APPENDIX A JOIST CROSS SECTION PROPERTIES



Figure A.1 Single Span Footbridge- Joist 1



Figure A.2 Single Span Footbridge- Joist 2



Figure A.3 Three Span Footbridge- Joist 1





















APPENDIX B

DESIGN GUIDE 11 CALCULATIONS FOR SINGLE SPAN FOOTBRIDGE

APPENDIX B

DESIGN GUIDE 11 CALCULATIONS FOR SINGLE SPAN FOOTBRIDGE

Weight Calculations





Concrete slab= 4.50" + 1.50" / 3 = 5.00"

Measured concrete density = $142.32 \text{ lbs} / \text{ft}^3$ w slab = ($142.32 \text{ lbs} / \text{ft}^3$)x(5" / 12") = 59.30 lbs / ft^2 W_c=59.30 x 30 x 7=12543 lbs

1.5VL22 Cold-formed steel deck = $1.78 \text{ lbs} / \text{ft}^2$ W_d= $1.78 \times 30 \times 7$ = 373.8 lbs

30K7 Open web steel joist = 12.3 lbs / ft

 $W_i=2 \ge 30 \ge 12.3 = 738$ lbs

4 reinforcement bars: 0.668 lb / ft

4 bars parallel to joists: 4 lines of 30 ft = 120 ft120 x 0.668=80.16 lbs# 4 bars perpendicular to joists: 18 lines of 6 ft = 108 ft108 x 0.668=72.144 lbs W_r = (120 x 0.668) + (108 x 0.668) = 152.304 lbs

6" deep pour stops = 1.949 lbs / ft

$$W_p=2 \ge (30+7) \ge 1.949 = 144.226$$
 lbs

Welded Wire Fabric: $6x6xW4xW4 = 58 \text{ lbs} / 100 \text{ ft}^2$

 $W_W = 4 \times 30 \times 0.58 = 69.6 \text{ lbs}$

Reinforcement bar chairs: 0.212 lb / ft

Chairs parallel to joists: 4 lines of 30 ft = 120 ft120 x 0.212=25.44 lbsChairs perpendicular to joists: 18 lines of 5 ft = 90 ft90 x 0.212=19.08 lbs $W_{ch}=(120 \times 0.212) + (90 \times 0.212) = 44.52$ lbs

Stand-off shear screws= 0.12 lbs

 $W_8 = (64) \times (0.12) = 7.68 \text{ lbs}$

Self-drilling screws: 3 lbs (estimated)

 $W_{\text{total}} = W_{\text{c}} + W_{\text{d}} + W_{\text{j}} + W_{\text{r}} + W_{\text{p}} + W_{\text{w}} + W_{\text{ch}} + W_{\text{s}} + W_{\text{ss}} = 13986.1 \text{ lbs}$ $\frac{W_{total}}{2} = 6993.1 \text{ lbs per joist}$ $(W_{\text{total}}) / 2 = 6993.1 \text{ lbs per joist}$ $w = \left(\frac{W_{total}}{2}\right) \left(\frac{1}{30}\right) \left(\frac{1}{1000}\right) = 0.2331 \text{ kips / ft per joist}$ = 0.0194 kips / in per joist

For the shell elements in the SAP2000 model, Sladki (1999) demonstrated that the unit weight per unit volume, W_{SHELL} , and mass per unit volume M_{SHELL} , of the shell material is given by:

$$W_{SHELL} = \left[\left(\frac{d + d_r/2}{12} \right) w_c + w_d + w_{deck} + w_1 + w_{coll} \right] \left(\frac{12}{d} \right) \left(\frac{1}{1,728,000} \right)$$
$$M_{SHELL} = \frac{W_{SHELL}}{386.1}$$

In these formulae, W_{SHELL} is the unit weight of the material (kips/in³), d is the depth of concrete above the metal deck (in.), d_r is the height of the metal deck (in.), w_c is the unit weight of concrete (pcf), w_d is the actual superimposed dead load (psf), w_{deck} is the weight of the deck (psf), w₁ is the actual live load (psf), and w_{coll} is the collateral loading (psf). Collateral loading is any load that is an addition to typical dead and live loads. The units for the unit mass used in SAP2000 are kip-s²/in⁴. The modulus of elasticity of shell material was set to the dynamic modulus of elasticity of the concrete as defined in the Design Guide, e.g. 1.35 times the static modulus of elasticity of the concrete. Also, the Poisson's ratio for the material, v, was set as 0.2.

According to Figure B.1 and above calculations, for the single span footbridge:

$$W_{SHELL} = \left[\left(\frac{d + d_r/3}{12} \right) w_c + w_d + w_{deck} + w_1 + w_{coll} \right] \left(\frac{12}{d} \right) \left(\frac{1}{1,728,000} \right)$$
$$W_{SHELL} = \left[\left(\frac{4.5 + 1.5/3}{12} \right) 142.32 + 1.78 + \left(\frac{152.3 + 144.2 + 69.6 + 44.5 + 7.7 + 3}{30.7} \right) \right] \left(\frac{12}{4.5} \right) \left(\frac{1}{1,728,000} \right)$$
$$W_{SHELL} = 9.736.10^{-5} \text{ kip/in}^3$$
$$M_{SHELL} = W_{SHELI} / 386.1 = 2.522.10^{-7} \text{ kip-s}^2 / \text{in}^4$$

M_{SHELL} and W_{SHELL} are used in the FE model as Slab material (shell element) properties.

Then, for the three span footbridge:

$$W_{total} = W_c + W_d + W_j + W_r + W_p + W_w + W_{ch} + W_s + W_{ss} = 40824.4 \text{ lbs}$$

And,

$$W_{SHELL} = \left[\left(\frac{d + d_r/3}{12} \right) w_c + w_d + w_{deck} + w_1 + w_{coll} \right] \left(\frac{12}{d} \right) \left(\frac{1}{1,728,000} \right)$$
$$W_{SHELL} = \left[\left(\frac{4.5 + 1.5/3}{12} \right) 138 + 1.78 + \left(\frac{(152.3 + 144.2 + 69.6 + 44.5 + 7.7 + 3)(3)}{90.7} \right) \right] \left(\frac{12}{4.5} \right) \left(\frac{1}{1,728,000} \right)$$
$$W_{SHELL} = 9.458.10^{-5} \text{ kip/in}^3$$

 $M_{SHELL} = W_{SHELL} / 386.1 = 2.45.10^{-7} \text{ kip-s}^{2}/\text{in}^{4}$

M_{SHELL} and W_{SHELL} are used in the FE model as Slab material (shell element) properties.

Cross Sectional Properties:



Joist top chord: 2L 2x2x0.149

 A_{tc} = 2(2 x 0.149 x 2 - 0.149 x 0.149) = 1.148 in²

Centroid of top chord, y_{tc}:

$$y_{tc} = \frac{\Sigma A_i y_i}{\Sigma A_i} = \frac{2[(2)(0.149)(1) + (2 - 0.149)(0.149)(0.149/2)]}{2[(2)(0.149) + (2 - 0.149)(0.149)]} = 0.555"$$



Moment of inertia of top chord, Itc:

$$I_{tc} = 2 \left[\frac{1}{12} (0.149)(2)^3 + (2)(0.149)(1 - 0.555)^2 \right]$$

+ 2 $\left[\frac{1}{12} (2 - 0.149)(0.149)^3 + (2 - 0.149)(0.149)(0.555 - 0.149/2)^2 \right]$

$$= 2[0.15834 + 0.06419] = 0.445in^{4}$$

Joist bottom chord: 2L 1.5x1.5x0.159

 $A_{bc}= 2(1.5 \text{ x } 0.159 \text{ x } 2 - 0.159 \text{ x } 0.159) = 0.903 \text{ in}^2$

Centroid of bottom chord, y_{bc}:

$$y_{bc} = \frac{\Sigma A_i y_i}{\Sigma A_i} = \frac{2[(1.5)(0.159)(0.75) + (1.5 - 0.159)(0.159)(0.159/2)]}{2[(1.5)(0.159) + (1.5 - 0.159)(0.159)]} = 0.434"$$





Moment of inertia of bottom chord, Ibc:

$$I_{bc} = 2 \left[\frac{1}{12} (0.159)(1.5)^3 + (1.5)(0.159)(0.75 - 0.434)^2 \right] + 2 \left[\frac{1}{12} (1.5 - 0.159)(0.159)^3 + (1.5 - 0.159)(0.159)(0.434 - 0.159/2)^2 \right] = 2 [0.06853 + 0.02724] = 0.192 in^4$$

Joist Overall:

 $A_j = 1.148 + 0.903 = 2.051 \text{ in}^2$

Centroid of joist, y_j:

$$y_{j} = \frac{\Sigma A_{i} y_{i}}{\Sigma A_{i}} = \frac{(1.148)(30 - 0.555) + (0.903)(0.434)}{1.148 + 0.903} = 16.672^{\circ}$$
$$= 16.672^{\circ} \text{ from bottom}$$
$$= (30^{\circ} - 16.672^{\circ}) = 13.328^{\circ} \text{ from top}$$

Moment of inertia of joist, $I_j = I_{chords}$

$$I_{j} = [0.445 + (1.148)(13.328 - 0.555)^{2}] + [0.192 + (0.903)(16.672 - 0.434)^{2}]$$
$$= 187.741 + 238.288 = 426.029in^{4}$$



Next, calculate composite section centroid:

Assume there is no tension in concrete.

$$y_{composite} = \frac{\Sigma A_i y_i}{\Sigma A_i} = \frac{(6.897)(4.5)(33.75) + (2.051)(16.672)}{(6.897)(4.5) + 2.051} = 32.691"$$

= 32.691" from bottom

= (36"-32.691") = 3.309" from top-- Concrete in Tension- Acceptable for floor vibration purposes.

Moment of inertia of composite cross section, Icomposite:

$$I_{composite} = \left[426.029 + (2.051)(32.691 - 16.672)^{2}\right] \\ + \left[\frac{1}{12}(6.897)(4.5)^{3} + (6.897)(4.5)(3.309 - 4.5/2)^{2}\right] \\ = \left[952.333 + 87.181\right] = 1039.514in^{4}$$

In Design Guide 11, C_r is the modification factor that accounts for the reduction in the moment of inertia due to shear deformations and joint eccentricity in the web members of joists and joist girders:

$$C_r = 0.8455 (1 - e^{-0.28(L/D)})^{2.8} \text{ for angle web joists } (6 \le L/D \le 24)$$

$$\frac{L}{D} = \frac{356}{30} = 6 < 11.867 < 24$$

$$C_r = 0.8455 (1 - e^{-0.28(356/30)})^{2.8} = 0.76288$$

For bare Joists:

$$I_{\text{mod}} = C_r I_{chords} = (0.76288)(426.029) = 325.009in^4$$

The effective composite moment of inertia for joist supported tee-beams is going to be less than the fully composite moment of inertia of the entire cross section due to shear deformations and joint eccentricity (Band and Murray 1996). Effective composite moment of inertia of joist supported tee-beams is given as:

$$I_{eff} = \frac{1}{\frac{\gamma}{I_{chords}} + \frac{1}{I_{comp}}}$$

where

$$\gamma = \frac{1}{C_r} - 1 = \frac{1}{0.76288} - 1 = 0.31082$$
$$I_{eff} = \frac{1}{\frac{0.31082}{426.029} + \frac{1}{1039.514}} = 591.172in^4$$

then,

$$f_n = \frac{\pi}{2} \sqrt{\frac{gE_s I_{eff}}{wL^4}} = \frac{\pi}{2} \sqrt{\frac{(386.1)(29000)(591.172)}{(0.2331/12)(356)^4}} = 7.235 Hz$$



For comparison purposes, let's look at the case where there is tension in the concrete:

Solving for d_c:

 $d_c = 3.106$ "

 $y_{composite} = (36-d_c) = (36-3.106) = 32.894"$

Moment of inertia of composite cross section, Icomposite:

$$\begin{split} I_{composite} &= \left[426.029 + (2.051)(32.894 - 16.672)^2 \right] \\ &+ \left[\frac{1}{12} (6.897)(3.106)^3 + (6.897)(3.106)(3.106/2)^2 \right] \\ &= \left[965.756 + 68.888 \right] = 1034.644 in^4 \\ C_r &= 0.8455 \left(1 - e^{-0.28(L/D)} \right)^{2.8} \text{ for angle web joists } (6 \le L/D \le 24) \end{split}$$

$$\frac{L}{D} = \frac{356}{30} = 6 < 11.867 < 24$$

$$C_r = 0.8455 \left(1 - e^{-0.28(356/30)}\right)^{2.8} = 0.76288$$

$$I_{eff} = \frac{1}{\frac{\gamma}{I_{chords}} + \frac{1}{I_{comp}}}$$

where

$$\gamma = \frac{1}{C_{r}} - 1 = \frac{1}{0.76288} - 1 = 0.31082$$
$$I_{eff} = \frac{1}{\frac{0.31082}{426.029} + \frac{1}{1034.644}} = 589.594in^{4}$$

then,

$$f_n = \frac{\pi}{2} \sqrt{\frac{gE_s I_{eff}}{wL^4}} = \frac{\pi}{2} \sqrt{\frac{(386.1)(29000)(589.594)}{(0.2331/12)(356)^4}} = 7.225 Hz \text{ (vs. 7.235 Hz)}$$
$$\frac{(7.235 - 7.225)}{7.235} 100 = 0.134\% \text{ difference}$$

APPENDIX C

STIFFNESS TEST RESULTS- THREE SPAN FOOTBRIDGE





APPENDIX C STIFFNESS TEST RESULTS-- THREE SPAN FOOTBRIDGE C.1 BARE JOIST TESTING



Bare Joists- J1 is loaded 0-600-0 lb- No Bottom Chord Extensions in Place

Figure C.2





Figure C.3



Bare Joists- J3 is loaded 0-600-0 lb- No Bottom Chord Extensions in Place

Figure C.4





Figure C.5



Bare Joists- J5 is loaded 0-600-0 lb- No Bottom Chord Extensions in Place

Figure C.6





Figure C.7



Bare Joists- J1 is loaded 0-600-0 lb- Interior Bottom Chord Extensions in Place

Figure C.8





Figure C.9



Bare Joists- J3 is loaded 0-600-0 lb- Interior Bottom Chord Extensions in Place

Figure C.10





Figure C.11



Bare Joists- J5 is loaded 0-600-0 lb- Interior Bottom Chord Extensions in Place

Figure C.12





Figure C.13



Bare Joists- J1 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.14



Bare Joists- J2 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.15



Bare Joists- J3 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.16



Bare Joists- J4 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.17



Bare Joists- J5 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.18



Bare Joists- J6 is loaded 0-600-0 lb- All Bottom Chord Extensions in Place

Figure C.19



J1 and J2 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place

Figure C.20

J1 and J2 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place



Figure C.21



J3 and J4 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place



J3 and J4 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place



Figure C.23



J5 and J6 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place



J5 and J6 are loaded 0-600-0 lb- Bare Joists- Interior Bottom Chord Extensions in Place



Figure C.25





Figure C.26

J1 and J2 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



Figure C.27

700 600 Point Load at the Joist Midspan (lb) 500 400 - S5 300 N5 S4 200 - N4 ۰FE 100 0 -200 0 200 400 600 800 1000

J1 and J2 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



Load Cell (lb)

J1 and J2 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



Figure C.29



J3 and J4 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



J3 and J4 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



Figure C.31


J3 and J4 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions Extensions in Place



J5 and J6 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place



Figure C.33





Figure C.34



J5 and J6 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place

Figure C.35



J5 and J6 are loaded 0-600-0 lb- Bare Joists- All Bottom Chord Extensions in Place

Figure C.36

C.2 WET CONCRETE LOADING MEASUREMENTS



Wet Concrete (Distributed Loading On Bare Joists) vs. Vertical Midspan Deflection

Figure C.37

Concrete Poured on July 1, 2004

Concrete Poured



Figure C.38







Figure C.40



Figure C.41



Wet Concrete (Distributed Loading On Bare Joists) vs. Interior Load Cells

Concrete Poured

Figure C.42

Load Cells (lb)

C.3 CURED CONCRETE JOIST TESTINGC.3.1 ALL BOTTOM CHORD EXTENSIONS IN PLACE (STAGE 1)



Figure C.43



Figure C.44



Figure C.45



Figure C.46







Figure C.48







Figure C.50







Figure C.52







Figure C.54







Figure C.56







Figure C.58



Figure C.59



Figure C.60







Figure C.62



Figure C.63



Figure C.64







Figure C.66



Figure C.68



Figure C.70

Load Cell (lb)

<u>−</u>∆− N4







Figure C.72







Figure C.74







Figure C.76







Figure C.78



Figure C.79

C.3.2 EXTERIOR BOTTOM CHORD EXTENSIONS TAKEN OUT (STAGE 2)



Figure C.80



Figure C.81



Figure C.82



Figure C.83







Figure C.85







Figure C.87







Figure C.89



Figure C.90



Figure C.91



Figure C.92



Figure C.93



Figure C.94



Figure C.95







Figure C.97



Figure C.98



Figure C.99





Figure C.101


Figure C.102

C.3.3 INTERIOR BOTTOM CHORD EXTENSIONS TAKEN OUT (STAGE 3)



Figure C.103



Figure C.104



Figure C.105



Figure C.106



Figure C.107



Figure C.108



Figure C.109



Figure C.110



Figure C.111

C.3.4 INTERIOR BOTTOM CHORD EXTENSIONS RE-INSTALLED (STAGE 4)







Figure C.113







Figure C.115







Figure C.117







Figure C.119





Figure C.121







Figure C.123







Figure C.125







Figure C.127







Figure C.129







Figure C.131



Distributed Load on the Slab (psf) 15 10 -**D**- S2 FE ▲ N2 5 0 -1000 -800 -600 -400 -200 0 200 400 600 800 1000 1200 1400 1600 Load Cell (lb)

Figure C.133



Figure C.134

C.3.5 EXTERIOR BOTTOM CHORD EXTENSIONS RE-INSTALLED(STAGE 5)



Figure C.135



Figure C.136







Figure C.138







Figure C.140



Figure C.142







Figure C.144







Figure C.146







Figure C.148







Figure C.150







Figure C.152



Figure C.153



Figure C.154



Figure C.155



Figure C.156



Figure C.158



Figure C.160



Figure C.162







Figure C.164







Figure C.166







Figure C.168





Figure C.170

Load Cell (lb)

400

600

800

1000

1200

200

0 ↓ -600

-400

-200

0


Figure C.172



Figure C.174



Figure C.175