

## **Chapter 5    CONTROL OF CASCADED-MULTILEVEL CONVERTER-BASED STATCOM**

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This chapter proposes a new control technique for the CMC-based STATCOM. The proposed STATCOM model, which was derived in Chapter 4, is employed in the design process. Based on its characteristics, the proposed control technique is named power decoupling control. Real and reactive power exchanged between the STATCOM and the power networks can be controlled independently by the proposed control technique, which is practical in both reactive and real power compensation applications. This dissertation, however, mainly focuses on the reactive power compensation.

Due to the imbalance problem among DC capacitor voltages in the CMC topology, a DC capacitor voltage balancing-technique, which is named cascaded PWM, is proposed. Theoretically, this technique can be applied in CMCs with any number of voltage levels; additionally, it is a single-phase approach, and can be realized by a field-programmable gate array (FPGA). The number of controlled capacitor voltages is solely limited by the calculation speed of the DSP and the clock speed of the FPGA. Combining the proposed DC-link-balancing technique with the proposed modeling technique, cascaded-multilevel VSCs with any number of voltage levels can be modeled as three-level cascaded VSCs.

The performance and stability of the proposed control technique is validated by both computer simulations and experiments. A scaled-down seven-level cascaded-based STATCOM prototype is implemented. A DSP associated with an FPGA is used as the main controller.

### **5.1    Control Analysis and Design**

The three-level cascaded-based STATCOM is used as a starting case. The control of the STATCOM is designed in DQ0 coordinates. The modeling accuracy and control performance are verified by computer simulations and experiments.

To validate the proposed DC bus voltage-balancing technique, a seven-level cascaded converter is employed as the VSC in the STATCOM system. Each phase of the cascaded seven-

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level converter consists of three H-bridge converters whose DC buses are regulated by the proposed balancing technique.

## **I. Control Law for the Cascaded-Multilevel Converter-Based STATCOM**

The proposed STATCOM system, as shown in Figure 5-1, is composed of a generic CMC, which is coupled to a power system via coupling reactors at the PCC. In the case of the STATCOM connected to a transmission network, the coupling reactors may be represented by the leakage inductance of the step-up power transformers. Figure 5-2 illustrates a single-line diagram of the generic CMC-based STATCOM system. The power network is modeled as three ideal voltage sources associated with their Thevenin impedances. In general, the voltage profile at the PCC varies with network operation, fault and protection schemes.

The STATCOM can operate properly and effectively as long as the following two sets of key electrical parameters are watchfully controlled: three-phase output currents and multiple DC capacitor voltages. The output currents determine the amount of reactive power exchanged with the power network. A single-line diagram of the STATCOM shown in Figure 5-2 is used as an example. At this point, the CMC is assumed to be lossless. The STATCOM behaves as an adjustable capacitive load, which injects reactive power into the power network, when its output voltage is controlled to be greater than that of the power network. Figure 5-3(a) illustrates phasor diagrams of the output voltage,  $V_o$ , voltage at the PCC,  $V_{pcc}$ , and output current,  $I_o$ , when the STATCOM operates in the capacitive mode. In contrast, as shown in Figure 5-3(b), the output voltage of the STATCOM is controlled to be less than that of the power network in order to absorb reactive power from the network.

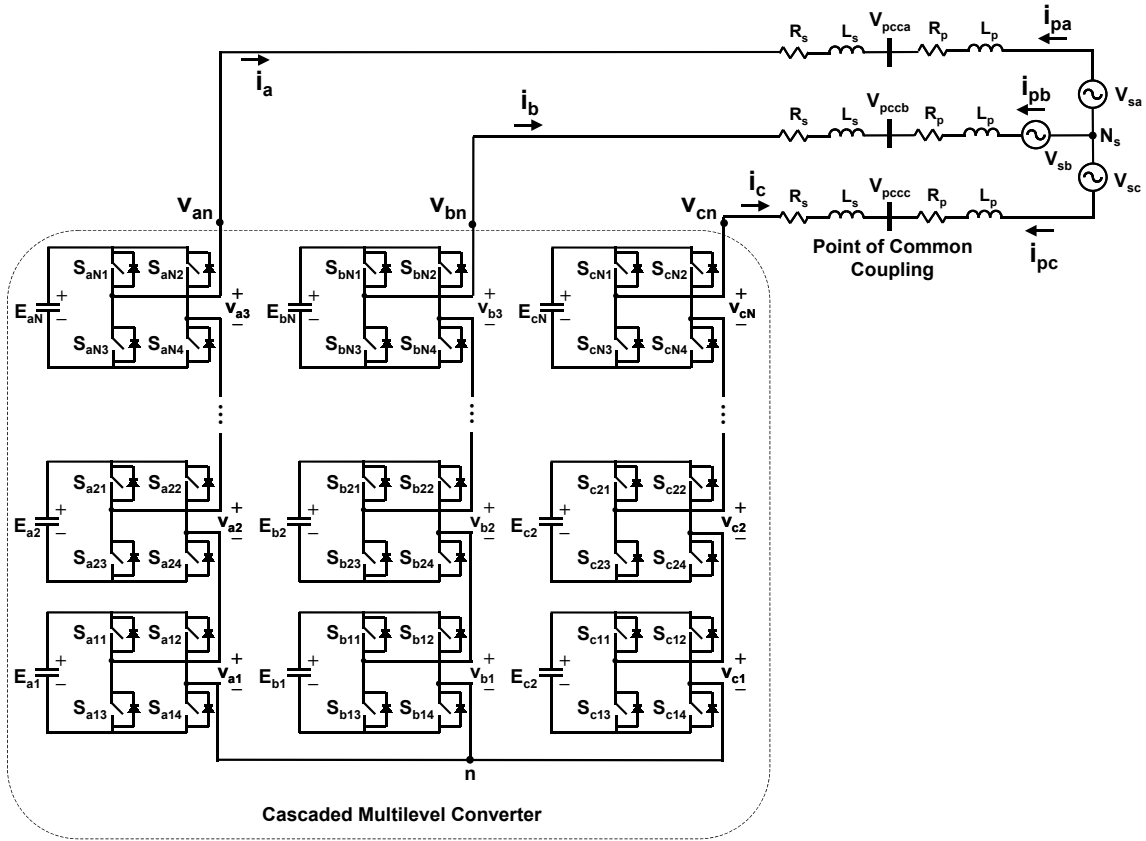


Figure 5-1. Schematic of the proposed cascaded-multilevel converter-based STATCOM system.

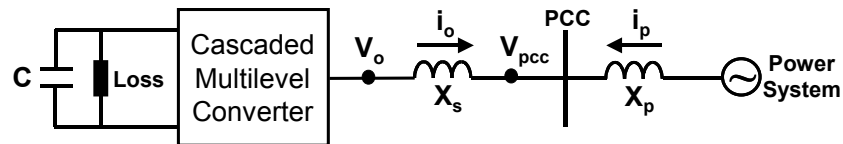


Figure 5-2. Single-line diagram of cascaded-multilevel converter-based STATCOM system.

From the phasor diagrams of the STATCOM in both operation modes, the amount of average reactive power exchanged at the PCC can be expressed as follows:

$$Q_{pcc} = 3 \frac{V_{pcc}^2}{X_s} \left( \frac{M}{M_{standby}} - 1 \right), \text{ and}$$

**Equation 5-1**

$$M_{standby} = \frac{\sqrt{2} \cdot V_{pcc}}{N \cdot E},$$

**Equation 5-2**

where  $V_{pcc}$  is the phase voltage at the PCC,  $X_s$  is the coupling impedance,  $E$  is the individual DC capacitor voltage,  $N$  is the number of H-bridge converters per phase,  $M$  is the modulation index, and  $M_{standby}$  is the modulation index for the STATCOM in the standby mode.

In practice, however, the CMC is not lossless. Real power imported from the network is required; otherwise, the voltages across the DC capacitors eventually collapse. To regulate the DC capacitor voltages, a small phase shift or power angle,  $\delta$ , is introduced between the converter output voltage and the voltage at the PCC, as shown in Figure 5-4. The average regulating power is then derived as a function of the power angle, as follows:

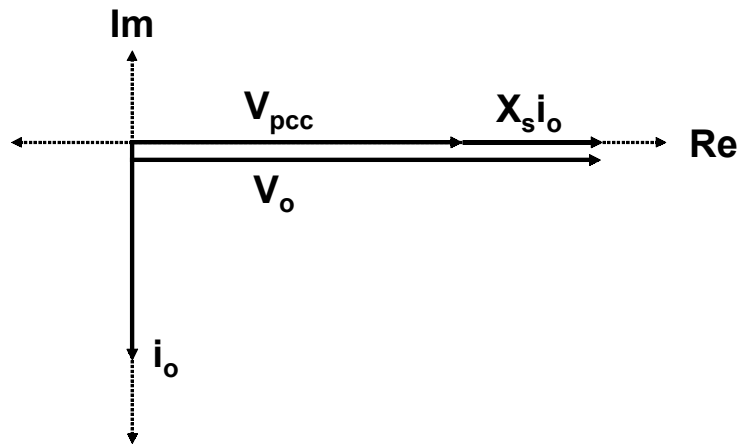
$$P_{req} = \frac{V_{pcc} \cdot M \cdot N \cdot E}{\sqrt{2} \cdot X_s} \sin(\delta),$$

**Equation 5-3**

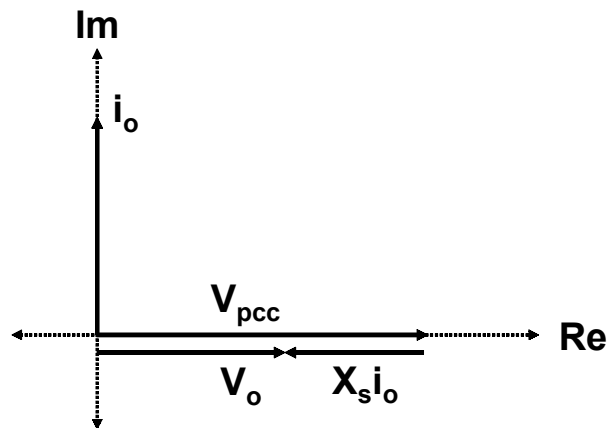
where  $V_{pcc}$  is the phase voltage at the PCC,  $X_s$  is the coupling impedance,  $E$  is the individual DC capacitor voltage,  $N$  is the number of H-bridge converters per phase,  $M$  is the modulation index, and  $\delta$  is the power angle.

In summary, two key control laws for the cascaded-multilevel VSC utilized in the STATCOM applications are as follows:

1. the amount of the transferred reactive power (Var, Q) can be controlled by adjusting the magnitude of the converter output voltage, and
2. the amount of the transferred real power (Watt, P) can be controlled by adjusting the phase displacement of the converter output voltage with respect to the voltage at the PCC.



(a)



(b)

**Figure 5-3. Operating phasor diagrams of the lossless three-level converter-based STATCOM:**  
(a) capacitive mode and (b) inductive mode.

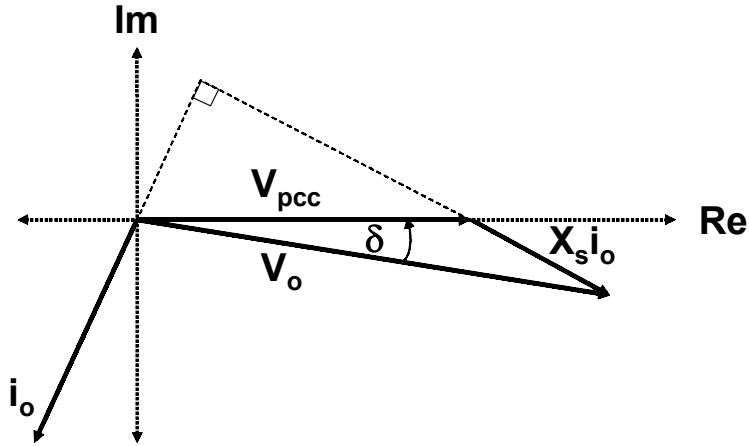


Figure 5-4. Operating phasor diagrams of non-ideal three-level converter-based STATCOM.

## II. Three-Level Cascaded-Based STATCOM Control Design

The control design starts with the three-level cascaded converter, which has the least number of output voltage levels. With only one H-bridge converter per phase, voltage-balancing problem does not exist in this case. The purpose of starting with the three-level converter is to verify the correctness and accuracy of the output currents and single DC capacitor voltage regulation.

This particular STATCOM system, as shown in Figure 5-5, is formed by a three-level cascaded converter that is coupled to a power system by the coupling reactors at the PCC.

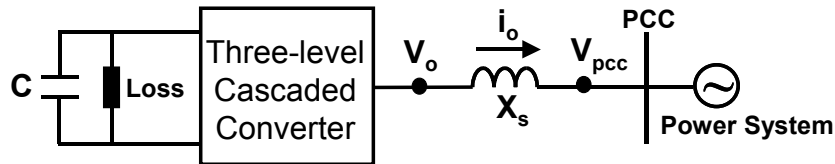


Figure 5-5. Single-line diagram of a STATCOM system utilizing the three-level cascaded converter.

The schematic of the completed power stage of the three-level cascaded-based STATCOM is shown in Figure 5-5. Each phase of the cascaded converter consists of an H-bridge converter, which can generate three levels of output voltages, i.e.,  $-E$ ,  $0$  and  $+E$ .

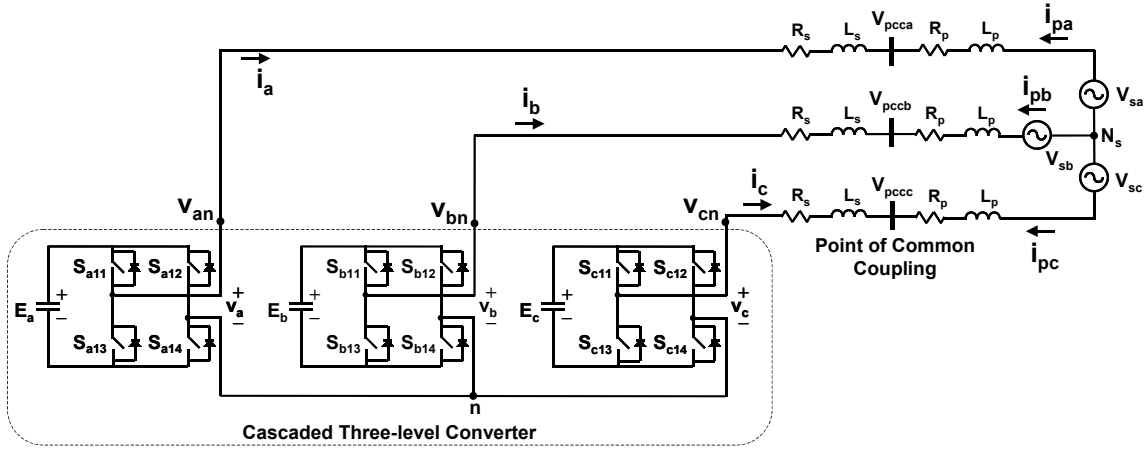


Figure 5-6. Schematic of the three-level cascaded-based STATCOM system.

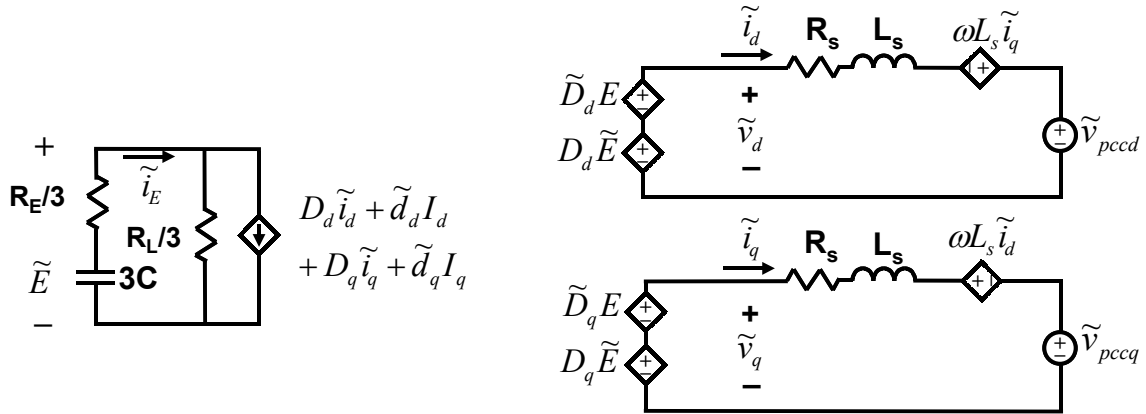


Figure 5-7. Small-signal model of the three-level cascaded-based STATCOM.

Based on the proposed HBBB discussed in Chapter 3, the electrical parameters of the cascaded three-level converter and the power network are designed as shown in Table 5-1.

TABLE 5-1. SPECIFICATION OF THE STUDIED SYSTEM.

<b>Three-Level Cascaded Converter</b>	
Individual DC Bus Voltage	2100 V $\pm$ 10%
Total DC Bus Voltage	2100 V $\pm$ 10%
Rated RMS Reactive Current	1250 A
Capacitor Impedance	$(2.5\text{m-j}/(\omega \cdot 10.5\text{mF})) \Omega$
Individual Switching Frequency/ Equivalent Switching Frequency	1 kHz/ 2 kHz
<b>Power System</b>	
Configuration	Balanced Three-Phase Three-Wire
Coupling Reactor Impedance	$(13\text{m-j}\omega \cdot 350\mu\text{H}) \Omega$
PCC Line Voltage	2100 V

#### A. System Transfer Functions

From the generic CMC-based STATCOM model derived in Chapter 4, with one H-bridge converter per phase, the simplified small-signal model for the three-level cascaded-based STATCOM can be depicted as shown in Figure 5-7. Due to the three-phase three-wire configuration, the 0-channel is omitted in this case.

Based on the small-signal model of the three-level cascaded-based STATCOM, five key transfer functions used for control design are derived as follows:



- Control-to-Output-Current Transfer Function,  $G_{idd}$  and  $G_{iqq}$

$$G_{idd} = \frac{\tilde{i}_d}{\tilde{d}_d} = \frac{K_{idd} \left( \frac{S}{\omega_z} + 1 \right)}{\left( \frac{S}{\omega_p} \right)^2 + \frac{S}{Q\omega_p} + 1},$$

**Equation 5-4**

where

$$K_{idd} = \frac{NER_s}{R_s^2 + (\omega L_s)^2}, \quad Q = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{2R_s},$$

$$\omega_p = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{L_s}, \text{ and } \omega_z = \frac{R_s}{L_s},$$

and

$$G_{iqq} = \frac{\tilde{i}_q}{\tilde{d}_q} = \frac{K_{iqq} \left( \frac{S}{\omega_z} + 1 \right)}{\left( \frac{S}{\omega_p} \right)^2 + \frac{S}{Q\omega_p} + 1},$$

**Equation 5-5**

where

$$K_{iqq} = \frac{NER_s}{R_s^2 + (\omega L_s)^2}, \quad Q = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{2R_s},$$

$$\omega_p = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{L_s}, \text{ and } \omega_z = \frac{R_s}{L_s}.$$

- Control-to-Cross-Coupling-Output-Current Transfer Function,  $G_{iqd}$  and  $G_{idq}$

$$G_{iqd} = \frac{\tilde{i}_q}{\tilde{d}_d} = \frac{K_{iqd}}{\left(\frac{S}{\omega_p}\right)^2 + \frac{S}{Q\omega_p} + 1},$$

**Equation 5-6**

where

$$K_{iqd} = \frac{-\omega L N E}{R_s^2 + (\omega L_s)^2}, \quad Q = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{2R_s},$$

$$\omega_p = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{L_s}, \text{ and } \omega_z = \frac{R_s}{L_s}.$$

Likewise,

$$G_{idq} = \frac{\tilde{i}_d}{\tilde{d}_q} = \frac{K_{idq}}{\left(\frac{S}{\omega_p}\right)^2 + \frac{S}{Q\omega_p} + 1},$$

**Equation 5-7**

where

$$K_{idq} = \frac{-\omega L N E}{R_s^2 + (\omega L_s)^2}, \quad Q = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{2R_s},$$

$$\omega_p = \frac{\sqrt{R_s^2 + (\omega L_s)^2}}{L_s}, \text{ and } \omega_z = \frac{R_s}{L_s}.$$

- Output-Current-to-DC-Bus-Voltage Transfer Function,  $G_{Eid}$

$$G_{Eid} = \frac{\tilde{E}}{\tilde{i}_d} = \frac{K_{Eid} \left( \frac{S}{\omega_z} + 1 \right)}{\left( \frac{S}{\omega_p} \right)^2 + \frac{S}{Q\omega_p} + 1},$$

**Equation 5-8**

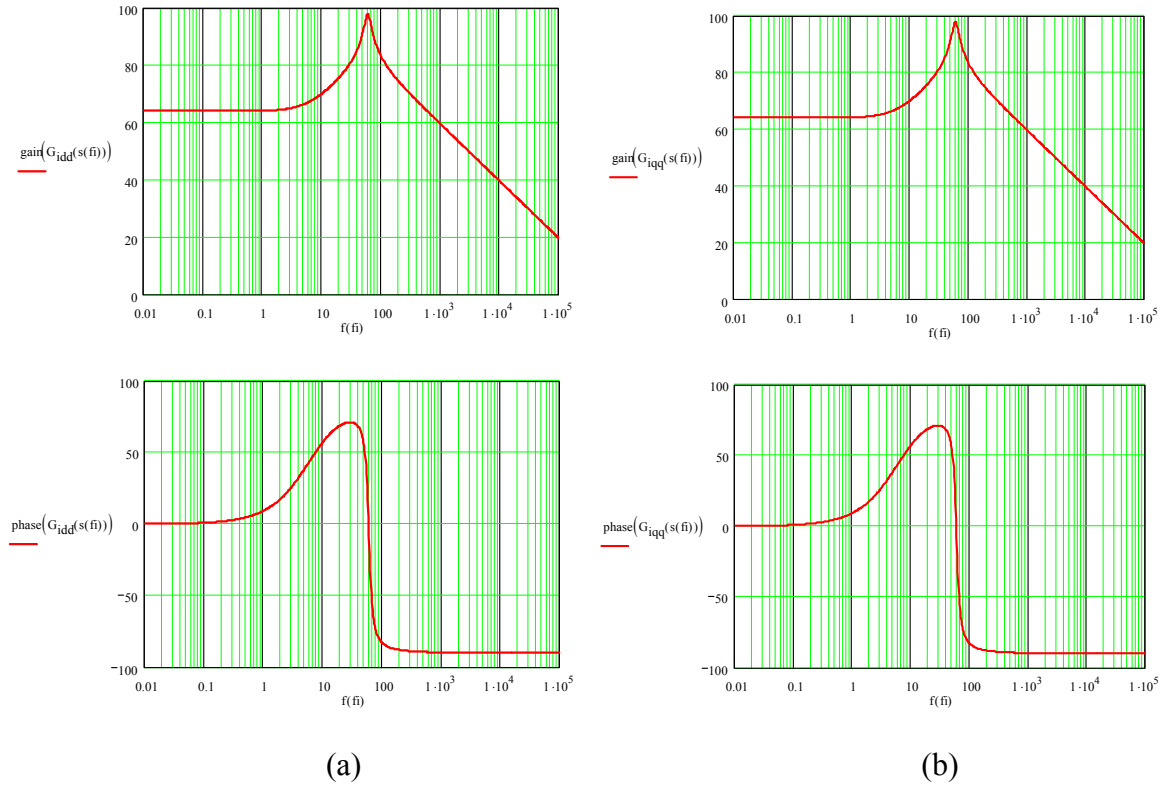
where

$$K_{Eid} = \frac{D_q \omega L_s + D_d R_s}{D_d D_q N}, \quad Q = \sqrt{\frac{D_{dj} D_{qj} N L_s}{3 C R_s^2}},$$

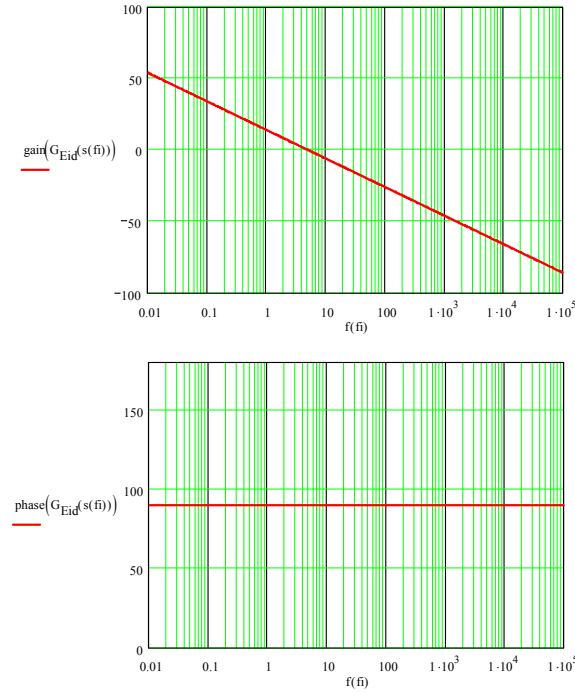
$$\omega_p = \sqrt{\frac{D_d D_q N}{3 C L_s}}, \text{ and } \omega_z = \frac{D_q \omega}{D_d} + \frac{R_s}{L_s}.$$

Based on the designed electrical parameters, Bode plots of the three key system transfer functions, i.e.,  $G_{idd}$ ,  $G_{iqq}$ , and  $G_{ied}$ , are shown in Figure 5-8 and Figure 5-9. Very high peaks appear at 60 Hz in  $G_{idd}$  and  $G_{iqq}$  because of the insignificant stray resistance in the coupling inductors and DC capacitors. This system is considered as a high-Q or a very-low loss system. The transfer function  $G_{ied}$  behaves as the integration due to the capacitive dominance in the DC links.

From these three Bode plots, their phases are constant at the high-frequency range because the non-ideal factors are not taken into account. Three major non-ideal factors include the switching frequency and the delay of the control and data-acquisition systems.



**Figure 5-8. Ideal open-loop transfer function of the control-to-output current in the (a) D-channel,  $G_{idd}$ , and (b) Q-channel,  $G_{iqq}$ .**



**Figure 5-9. Ideal open-loop transfer function of the D-channel current-to-DC-capacitor voltage,  $G_{Id}$ .**

### ***B. Effects of Various Delays on the Transfer Functions***

In practice, three important delays embedded in both the power stage and the controller must be considered: the switching, the calculation and the transducer delays.

- ***Switching Delay***

Limited by the system operation condition and its thermal capability, the recent high-power semiconductor devices can switch in a range of several hundred to a few kilohertz. The switching delay is, therefore, the most important factor of concern in the high-power electronic control design. To further explain how to determine the switching delay for the CMC, an H-bridge converter, as shown in Figure 5-10, is used as an example. An H-bridge converter basically consists of two phase legs. Each phase leg comprises two complementary switches. The relationship of the total output voltage and individual phase-leg voltages is simply expressed as follows:

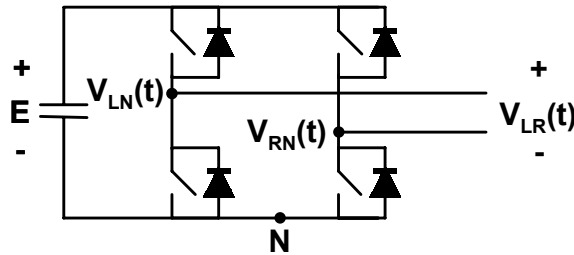
$$V_{LR}(t) = V_{LN}(t) - V_{RN}(t) .$$

**Equation 5-9**

Figure 5-11 shows the digital PWM synthesis for an H-bridge converter. The command duty cycle is compared to a linear slope; the intersection determines the switching event. Each phase leg is assumed to switch at  $1/T$  Hertz. The left phase leg is controlled by the positive duty cycle, whereas the right phase leg is controlled by the negative duty cycle, which is out of phase with the positive duty cycle. The duty cycle is updated every half-cycle. In other words, each phase leg responds to the duty cycle every half-cycle and has a half-cycle delay time. In Figure 5-11, the duty cycle is updated at times  $T$  and  $1.5 T$ . Although  $V_{LR}(t)$  has twice the switching frequency compared to each phase leg, the duty cycle is still updated every half-cycle. The double switching frequency provides improvement in the synthesized output waveform, but it does not shorten the delay time. Since the output of the CMC is the summation of  $N$  individual H-bridge converters, its switching delay is then:

$$T_{d\_sw}(t) = \frac{1}{2 \cdot N \cdot f_s} .$$

**Equation 5-10**



**Figure 5-10. Two phase legs forming an H-bridge converter.**

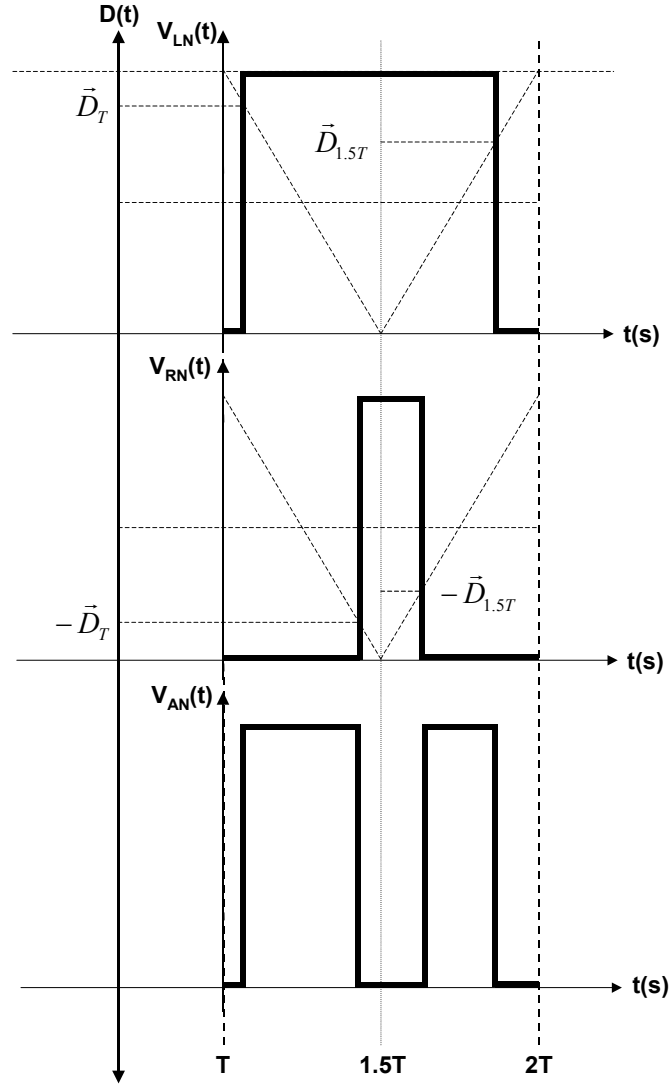


Figure 5-11. PWM-generation technique for the H-bridge converter.

- **Calculation Delay**

This delay is basically a function of the processor used in the controller. Due to its high-speed arithmetic units, the recent floating-point DSP is widely employed in real-time control applications. In this dissertation, a 133MHz DSP from Texas Instrument (TI), TMS320D6701, which can perform 800 mega floating-point operations per second (MFLOPS), is programmed to finish each feedback calculation in 100  $\mu$ s. The calculation delay is thus:

$$T_{d\_cal}(t) = 100 \mu s .$$

**Equation 5-11**

- **Transducer Delay**

In general, feedback parameters in a digital-based control system are acquired by analog-to-digital converters (ADCs). The transducer delay is also known as the sampling delay, which is indirectly proportional to the sampling frequency of the ADC. An ADC from TI, THS1206, is used as the data converters in this dissertation. It has 12 bits of resolution and a conversion rate of 6 megasamples per second (MSPS). The transducer delay is therefore 167 ns.

$$T_{d\_ADC}(t) = 167 ns .$$

**Equation 5-12**

- **Total Delay**

Basically, the total delay is the summation of these three previously discussed delays. Due to the dominance of the switching delay, the total delay time can be approximated by the switching delay, as shown in Equation 5-13.

$$T_d = T_{d\_sw} + T_{d\_cal} + T_{d\_ADC} \approx T_{d\_sw} .$$

**Equation 5-13**

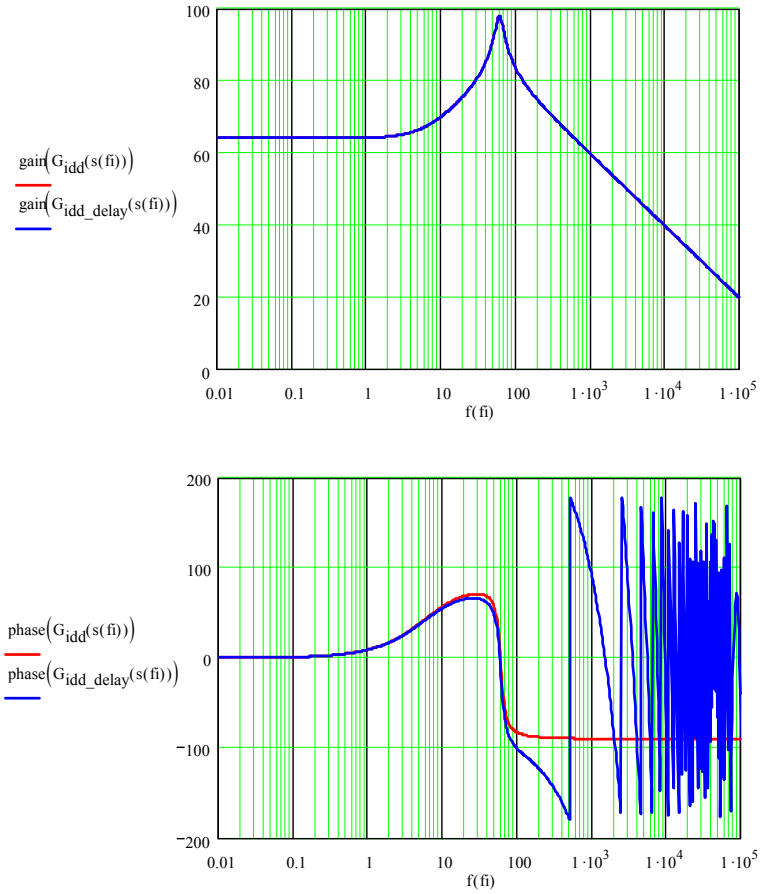
This delay mainly affects the phase delay of the loop gain, and can be modeled in Laplace form as follows:

$$\tau(s) = e^{-T_d s} .$$

**Equation 5-14**

By taking into account the system delay, the new open-loop transfer function,  $G_{idd}$ , can be plotted as shown in Figure 5-12. With a switching frequency of 1 kHz, the phase of  $G_{idd}$  rapidly rolls off at above 70 Hz. Obviously, this significantly limits the bandwidth of the feedback-current loop gain. Based on the controller processor and power stage of the converter, the switching delay has the most significant effect on the control design.





**Figure 5-12. Comparison of the transfer function,  $G_{idd}$ , without and with delay.**

### ***C. Cross-Coupling Effects***

To show the cross-coupling components between the D-channel and the Q-channel, the differential equation of the output current of the STATCOM is rewritten in Equation 5-15:

$$\frac{d}{dt} \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \\ \tilde{i}_0 \end{bmatrix} = \frac{E}{L_s} \begin{bmatrix} \tilde{d}_d \\ \tilde{d}_q \\ \tilde{d}_0 \end{bmatrix} + \frac{\tilde{E}}{L_s} \begin{bmatrix} D_d \\ D_q \\ D_0 \end{bmatrix} - \frac{1}{L_s} \begin{bmatrix} \tilde{v}_{vpccd} \\ \tilde{v}_{vpccq} \\ \tilde{v}_{vpcc0} \end{bmatrix} - \begin{bmatrix} \frac{R_s}{L_s} & -\omega & 0 \\ \omega & \frac{R_s}{L_s} & 0 \\ 0 & 0 & \frac{R_s}{L_s} \end{bmatrix} \cdot \begin{bmatrix} \tilde{i}_d \\ \tilde{i}_q \\ \tilde{i}_0 \end{bmatrix}.$$

**Equation 5-15**

From Equation 5-15, in the D-channel, a current-controlled voltage source is a function of the current  $i_q$ , while, in the Q-channel, a current-controlled-voltage source is a function of cross-coupling current,  $i_d$ . The amplitudes of both dependent voltage sources can be expressed in Equation 5-16:

$$v_{dq} = |\omega \cdot L \cdot i_q|,$$

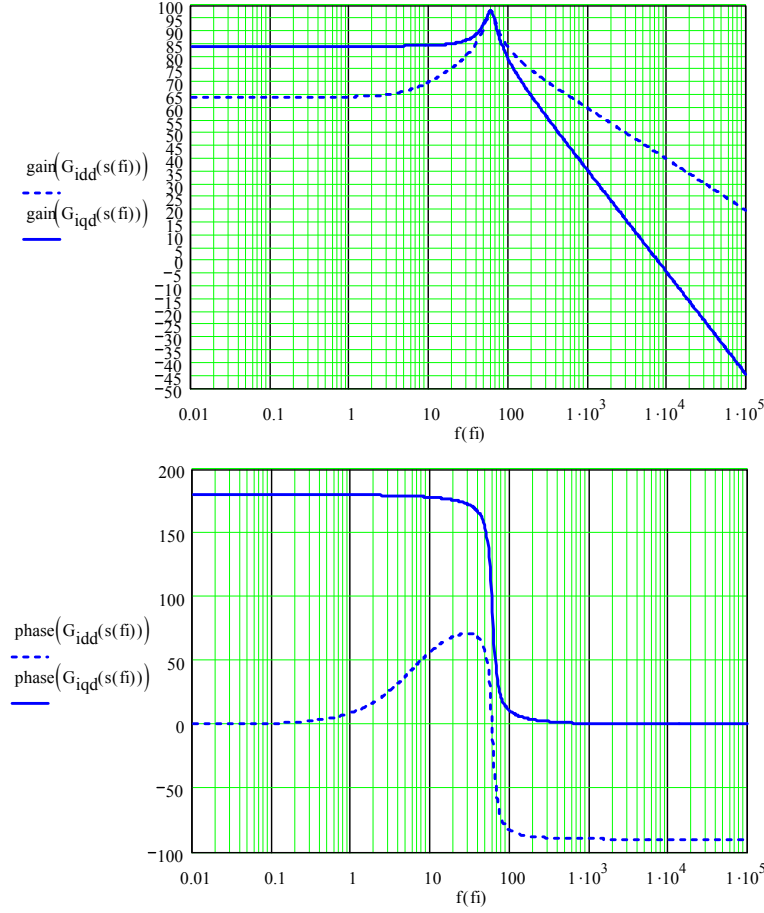
and

$$v_{qd} = |\omega \cdot L \cdot i_d|.$$

**Equation 5-16**

To show the cross-coupling effect, the Bode plot of  $G_{idd}$  and  $G_{iqd}$  are illustrated in Figure 5-13. Obviously, at frequencies lower than the corner frequency, which is roughly 60 Hz, the gain of  $G_{iqd}$  dominates that of  $G_{idd}$ . In other words, by controlling duty cycle d, the Q-channel current tends to react more than the D-channel current does, which is undesirable.

In order to alleviate the cross-coupling effect, the designed crossover frequency of the current closed-loop gain should be kept higher than the corner frequency, where the gain of  $G_{idd}$  is higher than that of  $G_{iqd}$ . To further improve the loop response, the decoupling technique is applied in the current loop gain, as discussed in the following section.



**Figure 5-13. Bode plot of control-to-output current,  $G_{idd}$  and  $G_{idq}$ .**

#### **D. Control Strategy**

In general, the PCC is a critical voltage bus in the power network that requires the special attention. The voltages at the PCC are, therefore, monitored and assigned as the reference for the proposed control system. Normally, a three-phase parameter in the ABC coordinates can be represented by a vector in the ABC space. A positive-sequence phase voltage at the PCC,  $\vec{V}_{pcc}(t)$ , for example, is represented as a voltage vector expressed in Equation 5-17. Figure 5-14 illustrates an instantaneous vector of the voltages at the PCC at time  $t$ ,  $\vec{V}_{pcc}(t)$ , in the ABC space. For a balanced three-phase system, the phase-voltage vector at the PCC rotates along the dotted

line with an angular velocity of  $\omega$ . Based on the plane created by the  $\vec{V}_{pcc}(t)$  rotation, a new coordinate called  $\alpha\beta\gamma$  is defined as follows:

1. the  $\alpha$ - $\beta$  plane is aligned with the surface  $A_{vpcc}$ , and
2. the  $\gamma$ -axis is perpendicular to the surface  $A_{vpcc}$ .

$$\vec{V}_{pcc}(t) = \begin{bmatrix} v_{pcca} \cos(\omega t) \\ v_{pccb} \cos(\omega t - \frac{2\pi}{3}) \\ v_{pccc} \cos(\omega t + \frac{2\pi}{3}) \end{bmatrix}$$

**Equation 5-17**

To be clearly shown, the space as shown in Figure 5-14 is depicts in Figure 5-15 by viewing it perpendicularly to surface  $A_{vpcc}$ . Since the  $\alpha\beta\gamma$  coordinate is stationary with respect to the ABC coordinate, the projection of vector  $\vec{V}_{pcc}(t)$  in the  $\alpha\beta\gamma$  coordinate is still time-variant. To achieve a time-invariant vector, another new coordinate is then introduced, and is named DQ0. In general, the  $\alpha\beta\gamma$  and DQ0 coordinates are identical except that the DQ0 coordinate rotates around the 0-axis at the speed of the reference vector.

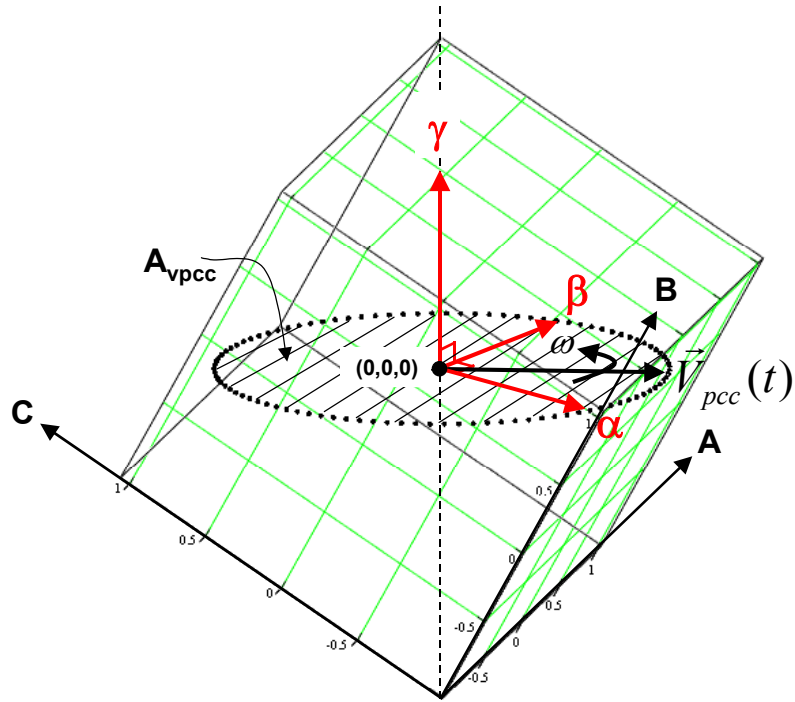


Figure 5-14. PCC voltage vector of a balanced three-phase system, plotted in the ABC space.

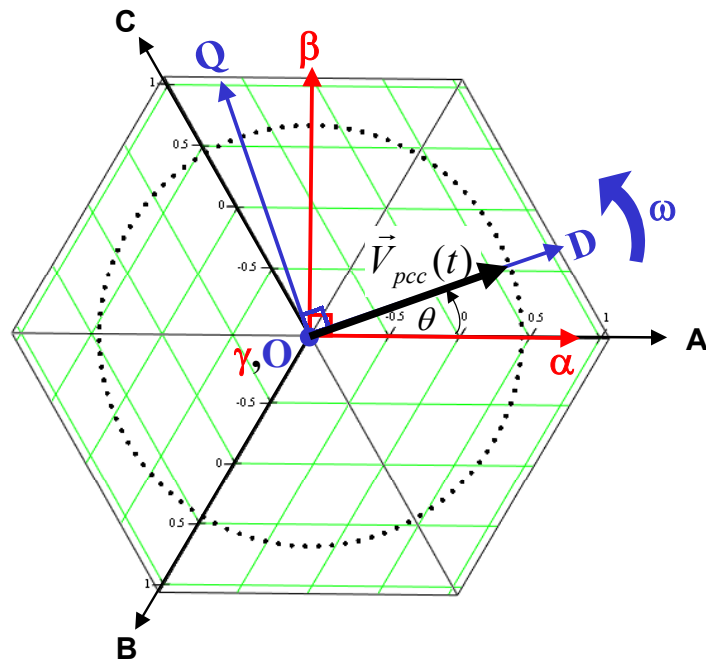


Figure 5-15. Vector of PCC voltage aligned with the D-axis in the DQ0 space.

From Figure 5-15, if the DQ0 coordinate rotates with the same angular velocity of that of  $\vec{V}_{pcc}(t)$ , vector  $\vec{V}_{pcc}(t)$  then becomes stationary in the DQ0 space. In other words, the behavior of balanced, three-phase, time-variant parameters in the ABC coordinates can be simply represented by two time-invariant parameters in the DQ0 coordinates. Park's transformation matrix<sup>1</sup>,  $\vec{T}_{dq0/abc}$ , is a tool for transferring parameters in the ABC into DQ0 coordinates.

To make a physical meaning for the control system,  $\vec{V}_{pcc}(t)$  is aligned with the D-axis (direct axis). By multiplying Park's transformation matrix with  $\vec{V}_{pcc}(t)$ , the  $v_{pccq}$  and  $v_{pcc0}$  become zero, while  $v_{pccd}$  is roughly 1.225 times the peak voltage at the PCC in the ABC coordinates.

$$\begin{bmatrix} v_{pccd} \\ v_{pccq} \\ v_{pcc0} \end{bmatrix} = \vec{T}_{dq0/abc} \begin{bmatrix} v_{pcca} \cos(\omega t) \\ v_{pccb} \cos(\omega t - \frac{2\pi}{3}) \\ v_{pccc} \cos(\omega t + \frac{2\pi}{3}) \end{bmatrix} = \begin{bmatrix} \sqrt{\frac{3}{2}} \cdot v_{pcca} \\ 0 \\ 0 \end{bmatrix}$$

**Equation 5-18**

By applying this rule, the parameters in the DQ0 coordinates in line with the D-axis provide real components, whereas the quadrature components represent the reactive components. Therefore, the relationship between the instantaneous three-phase power components in the DQ0 coordinates can be expressed in Equation 5-19. The amount of real power exchanged between the STATCOM and the power grid is the product of the D-channel voltage at the PCC and the D-channel output current of the STATCOM. This fraction of real power is usually used to regulate the DC capacitor voltages. On the other hand, the amount of reactive power exchanged between the STATCOM and the power grid is the product of the D-channel voltage at the PCC and the Q-

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<sup>1</sup> The Park's transformation matrix derivation is shown in Appendix A.

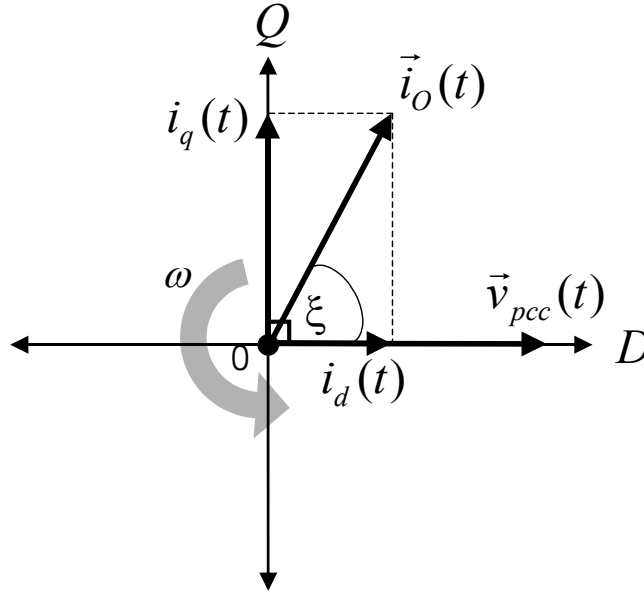
channel output current of the STATCOM. This reactive power is the key component to be controlled.

$$P(t) = 2 \cdot |V_{pccd}| \cdot |I_d|, \text{ and } Q(t) = -2 \cdot |V_{pccd}| \cdot |I_q|, \text{ or}$$

**Equation 5-19**

$$P(t) = 2 \cdot |\vec{V}_{pcc}| \cdot |\vec{I}_O| \cos(\xi), \text{ and } Q(t) = -2 \cdot |\vec{V}_{pcc}| \cdot |\vec{I}_O| \sin(\xi).$$

**Equation 5-20**



**Figure 5-16. Phasor diagram of the alignment of key control parameters.**

This obviously complies to the control law presented earlier, i.e., the amount of transferred reactive power (Var, Q) can be controlled by adjusting the magnitude of the converter output voltage, and the amount of transferred real power (Watt, P) can be controlled by adjusting the phase displacement of the converter output voltage with respect to the voltage at the PCC.

Figure 5-17 shows the complete proposed control block diagram for the three-level cascaded-based STATCOM system. The main objective of the feedback controller is to regulate the Q-channel current following its command as fast as possible.



In the Q-channel, the  $I_q$  command is generated by an external control, which is obtained either from the control person or the automatic controller. The  $I_q$  command is compared with the

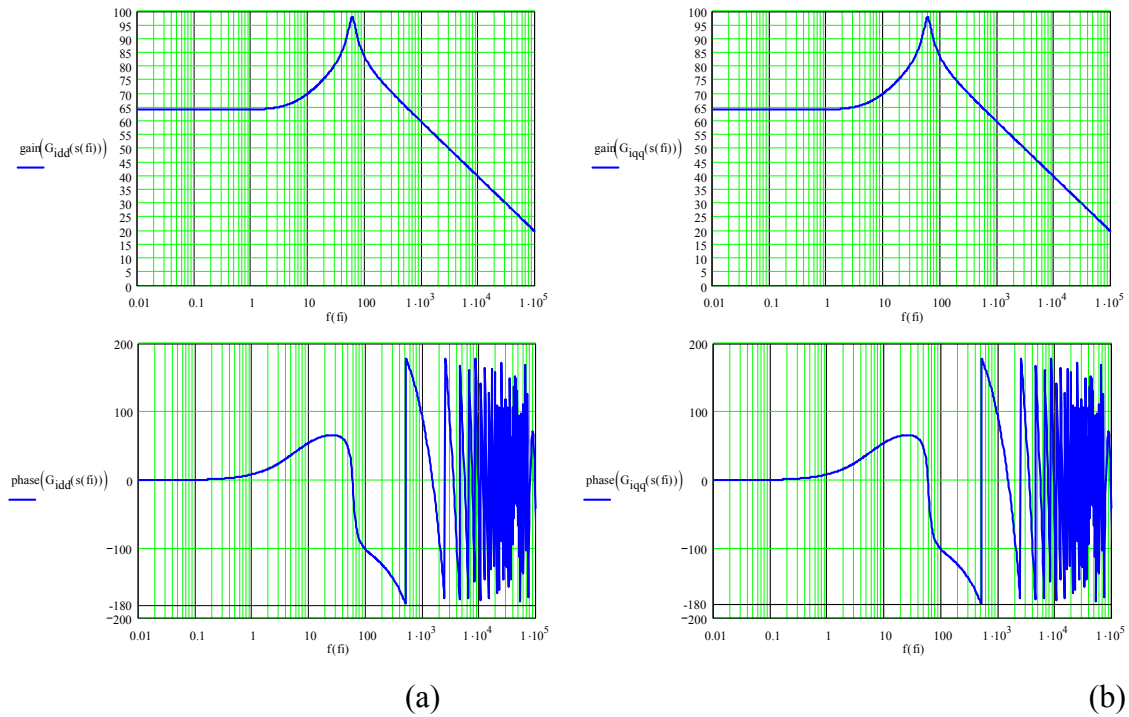


feedback  $I_q$ , and the error is compensated by the current compensator,  $H_{iq}$ , whose output is the Q-channel duty cycle command.

The control process starts with the internal control loop. The current compensators  $H_{id}$  and  $H_{iq}$  are first designed to meet the crossover frequency and phase margin requirement. In the D-channel, the voltage compensator  $H_{Eid}$  is then designed based on the new current-loop gain.

- **Design of Current Compensator,  $H_{id}$  and  $H_{iq}$**

Based on the designed power stage parameters, the Bode plots of the open-loop transfer functions  $G_{idd}$  and  $G_{iqq}$ , associated with the delay, are shown in Figure 5-18. Because the characteristics of  $G_{idd}$  and  $G_{iqq}$  are identical, only  $G_{idd}$  is used throughout the current-compensator design process.



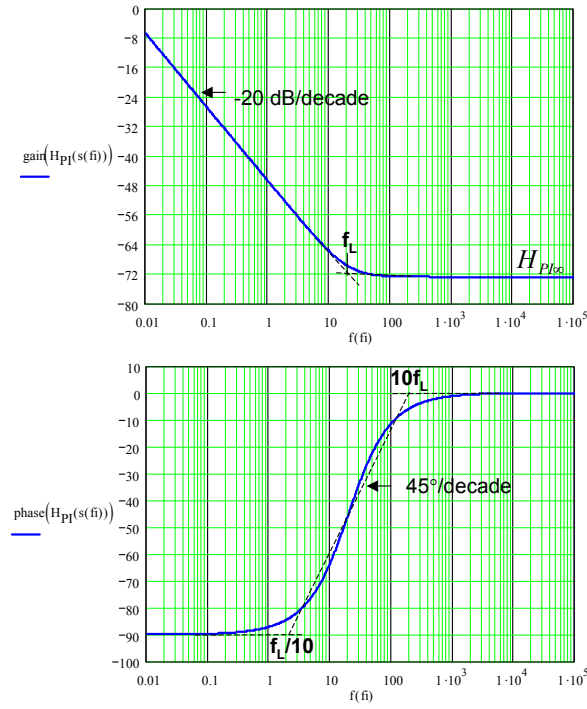
**Figure 5-18. Open-loop control-to-output-current transfer function associated with delay in the (a) D-channel,  $G_{idd}$  (b) Q-channel,  $G_{iqq}$ .**

Due to the Nyquist's criteria, the designed crossover frequency of the current loop should not be higher than half of the effective switching frequency, which equals twice the individual phase-leg switching frequency or 2 kHz in this case. Basically, an average model is capable of predicting the behavior of its switching model from DC up to half of the effective switching frequency. By designing the crossover frequency above this specific switching frequency, the stability prediction of the system is theoretically invalid. From the Bode plot shown in Figure 5-18, the loop gain of the compensated  $G_{idd}$  at the low-frequency range should be as high as possible, such that the output is well regulated at DC and at frequencies below the crossover frequency.

Among well-known compensators, the lag compensator or the proportional-plus-integral (PI) is the best candidate based on its simplicity and reliability. A general transfer function of the PI compensator  $H_{PI}(S)$  is given in Equation 5-21, and its magnitude and phase asymptotes are shown in Figure 5-19. To achieve a zero steady-state error for the current-loop gain, an inverted zero of the PI compensator is added at frequency  $f_L$ . Moreover, if  $f_L$  is sufficiently below the loop crossover frequency, the original phase margin is not disturbed by the PI compensator.

$$H_{PI}(S) = H_{PI\infty} \left( 1 + \frac{\omega_L}{S} \right)$$

**Equation 5-21**



**Figure 5-19. Bode plot of the PI compensator transfer function.**

Alternatively, the PI compensator can be expressed by its two sub-functions, i.e., proportion and integral, as follows:

$$H_{PI}(S) = K_p + \frac{K_i}{S},$$

**Equation 5-22**

where  $K_p = H_{PI\infty}$ , and  $K_i = H_{PI\infty} \cdot \omega_L$ .

According to the Bode plot of  $G_{idd}$ , as shown in Figure 5-18, a couple of undesirable factors complicate the design of compensator  $H_{id}(S)$ , i.e., very high Q in the gain and that the phase quickly rolls off in the vicinity of the designed crossover frequency.

With the compensator, the closed-loop transfer function of the D-channel current can be expressed as follows:

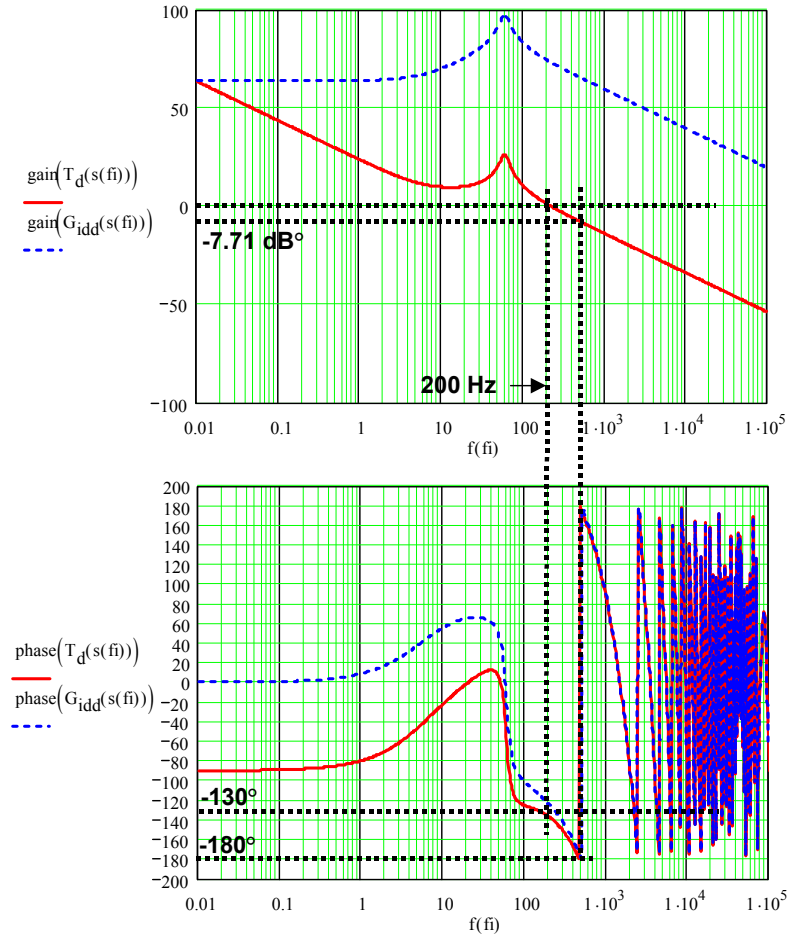
$$T_{id}(S) = H_{id}(S) \cdot G_{idd}(S).$$

**Equation 5-23**

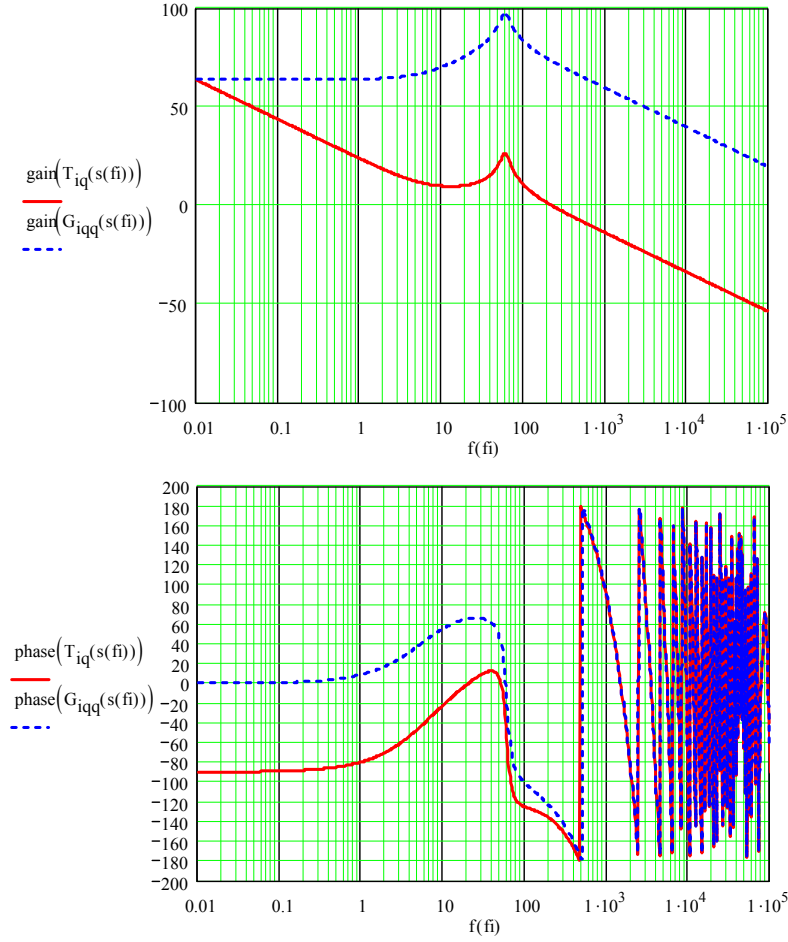
After the optimization process, the best-designed parameters for the PI compensator are given in Table 5-2. The current-loop gain is plotted, as shown in Figure 5-20, to verify its stability. The desired crossover is selected to be as high as possible, but must be less than 1 kHz, which is half of the effective switching frequency. Due to the severe switching delay, the designed crossover frequency is 200 Hz, with reasonably large phase margin of 50 degrees. The characteristics of current loop gain  $T_{id}(S)$  are listed in Table 5-2. Due to having a transfer function identical to that of the D-channel current, the Q-channel-current loop compensator  $H_{iq}(S)$  is designed, and its closed-loop magnitude and phase are plotted in Figure 5-21.

TABLE 5-2 DESIGNED PI COMPENSATOR PARAMETERS AND CURRENT LOOP GAIN CHARACTERISTICS.

Parameters		Values
<i>PI Compensator, <math>H_{id}(S)</math></i>		
	$K_p$	$2.12 \times 10^{-4}$
	$K_i$	$6.00 \times 10^{-3}$
<i>Loop Gain <math>T_{id}(S)</math> Characteristic</i>		
	Crossover Frequency (Hz)	200
	Phase Margin (degrees)	50
	Gain Margin (dB)	7.7



**Figure 5-20. Bode plots of the open-loop control-to-D-channel-current transfer function (dashed line) and the D-current loop gain (solid line).**



**Figure 5-21. Bode plots of the open-loop control-to-Q-channel-current transfer function (dashed line) and the Q-current loop gain (solid line).**

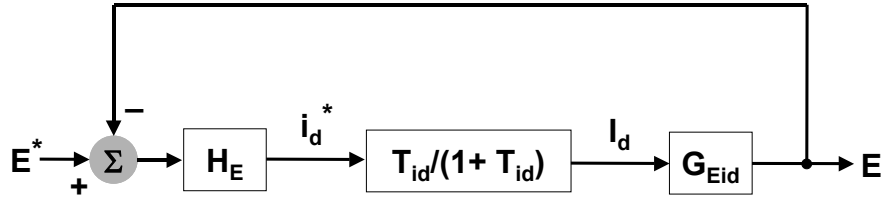
- **Design of DC Capacitor Voltage Compensator,  $H_{Ed}$**

With the D-channel current loop closed, the new transfer function, i.e., the reference current-to-DC-voltage transfer function,  $T_{Eid}(S)$ , is as follows:

$$T_{Eid}(S) = \frac{E}{i_d^*} = G_{Eid}(S) \cdot \frac{T_{id}(S)}{1 + T_{id}(S)},$$

**Equation 5-24**

where  $G_{Eid}(S)$  is open-loop output-current-to-DC-bus-voltage transfer function, and  $T_{id}(S)$  is the D-channel current-loop gain.



**Figure 5-22. Block diagram of the DC voltage loop.**

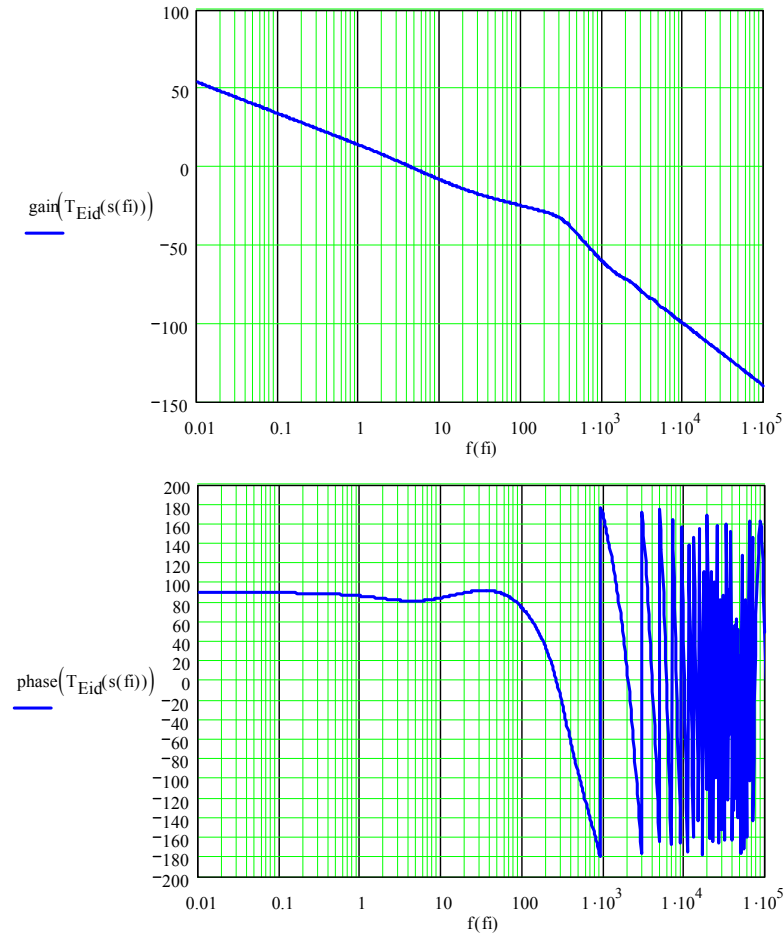
The Bode plot of transfer function  $T_{Eid}(S)$  is shown in Figure 5-23. A compensator is needed to improve the crossover frequency of  $T_{Eid}(S)$ , which is too low. Again, the PI compensator is capable of doing so. The D-channel voltage loop gain,  $T_{Ed}(S)$ , can be expressed as follows:

$$T_{Ed}(S) = H_{Ed}(S) \cdot T_{Eid}(S),$$

**Equation 5-25**

where  $H_{Ed}(S)$  is the PI compensator for the D-channel voltage loop.

The crossover frequency should be as high as possible; however, it needs to be limited at a frequency that is reasonably lower than the crossover frequency of the current-loop gain in order to avoid interferences between these two control loops. In this design, the crossover frequency of the voltage-loop gain is placed at 20 Hz, which is ten times lower than that of the current-loop gain. The corresponding phase margin is 157 degrees. This large phase margin is achieved due to relatively large capacitance of the DC capacitors. The compensated voltage-loop gain  $T_{Ed}(S)$  is plotted in Figure 5-24. In summary, the designed compensator parameters and characteristics of the DC voltage-loop gain are listed in Table 5-3.

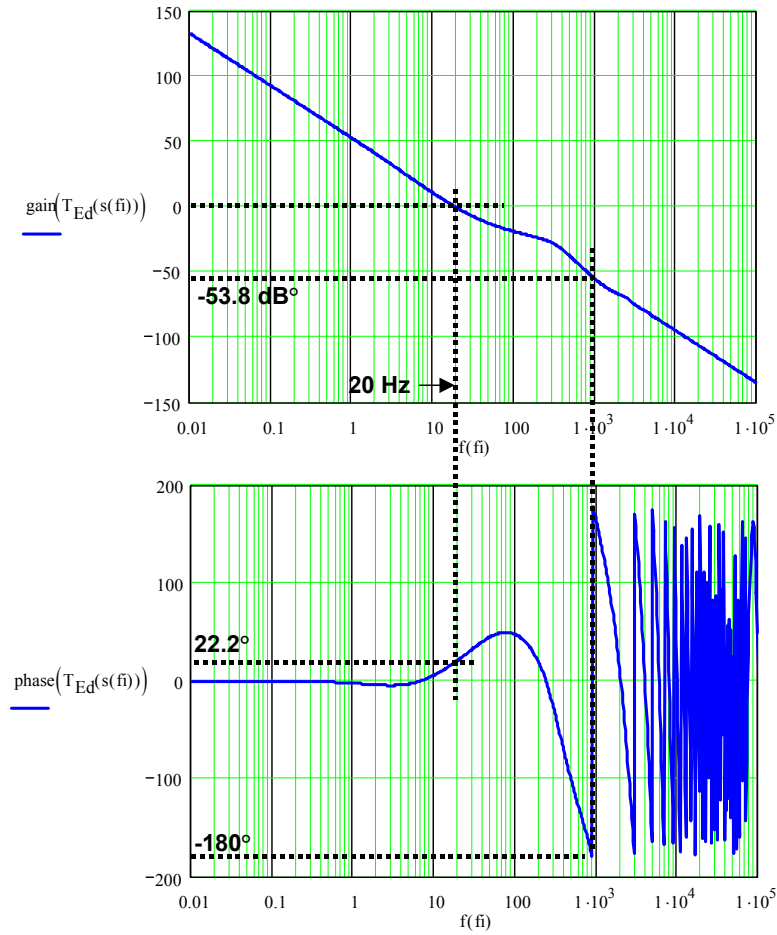


**Figure 5-23. Bode plot of the reference current-to-DC voltage transfer function,  $T_{Eid}(S)$ .**

**TABLE 5-3. DESIGNED PI COMPENSATOR PARAMETERS AND VOLTAGE-LOOP GAIN CHARACTERISTICS.**

Parameters		Values
<i>PI Compensator, <math>H_{Ed}(S)</math></i>		
	$K_p$	1.75
	$K_i$	550
<i>Loop Gain <math>T_{Ed}(S)</math> Characteristics</i>		
	Crossover Frequency (Hz)	20
	Phase Margin (degree)	158
	Gain Margin (dB)	53.8





**Figure 5-24. Bode plot of closed-loop D-channel voltage loop,  $T_{Ed}(S)$ .**

#### ***F. Simulation Results of the Average Model with the Designed Control***

To verify the stability and performance of the proposed control parameters, the average model of the three-level cascaded-based STATCOM with the designed feedback control is simulated. At the PCC, the power exchange between the STATCOM and the power network is defined, and is divided into the following three modes for the particular simulation:

1. standby mode is the mode in which the STATCOM generates zero real and reactive power ( $P = 0$  Watt and  $Q = 0$  Var),

2. inductive mode is the mode in which the STATCOM absorbs the reactive power from the power network (at full inductive mode,  $P = 0$  Watt and  $Q = -1.5$  MVar), and
3. capacitive mode is the mode in which the STATCOM injects the reactive power into the power network (at full capacitive mode,  $P = 0$  Watt and  $Q = +1.5$  MVar).

In this simulation, the STATCOM is commanded to operate in the following four modes:

1. at time 0 to 200 ms, the STATCOM operates in the standby mode,  $I_q = 0$  A,
2. at time 200 ms to 400 ms, the STATCOM operates in the full inductive mode,  $I_q = 2165$  A,
3. at time 400 ms to 600 ms, the STATCOM still operates in the inductive mode, except with a voltage sag at the PCC of 30% instead of the normal voltage, and
4. after 600 ms, the STATCOM operates in the full capacitive mode,  $I_q = -2165$  A.

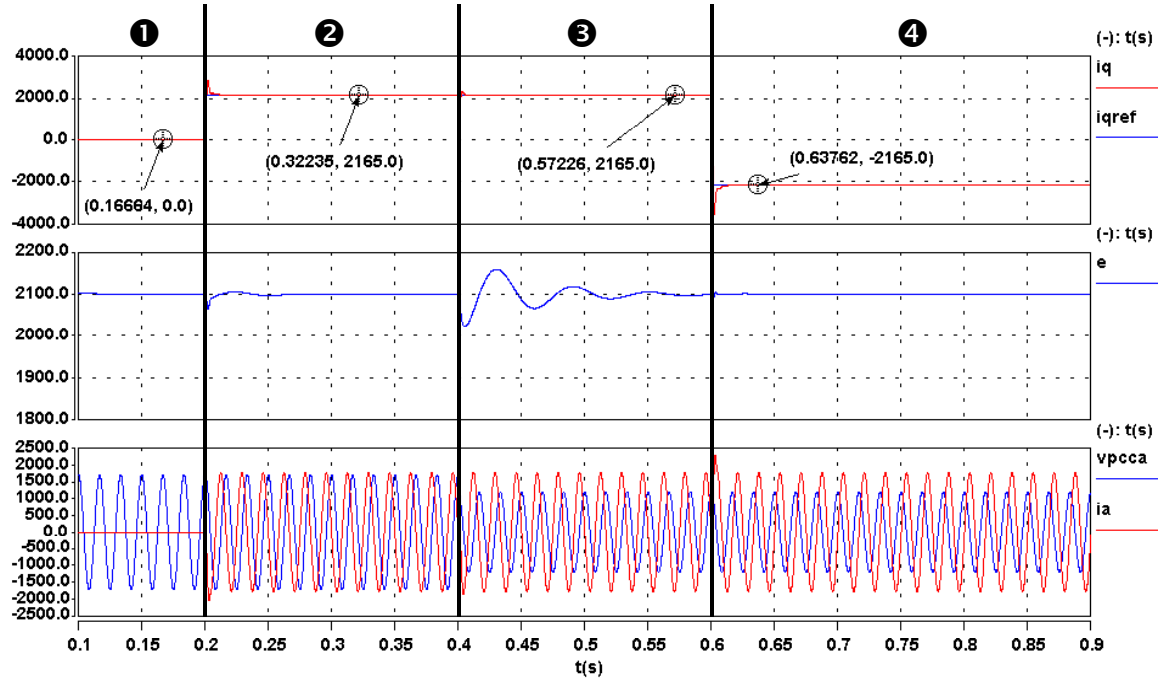
The command  $I_q$  at the full load is calculated from the full-load output current in the ABC coordinate. The relationship between the AC parameters in the DQ0 and ABC coordinates yields the following:

$$i_Q(t) = \sqrt{\frac{3}{2}} \cdot i_{A\_pk}(t),$$

**Equation 5-26**

where  $i_{A\_pk}(t)$  is the peak of the output-phase current.

Figure 5-25 shows the simulation results of the STATCOM operating in these four modes. The results indicate that the STATCOM stably operates for the entire range. The Q-channel output current closely follows the command. The average DC capacitor voltage is also regulated fairly well. At each transition period, the details of the simulation results are discussed and verified.



**Figure 5-25. Transient and steady-state responses of the proposed average model of three-level cascaded-based STATCOM with the designed feedback control operating in ❶ standby mode, ❷ full inductive mode, ❸ inductive mode under 30% voltage sag at the PCC and ❹ capacitive mode.**

- **Transition 1: from Mode 1 to Mode 2**

At time 200 ms, the STATCOM is commanded to abruptly change its operation mode from standby to full inductive mode by adjusting the  $I_q$  command from 0 to 2165 A. Due to the assigned current direction during the modeling procedure, the output current leads the  $V_{PCC}$  by  $90^\circ$  in the inductive mode and lags the  $V_{PCC}$  by  $90^\circ$  in the capacitive mode. In mode 2, the simulation result verifies that phase-A output current,  $i_a$ , leads  $V_{PCC}$  by  $90^\circ$ . The overshoot of  $I_q$  is 32%.

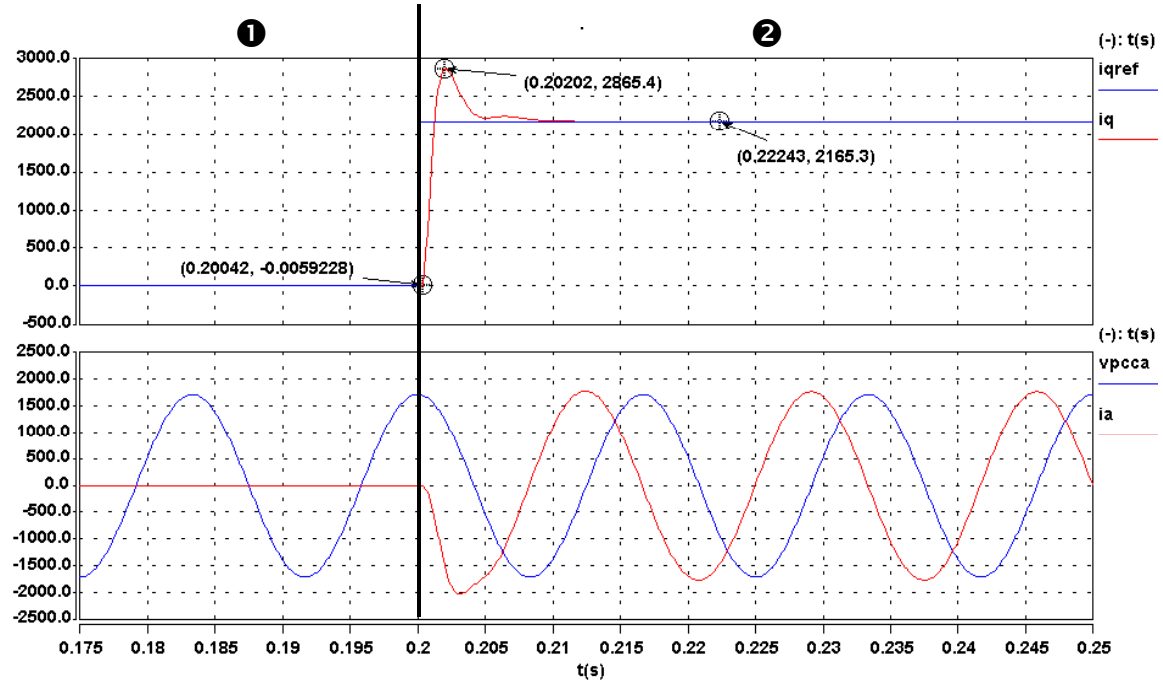
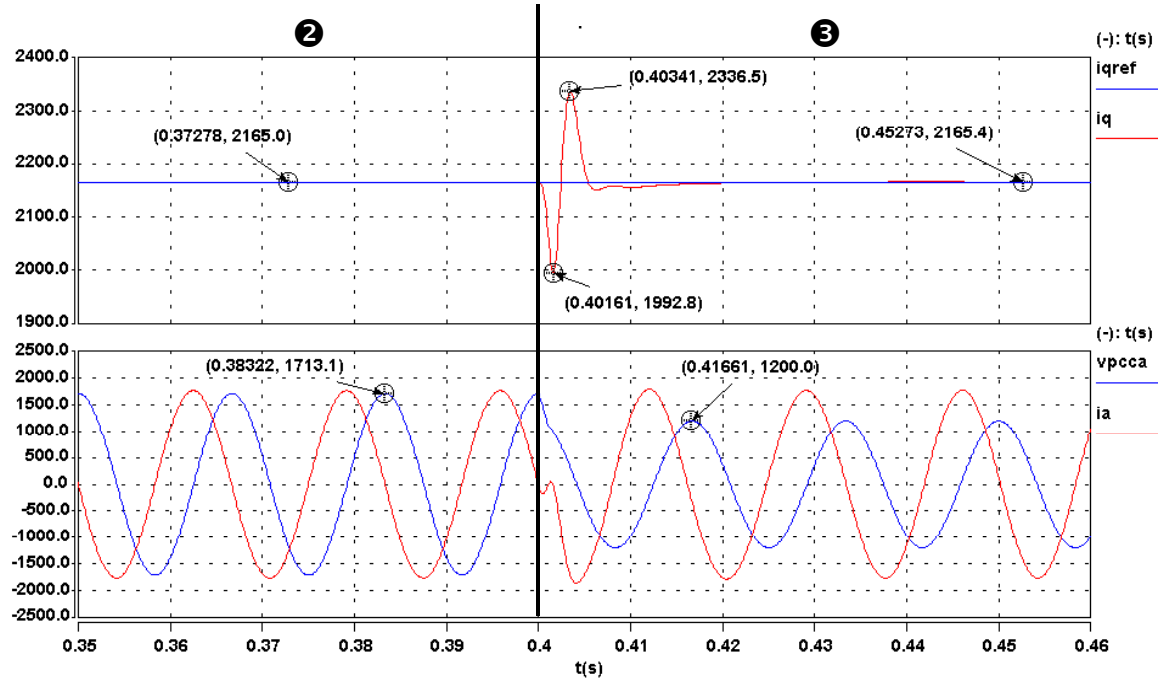


Figure 5-26. The STATCOM responds to the step change from standby mode (mode 1) to full inductive mode (mode 2) at 0.2 S.

- **Transition 2: from Mode 2 to Mode 3**

At this particular transient, while the STATCOM is commanded to absorb full reactive power from the power grid, at 400 ms, the three phase voltages at the PCC drop to 70% of the rated line-to-line voltage, which is 1470 V<sub>RMS</sub>. Figure 5-27 illustrates the simulated transient of the STATCOM. The command  $I_q$  is set at the full inductive mode for the entire transition. The current  $I_q$  very fast responds to the transient in the PCC voltage, and settles in the 5%-error range in 5 ms. The simulation results also show that the phase-A output current indicates the transient and goes to steady state very quickly.



**Figure 5-27. At 0.4 S, the STATCOM operates in full inductive mode (mode 2) and responds to the 30% sag in the voltage at the PCC (mode 3).**

- **Transition 3: from Mode 3 to Mode 4**

This transition is considered as the worst-case operation. Figure 5-28 shows the simulation results. The STATCOM is commanded to abruptly switch from absorbing full inductive current to generating full capacitive current. The current  $i_q$  follows its command with 32% overshoot, and settles down to the 5%-error command in less than 5 ms, which is about one-third of a line cycle. Since the same feedback parameters are used, the magnitude of the overshoot matches that in transition 1. In other words, no matter how much the step command is changed, the percentage of overshoot is always constant. The simulation result confirms this. Moreover, the phase-A output current leads the voltage  $V_{PCC}$  in mode 3 and lags  $V_{PCC}$  in mode 4; these are consistent with the STATCOM operating in the inductive and capacitive modes, respectively. Due to the switching delay introduced in the control system, phase lags are noticed in both  $i_q$  and  $i_a$ .

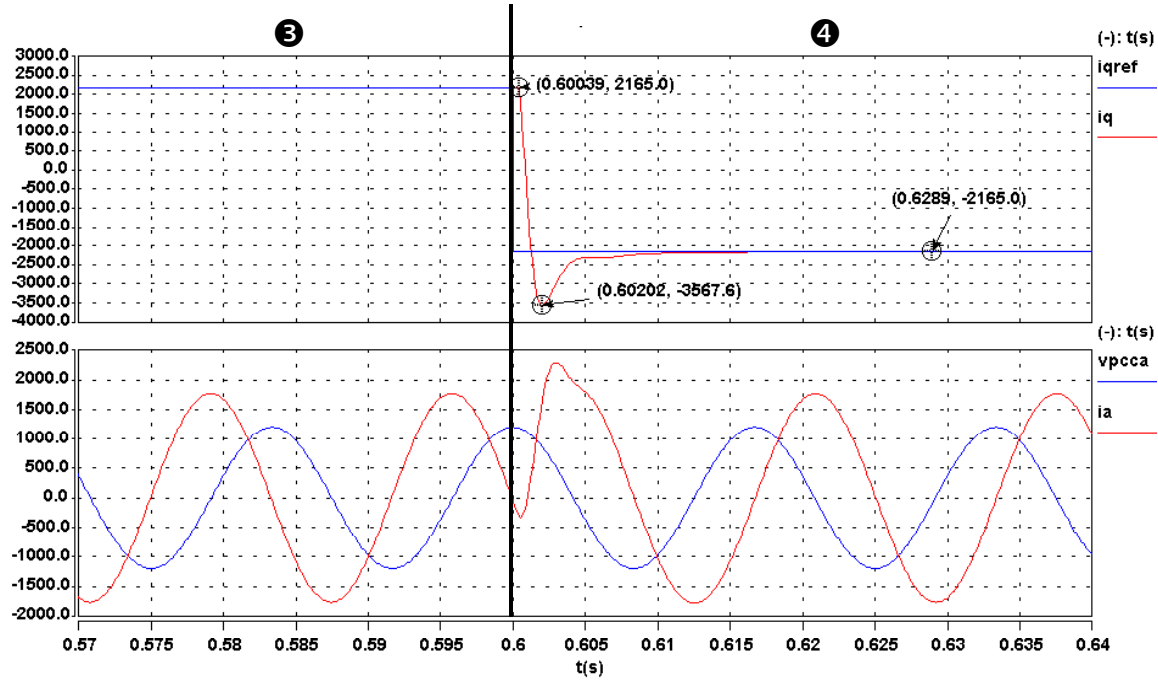


Figure 5-28. The STATCOM responds to the step change from full inductive mode (mode 3) to full capacitive current (mode 4).

### G. Proposed Control System for Three-level Cascaded-Based STATCOM

After being verified by the average model, the feedback-parameter acquisition must be modified before being applied in the real electrical circuit of the STATCOM in which all parameters are in the ABC coordinates. Figure 5-29 presents the completed block diagram of the proposed controller for the three-level cascaded-based STATCOM. Additions to the control designed for the average model of the three-level cascaded-based STATCOM are as follows: a Park's transformation, an inversed Park's transformation, a PWM generator and a phase lock loop (PLL). All feedback parameters are measured by using the signal transducers. Originally, these feedback signals are in ABC coordinates. With the proposed control technique, all signals are real-time transferred into DQ0 domain by Park's transformation matrix<sup>2</sup>. The PLL is the tool

<sup>2</sup> Derivation of the specific version of the Park's transformation matrix used in this dissertation is shown in Appendix A.

The diagram illustrates a control system for a three-phase PLL and current control. The inputs are Measurement Parameters:  $E_c, E_b, E_a$  (line voltages),  $i_a, i_b$  (line currents), and  $V_{pcca}, V_{pccb}, V_{pccc}$  (phase voltages). The PLL block outputs  $\cos(\theta)$  and  $\sin(\theta)$ . The current reference generator block takes  $E$  (average line voltage) and  $E_{ref}$  (reference voltage) as inputs and outputs  $i_{dref}$  and  $i_{qref}$ . The current control loops consist of two parallel paths: a d-axis path and a q-axis path. The d-axis path takes  $i_{dref}$  and  $i_d$  (d-axis current) as inputs and outputs  $d_d$ . The q-axis path takes  $i_{qref}$  and  $i_q$  (q-axis current) as inputs and outputs  $d_q$ . The d and q axes are transformed into the abc domain using a  $dqo$  and  $abc$  block, respectively, to produce the switching signals  $d_a, d_b, d_c$  for the Three-level SPWM stage.

The products of the feedback control are the duty cycles in the DQ0 coordinates:  $D_d$ ,  $D_q$  and  $D_0$ . Since the STATCOM is connected to the three-phase, three-wire power network, the zero channel can therefore be omitted. Consequently,  $D_0$  is set to zero. To be able to control the power stage of the STATCOM, the duty cycles must be transferred back into the ABC coordinates. Once the duty cycle in ABC coordinates, which are  $D_a$ ,  $D_b$  and  $D_c$ , are calculated, these three duty cycles are used as the input of the PWM generator in order to produce the proper switching signals for the power stage.

#### ***H. Simulation Results of the Cascaded Three-Level STATCOM with the Designed Controller***

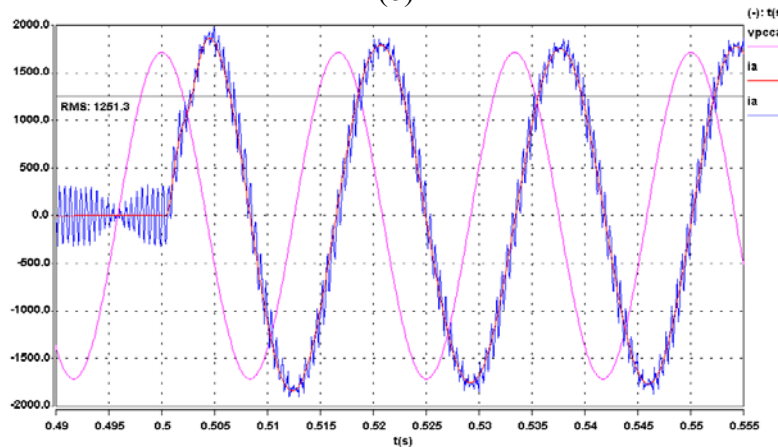
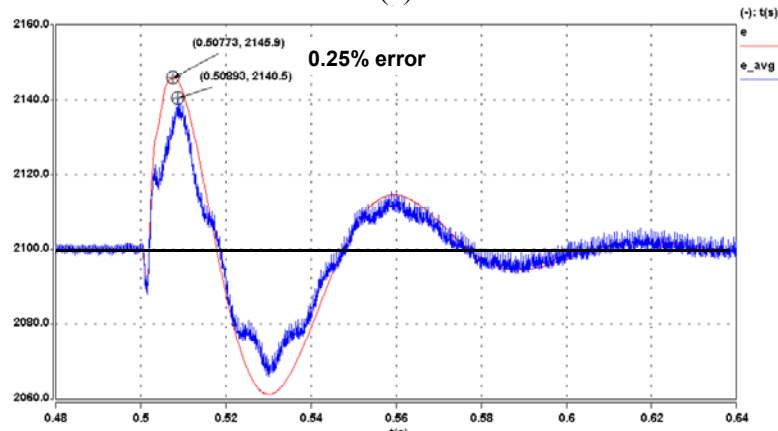
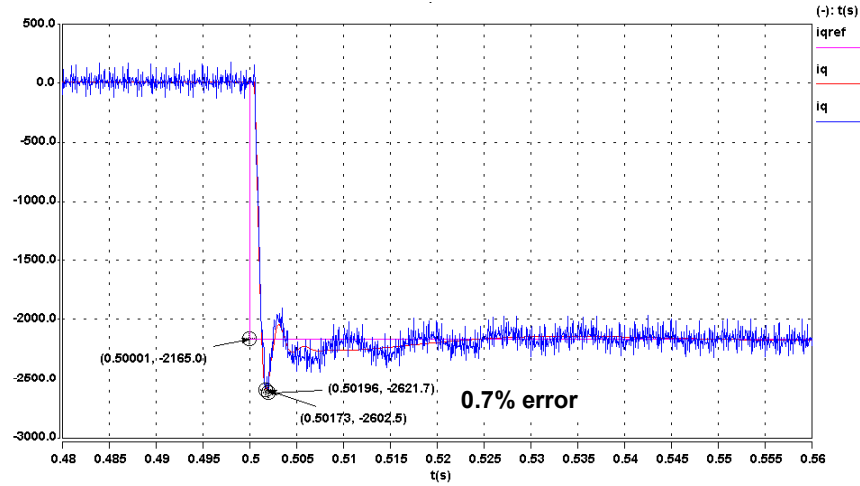
Based on the small-signal model of the three-level cascaded-based STATCOM, the feedback-control parameters are designed, as discussed in the feedback-control design section, and are applied in the completed electrical model of the proposed STATCOM in which the ideal switch and diode models are utilized. In addition, all parasitic components and power-stage losses are taken into account in the circuit.

- ***Comparison of Simulation Results of the Average and Electrical Models***

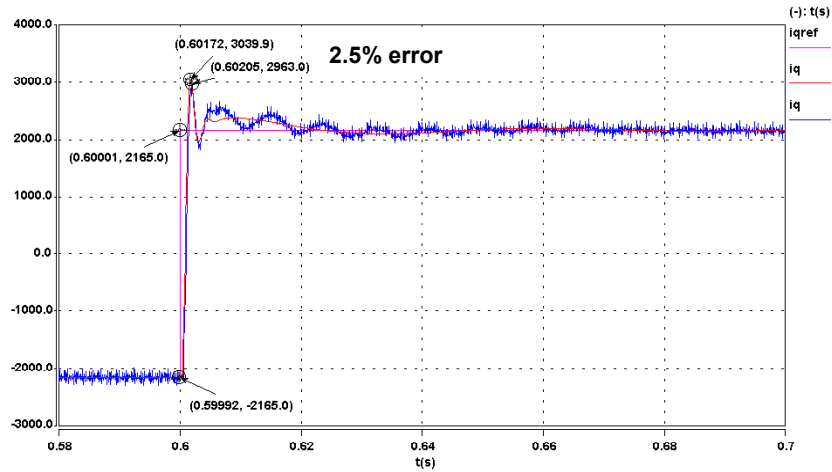
To verify the accuracy of the average model and the performance of the proposed control system, a set of simulations, which uses the STATCOM power electronics model as the reference, is performed. In the first simulation, the STATCOM is commanded to abruptly go from the standby mode to the full capacitive mode, and its simulation results are shown in Figure 5-30. Three major parameters are compared between the results from the average model and those from the electrical model: the Q-channel output current,  $I_q$ , the average DC capacitor voltage,  $e_{avg}$ , and the output current of phase A,  $I_a$ . Due to the switching action in the electrical model, the switching ripple appears in the simulation results.

In this case, the insignificant errors of the overshoot in  $I_q$  and  $e_{avg}$  are 0.7% and 0.25%, respectively. In Figure 5-30(c), the results show that by neglecting the switching ripple, the dynamic response of the phase-A output current can be very well represented by that of the average output current of phase A.

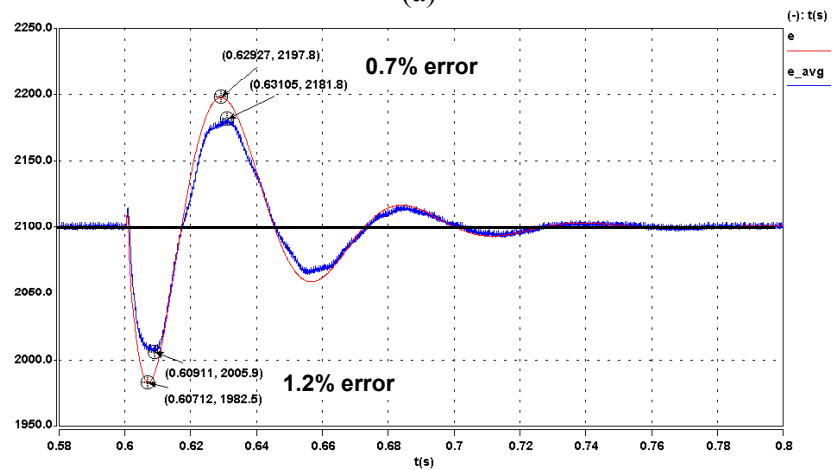




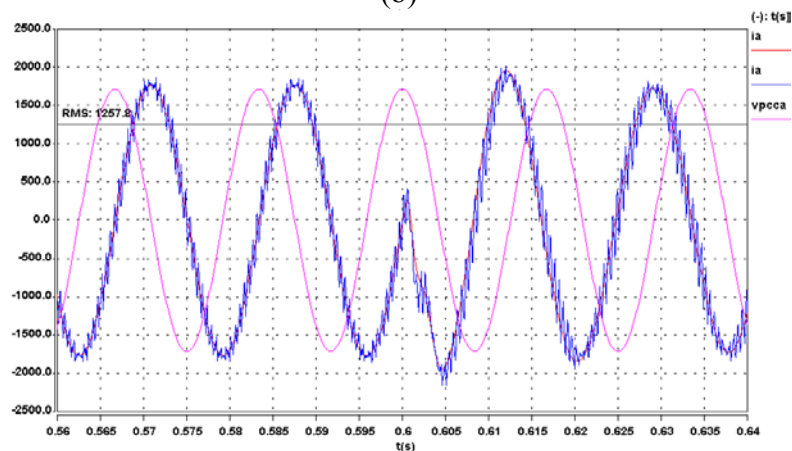
**Figure 5-30. Comparison between average model and electrical model of the STATCOM operating in the standby to full inductive modes: (a)  $I_q$  responses, (b) average DC capacitor voltages, and (c) output currents.**



(a)



(b)



(c)

**Figure 5-31. Comparison between average model and electrical model of the STATCOM operating in the full capacitive to full inductive modes: (a)  $I_q$  responses, (b) average DC capacitor voltages, and (c) output currents.**

The second simulation is for the worst-case operation in which the STATCOM is controlled to respond to the step command from full capacitive to full inductive modes. The simulation results are shown in Figure 5-31. In this case, the error of the overshoot in of  $I_q$  and  $e_{avg}$  are 2.5% and 1.2%, respectively. Again, the results show that, by neglecting the switching ripple, the dynamic response of the phase-A output current can be predicted by that of the average output current of phase A.

In conclusion, the results indicate that the proposed average model is very accurate and can very closely predict the dynamic behaviors of the three-level cascaded-based STATCOM.

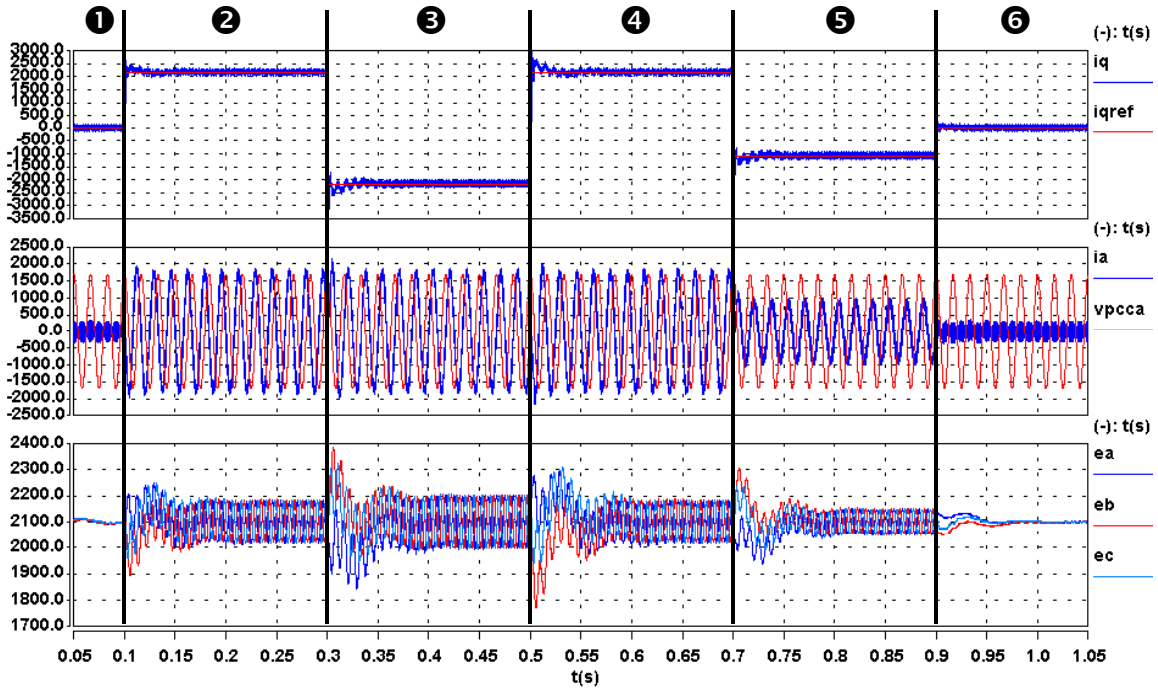
- ***Simulation Results of the Electrical Model with the Proposed Controller***

To further verify the stability and performance of the proposed STATCOM controller, more continuous operation modes are simulated. The STATCOM is commanded to operate in the following six modes:

1. at time 0 to 100 ms, the STATCOM operates in the standby mode,  $I_q = 0$  A, and  $I_a = 0$  A<sub>RMS</sub>,
2. at time 100 ms to 300 ms, the STATCOM operates in the full inductive mode,  $I_q = +2165$  A, and  $I_a = -1250$  A<sub>RMS</sub>,
3. at time 300 ms to 500 ms, the STATCOM operates in the full capacitive mode,  $I_q = -2165$  A and  $I_a = +1250$  A<sub>RMS</sub>,
4. at time 500 ms to 700 ms, the STATCOM again operates in the full inductive mode,  $I_q = +2165$  A, and  $I_a = -1250$  A<sub>RMS</sub>,
5. at time 700 ms to 900 ms, the STATCOM operates in the half inductive mode,  $I_q = +1083$  A, and  $I_a = -625$  A<sub>RMS</sub>, and
6. after 900 ms, the STATCOM finally returns to the standby mode.

The simulation results of the STATCOM operating in these six modes are illustrated in Figure 5-32. As shown, the STATCOM stably operates for the entire range. In general, the Q-channel output current,  $i_q$ , very closely follows its command. The average DC voltage is also

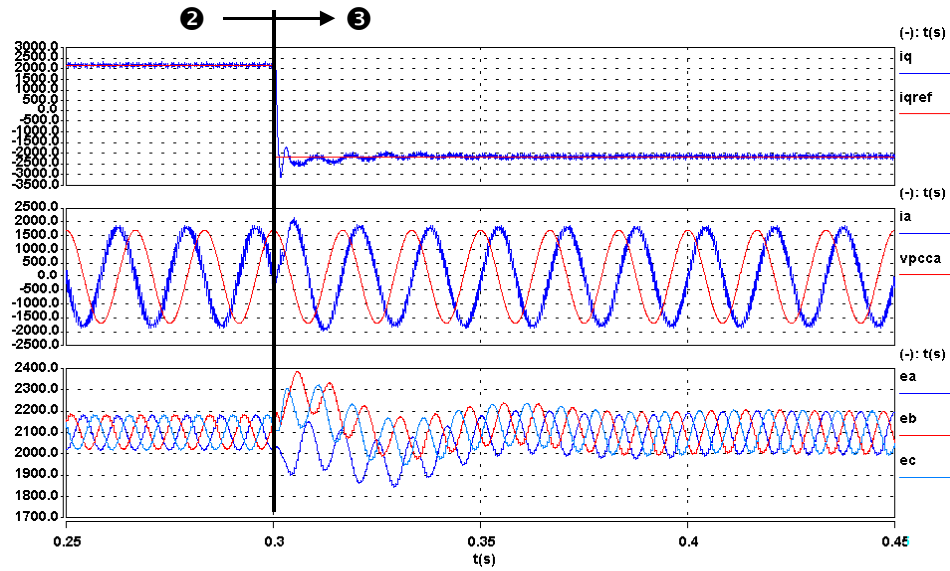
regulated fairly well. Five interesting transitions occur in this simulation. Detailed simulation results are discussed and verified.



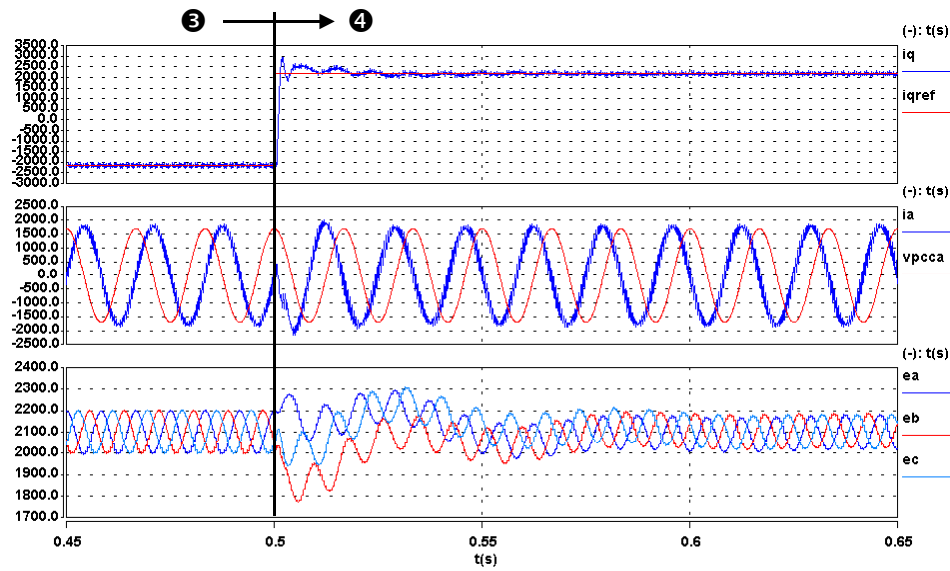
**Figure 5-32. Transient and steady-state responses of the three-level cascaded-based STATCOM with the proposed feedback controller, operating in ① standby mode, ② full inductive mode, ③ full capacitive mode, ④ full inductive mode, ⑤ half capacitive mode and ⑥ standby mode.**

The detail of the transition from modes 2 to 3 is shown in Figure 5-33(a). The STATCOM operation transfers from the full inductive to the full capacitive modes. The current  $i_q$  very quickly follows the command. The current  $i_a$  simultaneously transfer from  $90^\circ$  leading to  $90^\circ$  lagging  $V_{pcc}$  in less than half a line cycle. The results also show that all three DC capacitor voltages are very well regulated during the transient and steady states. The detail of the STATCOM response to the command to go from full capacitive to full inductive modes is

illustrated in Figure 5-34(b). From the simulation results, the voltage ripple of the DC capacitor in the inductive mode is slightly less than that of the capacitive mode due to the different amount of average current flowing into the DC capacitor. As mentioned in the converter modeling process, the capacitor current is a product of the output current and the duty cycle of the converter. Basically, the duty cycle in the inductive mode is less than that in the standby mode, whereas the duty cycle in the capacitive mode is greater than that in the standby mode. In other words, the duty cycle of the converter during the inductive mode is always less than that in the capacitive mode. As a result, with the same amount of output current, the average amount of the DC capacitor current during the inductive mode is always less than that of the capacitive mode. Therefore, the capacitor needs to be designed to handle the worst-case voltage ripple, which occurs when the STATCOM operates in the capacitive mode.

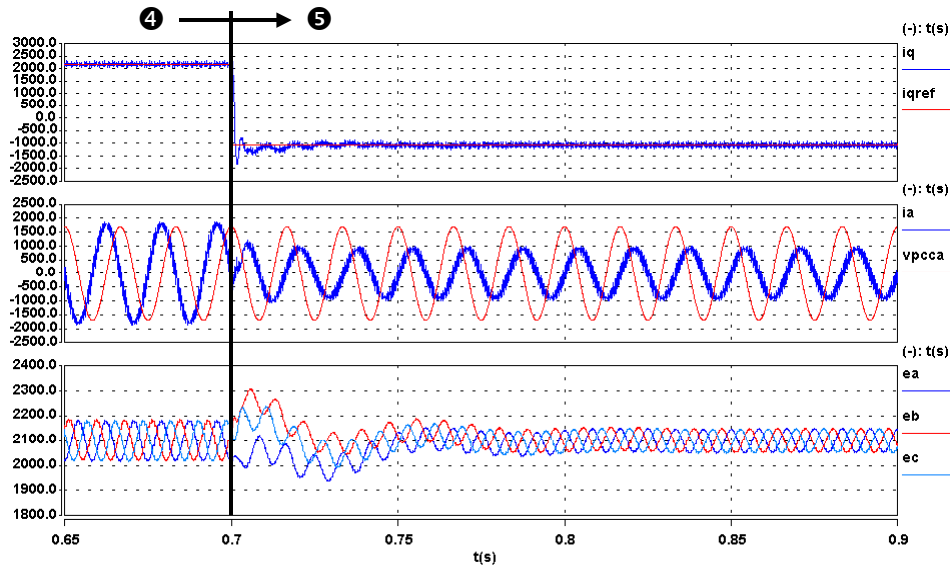


(a)

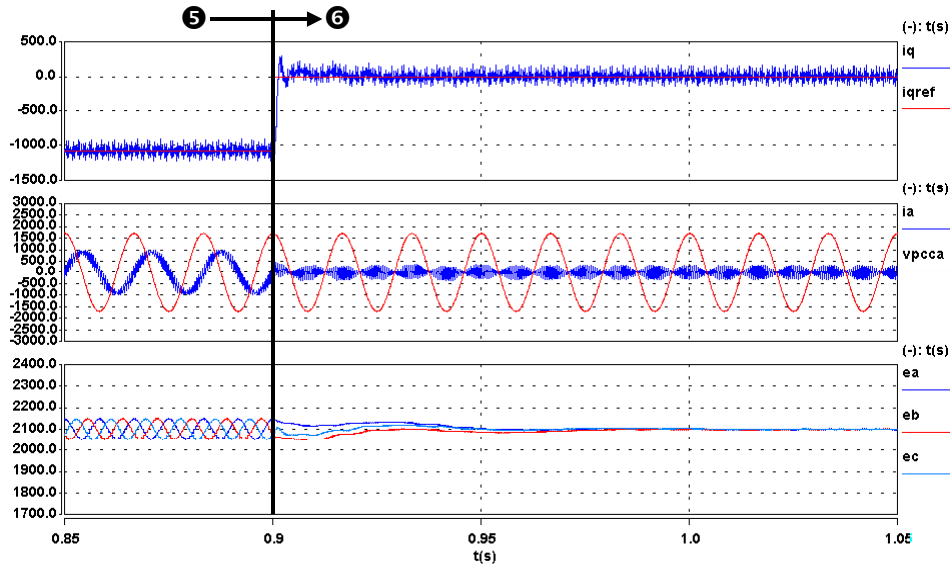


(b)

**Figure 5-33. The STATCOM responds to the step change (a) from full inductive mode (mode 2) to full capacitive mode (mode 3) at 0.3 S, and (b) from full capacitive mode (mode 3) to full inductive mode (mode 4) at 0.5 S.**



(a)



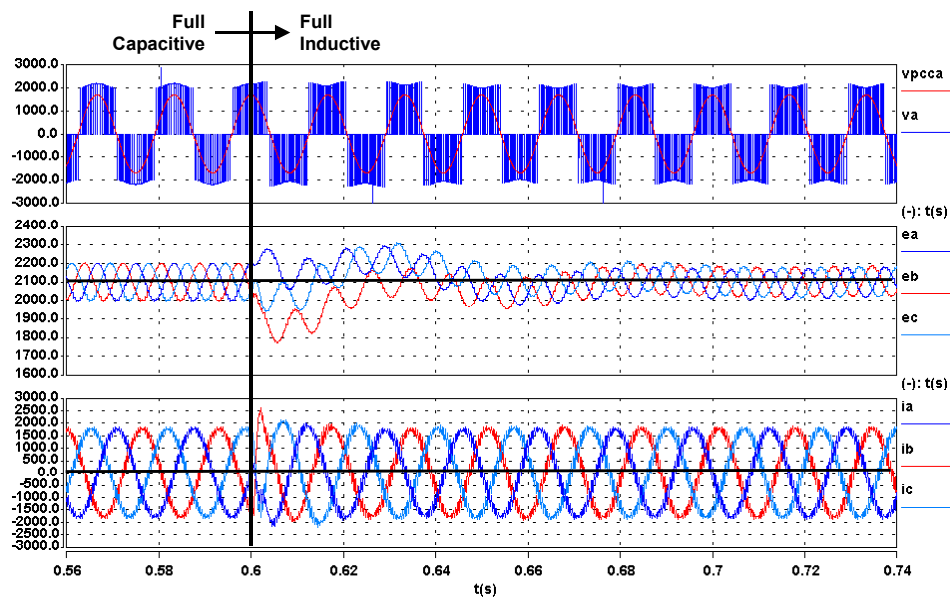
(b)

**Figure 5-34. The STATCOM responds to the step change (a) from full inductive mode (mode 4) to half capacitive mode (mode 5) at 0.7 S, and (b) from half capacitive mode (mode 5) to standby mode (mode 5) at 0.9 S.**

At 0.7 s, the STATCOM is commanded to generate a half-rated reactive current in mode 5 following mode 4. The simulation results for this transition are shown in Figure 5-34(a). The

current is decreased from full to half rating following the command. All three capacitor voltages go to the steady state in about 0.2 s. The last transition at 0.9 s is shown in Figure 5-34(b). The STATCOM is finally commanded to go back to the standby mode in which it exchanges no power with the power network. The average STATCOM output current becomes zero, although the switching ripple in the current still exists. The three capacitor voltages go back to the reference with no ripple, which indicates that there is no reactive power circulating in the capacitors.

Figure 5-35 shows voltage and current waveforms for a transient period of the STATCOM transferring from full capacitive to full inductive modes. The phase-A output voltage of the STATCOM is almost always in phase with the voltage at the PCC. A small phase shift is, however, applied when the capacitor voltages need to be adjusted. In addition, the results verify that all three capacitor voltages and three output currents are very well regulated. According to the control design criteria, the response of the DC-voltage loop is about 10 times slower than that of the output-current loops. As a result, the DC capacitor voltages go to the steady state approximately 10 times later than the output currents do.



**Figure 5-35. Waveforms of the STATCOM system transitioning from the full capacitive to full inductive modes.**



## I. Experimental Validation

To firmly verify the proposed STATCOM model and feedback controller, a real-time IGBT-based STATCOM testbed<sup>3</sup> is implemented. The STATCOM testbed is basically composed of three parts: the IGBT-based CMC, the DSP-based controller, and the passive components. The schematic of the testbed is shown in Figure 5-36. The reactive current command is fed into the controller through the user interface. The feedback parameters are measured by the analog transducers, and are converted to digital domain by the ADCs. The feedback-control routine is coded and downloaded to the program memory of the DSP.

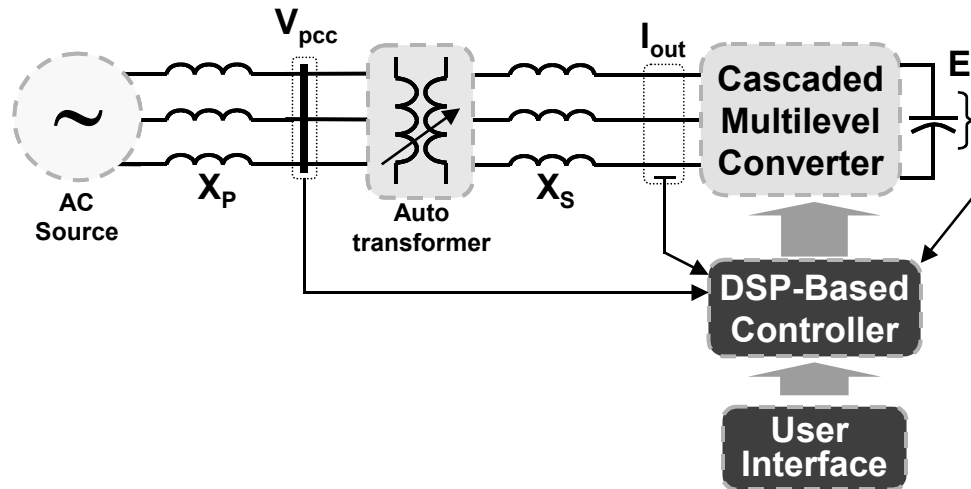


Figure 5-36. The schematic of the STATCOM testbed.

### • Testbed Power Stage Operating Parameters

The operating point of the testbed is selected based on the limitation of the laboratory facilities. The main switching device is the IGBT in which a freewheeling diode is internally connected in parallel. To properly verify the proposed models, the constraints of the testbed

<sup>3</sup> Details of the STATCOM testbed are given in Appendix B.

power stage are kept identical to those of the high-power system. Those parameters are as follows:

1. the switching frequency,
2. the dead-time, and
3. the percentage of the DC capacitor voltage ripple.

Table 5-4 shows the final parameters of the testbed operating point. The three-phase AC input voltages are transformed from 208 V to 100 V by the autotransformer. The switching frequency is kept at 1 kHz. The DC capacitor voltage ripple at the full capacitive load is 10%. The coupling reactor impedance is the combination of the leakage inductance of the autotransformer and the additional inductors.

TABLE 5-4. SPECIFICATIONS OF THE TESTBED AT THE OPERATING POINT.

<b>Three-Level Cascaded Converter</b>	
Individual DC Bus Voltage	100 V $\pm$ 10%
Total DC Bus Voltage	100 V $\pm$ 10%
Rated RMS Reactive Current	10 A
Capacitor Impedance	$(0.5\text{m-j}/(\omega \cdot 2.0\text{mF})) \Omega/\text{Phase}$
Individual Switching Frequency/ Equivalent Switching Frequency	1 kHz/ 2 kHz
<b>Power System</b>	
Configuration	Balanced Three-Phase Three-Wire
Coupling Reactor Impedance	$(72\text{m-j}\omega \cdot 2.0\text{mH}) \Omega/\text{Phase}$
PCC Line Voltage	100 V

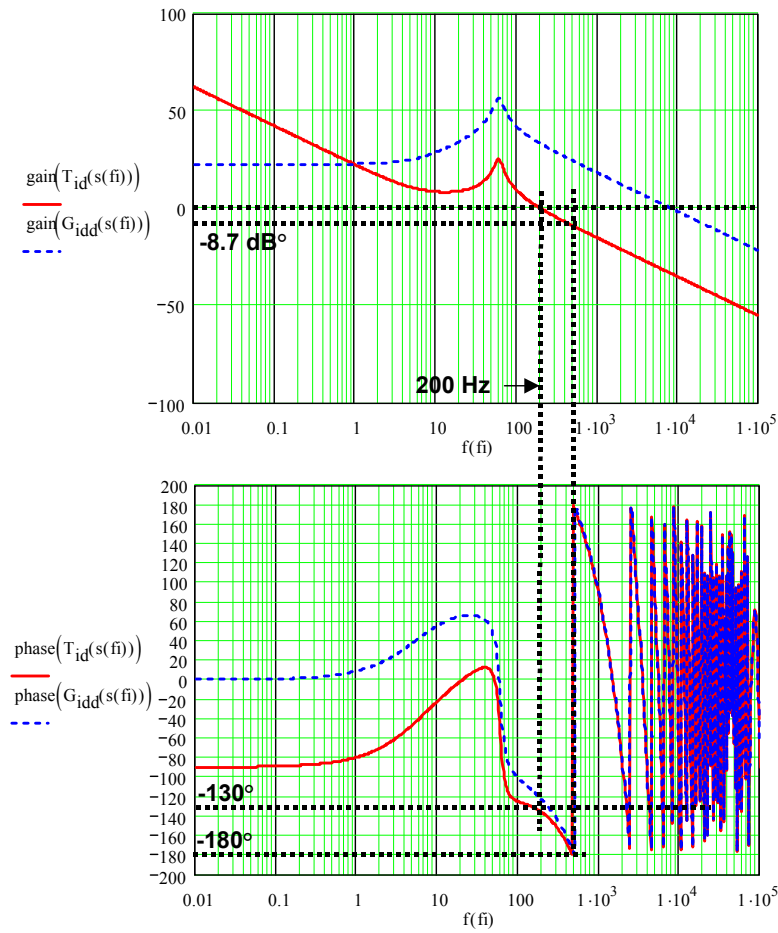
- ***Control System Parameters***

Besides the same constraint of the power stage, the control parameters are also designed in such a way that the same bandwidths and phase margins are achieved for both the current and the voltage loops. As a result, the percentages of the testbed responses are identical to those in the high-voltage STATCOM system. Based on the same approach used in the simulation, the designed control parameters for the testbed at the proposed operating point are given in Table 5-5.

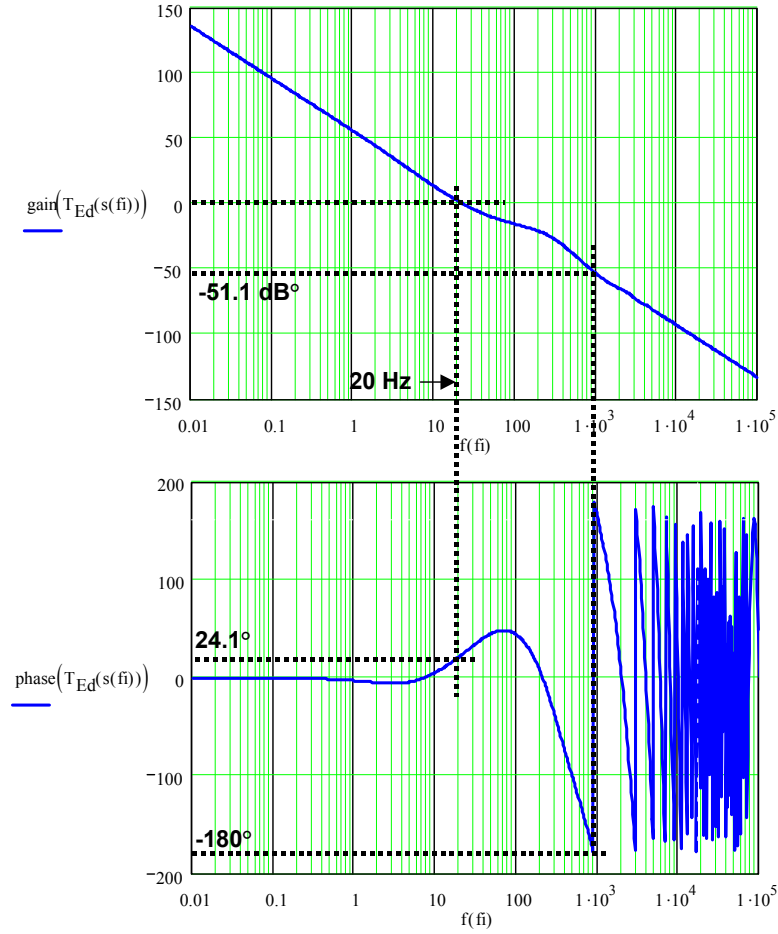
TABLE 5-5. DESIGNED PI COMPENSATOR PARAMETERS AND CURRENT AND VOLTAGE-LOOP GAINS CHARACTERISTICS OF THE TESTBED.

Parameters	Values
Current Loop	
<i>PI Compensator, <math>H_{id}(S)</math></i>	
$K_p$	0.021
$K_i$	6.0
<i>Loop-Gain <math>T_{id}(S)</math> Characteristics</i>	
Crossover Frequency (Hz)	200
Phase Margin (Degrees)	50
Gain Margin (dB)	8.7
Voltage Loop	
<i>PI Compensator, <math>H_{Ed}(S)</math></i>	
$K_p$	0.477
$K_i$	150
<i>Loop-Gain <math>T_{Ed}(S)</math> Characteristics</i>	
Crossover Frequency (Hz)	20
Phase Margin (Degrees)	156
Gain Margin (dB)	51.1

To verify the designed loop-gain characteristics shown in Table 5-5, the Bode plots of both current and voltage loop gains are illustrated in Figure 5-37 and Figure 5-38, respectively. The crossover frequency of the current loop is designed at 200 Hz, with a phase margin of 50°, while that of the voltage loop is at 20 Hz, with a phase margin of 156°.



**Figure 5-37. Bode plots of the open-loop control-to-D-channel-current transfer function (dashed line) and the D-current loop gain (solid line) of the testbed at the operating point.**



**Figure 5-38. Bode plot of the reference current-to-DC voltage transfer function,  $T_{Ed}(S)$ .**

- **Experimental Results**

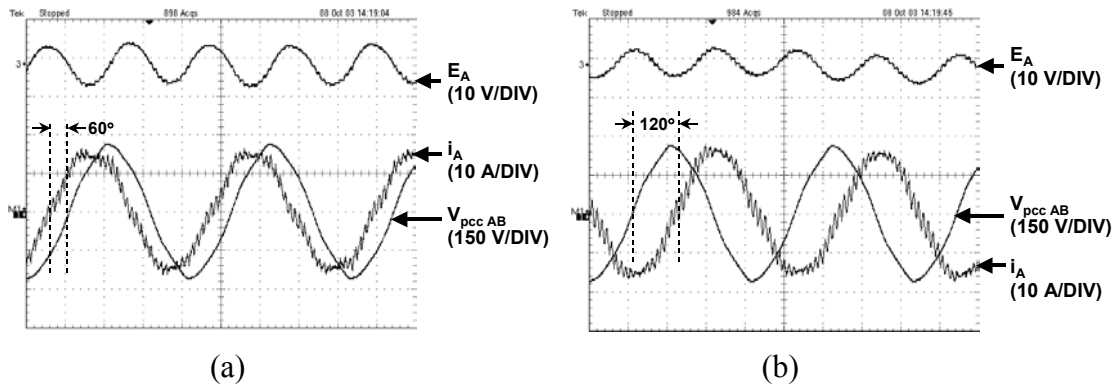
The proposed feedback routine is digitally coded and downloaded to the program memory of the DSP. The testbed system, as shown in Figure 5-36 is set up. Several experiments are conducted.

— **Steady-State Compensation**

The experimental results of the steady-state compensation in both capacitive and inductive modes are shown in Figure 5-39(a) and (b), respectively. To show the capacitor and inductor characteristics of the STATCOM, the direction of the STATCOM current in these experimental

results is from the power network to the STATCOM, which is opposite to that in the simulation. From Figure 5-39(a), the 10%, 120Hz ripple is noticed on top of the DC capacitor voltage,  $E_A$ . Again, to minimize the DC capacitance, an expectable voltage ripple must be allowed. The output current of phase A,  $i_A$ , leads the line voltage  $V_{pcc\ AB}$  by  $60^\circ$ . In other words, the phase-A voltage at the PCC lags the current  $i_A$  by  $90^\circ$ , which is consistent with the simulation results.

In the inductive mode, as shown in Figure 5-39(b), the current  $i_A$  lags the line voltage  $V_{pcc\ AB}$  by  $120^\circ$ , which agrees with the simulation results. As explained in the simulation results, the experimental results indicate that the voltage ripple of the DC capacitor in the inductive mode is less than that in the capacitive mode.



**Figure 5-39. Steady-state compensations in: (a) full-capacitive mode and (b) full-inductive mode.**

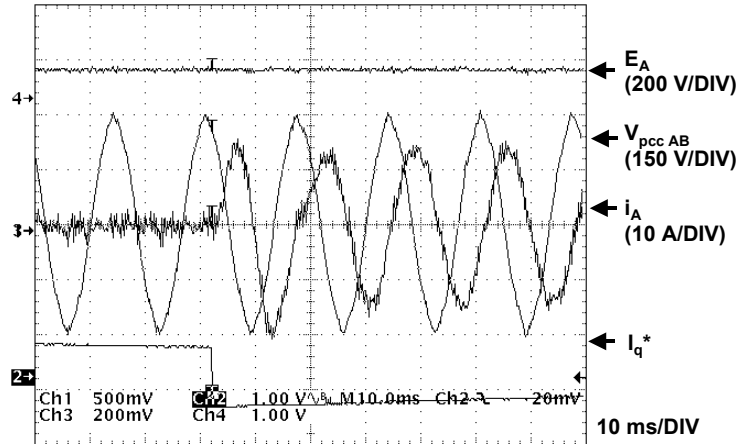
#### — *Transition from Standby to Full Capacitive Modes*

The experimental results of the STATCOM responding to the step command from standby to full capacitive mode is shown in Figure 5-40. The DC capacitor voltage,  $E_A$ , is very well regulated during the transient. After the transient, as shown in Figure 5-40(a), the current  $i_A$  lags the line voltage  $V_{pcc\ AB}$  by  $120^\circ$ . In other words, the phase-A voltage at the PCC leads the current  $i_A$  by  $90^\circ$ , which is consistent with the simulation results. In Figure 5-40(b), the DC

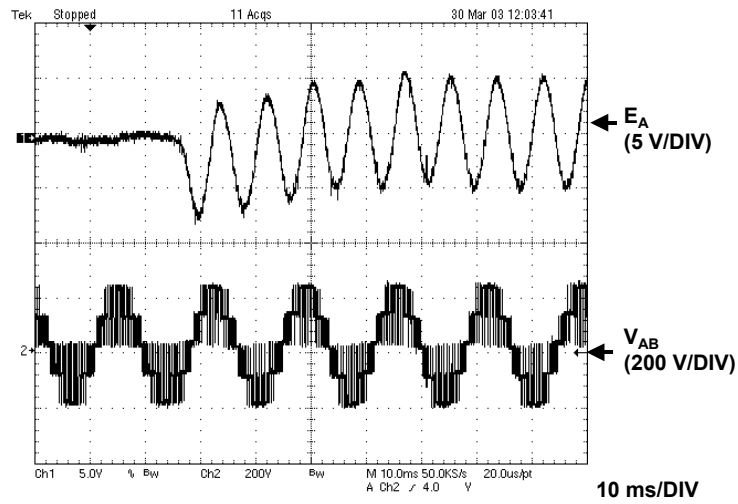
voltage  $E_A$  is shown in detail. The peak-to-peak ripple voltage is about 10 V, which is 10% of the DC voltage setting of 100 V.

— *Transition from Full Capacitive to Full Inductive Mode and Vice Versa*

The simulation results, as illustrated in Figure 5-41, validate the stability and the performance of the proposed control system reacting to the worst-case commands. The STATCOM is commanded to go from full capacitive to full inductive modes and vice versa, as shown in Figure 5-41(a) and (b), respectively. The voltage  $E_A$  is very finely regulated during both transitions and steady states. The output current  $i_A$  responds very quickly to the step command, and goes smoothly to the steady state.



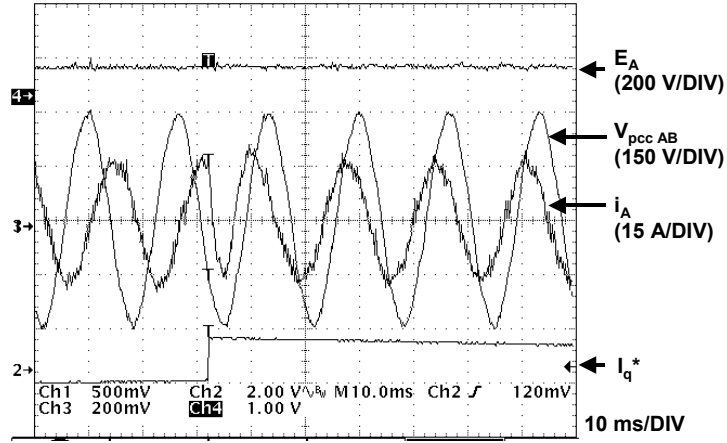
(a)



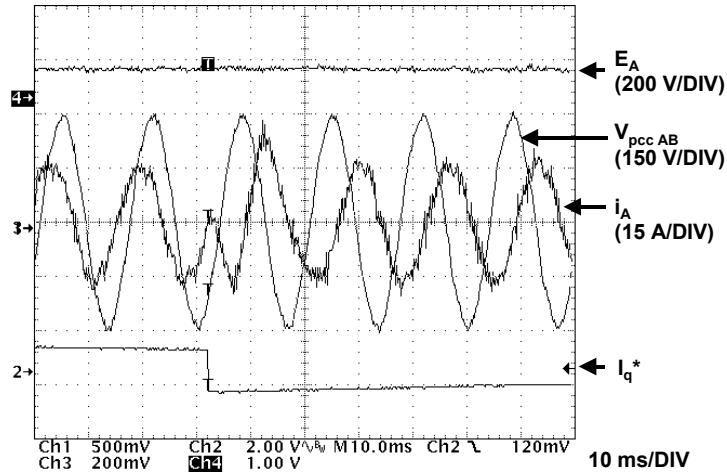
(b)

**Figure 5-40. Experimental results of the testbed responding to a step command from standby to full capacitive mode: (a) DC capacitor voltage of phase A ( $E_A$ ), the voltage at the PCC between phases A and B ( $V_{pcc AB}$ ), phase A output current ( $i_A$ ) and the reactive current command ( $I_q^*$ ) and (b) the detail of  $E_A$  and the output line-to-line voltage of the cascaded three-level converter ( $V_{AB}$ ).**





(a)

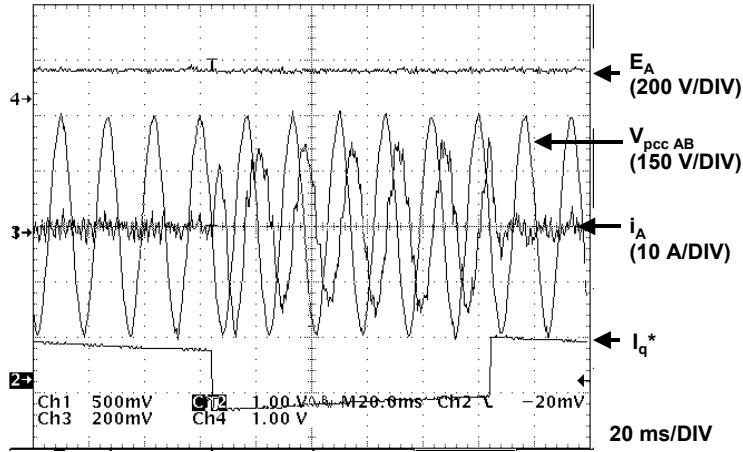


(b)

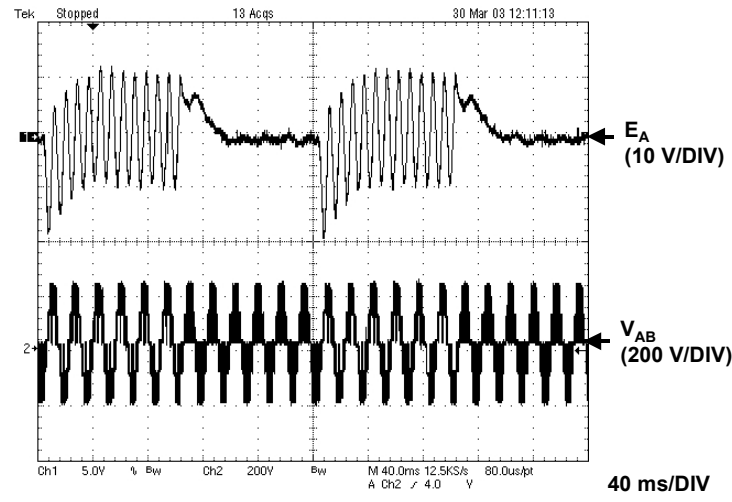
**Figure 5-41.** The experimental results of the DC capacitor voltage of phase A ( $E_A$ ), the voltage at the PCC between phases A and B ( $V_{pcc\ AB}$ ), phase A output current ( $i_A$ ) and the reactive current command ( $I_q^*$ ) of the testbed responding to a step command: (a) from full capacitive to full inductive mode and (b) from full capacitive to full inductive mode.

— *Periodic Transition from Standby Mode to full capacitive Mode and Vice Versa*

In this experiment, the STATCOM is commanded to generate the pulsating reactive power, which is generally required in the flicker-mitigation applications. The frequency of the pulsating power is set at 5 Hz. As shown in Figure 5-42(a), the STATCOM injects the full capacitive current for 100 ms and no current for another 100 ms. The capacitor voltage,  $E_A$ , is kept constant by the feedback voltage loop. Figure 5-42(b) illustrates the detail of the DC capacitor voltage and the output voltage of the converter. The 10% voltage ripple of voltage  $E_A$  can be noticed during the full capacitive compensation. From full capacitive to standby mode, voltage  $E_A$  goes back to the setting value. Due to the lack of compensated current, there is no ripple across the capacitor during the standby mode.



(a)



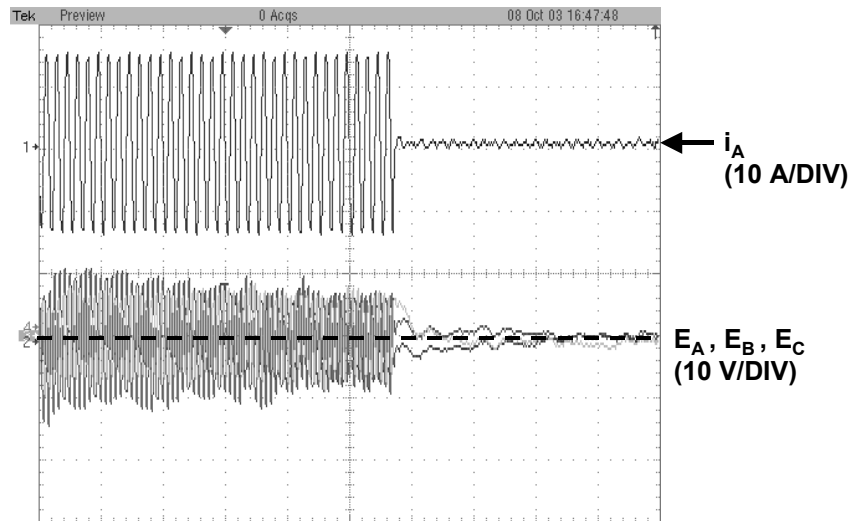
(b)

**Figure 5-42. The STATCOM generates pulsating reactive power: (a) the DC capacitor voltage of phase A ( $E_A$ ), the voltage at the PCC between phases A and B ( $V_{pcc AB}$ ), phase A output current ( $i_A$ ) and the reactive current command ( $I_q^*$ ) and (b) the details of  $E_A$  and the converter output voltage ( $V_{AB}$ ).**

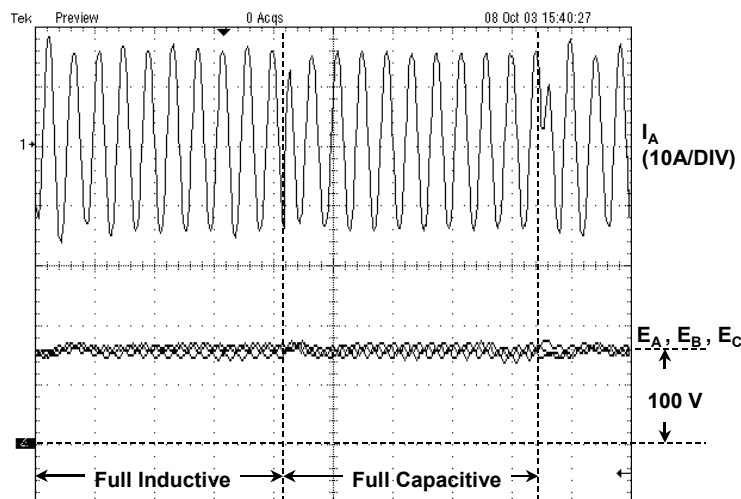
#### — Convergence of Three DC Capacitor Voltages, $E_A$ , $E_B$ and $E_C$

This experiment is to verify the convergence of all three DC capacitor voltages,  $E_A$ ,  $E_B$  and  $E_C$ . The experimental results, as shown in Figure 5-43, demonstrate that during both full

capacitive and standby modes, all three DC capacitor voltages are well regulated and converge to the reference, which is 100 V in this case. Moreover, the extreme case is shown in Figure 5-44, in which the STATCOM periodically operates between full capacitive and full inductive modes. Again, all three DC capacitors are well regulated and converge to the reference.



**Figure 5-43.** The STATCOM goes from full capacitive to standby mode.



**Figure 5-44.** The STATCOM goes from full capacitive to full inductive mode and vice versa.

## ***J. Summary***

Based on the assumption of the effective DC voltage-balancing technique, the accuracy of the proposed model of the CMC-based STATCOM was initially validated by both simulation and experimental results obtained by the STATCOM utilizing the cascaded three-level converter. The experimental results are consistent with the simulation results.

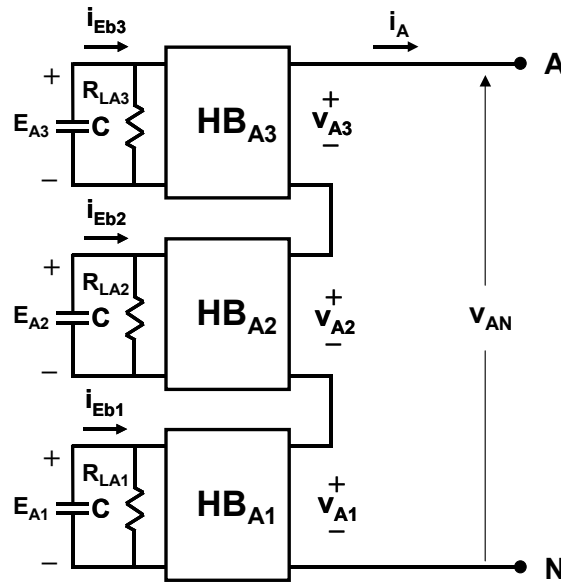
In the high-voltage STATCOM system, due to the limitation of the recent power semiconductor device technology, a higher number of voltage levels is required in the CMC topology. Besides improving the voltage capability, several other advantages can be achieved by utilizing the CMC in STATCOM applications. With the knowledge acquired from the cascaded three-level converter results, the performance of the STATCOM system can be greatly improved by the following factors: higher switching frequency, faster dynamic responses, better output-waveform quality, and better redundancy and stability. However, it is not possible to achieve these advantages in the CMC-based STATCOM, unless an effective voltage-balancing technique is applied to its DC capacitor voltages.

## **III. DC Capacitor Voltage-Balance Control Approaches**

### ***A. Imbalance of DC Capacitor Voltages in the Cascaded-Multilevel Converter-Based STATCOM***

Obviously, the primary attraction of the CMC topology is its modularity. However, this topology requires an excessive amount of DC voltage sources. The most important factors causing the voltage imbalance among these DC capacitors are the difference in the DC-link utilizations, the power stage losses and the component tolerances. Figure 5-45, for example, shows a phase leg of a cascaded seven-level converter. The resistor  $R_{LA1}$ ,  $R_{LA2}$  and  $R_{LA3}$ , represented the internal losses in the H-bridge converters in levels 1, 2 and 3, respectively. The internal losses may be differently influenced by the switching and conduction activity and the component tolerances. Firstly, these H-bridge converters are assumed to be lossless, and their capacitor voltages have the same initial values. To achieve steady-state, balanced voltages, these DC capacitors must have the same amount of real power utilization in a given period of time. Due to sharing the same output current, the differences in the capacitor currents are caused by the different duty cycles, because a capacitor current is a product of a duty cycle and an output

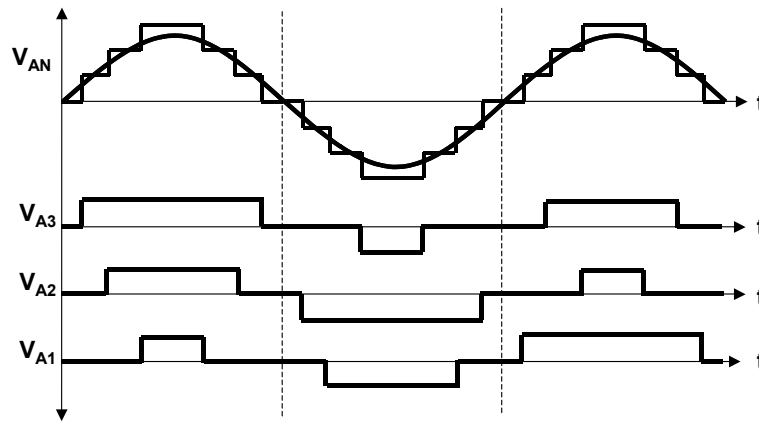
current. Therefore, the average switching functions or duty cycles in these H-bridge converters must be identical or else different in the DC voltages will be introduced. A couple of suitable modulation techniques can solve this problem.



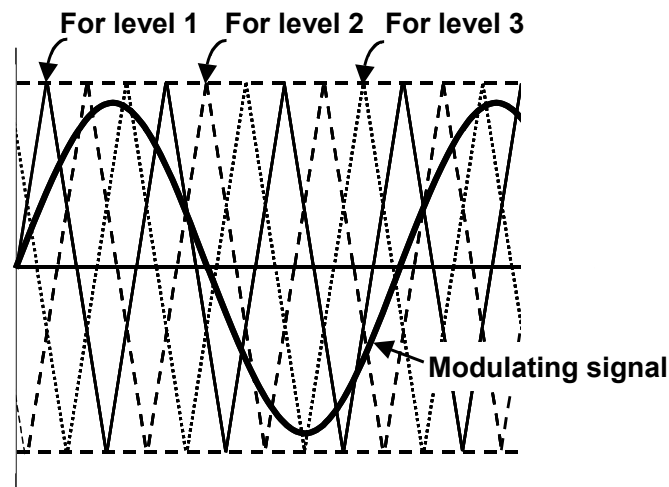
**Figure 5-45. One phase leg of a seven-level cascaded converter.**

The first technique, as shown in Figure 5-46(a), is called the rotating-pulse staircase, which is suitable to be applied with high numbers of voltage levels. A seven-level case is used as an example. Theoretically, the average amount of current flowing into and out of the capacitors is equal after  $N/2$  cycles, where  $N$  is the number of the H-bridge converters per phase. In a higher number of voltage levels, this process, therefore, takes a longer time and introduces a voltage ripple, whose frequency is  $120/N$  Hz for the case of line frequency of 60Hz. Figure 5-46(b) illustrates the second technique, called the phase-shifted carrier SPWM [10], which was proposed to improve the quality of the output waveforms of the multi-converter modules in high-voltage direct current (HVDC) applications. In the seven-level case, three carriers are  $120^\circ$  apart

from each other. Because of the use of equally distributed carrier signals, the fundamental components of the waveforms in different levels are theoretically identical; therefore, the amount of charges moving into and out of the capacitors in a period of time are equal.



(a)



(b)

**Figure 5-46. PWM techniques equally utilizing the DC capacitor voltages: (a) rotating-pulse staircase and (b) phase-shifted carrier SPWM.**

By applying one of these two techniques, the capacitor voltage can be balanced in the lossless STATCOM system. This is, however, not true in the case of the real STATCOM system, because the H-bridge converters are not identical. The internal losses and the component

tolerances are, for example, different. To proof this, a seven-level cascaded-based STATCOM, as shown in Figure 5-47, is used as an example.

The specifications of an example STATCOM system are shown in Table 5-6. The internal losses in the phase-A H-bridge converters are slightly different. Losses in the H-bridge converters in levels 1, 2 and 3 are 0.1%, 0.5% and 1% of its full power rating, respectively. The control proposed in the case of the three-level cascaded-based STATCOM is used in this study.

The phase-shifted carrier SPWM is used to generate the switching signals for the cascaded seven-level converter. Basically, the same duty cycle is used for all three H-bridge converters in the same phase leg, regardless to the amplitudes of their DC capacitors.

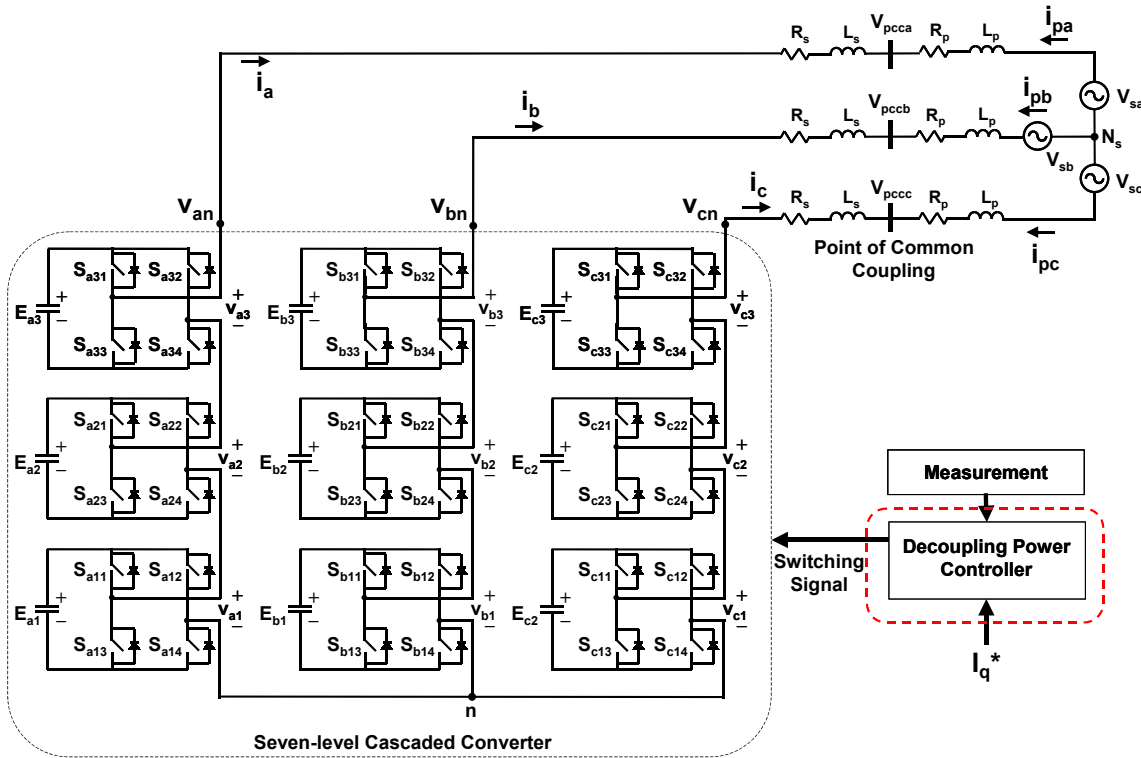


Figure 5-47. The schematic of the seven-level cascaded-based STATCOM.

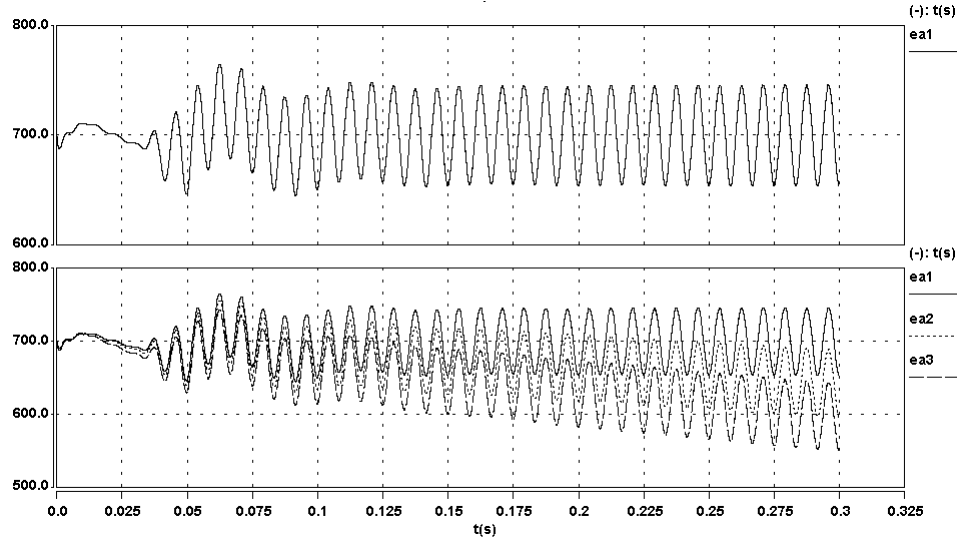


TABLE 5-6. SPECIFICATIONS OF THE STUDIED SEVEN-LEVEL CASCADED-BASED STATCOM SYSTEM.

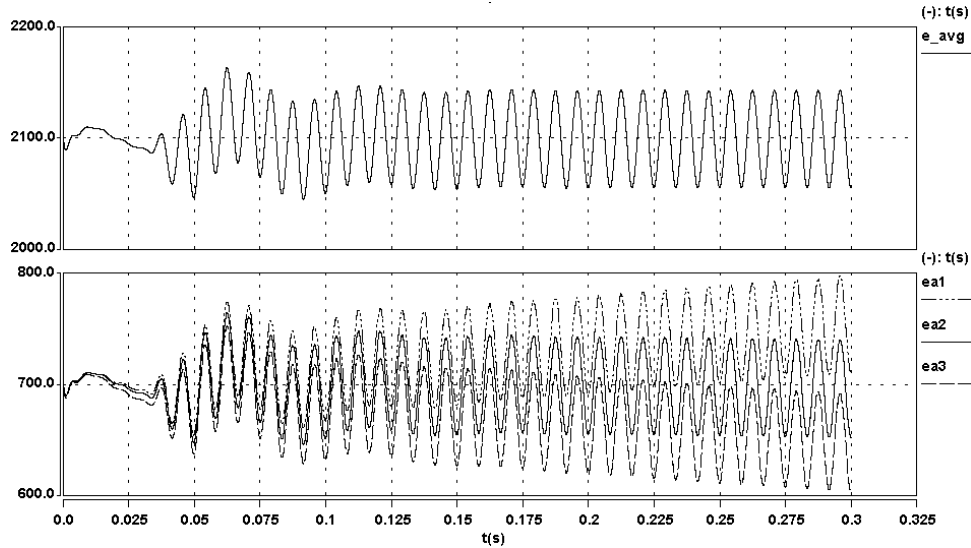
<b>Seven-Level Cascaded Converter</b>	
Individual DC Bus Voltage	700 V $\pm$ 10%
Total DC Bus Voltage	2100 V $\pm$ 10%
Rated RMS Reactive Current	1250 A
Capacitor Impedance	$(0.8m-j/(\omega \cdot 31.5mF)) \Omega$
Individual Switching Frequency/ Equivalent Switching Frequency	1 kHz/ 6 kHz
<b>Power System</b>	
Configuration	Balanced Three-Phase Three-Wire
Coupling Reactor Impedance	$(13m-j\omega \cdot 350\mu H) \Omega$
PCC Line Voltage	2100 V
Phase-A Losses	
Level 1	0.1 %
Level 2	0.5 %
Level 3	1.0 %

The first case study is that only the voltage of the phase-A level-one capacitor,  $E_{a1}$ , is regulated by the voltage loop of the controller. The rest of them are unregulated. The second case study is the same as the first case except that the average voltage of all three capacitor voltages is regulated. In both cases, the STATCOM is commanded to operate in the standby mode from startup, and, at time 30 ms, the STATCOM is commanded to operate in the full capacitive mode. The simulation results of the first and second cases are shown in Figure 5-48(a) and (b), respectively.

In the first case, the voltage  $E_{a1}$  is very well regulated, whereas the other two are decreasing. This is because only  $E_{a1}$  is used as the feedback parameter. Since the other two H-bridge converters have more losses, they need more real power from the capacitors to compensate those losses. In the second case, none of capacitor voltages is well regulated, because their average voltage is used as the feedback parameter. Due to the amount of losses, the voltage  $E_{a2}$  seems to be better regulated than the others, because its loss is close to the mean of the average losses.



(a)



(b)

**Figure 5-48. The DC capacitor voltages of the three-level cascaded-based STATCOM without the voltage-balancing technique: (a) using phase-A capacitor voltage as the feedback and (b) using the average of all three capacitor voltages as the feedback.**

From both simulation cases, it can be verified that the DC capacitor voltages cannot be balanced by solely applying suitable PWM techniques. Either an individual voltage control loop or newly designated PWM techniques must be included in the feedback-control system.

## 5.2 Proposed DC Capacitor Voltage-Balancing Techniques

The previous work on the DC capacitor voltage-balancing technique basically adds individual DC voltage loops into the main control loop. The compensators of each individual loop are very difficult to design because of the complexity of the voltage-loop transfer functions. Basically, trial and error provides the simplest way to achieve a good compensator. This process is very time-consuming. Moreover, the greater number of voltage levels, the more complex the control design. The main controller, which is the DSP-based, must perform all of those feedback controls. As a result, this approach potentially reduces the reliability of the controller.

This research, therefore, proposes an effective technique, which has the following features:

1. it is suitable for any number of H-bridge converters,
2. it offers hardware-based realization,
3. modularity, and
4. its complexity is not affected by the number of voltage levels.

Since the proposed technique can be realized by hardware circuitry, the calculation time in the DSP is just slightly increased when more voltage levels are employed. The basic structure of the proposed technique is modular; therefore, it is suitable for any number of H-bridge converters. With these features, the complexity of the DSP programming for the control loop is not affected by increasing the number of voltage levels.

### I. Redundancy in the Cascaded-Multilevel Converters

The CMC synthesizes its output voltages by adding many individual voltages together. In the cascaded seven-level converter, for example, seven output-phase voltage levels can be generated by seven combinations of the three H-bridge converter voltages, as shown in Figure 5-49. However, considering Figure 5-49(b), (c), (e) and (f), more than one combination can generate the same output voltages. Redundancies to generate level +2, +1 and 0 voltage are shown in Figure 5-50, Figure 5-51 and Figure 5-52, respectively. Even though the same output voltages are generated, the currents flowing in the circuits have different paths. This means that different DC capacitors see different current waveforms. Consequently, the DC capacitors have different

voltage profiles. Ironically, these redundancies can be used to adjust the individual capacitor voltages and help balance these voltages. The redundancies, as shown in Figure 5-50, are used as an example. If the DC voltage of the middle H-bridge converter is the lowest, then, for the given current direction, to generate the output voltage of  $2E$  V, the combination shown in Figure 5-50(b) is used, because the middle DC capacitor is disconnected from the output; with the large capacitor, its voltage is basically maintained. Due to the discharge processes, the DC capacitor voltages of the top and bottom H-bridge converters are decreased. Systematically, if this process is kept going, the capacitor voltages of these three H-bridge converters will become equal.

To achieve minimal operating losses, not all of the redundancies can be used. To generate the output voltage of  $E$  V, for example, circuits (e) through (g), as shown in Figure 5-51, generate three times as much conduction losses as circuits (a) through (c) do. Therefore, circuits (e), (f) and (g) are not suitable to be used in either very high-power application or the proposed-voltage balancing technique.

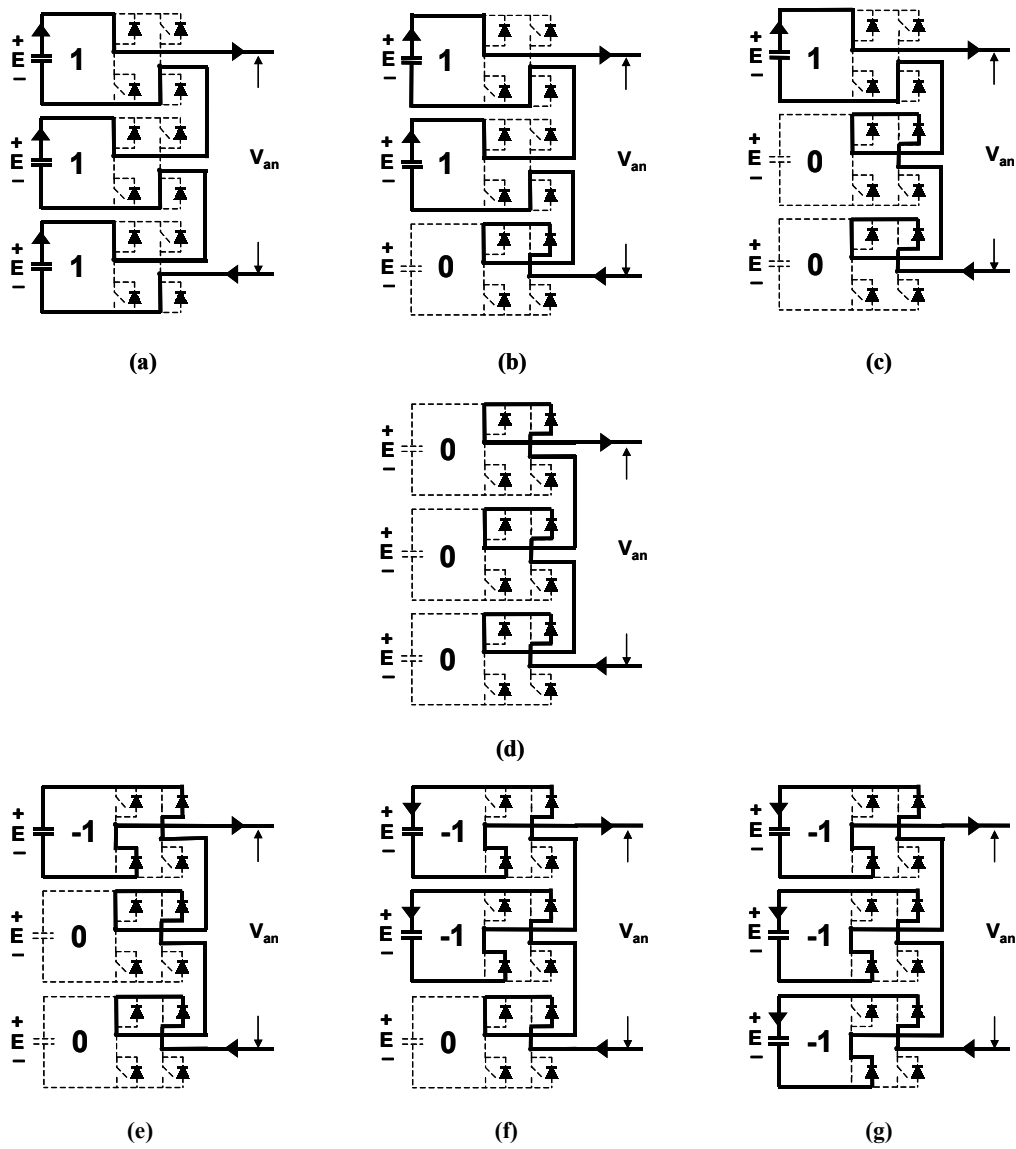


Figure 5-49. Seven synthesized output voltage for the single-phase cascaded seven-level converter: (a)  $+3V$ , (b)  $+2V$ , (c)  $+1V$ , (d)  $0V$ , (e)  $-1V$ , (f)  $-2V$  and (g)  $-3V$ .

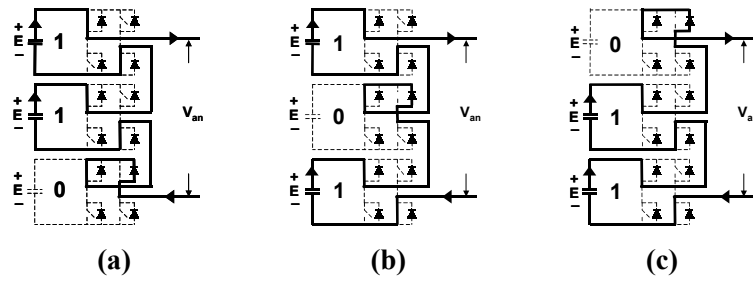


Figure 5-50. Redundancy of voltage at level +2.

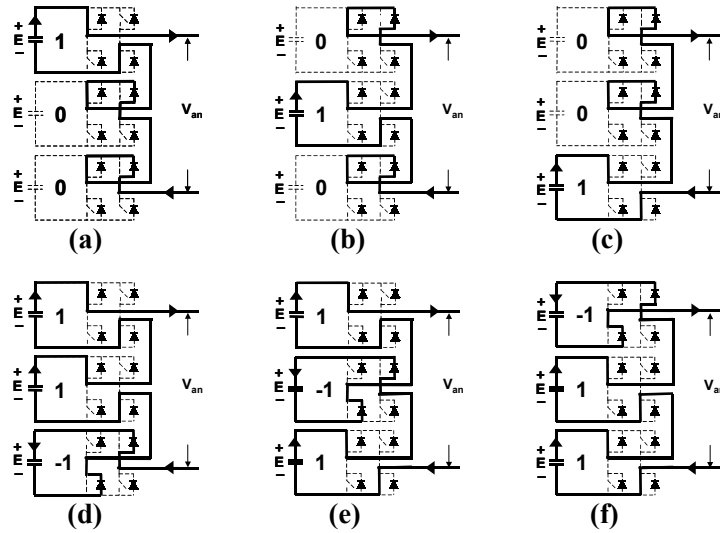
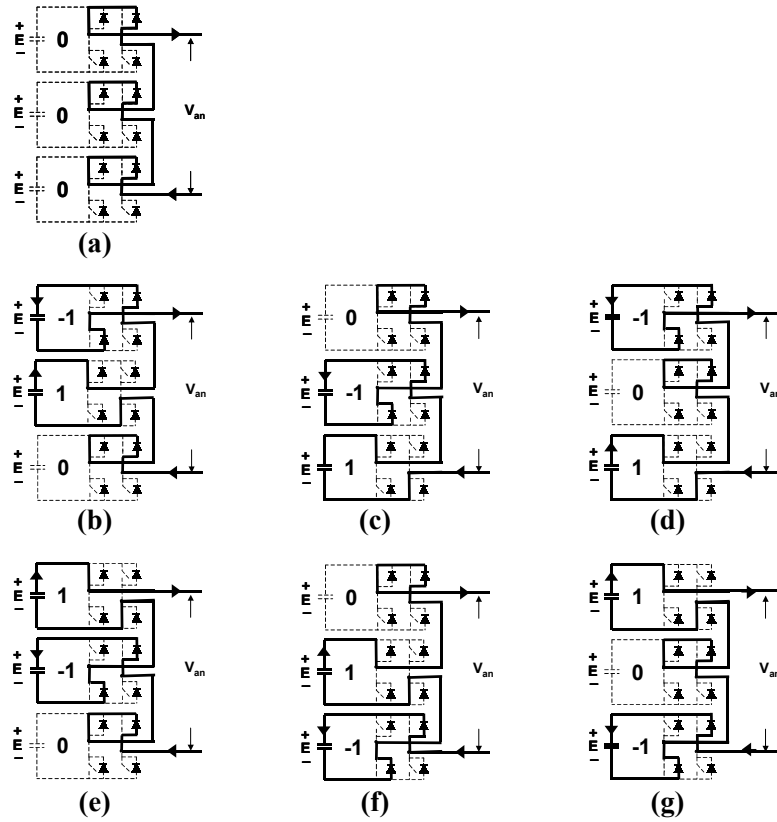


Figure 5-51. Redundancy of voltage at level +1.



**Figure 5-52. Redundancy of voltage at level 0.**

Regarding the optimization concern, the selected operation modes used to generate the positive and zero output voltages for a seven-level cascaded converter are shown in Figure 5-53. The redundancy combination used to generate the output voltages of +3, +2, +1, and 0 are one, three, three, and one, respectively. This also applies for the negative output voltages. Therefore, the total number of operation modes for the seven-level cascaded converter is 15, which breaks down as seven for the positive voltage, seven for the negative voltage, and one for the zero voltage.

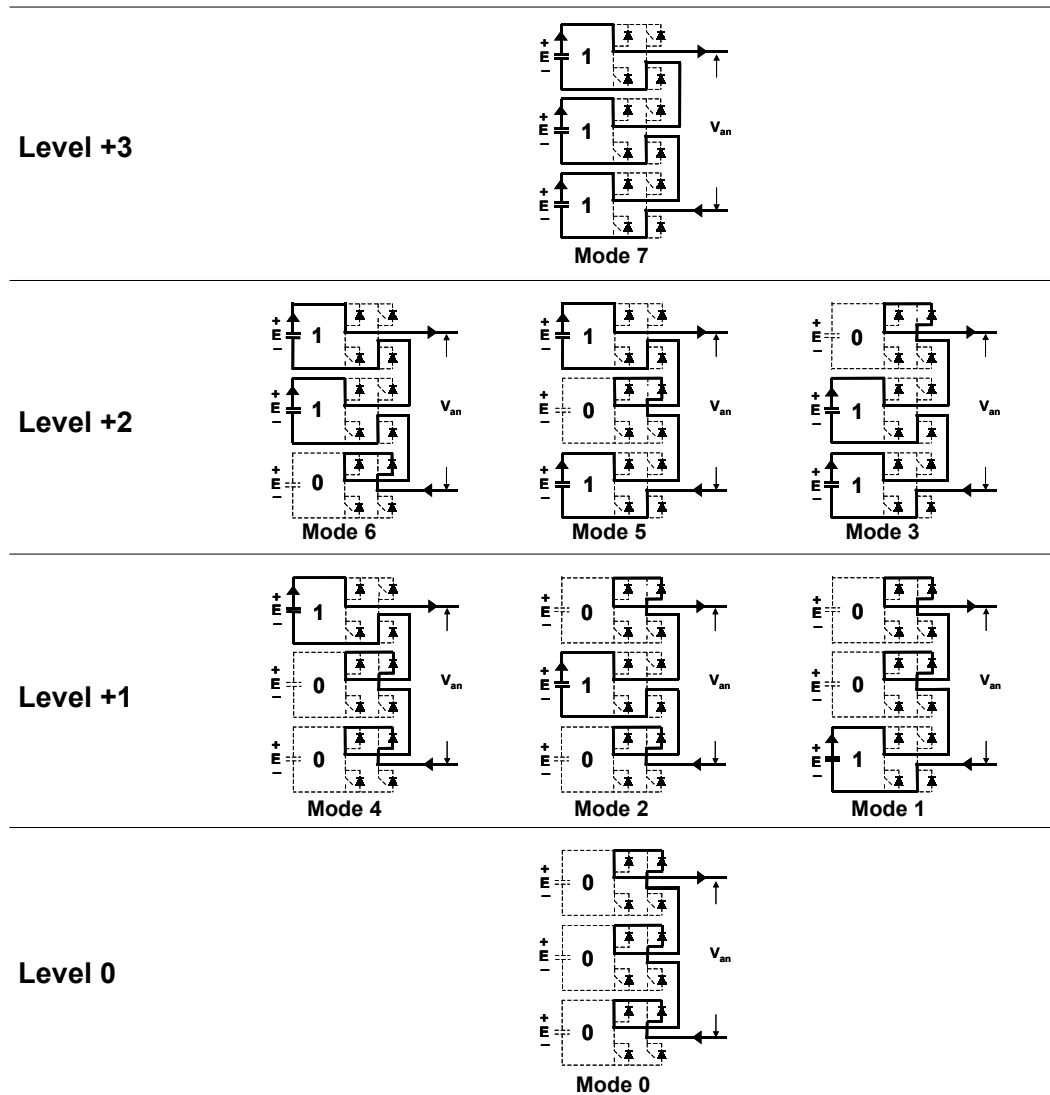


Figure 5-53. The redundancy combination and mode assignment used to generate the positive and zero output voltages for a cascaded seven-level converter.



TABLE 5-7. NUMBER OF REDUNDANCY MODES IN EACH OUTPUT VOLTAGE LEVEL FOR DIFFERENT NUMBERS OF H-BRIDGE CONVERTERS PER PHASE.

N	2N+1	Number of redundancies at level															Total no. of operation modes
		+7	+6	+5	+4	+3	+2	+1	0	-1	-2	-3	-4	-5	-6	-7	
1	3	0	0	0	0	0	0	1	1	1	0	0	0	0	0	0	$3=2^2-1$
2	5	0	0	0	0	0	1	2	1	2	1	0	0	0	0	0	$7=2^3-1$
3	7	0	0	0	0	1	3	3	1	3	3	1	0	0	0	0	$15=2^4-1$
4	9	0	0	0	1	4	6	4	1	4	6	4	1	0	0	0	$31=2^5-1$
5	11	0	0	1	5	10	10	5	1	5	10	10	5	1	0	0	$63=2^6-1$
6	13	0	1	6	15	20	15	6	1	6	15	20	15	6	1	0	$127=2^7-1$
7	15	1	7	21	35	35	21	7	1	7	21	35	35	21	7	1	$255=2^8-1$

Table 5-7 shows the number of redundancies for each output-voltage level with different values of N, where N is the number of H-bridge converters per phase. The number of phase voltage levels is 2N+1. The total number of operation modes, which is the summation of all redundancies, is  $2^{N+1}-1$ . The redundancies for each-output voltage level can be simply calculated by adding together the redundancies of the lower N. N equal to 7 is used as an example. From Table 5-7, the arrows point out the two numbers used to calculate the number of redundancies. For example, with an output level of +6, a redundancy of seven is the summation of 6 and 1 from the case of N = 6. For a high number of N, the number of the redundancy can be found by this systematic calculation.

## II. Cascaded Pulse-Width Modulation Technique

Given the troublesome previous work and the redundancy of the CMC, a new PWM technique, which is specially designed for the CMC-based STATCOM, is proposed in this section. Figure 5-54 shows the proposed block diagram of the CMC-based STATCOM controller, which is basically identical to that of the three-level cascaded-based STATCOM except that the voltage loop is different. The proposed PWM is called the cascaded PWM in

which the DC capacitor voltages, the output currents and the three-phase multilevel duty cycle command are used as its inputs.

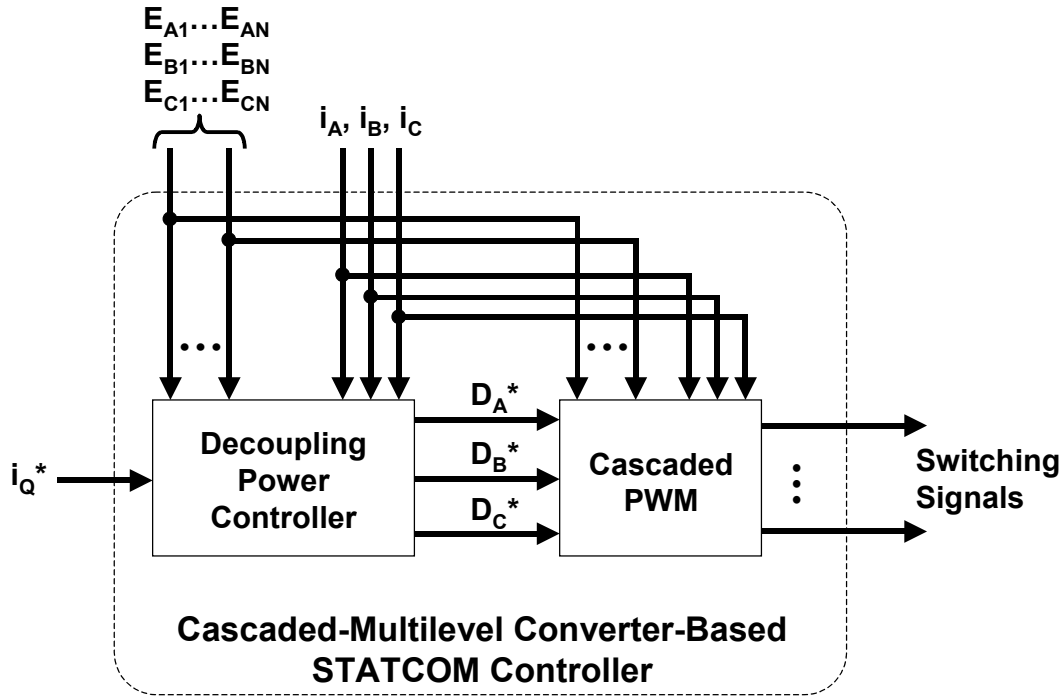


Figure 5-54. Proposed cascaded-multilevel converter-based STATCOM controller.

The details of the proposed cascaded-PWM block diagram are shown in Figure 5-55. The diagram is composed of six different blocks: the boundary and duty cycle assignment, the direction and polarity check, the sorting network, the index generator, the combined switching table, and the PWM. These six blocks can be simply realized by programmable integrated circuits such as the FPGA. To avoid confusion, the clock signals for each block are not included in the block diagram.

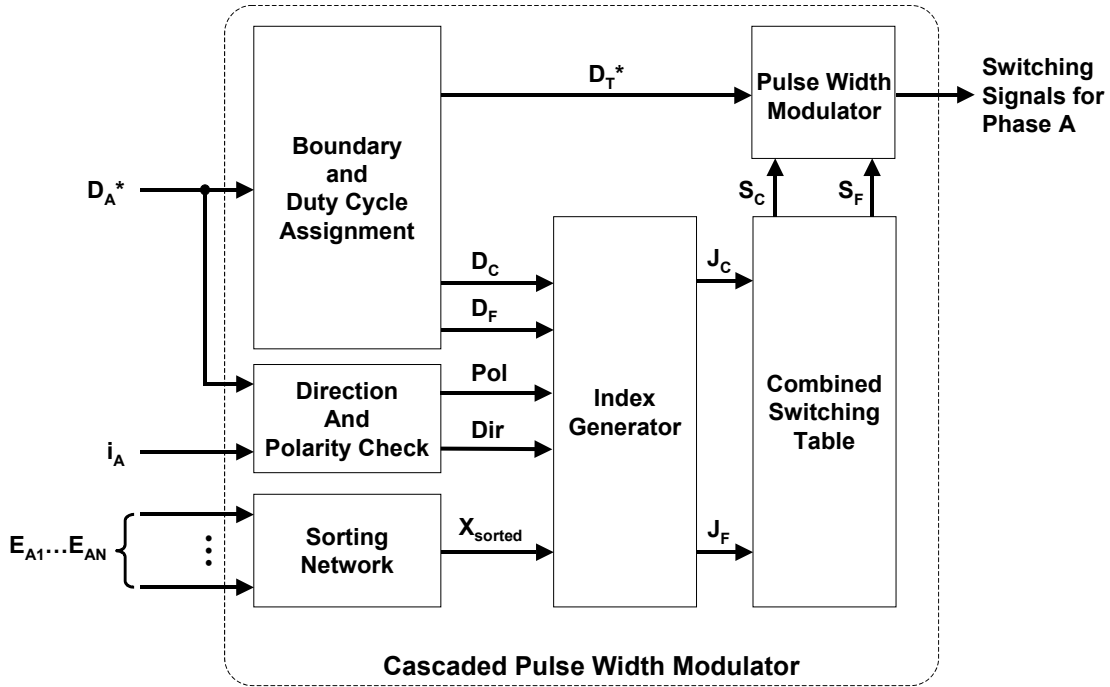


Figure 5-55. Block diagram of the proposed cascaded pulse width modulator.

#### A. Boundary and Duty Cycle Assignment

To produce a clear explanation, a cascaded seven-level VSC is used as an example. Based on the  $2N+1$  formula, each phase of the converter consists of three identical H-bridge converters. Seven voltage levels, as shown in Figure 5-56, can be synthesized, i.e., +3, +2, +1, 0, -1, -2, and -3. In the CMC, the relationship between the modulation index and the duty cycle can be expressed as follows:

$$D = M \cos(\omega t + \phi), \text{ and}$$

**Equation 5-27**

$$M = \frac{V_{pk}}{\sum_{j=1}^N E_j},$$

**Equation 5-28**

where  $D$  is the duty cycle,  $M$  is the modulation index,  $\omega$  is the angular velocity,  $\phi$  is the displacement angle,  $V_{pk}$  is the peak output voltage,  $E_j$  is the  $j^{\text{th}}$  DC-link voltage, and  $N$  is the number of H-bridge converters per phase.

From the plane shown in Figure 5-56, vector  $\vec{M}_A$  is defined as the phasor of the reference modulation index of the phase-A output voltage of the converter. In general, the modulation index for the CMC, as shown in Equation 5-28, is defined as a ratio of the converter output peak voltage to the total DC-link voltage.  $N$  is equal to 3 in this example. Phasor  $\vec{M}_A$  rotates with the angular velocity of  $\omega$  or  $2\pi f$ , where  $f$  is the line frequency. From Equation 5-27, the duty cycle phasor,  $\vec{D}_A$ , is basically the projection of  $\vec{M}_A$  to the y-axis.

The magnitude of  $\vec{D}_A$  determines the levels of the synthesis voltages. Three circles on the xy plane shown in Figure 5-56 represents the six different combinations of the levels of the synthesized voltage. The positive y is where the positive half cycle of the output voltage is, whereas the negative y is where the negative half-cycle of the output voltage is. For example,  $\vec{M}_A$  is assumed to equal 2.34 and lays in the level between +2 and +3, as shown in Figure 5-56. At that moment, the vector  $\vec{D}_A$ , which represents the instantaneous output voltage of the converter, is equal to +1.50 in the boundary between the +1 and the +2.

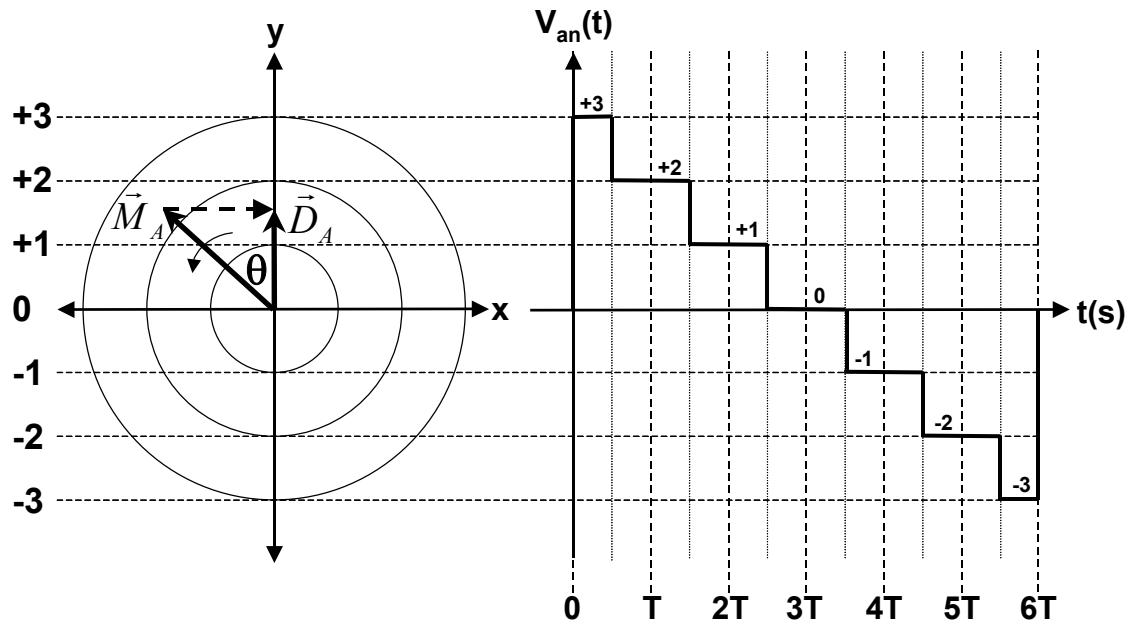


Figure 5-56. Multilevel voltage synthesis.

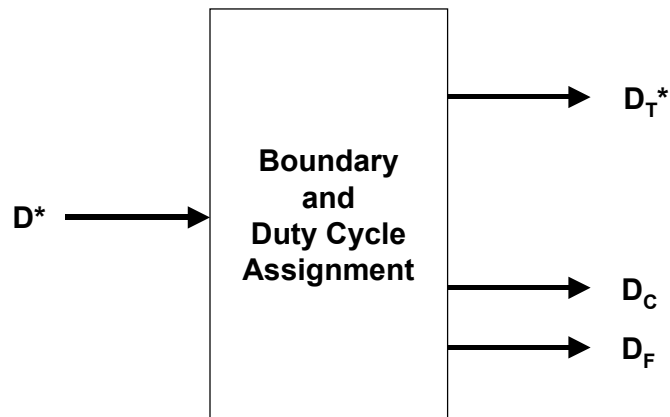


Figure 5-57. Input and output signals of the boundary and duty cycle assignment.

The boundary and duty cycle assignment (BDCA) block is used to determine the level of the output voltage and the normalized duty cycle. The input of the BDCA block is the command multilevel duty cycle,  $D_A^*$ , from the decoupling power controller, and its outputs are the normalized duty cycle,  $D_T^*$ , the ceiling duty cycle,  $D_C$ , and the floor duty cycle,  $D_F$ . The duty

cycles  $D_C$  and  $D_F$  are integers from 0 to N, where N is the number of H-bridge converters per phase. The relationship between duty cycles  $D_C$  and  $D_F$  is as follows:

$$D_F < D_C \text{ and } D_F = D_C - 1.$$

**Equation 5-29**

The duty cycles  $D_C$  and  $D_F$  are determined from the duty cycle  $D_A^*$  by the following relationship:

$$D_F < D_A^* < D_C.$$

**Equation 5-30**

Then, the duty cycle  $D_T^*$  can be calculated by

$$D_T^* = D_A^* - D_F.$$

**Equation 5-31**

For example, a given seven-level duty cycle of the phase-A output voltage is

$$D_A^* = 2.34.$$

Then, by applying Equation 5-29 through Equation 5-31, the other variables can be determined, as follows:

$$D_F = 2,$$

$$D_C = 3, \text{ and}$$

$$D_T^* = 0.34.$$

### ***B. Direction and Polarity Check***

The direction and polarity check (DPC) block is used to determine the direction of the capacitor currents, as well as the polarity of the duty cycle. The inputs of the DPC block are the

multilevel duty cycle  $D_A^*$  and the output current of the converter. The outputs of the DPC blocks are the polarity of the duty cycle, Pol, and the direction of the capacitor current, Dir.

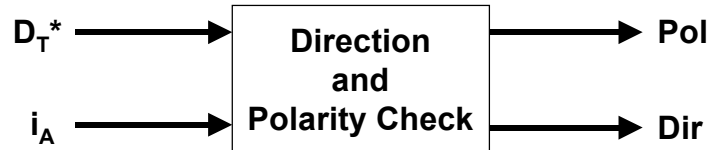


Figure 5-58. Input and output signals of the direction and polarity check block.

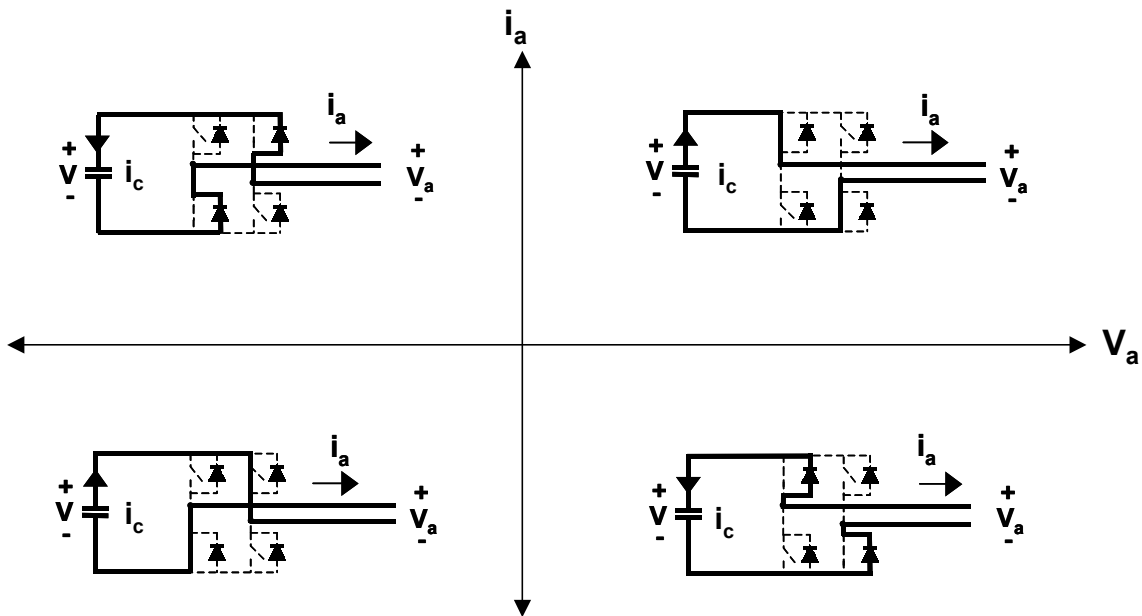


Figure 5-59. Capacitor current in the four-quadrant operations of an H-bridge converter.

The polarity of the duty cycle,  $Pol$ , is defined as follows:

$$Pol = \begin{cases} 0, & \text{when } D_A^* < 0 \\ 1, & \text{when } D_A^* \geq 0 \end{cases}.$$

**Equation 5-32**

The direction of the capacitor current,  $Dir$ , is a function of the directions of the output voltage and current. Figure 5-59 demonstrates the direction of the capacitor current in all four quadrants of the  $I_a$ - $V_a$  plane. The capacitor is discharged when the polarity of the current  $I_a$  and voltage  $V_a$  are the same, while the capacitor is charged when the polarity of the current  $I_a$  and voltage  $V_a$  are different. As a result, to determine the direction of the capacitor current, the logic operator exclusive OR can be applied to the direction of the output voltage and current as follows:

$$Dir = \vec{i}_a \oplus Pol,$$

**Equation 5-33**

where  $\vec{i}_a$  is the direction of the output current, which equals 0 when flowing out of the converter and 1 when flowing into the converter, and  $Dir$  is the direction of the capacitor current, which equals 0 when discharged and 1 when charged.

### **C. Sorting Circuit**

The sorting network (SN), as shown in Figure 5-60, is used to perform descending sorting on the DC capacitor voltages. The inputs of the SN are  $N$  capacitor voltages in the same phase leg of the CMC. After sorting, the result is a register containing  $N$  indices, which represent the sorting information of the capacitor voltages. The heart of the SN is the sorting algorithm. Referring to the data architecture, among well-known sorting algorithms, Bubble sorting shows the following feasibilities to be used in this task: it is very simple, and it provides modularity and high fault tolerance. The proposed SN for a general cascaded  $N$ -level converter is presented in Figure 5-61. The basic unit of the SN is the comparator (CP). The CP block diagram is shown in Figure 5-62, and its transfer function is as follows:



$$\begin{aligned} H &= \max(a, b) \\ L &= \min(a, b) \end{aligned}$$

Equation 5-34

where  $\max$  is the maximum function, and  $\min$  is the minimum function.



Figure 5-60. Inputs and output of the sorting network.

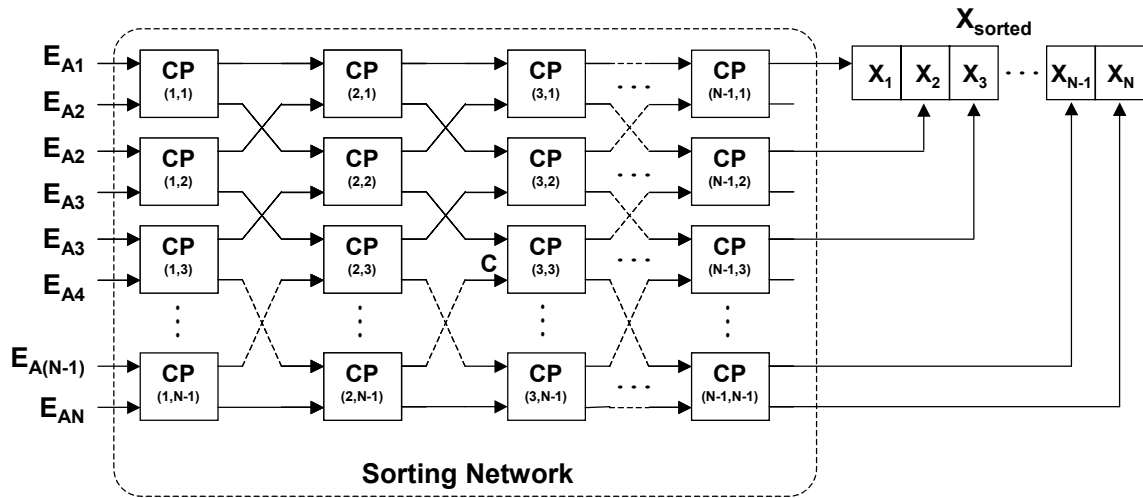
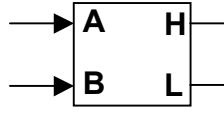
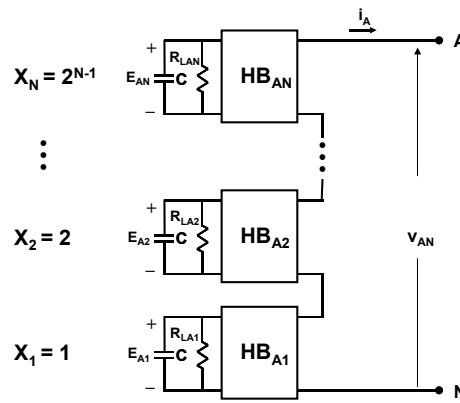


Figure 5-61. The proposed N-level sorting network.



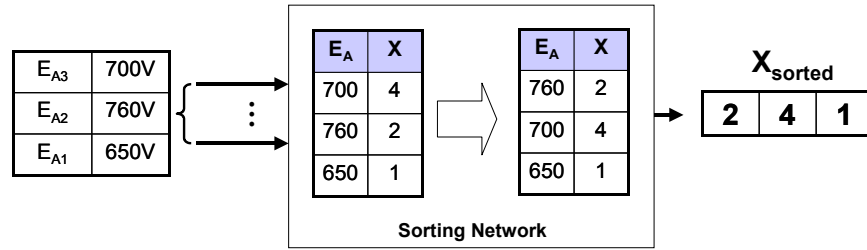
**Figure 5-62. Inputs and outputs of a comparator unit.**

The index  $X$  is the number representing the capacitor position in the phase leg, and is assigned as shown in Figure 5-63.



**Figure 5-63. The embedded indices to represent the capacitor positions.**

Figure 5-64 demonstrates how the proposed SN works. The SN reads the voltage contents of the capacitor voltages of phase A of a cascaded seven-level converter-based STATCOM. Then, the embedded indices are assigned and are passed through the sorting algorithm. After three clock cycles, the sorted result is achieved, and the register  $X_{\text{sorted}}$  can be accessed by the other function blocks.

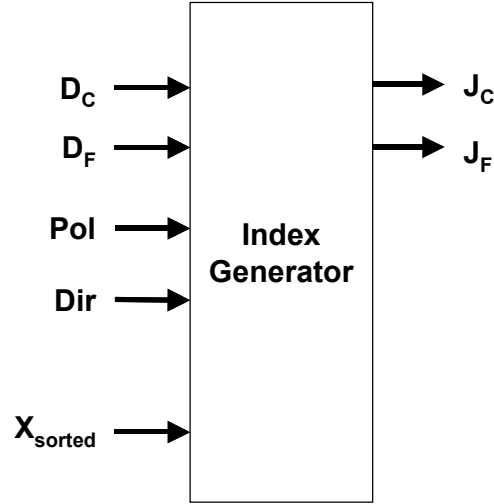


**Figure 5-64. Operation of the proposed sorting network for a cascaded seven-level converter.**

#### **D. Index Generator**

The index generator (IG) is used to calculate the ceiling and floor indices, which are used to point to the ceiling and floor switching signals from the combined switching table. The inputs of the IG are the two outputs of the BDCA block: DC and DF, the two outputs of the DPC block: Pol and Dir, and the output of the SN:  $E_{sorted}$ . For a given multilevel duty cycle, based on the content of their capacitor voltages, the IG identifies its outputs by which H-bridge converters are used to generate the output voltages. The output  $J_C$  corresponds to the input  $D_C$ ; likewise for  $J_F$  and  $D_F$ . Therefore, the explanation of the  $J_C$  case will also be applied in the case of  $J_F$ .

Using the ceiling index as an example, in the IG, the duty cycle  $D_C$  represents the number of H-bridge converters used to generate the output voltage. The polarity of the output voltage is based on the parameter Pol.



**Figure 5-65. Inputs and outputs of the index generator.**

For  $Dir = 0$  and  $Pol = 1$ ,  $D_C$  H-bridge converters whose DC capacitor voltages are the highest are used to generate the positive output voltage. In contrast, for  $Dir = 1$  and  $Pol = 1$ ,  $D_C$  H-bridge converters whose DC capacitor voltages are the lowest are used to generate positive output voltage. In the case of  $Pol = 0$ , for  $Dir = 0$ ,  $D_C$  H-bridge converters whose DC capacitor voltages are the highest are used to generate the negative output voltage. In contrast, for  $Dir = 1$  and  $Pol = 0$ ,  $D_C$  H-bridge converters whose DC capacitor voltages are the lowest are used to generate the negative output voltage. Based on this logic,  $Dir$  indicates whether the H-bridge converters with the highest or lowest DC voltages are used to synthesize the output voltage. When  $Dir = 1$ , the IG performs the summation of the  $X_{sorted}$  contents from the left to the right-hand side and from the right to the left-hand side when  $Dir = 0$ . Parameter  $Inx_L$  contains the summation result. The direction of the summation is illustrated in Figure 5-66(a). The following algorithm is used as an example for the case of the ceiling parameter,  $D_C$ :

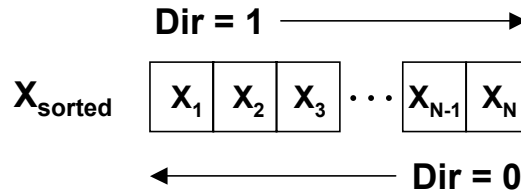
*if*  $Dir = 1$

$$Inx_L = \sum_{i=1}^{D_C} X_{sorted}[i]$$

*else*

$$Inx_L = \sum_{i=(N+1)-D_C}^N X_{sorted}[i],$$

and the final format of the IG output  $J_C$  is shown in Figure 5-66(b).



(a)



(b)

**Figure 5-66. (a) The direction of the summation of the indices, which is directed by the parameter Dir and (b) the final format of the generated index.**

### ***E. Combined Switching Table***

After achieving the ready signal from the IG, the indices  $J_C$  and  $J_F$  are used to point to the desirable switching signals for all main semiconductor devices. Table 5-8 is an example for the seven-level cascaded converter case. The table consists of the index (the first and second columns), corresponding hex (the third column), and the status of the top switches of the level-3 H-bridge converter (the fourth column), the level-2 H-bridge converter (the fifth column), and the level-1 H-bridge converter (the sixth column). The 0 and 1 in the fourth though sixth columns represent the top switches turned off and on, respectively. Due to complementary switching, the top and bottom switching statuses derived from the four possible combinations of the two top switches are given in Table 5-9.

TABLE 5-8. COMBINED SWITCHING TABLE FOR THE CASCADED SEVEN-LEVEL CONVERTER.

Pol	In <sub>xL</sub>	Hex	S <sub>A31</sub> ,S <sub>A32</sub>	S <sub>A21</sub> ,S <sub>A22</sub>	S <sub>A11</sub> ,S <sub>A12</sub>
0	0	0000	0,0	0,0	0,0
0	1	0001	0,0	0,0	1,0
0	2	0010	1,1	1,0	0,0
0	3	0011	1,1	1,0	1,0
0	4	0100	1,0	1,1	1,1
0	5	0101	1,0	1,1	1,0
0	6	0110	1,0	1,0	1,1
0	7	0111	1,0	1,0	1,0
1	0	0000	0,0	0,0	0,0
1	1	0001	0,0	0,0	0,1
1	2	0010	1,1	0,1	0,0
1	3	0011	1,1	0,1	0,1
1	4	0100	0,1	1,1	1,1
1	5	0101	0,1	1,1	0,1
1	6	0110	0,1	0,1	1,1
1	7	0111	0,1	0,1	0,1

TABLE 5-9. SWITCHING STATUSES OF FOUR POSSIBLE COMBINATIONS OF TOP AND BOTTOM SWITCHES.

S <sub>A1</sub> ,S <sub>A2</sub>	S <sub>A1</sub>	S <sub>A2</sub>	S <sub>A3</sub>	S <sub>A4</sub>
0,0	0	0	1	1
0,1	0	1	1	0
1,0	1	0	0	1
1,1	1	1	0	0

#### ***F. Pulse-Width Modulator***

Basically, the PWM transforms the average switching function or the duty cycle into the two-stage switching action for the individual switch. The inputs and output of the PWM are shown in

Figure 5-67. Due to the relatively slow switching rate of the high-power semiconductor devices, the double-updated PWM, as shown in Figure 5-68, is employed to minimize the delay time. Figure 5-68 illustrates the PWM waveform of the phase-A voltage generated from the given seven-level duty cycle command between time 0 and  $T$ , where  $T$  is the switching period. The PWM reads the duty cycle commands twice every switching cycle at 0 and  $0.5T$ , in order to generate the waveforms in the  $0-0.5T$  and the  $0.5T-T$  durations, respectively.

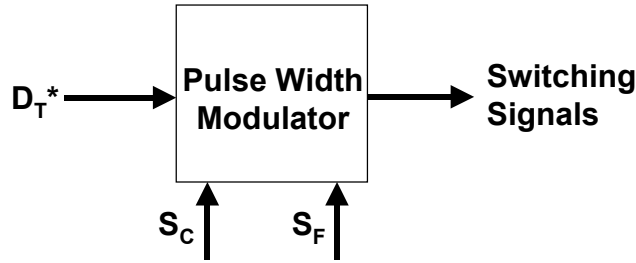


Figure 5-67. Inputs and output of the pulse-width modulator.

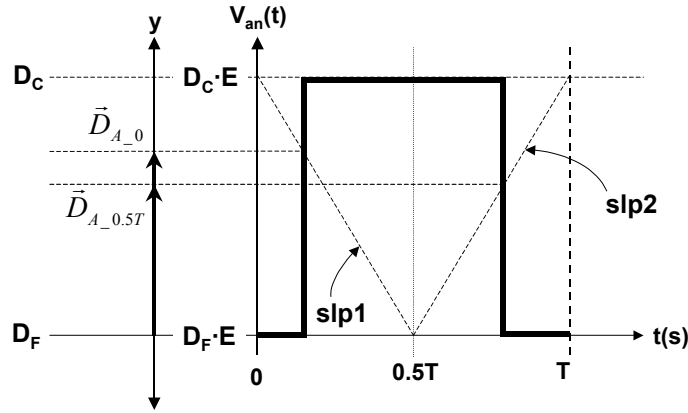


Figure 5-68. Double-updated pulse generated by the pulse-width modulator.

A general PWM waveform synthesized by the proposed PWM, as shown in Figure 5-68, is used as an example. In the period between  $T$  and  $1.5T$  s, the duty cycle  $\bar{D}_{A_T}$  is read. The switching signals corresponding to the index  $J_F$  are sent to the main switches. At the moment that the negative slope  $slp1$  intersects  $\bar{D}_{A_T}$ , the main switches are switched to the switching signals

corresponding to the index  $J_C$ . In the second half-cycle, the duty cycle is updated to  $\bar{D}_{A_{0.5T}}$ . The status of the main switches is, however, still unchanged. Until the moment at which the positive slope  $slp2$  intersects  $\bar{D}_{A_{0.5T}}$ , the main switches are switched back to the switching signals corresponding to the index  $J_F$ . This completes a switching cycle.

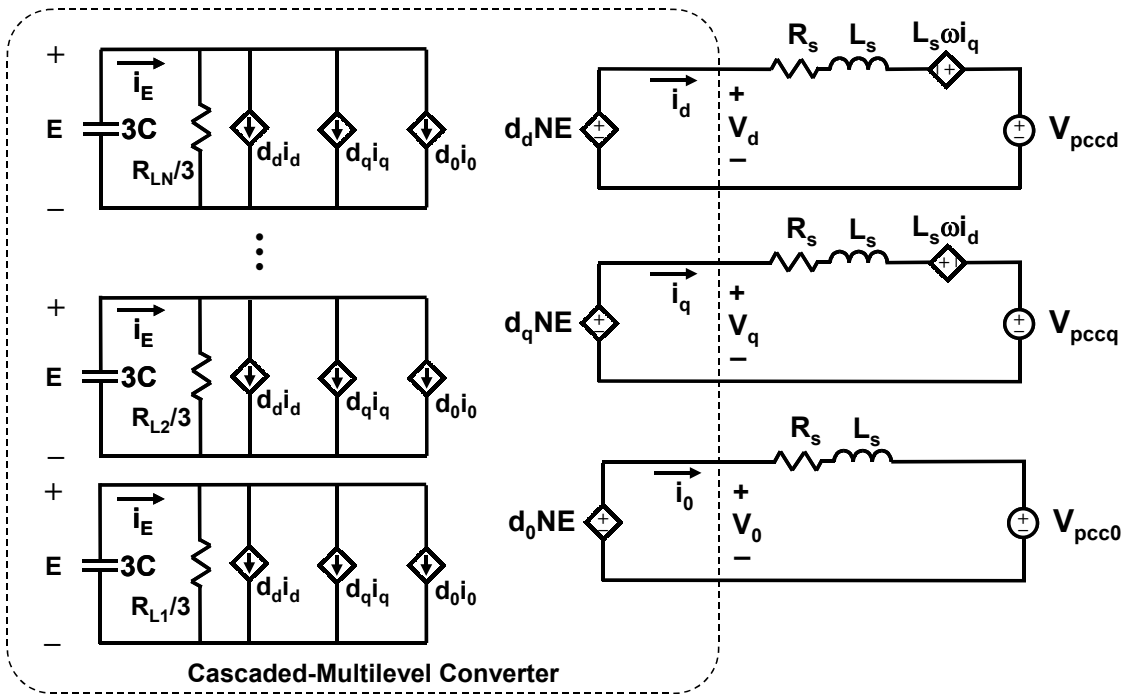


Figure 5-69. The average model for the CMC-based STATCOM with the proposed PWM.

### III. Simplified Model for the Cascaded-Multilevel Converter-Based STATCOM Utilizing the Cascaded Pulse-Width Modulator

By applying the proposed cascaded PWM, the model for the CMC-based STATCOM can be further simplified. Based on the generic average model of the CMC-based STATCOM, as shown in Figure 4-14, its simplified model is depicted in Figure 5-69.

Mathematically, on the DC side, the DC capacitors can be connected in parallel, as shown in Figure 5-70. The capacitor current can be expressed as follows:

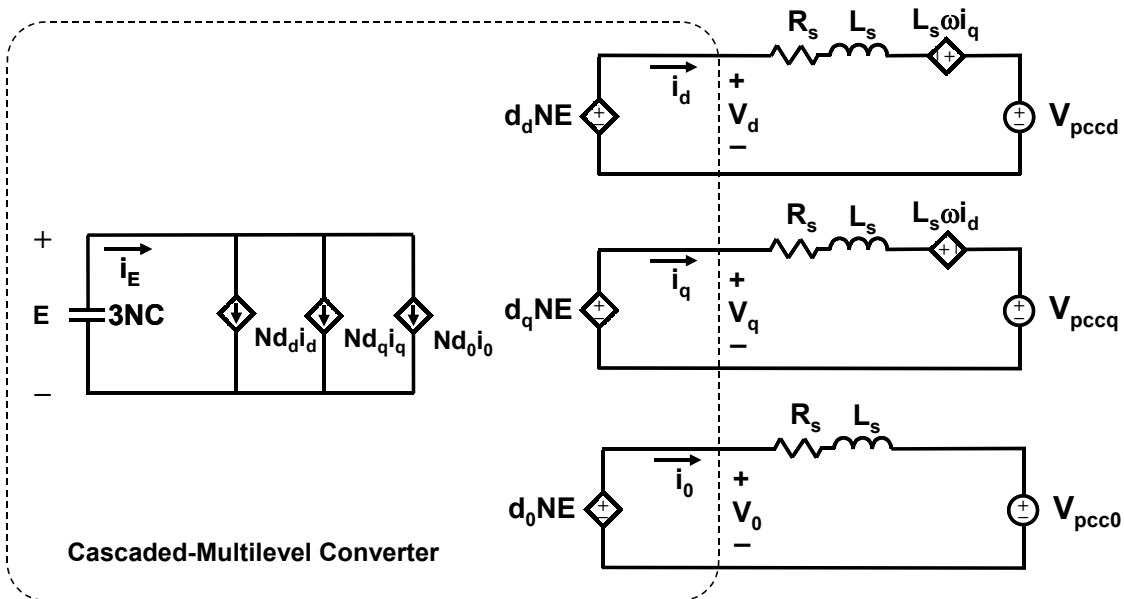


$$N \cdot 3C \frac{dE}{dt} = N \cdot (d_d i_d + d_q i_q + d_0 i_0), \text{ or}$$

$$3C \frac{dE}{dt} = d_d i_d + d_q i_q + d_0 i_0.$$

**Equation 5-35**

From Equation 5-35, due to the cancellation of  $N$  on both sides, the number of H-bridge converters per phase is not a factor. This leads to the conclusion that if the cascaded PWM is utilized, the DC side of the CMC can be modeled as that of the three-level cascaded converter, as shown in Figure 5-71. However, the difference in the AC side from that of the cascaded three-level converter is the multiplier  $N$  of the voltage-controlled voltage sources.



**Figure 5-70. The simplified average model for the CMC-based STATCOM with the proposed PWM.**

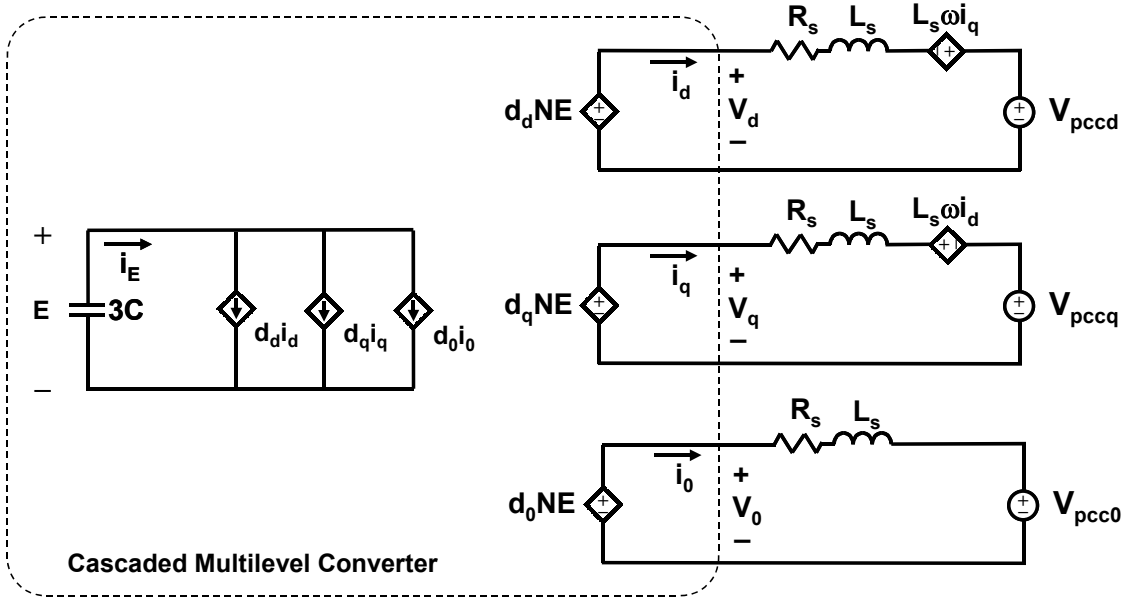


Figure 5-71. The average model for the CMC-based STATCOM with the proposed PWM.

#### IV. Feedback Design for the CMC-Based STATCOM

To evaluate the performance of the proposed cascaded PWM, the cascaded seven-level converter-based STATCOM, as shown in Figure 5-47, is used as an example. The power stage parameters of the converter are given in Table 5-6. The simplified average model of the seven-level converter-based STATCOM, from which the small-signal model is derived, is shown in Figure 5-72. Based on the same approach used in the three-level case, the key transfer functions are determined, and the control parameters are then designed, as given in Table 5-10.

Due to the shorter delay in the cascaded seven-level converter, the bandwidth of the current and voltage loops can be increased. As a result, the faster system response is achieved. The control-to-current transfer function and the current-loop gain are shown in Figure 5-73(a). Figure 5-73(b) shows the D-channel current-to-DC-capacitor-voltage transfer function and the main voltage-loop gain. From the results, the main current-loop bandwidth is 200 Hz, and the main voltage-loop bandwidth is 18 Hz.

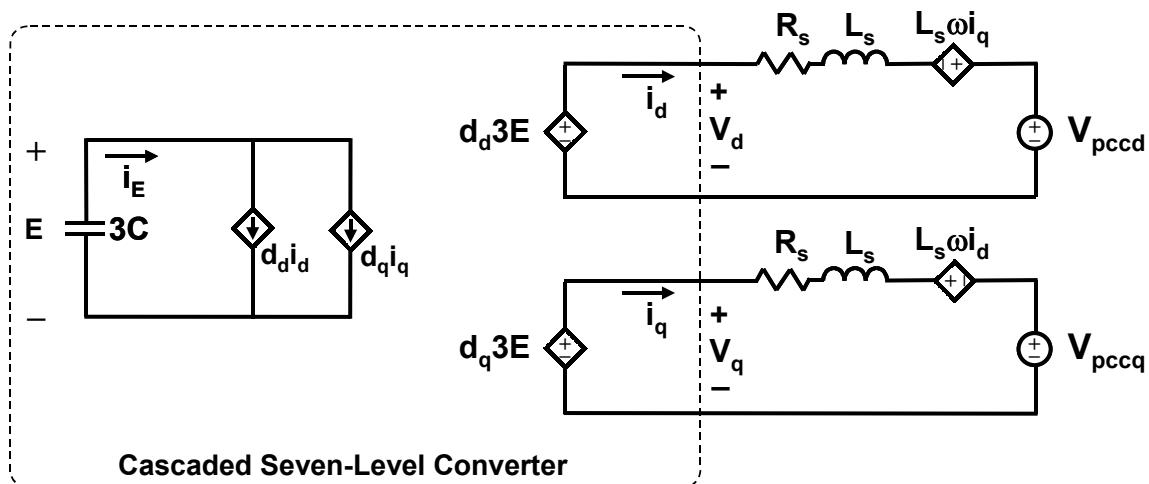
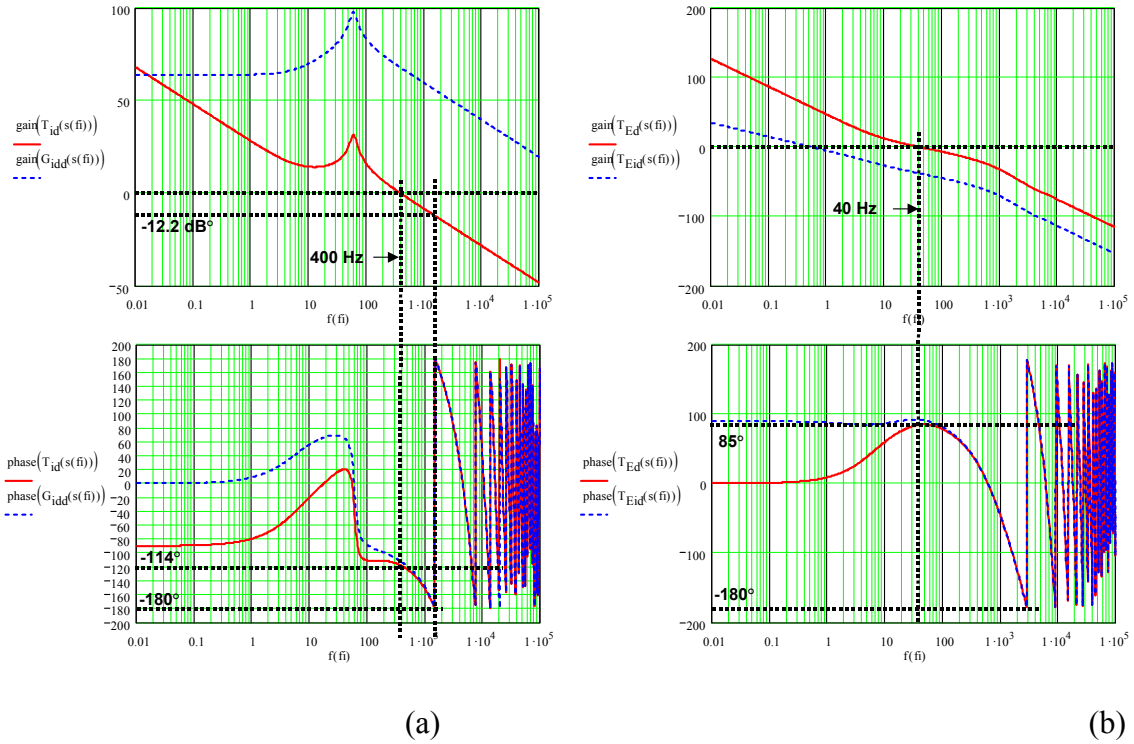


Figure 5-72. The simplified average model for the seven-level cascaded-based STATCOM.

TABLE 5-10. CONTROL PARAMETERS FOR THE SEVEN-LEVEL CASCADED CONVERTER-BASED STATCOM.

Parameters	Values
Current Loop	
<i>PI Compensator, <math>H_{id}(S)</math></i>	
$K_p$	0.398m
$K_i$	0.1
<i>Loop-Gain <math>T_{id}(S)</math> Characteristics</i>	
Crossover Frequency (Hz)	400
Phase Margin (Degrees)	66
Gain Margin (dB)	12.2
Voltage Loop	
<i>PI Compensator, <math>H_{Ed}(S)</math></i>	
$K_p$	79.6
$K_i$	2.5k
<i>Loop-Gain <math>T_{Ed}(S)</math> Characteristics</i>	
Crossover Frequency (Hz)	40
Phase Margin (Degrees)	95



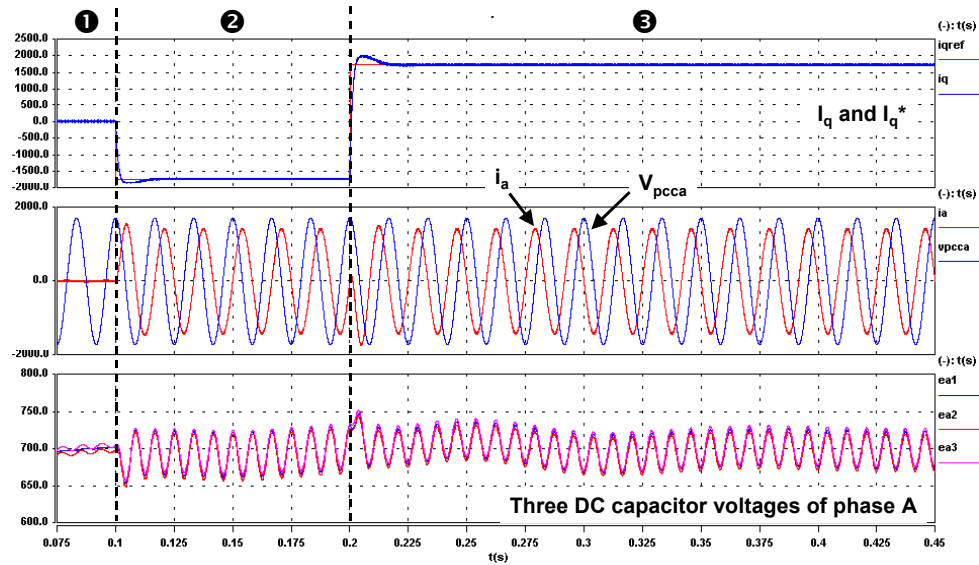
**Figure 5-73. (a) Bode plots of the control-to-current transfer function and the current-loop gain; (b) Bode plots of the D-channel current-to-DC-voltage transfer function and main voltage-loop gain.**

### A. Simulation Results

Figure 5-74 shows the results of the dynamic responses of the STATCOM operating in standby, full capacitive and full inductive modes. The results include the command  $I_q$  and its response, the phase-A converter output current and voltage at the PCC, and the DC bus voltages of each level. The details are shown in Figure 5-75, in which the STATCOM receives the step command from the full capacitive to full inductive mode. According to the defined current direction, the converter current lags the PCC voltage by about  $90^\circ$  in full capacitive mode, while the converter current leads the PCC voltage by about  $90^\circ$  in full inductive mode. However, converter currents and voltages at the PCC are not exactly  $90^\circ$  because of the real power exchange. The results show that the STATCOM reacts to the step command in the order of a

sub-line cycle, even though the switching frequency of each H-bridge converter is only 1 kHz. Figure 5-76 shows all three phase output voltages and currents, and the voltages at the PCC.

To verify the DC bus voltage-balancing, all nine DC voltage waveforms across the bus capacitors are shown in Figure 5-77 and Figure 5-78. In Figure 5-77, the DC voltages are grouped in the same phases. The results show that the DC voltages in each phase are well balanced. The worst case of DC response is for phase “B”; however, the controller is able to bring the voltages back to the setting, which is 700 V. Figure 5-78 shows the DC voltages in groups of the same levels. Based on the average DC voltage control scheme, the DC voltages of all three levels are identical, as expected.



**Figure 5-74. The STATCOM operates in standby mode (zero reactive power injection), full capacitive mode (+Q) and full inductive mode (-Q).**

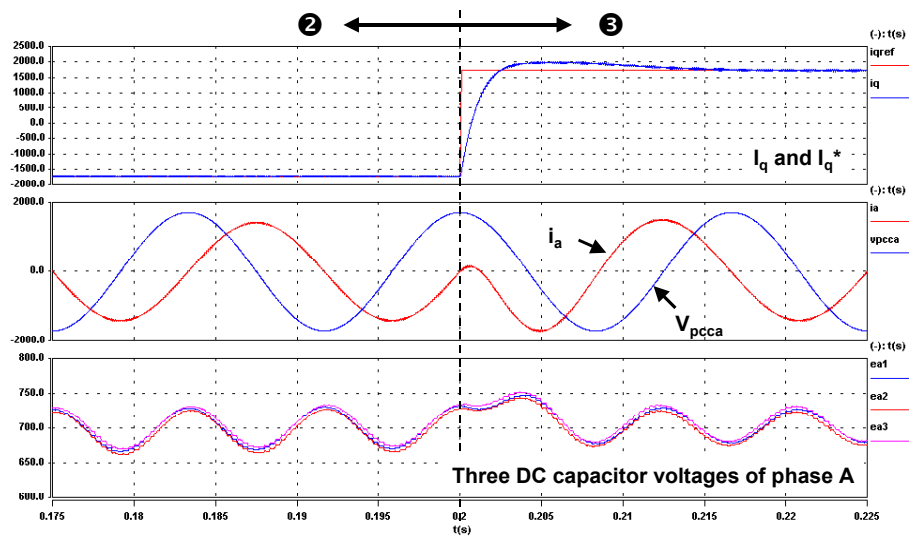


Figure 5-75. Step response of the STATCOM from full capacitive mode (+Q) to full inductive mode (-Q).

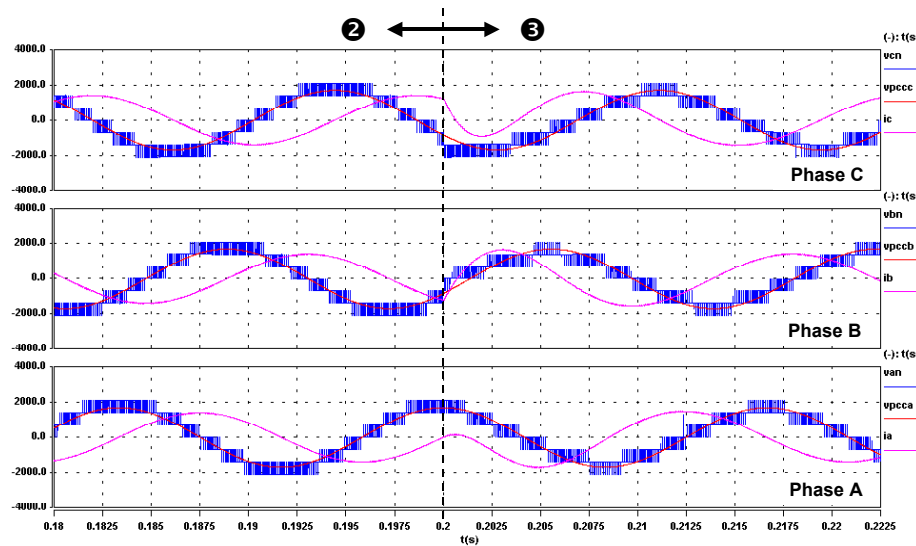


Figure 5-76. Output currents and voltages of the converter and the voltages at the PCC.

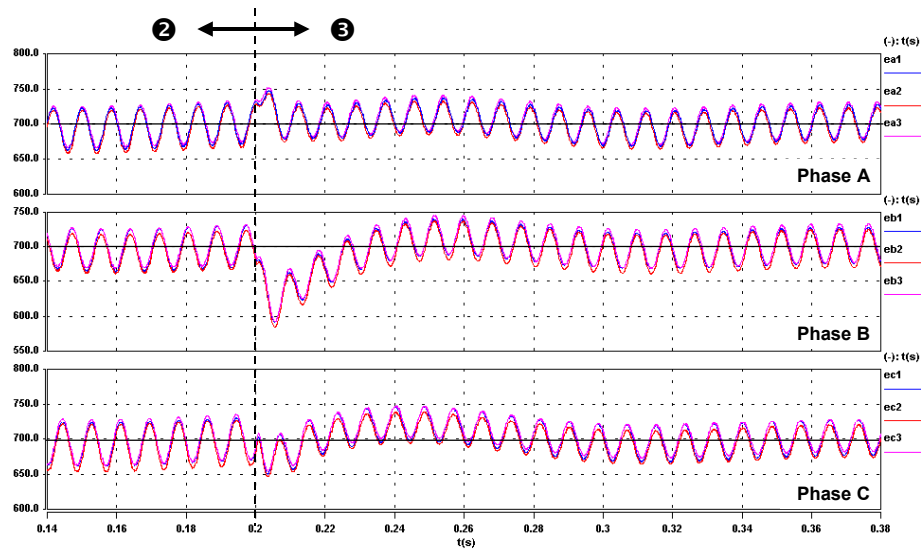


Figure 5-77. All nine capacitor voltages in groups of the same phase.

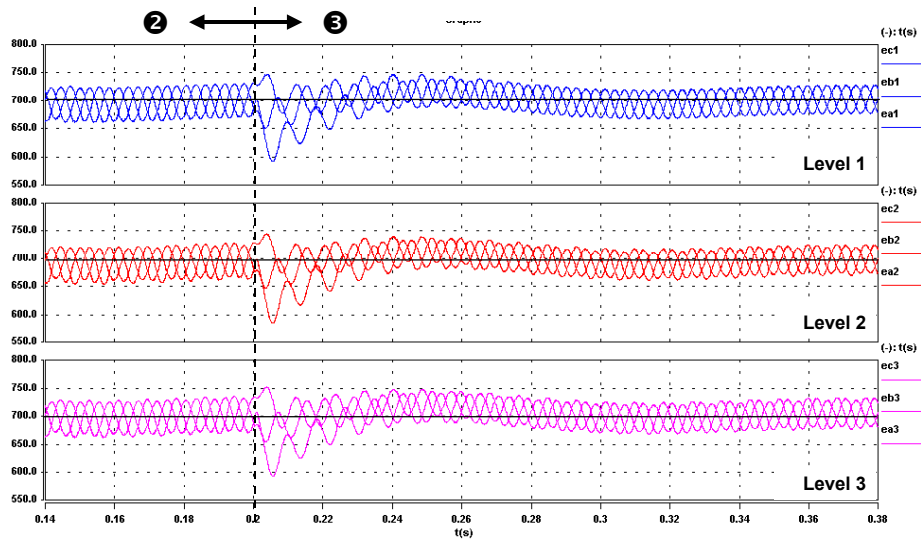


Figure 5-78. All nine capacitor voltages in groups of the same level.

## B. Experimental Results

To validate the performance of the cascaded PWM technique, a single-phase, seven-level cascaded-based STATCOM with the DSP-based controller is set up in the small-scale testbed. Two experiments are conducted to demonstrate the balanced DC capacitor voltages through the transient to the step commands and the DC capacitor voltage disturbances.

The specifications for the experimental setup of the seven-level cascaded-based STATCOM are given in Table 5-11.

TABLE 5-11. SPECIFICATIONS FOR THE STUDIED SEVEN-LEVEL CASCADED-BASED STATCOM TESTBED SYSTEM.

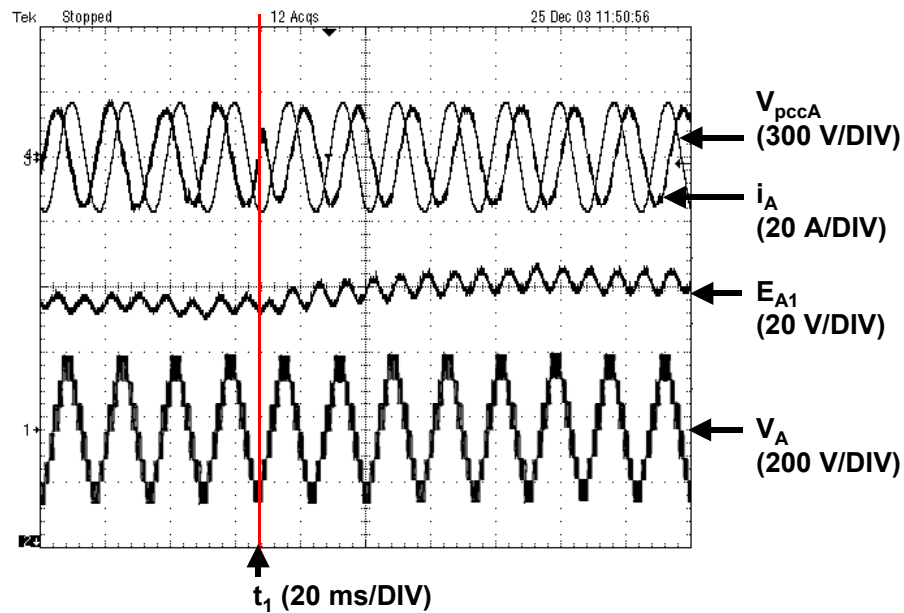
<b>Seven-Level Cascaded Converter</b>	
Individual DC Bus Voltage	70 V $\pm$ 10%
Total DC Bus Voltage	210 V $\pm$ 10%
Rated RMS Reactive Current	10 A
Capacitor Impedance	(0.8m-j/( $\omega$ ·2mF)) $\Omega$
Individual Switching Frequency/ Equivalent Switching Frequency	333 Hz/ 2 kHz
<b>Power System</b>	
Configuration	Balanced Single-Phase Three-Wire
Coupling Reactor Impedance	(64m-j( $\omega$ ·4mH)) $\Omega$
PCC Line Voltage	208 V

### • DC Voltage-Balancing during the Transient

In this experiment, the STATCOM operates in the worst-case transient, which is either from the full capacitive to full inductive mode or vice versa. From the experimental results as shown in Figure 5-79, at time  $t_1$ , the STATCOM is commanded to abruptly transfer from the full inductive to the full capacitive mode. Before time  $t_1$ , the output current  $i_A$ , which is leading the voltage at the PCC,  $V_{pccA}$ , by  $90^\circ$ , indicates that the STATCOM operates in the inductive mode, while the output current  $i_A$  lagging  $V_{pccA}$  by  $90^\circ$  after time  $t_1$  indicates that the STATCOM operates in the capacitive mode. The result shows the fast response of  $i_A$  to the step command. During the full capacitive mode, the 120Hz voltage ripple across the DC capacitor is at its

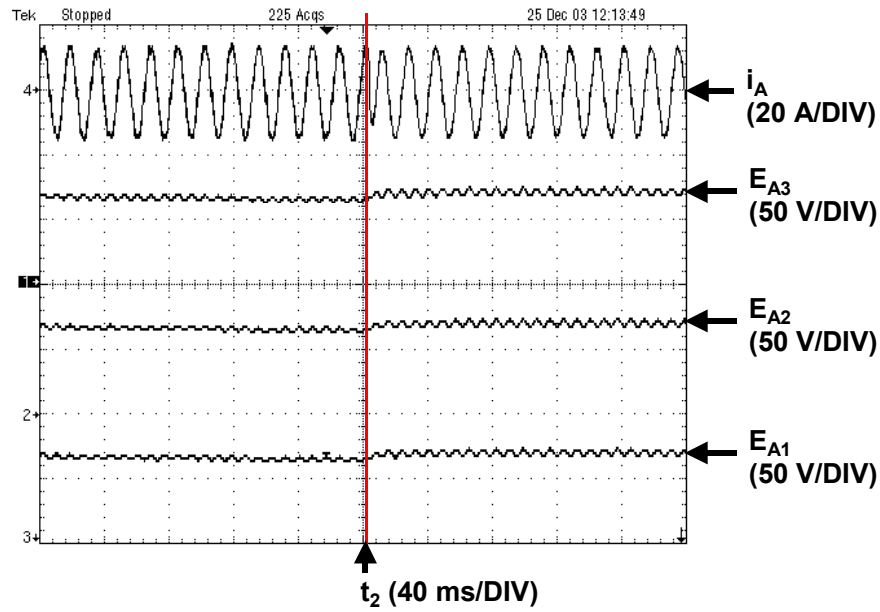


maximum, which is approximately  $7 V_{\text{peak-to-peak}}$  or 10% of the DC voltage setting of 70 V, and which is consistent with the  $E_{A1}$  waveform, as shown in Figure 5-79. Since three H-bridge converters are used in one phase leg, the output voltage  $V_A$  then has seven levels. Although the lower individual switching frequency of 333 Hz is used, the same current-loop bandwidth as that of 1 kHz in the three-level case can be achieved.

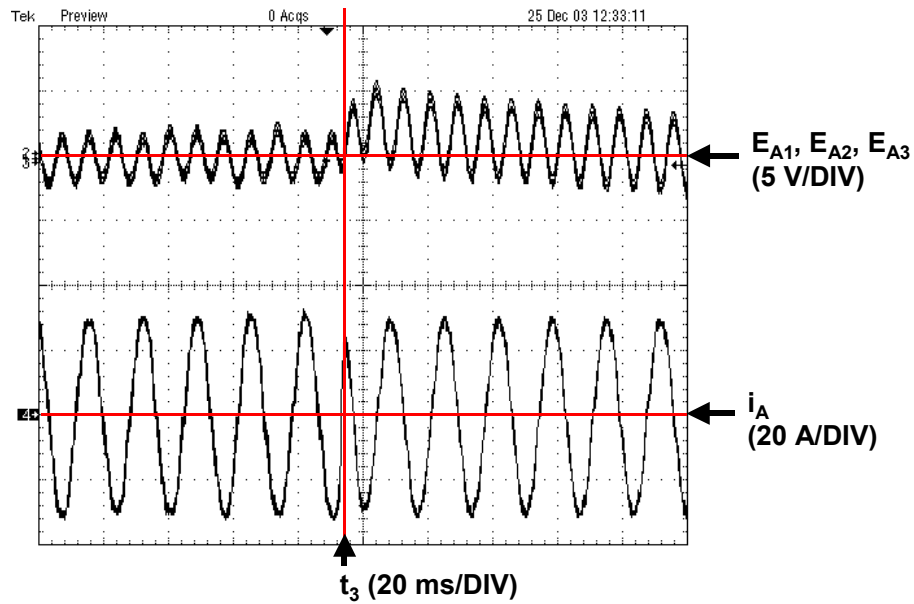


**Figure 5-79. The transient from the full inductive to the full capacitive mode of the seven-level cascaded-based STATCOM operation: (from the top) the voltage at the PCC, the converter output current and the first-level DC capacitor voltage and the converter output voltage.**

Figure 5-80(a) shows the response of the three DC capacitor voltages of the seven-level cascaded converter during the same transient at time  $t_2$ , which is from the full inductive to full capacitive mode. The results show that these three DC capacitor voltages,  $E_{A1}$  through  $E_{A3}$ , are very well regulated to the setting value in the steady state. As shown in Figure 5-80(b)  $E_{A1}$  through  $E_{A3}$  are aligned with the same reference in order to show their balance. The results indicate that all three voltages have the same voltage ripple and are very well balanced in both the steady state and the transient. Again, the maximum peak-to-peak voltage ripples across the DC capacitors are about 7 V during the full capacitive operation mode.



(a)

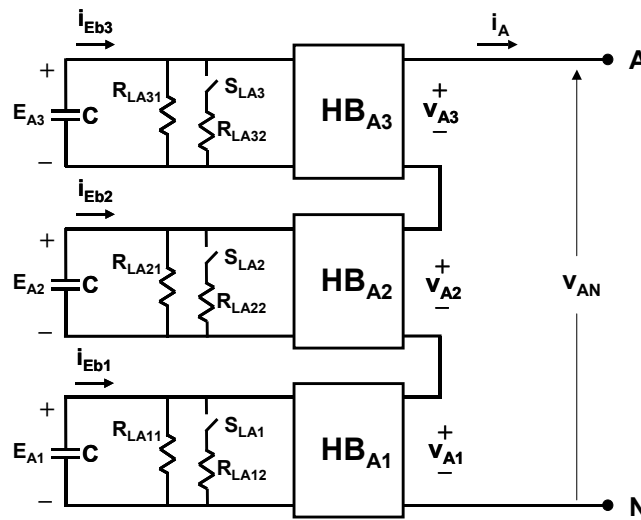


(b)

Figure 5-80. The transient from the full inductive to the full capacitive mode of the seven-level cascaded-based STATCOM operation: (a) (from the top) the output current and the third-level, the second-level and the first-level DC capacitor voltages and (b) in detail at time  $t_2$ .

- ***DC Voltage-Balancing during the Capacitor Voltage Disturbance***

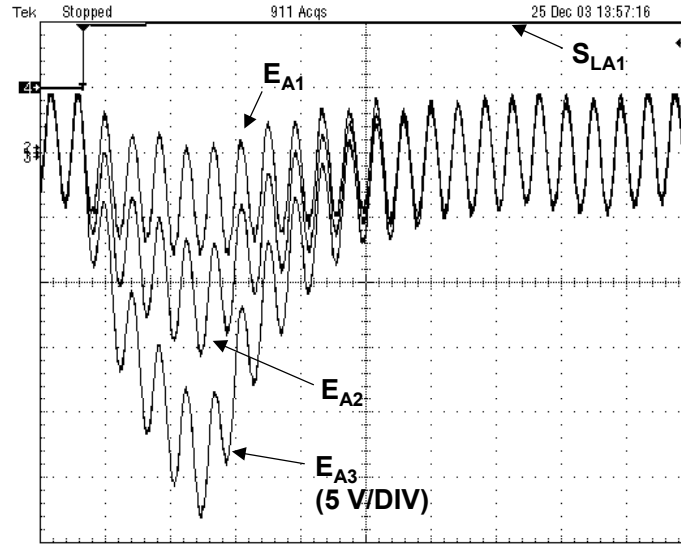
To further verify the performance of the proposed cascaded PWM technique, phase A of the seven-level cascaded converter is set up as shown in Figure 5-81. Paralleled with the DC capacitors, a set of resistors, which represent the additional losses of the H-bridge converters, is realized. The semiconductor switches  $S_{LA1}$  through  $S_{LA3}$  are used to control the resistance across the DC capacitors. With the combination of these three switches, several different resistances across the DC capacitors can be realized during different STATCOM operation modes.



**Figure 5-81. System under test for verifying the proposed cascaded PWM.**

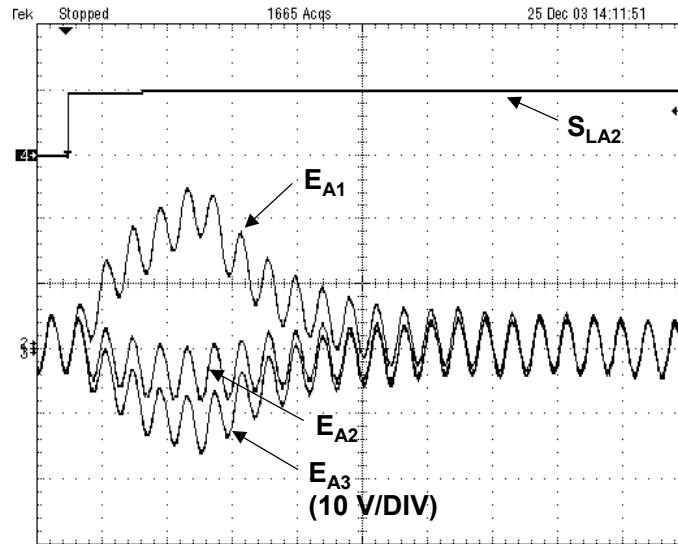
In the first case, during the full-capacitive mode, the losses of all three H-bridge converters are increased by connecting three different resistors in parallel with the DC-bus capacitors. The response of the three DC capacitors voltages,  $E_{A1}$  through  $E_{A3}$ , to the disturbance at the DC links is shown in Figure 5-82. The rising edge of the  $S_{LA1}$  gate signal indicates the beginning of the DC-capacitor voltage disturbance. Because it is connected to the largest resistance, the DC capacitor of the third-level H-bridge converter has the lowest voltage. All voltages are initially decreasing because the amounts of compensated currents are less than the discharge currents.

With the help of the feedback voltage loop and the cascaded PWM, all three DC capacitor voltages are increased and can convert to the setting voltage, which is 70 V in this experiment.



**Figure 5-82. The response of the three DC capacitor voltage waveforms,  $E_{A1}$  through  $E_{A3}$ , to the disturbance at the rising edge of the  $S_{LA1}$  gate signal.**

In the second case, during that the STATCOM operates in the full-capacitive mode, the losses in the second and third-level H-bridge converters are increased, and the losses in the first-level H-bridge converter is decreased by turning on  $S_{LA2}$  and  $S_{LA3}$  and turning off  $S_{LA1}$ , respectively. The response of the three DC capacitors voltages,  $E_{A1}$  through  $E_{A3}$ , to the disturbance at the DC links is shown in Figure 5-83. The rising edge of the  $S_{LA2}$  gate signal indicates the beginning of the DC-capacitor voltage disturbance. After the disturbance, the DC-capacitor voltage of the first-level H-bridge converter increases due to the over-compensated current, while the other two are decreased due to the additional losses. The third-level DC-capacitor voltage drops further than that of the second-level one because of the larger paralleled resistor. With the help of the feedback voltage loop and the cascaded PWM, all three DC capacitor voltages are again increased, and can convert to the setting voltage.



**Figure 5-83. The response of the three DC capacitor voltage waveforms,  $E_{A1}$  through  $E_{A3}$ , to the disturbance at the rising edge of the  $S_{LA2}$  gate signal.**

In conclusion, caused by the severe and unusual disturbance presented in both cases, the DC-capacitor voltage imbalance in three different levels of the seven-level cascaded converter can be eliminated by utilizing the proposed PWM technique and the feedback voltage-loop control. This technique can also be applied in the CMC topology with any number of voltage levels.

### 5.3 CONCLUSIONS

This chapter presented the completed feedback-control design for the CMC-based STATCOM. By utilizing the cascaded PWM, all DC capacitor voltages can be balanced in all operation conditions. Based on the philosophy behind the proposed technique, CMC with any number of voltage levels can be modeled as three-level cascaded converters. This dramatically simplifies the entire control design process.

Based the proposed STATCOM model, the feedback-control technique for the three-level cascaded-based STATCOM was first presented and verified by both computer simulations and experiments. This control technique allows reactive and real power to be independently controlled. The experimental results were very consistent with the simulation results. Moreover, the results demonstrated the accuracy of the model and the superior performance of the control

technique. A new multilevel-voltage modulation technique, named the cascaded PWM, was proposed to overcome the imbalance problem among the DC-capacitor voltages in the CMC-based STATCOM. The cascaded PWM can be directly realized by FPGA, which minimizes the complexity of the main control loop and significantly improves the reliability of the entire control system.

To validate the proposed control system, the seven-level cascaded-based STATCOM is used as an example. The performance of the feedback control, which is derived from that used in the three-level cascaded-based STATCOM, is verified by both simulations and experiments. The results show the superior performance of the designed controller. Very fast responses to the step commands are achieved. In addition, the DC capacitors are well balanced in both steady state and transient period.