
C...FROM TAPE. IF LSTRCD IS NONZERO THEN THE RECORD JUST READ WAS THE DAN30990
C...LAST.                                     DAN31000
    IF(LSTRCD.EQ.0) GO TO 1                 DAN31010
    RETURN                                  DAN31020
C...ERROR EXIT FOR INCORRECT VALUE OF NINTS (POSSIBLE TAPE READ ERROR). DAN31030
500  WRITE(6,510)                           DAN31040

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CALL ABT                               DAN31050
STOP                                 DAN31060
510 FORMAT(22HREAD ERROR IN ADDT      )
END                                  DAN31070
CABT       SUBROUTINE ABT             DAN31080
SUBROUTINE ABT                         DAN31090
A=2./0.                                DAN31100
A=A+2.                                DAN31110
STOP                                 DAN31120
END                                  DAN31130
DAN31140
CMWRITE      SUBROUTINE MWRITE        DAN31150
SUBROUTINE MWRITE(A,WA,WB,WC,ITR,NR,NC,NRX)
IMPLICIT REAL*8 (A-H,O-Z)           DAN31160
DAN31170
C...THIS SUBROUTINE PRINTS OUT THE MATRIX A.
DIMENSION A(NRX,NRX)                 DAN31180
REAL*8 WA,WB,WC,ILBL,ILAB            DAN31190
COMMON/LABELS/ILBL(12),ILAB(12)      DAN31200
WRITE(6,100) (ILBL(I),I=1,12),WA,WB,WC
IF(ITR.GT.0) WRITE(6,101) ITR
WRITE(6,102) (M,M=1,10)
DO 1 I=1,NR
WRITE(6,104) I,(A(I,J),J=1,NC)
1 CONTINUE
RETURN
100 FORMAT(1H1///31X,12A6/58X,3A6)    DAN31270
101 FORMAT(61X,10HITERATION ,I3)      DAN31280
102 FORMAT(4HOROW,5X,I2,9(10X,I2))   DAN31290
104 FORMAT(14,10F12.7/(4X,10F12.7))
END
CREORD      SUBROUTINE REORD         DAN31300
SUBROUTINE REORD(A,B,X,X1,NR,NC,NRX)
C                                     DAN31310
DAN31320
DAN31330
DAN31340
DAN31350
DAN31360

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C      ORDERS EIGENVECTORS FROM LOWEST TO HIGHEST EIGENVALUES.      DAN31370
C      EIGENVECTORS ARE IN B. REORDERED EIGENVECTORS ARE IN A.      DAN31380
C      REORDERED EIGENVALUES ARE IN X.      DAN31390
C
C      IMPLICIT REAL*8(A-H,O-Z)      DAN31400
DIMENSION A(NRX,NRX),B(NRX,NRX),X(NRX),X1(NRX)      DAN31410
AB=X1(1)      DAN31420
DO 20 I=2,NR      DAN31430
IF(X1(I).LE.AB)GO TO 20      DAN31440
AB=X1(I)      DAN31450
20 CONTINUE      DAN31460
BA=2.D0*DABS(AB)      DAN31470
DO 30 K=1,NR      DAN31480
J=1      DAN31490
AB=X1(1)      DAN31500
DO 40 I=2,NR      DAN31510
IF(X1(I).GE.AB)GO TO 40      DAN31520
AB=X1(I)      DAN31530
J=I      DAN31540
40 CONTINUE      DAN31550
X(K)=X1(J)      DAN31560
X1(J)=BA      DAN31570
DO 50 I=1,NC      DAN31580
50 A(K,I)=B(J,I)      DAN31590
30 CONTINUE      DAN31600
RETURN      DAN31610
END      DAN31620
DAN31630
CFMDMB          SUBROUTINE FMDMB      DAN31640
SUBROUTINE FMDMB(Y,D,FR,GA,NSOS,NBFNS,NBMX)      DAN31650
IMPLICIT REAL*8 (A-H,O-Z)      DAN31660
DIMENSION Y(NBMX,NBMX),D(NBMX,NBMX),FR(1)      DAN31670
DOUBLE PRECISION DD      DAN31680

```

C...THIS SUBROUTINE COMPUTES THE DENSITY MATRIX, D, FROM THE MOLECULAR DAN31690
 C...ORBITAL COEFFICIENTS STORED IN THE ROWS OF Y. THUS - DAN31700
 C...
 C...
 C... WHERE FR(K) IS THE FRACTIONAL OCCUPANCY OF THE KTH ORBITAL AND DAN31720
 C... GA IS A CONSTANT GIVEN BY THE CALLING ROUTINE. DAN31730
 C... SINCE D IS SYMMETRIC ONLY ITS LOWER TRIANGULAR HALF (INCLUDING DAN31740
 C... THE DIAGONAL) IS COMPUTED AND RETURNED TO THE CALLING PROGRAM. DAN31750

```

    DO 2 I=1,NBFNS          DAN31760
    DO 2 J=1,I              DAN31770
    DD=0.0DO                DAN31780
    DO 1 K=1,NSOS           DAN31790
    FRO=FR(K)               DAN31800
    IF(FRO.EQ.0.) GO TO 1   DAN31810
    DD=DD+Y(K,I)*Y(K,J)*FRO DAN31820
    1 CONTINUE               DAN31830
    D(I,J)=GA*DD             DAN31840
    2 CONTINUE               DAN31850
    RETURN                  DAN31860
    END                     DAN31870
  
```

CFMDTB SUBROUTINE FMDBT8
 SUBROUTINE FMDBT8(A,B,C,T,NC,NRX) DAN31880
 IMPLICIT REAL*8 (A-H,O-Z) DAN31890
 DIMENSION A(NRX,1),B(NRX,1),C(NRX,1) DAN31900
 C...THIS SUBROUTINE FORMS THE MATRIX C WHERE DAN31910
 C...
 C(I,J) = A(I,J) + T*B(I,J) DAN31920
 C...THE MATRICES A, B, AND C ARE PRESUMABLY SYMMETRIC, AND THEREFORE DAN31930
 C...ONLY THE LOWER TRIANGULAR HALF (INCLUDING THE DIAGONAL) OF C IS DAN31940
 C...FORMED FROM THE CORRESPONDING SECTIONS OF A AND B. DAN31950

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    DO 2 J=1,NC              DAN31960
    DO 1 I=J,NC              DAN31970
    C(I,J)=A(I,J)+T*B(I,J)  DAN31980
    1 CONTINUE                DAN31990
  
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2 CONTINUE                               DAN32010
RETURN                                 DAN32020
END                                    DAN32030
CTEST2        SUBROUTINE TEST2(NT,JNAM)    DAN32040
SUBROUTINE TEST2(NT,JNAM)                DAN32050
C   TEST2 REWINDS TAPE NO. NT AND CHECKS TO SEE IF THE CORRECT TAPE DAN32060
C   HAS BEEN MOUNTED. IN CASE OF ERROR PROGRAM IS TERMINATED.      DAN32070
REAL*8 IEOF,JNAM,NAMTAP,IWRD          DAN32080
COMMON /IOIND/ ICON(24)                 DAN32090
DATA IEOF /6H***EOF/                  DAN32100
NTAPE=NT                                DAN32110
REWIND NTAPE                            DAN32120
1  READ(NTAPE) IWRD                     DAN32130
IF(IWRD.NE.IEOF) GOTO1                DAN32140
READ(NTAPE) NAMTAP                     DAN32150
CALL EFSKIP (NTAPE,-1)                 DAN32160
IF(JNAM.EQ.NAMTAP) GOTO6              DAN32170
4  WRITE(6,5) NTAPE                    DAN32180
CALL ABT                                DAN32190
6  IF(ICON(10).GT.0) WRITE(6,3) NTAPE,JNAM DAN32200
RETURN                                 DAN32210
5  FORMAT(3OH0 WRONG TAPE NAME ON TAPE NO. I3) DAN32220
3  FORMAT(70X,4HTAPE I3,2X,24HIS LOADED WITH THE NAME     A6) DAN32230
END                                    DAN32240
CMWRITB        SUBROUTINE MWRITB        DAN32250
SUBROUTINE MWRITB(A,WA,WB,WC,ITR,NC,NRX) DAN32260
IMPLICIT REAL*8 (A-H,O-Z)             DAN32270
C...THIS SUBROUTINE PRINTS OUT THE LOWER TRIANGULAR HALF (INCLUDING THE DAN32280
C...DIAGONAL) OF THE MATRIX A.
DIMENSION A(NRX,1)                   DAN32290
REAL*8 WA,WB,WC,ILBL,ILAB            DAN32300
COMMON/LABELS/ ILBL(12),ILAB(12)      DAN32310
                                         DAN32320

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      WRITE(6,100) (ILBL(I),I=1,12),WA,WB,WC          DAN32330
      IF(ITR.GT.0) WRITE(6,101) ITR                   DAN32340
      WRITE(6,102) (M,M=1,10)                         DAN32350
      DO 1 I=1,NC                                     DAN32360
      WRITE(6,104) I,(A(I,J),J=1,I)                  DAN32370
1    CONTINUE                                         DAN32380
      RETURN                                           DAN32390
100 FORMAT(1H1///31X,12A6/58X,3A6)                 DAN32400
101 FORMAT(61X,10HITERATION ,I3)                  DAN32410
102 FORMAT(4HORDW,5X,I2,9(10X,I2))                DAN32420
104 FORMAT(I4,10F12.7/(4X,10F12.7))              DAN32430
      END                                              DAN32440
CMODBLK   SUBROUTINE MODBLK
      SUBROUTINE MODBLK(V,F,Y,NS,OE,GQ,CA,NSOS,NBFNS,NBMX,WA,ITR,IX) DAN32450
      IMPLICIT REAL*8 (A-H,O-Z)                      DAN32470
      DIMENSION CA(NBMX,NBMX)                        DAN32480
      DIMENSION V(NBMX,NBMX),F(NBMX,NBMX),Y(NBMX,NBMX), DAN32490
      1           NS(1),OE(1),GQ(1)                  DAN32500
      REAL*8 WA                                       DAN32510
      DAN32520
C         THE MATRIX TO BE BLOCK DIAGONALIZED IS STORED IN F. THE DAN32530
C         SYMMETRY BLOCKING TRANSFORMATION MATRIX IS STORED IN V. DAN32540
C         THE SYMMETRY BLOCKED MATRIX, F, IS DIAGONALIZED A BLOCK AT A DAN32550
C         TIME. THE EIGENVALUES ARE ORDERED BY BLOCKS - MOST NEGATIVE DAN32560
C         FIRST - AND THEN THE EIGENVECTORS ARE TRANSFORMED BACK INTO DAN32570
C         THE BASIS FUNCTION REPRESENTATION.             DAN32580
C                                                 DAN32590
C...TAKE TRACE OF F MATRIX
      5  TRFM=0.                                      DAN32600
      DO 1 I=1,NSOS                                    DAN32610
      1  TRFM=TRFM+F(I,I)                           DAN32620
C...INITIALIZE EIGENVECTOR MATRIX                 DAN32630
      DAN32640

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    CALL MCLEAR(Y,NSOS,NSOS,NBMX)                               DAN32650
C...PERFORM DIAGONALIZATION BY BLOCKS
    NR=0                                         DAN32660
    ISYM=1                                         DAN32670
    ILO=1                                         DAN32680
    2 NSYM=NS(ISYM)                                     DAN32690
C...DIAGONALIZE THE BLOCK OF FSYM WHOSE 1,1 ELEMENT IS AT F(ILO,ILO) DAN32700
C...THE EIGENVECTORS OF THAT BLOCK ARE STORED IN THE NSYM BY NSYM DAN32710
C...BLOCK OF Y STARTING WITH Y(ILO,ILO)                   DAN32720
    IF(NSYM.EQ.0) GOTO4                                 DAN32730
    CALL HDIAG(F(ILO,ILO),Y(ILO,ILO),OE,GQ,NSYM,NBMX,0,NROT) DAN32740
    NR=NR+NROT                                         DAN32750
    ILO=ILO+NSYM                                       DAN32760
4   CONTINUE                                         DAN32770
    ISYM=ISYM+1                                         DAN32780
    IF(ILO.LE.NSOS) GO TO 2                           DAN32790
C...ORDER THE EIGENVALUES AND EIGENVECTORS SUCH THAT THE I+1 TH EIGEN- DAN32800
C...VALUE IS GREATER THAN THE ITH AND SUCH THAT THE EIGENVECTOR DAN32810
C...CORRESPONDING TO THE ITH EIGENVALUE IS IN THE ITH COLUMN OF Y. DAN32820
    CALL ORDREI(F,Y,OE,NS,GQ,NSOS,NBMX)                DAN32830
C...TRANSFORM EIGENVECTORS BACK TO ORIGINAL NON BLOCKED BASIS DAN32840
C...AT THIS POINT THE EIGENVECTORS OF FSYM, W, ARE CONTAINED IN THE DAN32850
C...COLUMNS OF Y. TO EFFECT THE TRANSFORMATION OF W BACK TO THE ORIGINAL DAN32860
C...BASIS PERFORM THE FOLLOWING -
C...          X = WT * V                                DAN32870
C...WHERE X IS THE MATRIX OF EIGENVECTORS IN THE ORIGINAL BASIS DAN32880
C...AND CONTAINS THOSE EIGENVECTORS AS ROWS.             DAN32890
C...ON ENTRY TO MMATB1 THE MATRIX W IS CONTAINED IN Y AND THE MATRIX V DAN32900
C...IS CONTAINED IN X.                                    DAN32910
C...ON RETURN FROM MMATB1 THE MATRIX X IS CONTAINED IN Y. DAN32920
    CALL MMATB1(Y,CA,NSOS,NSOS,NBFNS,GQ,NBMX)           DAN32930
C...TAKE TRACE OF EIGENVALUES                         DAN32940
                                                DAN32950
                                                DAN32960

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TROE=0.                                            DAN32970
DO 3 I=1,NSOS                                         DAN32980
 3 TROE=TROE+DE(I)                                     DAN32990
C...DOE IS THE DIFFERENCE BETWEEN THE TRACE BEFORE AND AFTER
C...DIAGONALIZATION.                                    DAN33000
  DOE=TROE-TRFM                                       DAN33010
  WRITE(6,130) WA,DOE,NR                               DAN33020
  RETURN                                              DAN33040
130 FORMAT(1H0,60X,A6,35H FSYM MATRIX DIAGONALIZATION ERROR ,
  1          E15.8/30X, 20HNUMBER OF ROTATIONS ,I6)      DAN33050
  END                                                 DAN33060
CORDREI      SUBROUTINE ORDREI                         DAN33070
  SUBROUTINE ORDREI(F,U,OE,NS,NEXT,N,NBMX)           DAN33080
  IMPLICIT REAL*8 (A-H,O-Z)                          DAN33090
  DIMENSION F(NBMX,NBMX),U(NBMX,NBMX),OE(1),NS(1),NEXT(1) DAN33100
C...THIS SUBROUTINE ORDERS THE EIGENVALUES, WITHIN SYMMETRY BLOCKS,
C...PLACING THE MOST NEGATIVE FIRST.                  DAN33120
C...ON ENTRY TO THIS SUBROUTINE THE DIAGONAL ELEMENTS OF F CONTAIN DAN33140
C...THE EIGENVALUES, DIAGONAL ELEMENTS 1 THRU NS(1) BELONG TO THE FIRST DAN33150
C...BLOCK, ELEMENTS NS(1)+1 THRU NS(2) +NS(1) TO THE SECOND BLOCK, ETC. DAN33160
C...THE CORRESPONDING COLUMNS OF U CONTAIN THE EIGENVECTORS.        DAN33170
C...ON EXIT FROM THIS SUBROUTINE THE ORDERED EIGENVALUES ARE IN OE AND DAN33180
C...THE EIGENVECTORS IN THE CORRESPONDING ORDER ARE IN U (AS COLUMNS). DAN33190
  ILO=1                                              DAN33200
  ISYM=1                                             DAN33210
  1  IF(NS(ISYM).EQ.0) GOTO19                         DAN33220
    IH1=ILO+NS(ISYM)-1                                DAN33230
    IF(ILO.EQ.IH1) GOTO9                            DAN33240
    DO 2 I=ILO,IH1                                     DAN33250
  2  NEXT(I)=I                                         DAN33260
    KLO=ILO                                           DAN33270
  3  K=NEXT(KLO)                                      DAN33280

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FMAX=F(K,K) DAN33290
KLP1=KLO+1 DAN33300
DO 4 I=KLP1,IHI DAN33310
J=NEXT(I) DAN33320
IF(F(J,J).GE.FMAX) GO TO 4 DAN33330
M=NEXT(KLO) DAN33340
NEXT(KLO)=J DAN33350
NEXT(I)=M DAN33360
FMAX=F(J,J) DAN33370
4 CONTINUE DAN33380
KLO=KLP1 DAN33390
IF(KLP1.LT.IHI) GO TO 3 DAN33400
I=ILO DAN33410
5 J=NEXT(I) DAN33420
FMAX=F(I,I) DAN33430
DO 6 K=1,N DAN33440
6 OE(K)=U(K,I) DAN33450
F(I,I)=F(J,J) DAN33460
F(J,J)=FMAX DAN33470
DO 7 K=1,N DAN33480
U(K,I)=U(K,J) DAN33490
7 U(K,J)=OE(K) DAN33500
DO 8 M=ILO,IHI DAN33510
IF(NEXT(M).EQ.I) NEXT(M)=J DAN33520
8 CONTINUE DAN33530
I=I+1 DAN33540
IF(I.LT.IHI) GO TO 5 DAN33550
9 ILO=IHI+1 DAN33560
19 ISYM=ISYM+1 DAN33570
IF(ILO.LE.N) GO TO 1 DAN33580
DO 10 KK=1,N DAN33590
10 OE(KK)=F(KK,KK) DAN33600

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        RETURN                               DAN33610
        END                                DAN33620
CMABAT          SUBROUTINE MABAT           DAN33630
                SUBROUTINE MABAT(A,B,NR,NC,Y,NBMX)   DAN33640
                IMPLICIT REAL*8 (A-H,O-Z)           DAN33650
                DIMENSION A(NBMX,1),B(NBMX,1),Y(NBMX,1) DAN33660
C...THIS SUBROUTINE TAKES THE MATRIX PRODUCT -      DAN33670
C...      C = A * B * AT                  DAN33680
C...WHERE THE MATRIX AT IS THE TRANSPOSE OF A, A IS NR BY NC, B IS DAN33690
C...NC BY NC, AND C IS NR BY NR.                   DAN33700
C...THE MATRIX B IS ASSUMED SYMMETRIC THUS ONLY ITS UPPER TRIANGULAR DAN33710
C...HALF (INCLUDING THE DIAGONAL) IS USED. THE MATRIX C IS ALSO ASSUMED DAN33720
C...TO BE SYMMETRIC, AND THEREFORE ONLY ITS UPPER TRIANGULAR HALF IS DAN33730
C...CALCULATED. THIS UPPER TRIANGULAR HALF OF C IS RETURNED IN THE UPPER DAN33740
C...TRIANGULAR HALF OF B.                         DAN33750
C...COMPUTE A * B . STORE THAT IN Y TEMPORARILY.    DAN33760
        DOUBLE PRECISION SUM                 DAN33770
        DO 10 I=1,NR                         DAN33780
        DO 10 K=1,NC                         DAN33790
        SUM=0.0D0                           DAN33800
        DO 8 J=1,K                          DAN33810
        SUM=SUM+A(I,J)*B(J,K)              DAN33820
8     CONTINUE                           DAN33830
        K1 = K + 1                         DAN33840
        IF(K1.GT.NC) GOTO13               DAN33850
        DO 9 J=K1,NC                      DAN33860
        SUM=SUM+A(I,J)*B(K,J)              DAN33870
9     CONTINUE                           DAN33880
13    Y(I,K)=SUM                        DAN33890
10    CONTINUE                           DAN33900
C...MULTIPLY Y * A TO GET UPPER HALF OF C, STORING THAT IN B.    DAN33910
        DO 12 K=1,NR                      DAN33920

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DO 12 I=1,K                               DAN33930
SUM=0.0D0                                DAN33940
DO 11 J=1,NC                             DAN33950
SUM=SUM+Y(I,J)*A(K,J)                   DAN33960
11  CONTINUE                               DAN33970
B(I,K)=SUM                                DAN33980
12  CONTINUE                               DAN33990
RETURN                                    DAN34000
END                                       DAN34010
CMPRY2          SUBROUTINE MPRY2           DAN34020
SUBROUTINE MPRY2(A,E,FR,WA,WB,WC,ITR,NR,NC,NRX)
C...THIS SUBROUTINE PRINTS OUT THE MOLECULAR ORBITALS (IN COLS), THEIR
C...EIGENVALUES, AND FRACTIONAL OCCUPANCIES(IF ITR .NE.0)
IMPLICIT REAL*8 (A-H,O-Z)                 DAN34030
DIMENSION A(NRX,1),E(1),FR(1),NS(1),NSN(1)   DAN34040
COMMON/LABELS/ILBL(12),ILAB(12)             DAN34050
REAL*8 WA,WB,WC,ILBL,ILAB                  DAN34060
C...THIS SUBROUTINE PRINTS OUT THE MOLECULAR ORBITALS WITH THEIR
C...SYMMETRY DESIGNATIONS, THEIR EIGENVALUES, AND THEIR FRACTIONAL
C...OCCUPANCIES.
WRITE(6,100) (ILBL(I),I=1,12),WA,WB,WC    DAN34070
WRITE(6,102) (M,M=1,10)                      DAN34080
DO 4 I=1,NR                                 DAN34090
IF(ITR)1,2,1
1  WRITE(6,103)M,E(I),FR(I)                DAN34100
GO TO 3                                     DAN34110
2  WRITE(6,103)M,E(I)                      DAN34120
3  WRITE(6,104)I,(A(J,I),J=1,NC)           DAN34130
4  CONTINUE                                  DAN34140
5  CONTINUE                                  DAN34150
6  RETURN                                    DAN34160
100 FORMAT(1H1///31X,12A6/58X,3A6)          DAN34170
                                              DAN34180
                                              DAN34190
                                              DAN34200
                                              DAN34210
                                              DAN34220
                                              DAN34230
                                              DAN34240

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102 FORMAT(4HOROW,5X,I2,9(10X,I2)) DAN34250
103 FORMAT('0',I3,F15.7,F10.5) DAN34260
104 FORMAT(I4,10F12.7/(4X,10F12.7)) DAN34270
END DAN34280
CMPRY1 SUBROUTINE MPRY1 DAN34290
SUBROUTINE MPRY1(A,E,FR,WA,WB,WC,ITR,NR,NC,NRX) DAN34300
IMPLICIT REAL*8 (A-H,O-Z) DAN34310
DIMENSION A(NRX,1),E(1),FR(1),NS(1),NSN(1) DAN34320
COMMON/LABELS/ILBL(12),ILAB(12) DAN34330
REAL*8 WA,WB,WC,ILBL,ILAB DAN34340
C...THIS SUBROUTINE PRINTS OUT THE MOLECULAR ORBITALS (ALREADY IN ROWS) DAN34350
C...TOGETHER WITH THEIR EIGENVALUES AND FRACTIONAL OCCUPANCIES(IF .TR .NDAN34360
      WRITE(6,100) (ILBL(I),I=1,12),WA,WB,WC DAN34370
      WRITE(6,102) (M,M=1,10) DAN34380
      DO 4 I=1,NR DAN34390
      IF(ITR)1,2,1 DAN34400
1  WRITE(6,103)M,E(I),FR(I) DAN34410
      GO TO 3 DAN34420
2  WRITE(6,103)M,E(I) DAN34430
3  WRITE(6,104)I,(A(I,J),J=1,NC) DAN34440
4  CONTINUE DAN34450
5  CONTINUE DAN34460
6  RETURN DAN34470
100 FORMAT(1H1///31X,12A6/58X,3A6) DAN34480
102 FORMAT(4HOROW,5X,I2,9(10X,I2)) DAN34490
103 FORMAT('0',I3,F15.7,F10.5) DAN34500
104 FORMAT(I4,10F12.7/(4X,10F12.7)) DAN34510
END DAN34520

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SPIN PROJECTION OF SEMI-EMPIRICAL AND AB INITIO
UNRESTRICTED HARTREE-FOCK WAVEFUNCTIONS

by

Dana Alice Brewer

(ABSTRACT)

The method of spin projection was examined by developing and applying computer programs to calculate projected semi-empirical and ab initio unrestricted Hartree-Fock (UHF) wavefunctions.

The electronic spectra of naphthalene, anthracene, naphthacene and pentacene were calculated using the Pariser-Pople-Parr (PPP) π -electron approximations and both UHF and configurational interaction (CI) techniques. The results of both techniques were compared with experimentally determined spectra with reasonable agreement between the CI and projected UHF results. While the CI calculations generally produced lower energies for the triplet states than the UHF calculations, the spectra from UHF calculations were in somewhat better agreement with experiment. Anomalies encountered with degeneracies and the presence of open shell ground states are also discussed.

The geometry of monohomocyclooctatetraene anion radical (MHCOT) was studied using spin projection of the UHF INDO wavefunction. The theoretical molecular geometry was varied until the

experimental hyperfine coupling constants matched hyperfine constants obtained from using both projected and unprojected UHF wavefunctions. The two types of calculations resulted in slightly different energies and geometries with the projected calculations giving a higher energy for the doublet state; essentially no differences were noted in the bond orders obtained from the two types of calculations. The geometry from the projected calculations was a somewhat more strained conformation than the geometry from the unprojected calculation.

Ab initio UHF calculations with spin projection were performed on H₂O(+) to compare the energies of pure spin states from ab initio multi-configurational self-consistent field with CI (MCSCF/CI) with those from spin projection. The MCSCF/CI calculations are superior to the UHF plus spin projection calculations. This result will always be observed when the UHF wavefunction is very close to a pure spin state before spin projection.

The dissociation of CF₂O was studied using ab initio wavefunctions. The energies of the unprojected UHF wavefunctions were examined along with those for the dissociated CF₂ + O fragments. Good agreement exists between the calculated and experimental vertical ionization potentials for CF₂O at the equilibrium geometry.